# Implementing Collections - LinkedSet

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 $V_1$   $\Box$ 

 $V_2$ 

 $V_3$ 

#### **Problem Overview**

This assignment requires you to implement a set collection using a doubly-linked list as the underlying data structure. You are provided with the <code>set</code> interface and a shell of the <code>LinkedSet</code> implementing class. You must not change anything in the <code>set</code> interface, but you must create correct implementations of the methods in the <code>LinkedSet</code> class. In doing so you are allowed to add any number of private methods and nested classes that you need, but you may not create or use any other top-level class and you may not create any public method. You must also use without modification the existing fields of the <code>LinkedSet</code> class.

The <code>Set</code> interface is generic and makes no restrictions on the type that it can contain. The <code>LinkedSet</code> class is also generic, but it does make a restriction on the type variable: Any type bound by a client to <code>T</code> must be a class that implements the <code>Comparable</code> interface for that type. Thus, there is a natural order on the values stored in an <code>LinkedSet</code>, but not (necessarily) on those stored in another class that implements the <code>Set</code> interface. This is an important distinction, so pause here long enough to make sure you understand this point.

The following sections describe each method to be implemented, organized according to the methods appearing in the <code>Set</code> interface and those specific to the <code>LinkedSet</code> class. Each method's behavior is described below and in comments in the provided source code. You must read both. Note that in addition to correctness, your code must meet the stated performance requirements.

#### General Collection Methods of the Set Interface

These methods correspond to the general methods that would be supported by most any type of collection, but some have behavior specific to a set.

#### add(T element)

The add method ensures that this set contains the specified element. Neither duplicates nor null values are allowed. The method returns true if this set was modified (i.e., the element was added) and false otherwise. Note that the constraint on the generic type parameter  ${\tt T}$  of the Linkedset class ensures that there is a natural order on the values stored in an Linkedset. You must maintain the internal doubly-linked list in ascending natural order at all times. The time complexity of the add method must be O(N), where N is the number of elements in the set.

Note that one element being a *duplicate* of another means that the two elements are *equal*. Since duplicates are not allowed to be added to any implementing class of the set interface, this is an example of why it's important for the equals method and the compareTo method of a class to be consistent.

#### remove(T element)

The remove method ensures that this set does not contain the specified element. The method returns true if this set was modified (i.e., an existing element was removed) and false otherwise. The remove method must maintain the ascending natural order of the doubly-linked list. The time complexity of the remove method must be O(N), where N is the number of elements in the set.

#### contains(T element)

The contains method searches for the specified element in this set, returning true if the element is in this set and false otherwise. The time complexity of the contains method must be O(N), where N is the number of elements in the set.

#### size()

The size method returns the number of elements in this set. This method is provided for you and must not be changed. The time complexity of the size method is O(1).

## isEmpty()

The <code>isEmpty</code> method returns true if there are no elements in this set and false otherwise. This method is provided for you and must not be changed. The time complexity of the <code>isEmpty</code> method is O(1). Any set for which <code>isEmpty()</code> returns true is considered the "empty set" ( $\varnothing$ ) for purposes of <code>union</code>, <code>intersection</code>, and <code>complement</code> described below.

#### iterator()

The iterator method returns an Iterator over the elements in this set. Although the interface specifies that no particular order can be assumed (by a client), the Linkedset implementation must ensure that the resulting iterator returns the elements in ascending natural order. The associated performance constraints are as follows: iterator(): O(1); hasNext(): O(1); next(): O(1); required space: O(1).

## **Set Operator Methods of the Set Interface**

These methods correspond to the basic mathematical set operations. Each method takes a parameter of type <code>set</code>; that is, an object of some class that implements the <code>set</code> interface. Since the implementing class is unknown, it may or may not be a <code>LinkedSet</code>. Thus, none of these methods can assume that the parameter set maintains its elements in any particular order.

## equals(Set<T> s)

Two sets are equal if and only if they contain exactly the same elements, regardless of order. If  $A = \{1,2,3\}, B = \{3,1,2\}, and C = \{1,2,3,4\}, then A = B and A != C. The equals method returns true if this set is equal to the parameter set, and false otherwise. The time complexity of the equals method must be <math>O(N^2)$  where N is the size of each set.

## union(Set<T> s)

The union of set A with set B, denoted A  $\cup$  B, is defined as  $\{x \mid x \in A \text{ or } x \in B\}$ . Note that A  $\cup$  B = B  $\cup$  A and A  $\cup$   $\emptyset$  = A. The union method returns a set that is the union of this set and the parameter set. The result set must be in ascending natural order. The time complexity of the union method must be  $O(N^2)$  where N is the size of the larger of the two sets involved.

## intersection(Set<T> s)

The intersection of set A with set B, denoted A  $\cap$  B, is defined as  $\{x \mid x \in A \text{ and } x \in B\}$ . Note that A  $\cap$  B = B  $\cap$  A and A  $\cap \varnothing = \varnothing$ . The intersection method returns a set that is the intersection of this set and the parameter set. The result set must be in ascending natural order. The time complexity of the intersection method must be  $O(N^2)$  where N is the size of the larger of the two sets involved.

#### complement(Set<T> s)

The relative complement of set B with respect to set A, denoted A \ B, is defined as  $\{x \mid x \in A \text{ and } x \in /B\}$ . Note that A \ B != B \ A, A \  $\emptyset$  = A, and  $\emptyset$  \ A =  $\emptyset$ . The complement method returns a set that is the relative complement of the parameter set with respect to this set. The result set must be in ascending natural order. The time complexity of the complement method must be  $O(N^2)$  where N is the size of the larger of the two sets involved.

#### Additional Methods of the LinkedSet Class

In addition to the methods from the Set interface, the LinkedSet class also implements its own class-specific methods. Most of these methods are designed to take advantage of the underlying representation, while some of them simply provide added functionality.

## **Constructors**

The only public constructor that is allowed has been provided for you and you must not change it in any way. You may, however, find it helpful to write your own private constructor; one that offers direct support for building an Linkedset from an existing doubly-linked list. Such a constructor will be helpful but it is not required and will not be graded.

#### equals(LinkedSet<T> s)

The external behavior of this overloaded method is identical to the equals method from the set interface described above. However, since the parameter is typed as an LinkedSet, this method can directly access the doubly-linked list in this set as well as in the parameter set. Having access to the underlying representation of both sets allows a more efficient algorithm for this method. The time complexity of this equals method must be O(N) where N is the size of this set.

## union(LinkedSet<T> s)

The external behavior of this overloaded method is identical to the union method from the Set interface described above. However, since the parameter is typed as an LinkedSet, this method can directly access the doubly-linked list in this set as well as in the parameter set. Having access to the underlying representation of both sets allows a more efficient algorithm for this method. The time complexity of the union method must be O(N) where N is the size of the larger of the two sets involved.

#### intersection(LinkedSet<T> s)

The external behavior of this overloaded method is identical to the intersection method from the set interface described above. However, since the parameter is typed as an LinkedSet, this method can directly access the doubly-linked list in this set as well as in the parameter set. Having access to the underlying representation of both sets allows a more efficient algorithm for this method. The time complexity of the intersection method must be O(N) where N is the size of the larger of the two sets involved.

#### complement(LinkedSet<T> s)

The external behavior of this overloaded method is identical to the complement method from the Set interface described above. However, since the parameter is typed as an LinkedSet, this method can directly access the doubly-linked list in this set as well as in the parameter set. Having access to the underlying representation of both sets allows a more efficient algorithm for this method. The time complexity of the complement method must be O(N) where N is the size of the larger of the two sets involved.

## descendingIterator()

The descendingIterator method returns an Iterator over the elements in this set in descending natural order. The associated performance constraints are as follows: O(1); O(1); O(1); O(1); O(1); O(1); required space: O(1).

## powerSetIterator()

The power set of a set S, denoted P(S), is defined as  $\{T \mid T \subseteq S\}$ ; that is, the set of all subsets of S. There are 2^N members of P(S) where N is the number of elements in S. For example, if S =  $\{A,B,C\}$ , then P(S) =  $\{\emptyset,\{A\},\{B\},\{C\},\{A,B\},\{B,C\},\{A,C\},\{A,B,C\}\}\}$ . (Note that the empty set  $\emptyset$  is a member of every set.) The powersetIterator method returns an Iterator over the elements in the power set of this set. The iterator makes no guarantees regarding the order in which the elements of P(S) will be returned. The

associated time complexities are as follows: powerSetIterator(): O(N); powerSetIterator(): O(N); powerSetIterator(): O(N); powerSetIterator(): O(N); powerSetIterator(): powerSetI