

Math 1271 - Lectures 010 and 030

Name (Print):

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Fall 2017

Quiz 8C

11/07/17

Time Limit: 25 Minutes

Teaching Assistant

David Denmark

You may *not* use your books, notes, graphing calculator, phones or any other internet devices on this exam.

You are required to show your work on each problem on this quiz.

Problem	Points	Score
1	3	3
2	4	1.75
3	3	.25
Total:	10	5.0

1. (3 points) Starting with the initial guess $x_1 = -2$, use Newton's method to approximate a root to the equation $e^x + x^2 - 3 = 0$ to eight decimal places.

$$x_2 = x_1 - \frac{f(x_1)}{f'(x_1)} = -2 - \frac{e^{-2} + 4 - 3}{e^{-2} - 4} = -2 - \frac{1.13533528}{-3.86466471} = -1.70622670$$

$$x_3 = x_2 - \frac{f(x_2)}{f'(x_2)} = -2 - \frac{e^{-1.70622670} + 2.91120955 - 3}{e^{-1.70622670} - 3.41245340} = -1.70622670 - \frac{0.9275909}{-3.23090386} = -1.67751675$$

$$x_4 = x_3 - \frac{f(x_3)}{f'(x_3)} = -1.67751675 - \frac{.18683736 + 2.81406245 - 3}{.18683736 - 3.3583350} = -1.67751675 - \frac{.00089981}{-3.16849764} = -1.67723274$$

$$x_5 = -1.67723274 - \frac{.18689044 + 2.81310966 - 3}{.18689044 - 3.3544659} = -1.67723274 - \frac{.0000001}{-3.16757506} = -1.67723271$$

$$x_6 = -1.67723271 \quad + 3 \quad \text{stop at } x_6$$

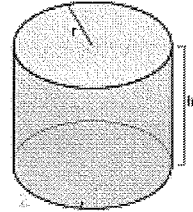
2. (4 points) If 600π cm² material is available to make a cylinder with an open top, find the largest possible volume of the cylinder.

Hint: The surface area of a cylinder with an open top is $\pi r^2 + 2\pi rh$, where r is the base radius, h is the height.

$$h = \frac{-\pi r^2}{2\pi r} \quad SA = \pi r^2 + 2\pi r \left(\frac{-\pi r^2}{2\pi r} \right)$$

$$600\pi = \pi r^2 + 2\pi r \left(\frac{-\pi r^2}{2\pi r} \right)$$

+1.75



find r using 600π cm²
 use the equation I found
 then when you find r
 you use $h = \frac{-\pi r^2}{2\pi r}$ to get
 h & you have height &
 radius.

3. (3 points) Show that the curve $y = \sqrt{x^2 + 5} + 2x$ has one slant asymptote at $y = 3x$ and one horizontal asymptote at $y = 0$.

$$y = \frac{2x}{x + \sqrt{5}} \sim 2x \text{ assumption}$$

$$\lim_{x \rightarrow \infty} f(x) - 2x = y \text{ int}$$

+1.75