1 Declarative system

 $\overline{|\Gamma \vdash A \unlhd B|}$ Top-level polymorphic instantiation

$$\frac{\Gamma \vdash w \Leftarrow A \quad \Gamma \vdash [w/x]B \unlhd C}{\Gamma \vdash \forall x : A. B \unlhd C} \quad \text{De_inst_Forall}$$

$$\frac{A \neq \forall x : B. C}{\Gamma \vdash A \unlhd A} \quad \text{De_inst_Base}$$

 $\Gamma \vdash v \Leftarrow A$ Declarative checking

$$\frac{\Gamma \vdash A \quad \Gamma, x : A \vdash v \Leftarrow B}{\Gamma \vdash v \Leftarrow \forall x : A . B} \quad \text{De_CHECK_GEN}$$

$$\frac{\Gamma \vdash A \quad \Gamma, x : A \vdash v \Leftarrow B}{\Gamma \vdash \lambda x . v \Leftarrow \Pi x : A . B} \quad \text{De_CHECK_PI}$$

$$\frac{\Gamma \vdash v \equiv w \Leftarrow A}{\Gamma \vdash \text{refl} \Leftarrow \text{eq} A v w} \quad \text{De_CHECK_REFL}$$

$$\frac{\Gamma \vdash v \Rightarrow A \quad \Gamma \vdash A \leqslant B}{\Gamma \vdash v \Leftarrow B} \quad \text{De_CHECK_SUB}$$

 $\Gamma \vdash v \Rightarrow A$ Declarative inference

$$\frac{\Gamma \vdash e \Rightarrow \operatorname{eq} A \ v \ w \quad \Gamma, x : A, p : \operatorname{eq} A \ v \ x \vdash X \quad \Gamma \vdash f \Leftarrow [\operatorname{refl}/p][v/x]X}{\Gamma \vdash \operatorname{rec}_{eq}^{x.p.X}(e, f) \Rightarrow [e/p][w/x]X} \quad \text{De_{INF_RECEQ}}$$

 $\Gamma \vdash A$ Declarative type well-formedness

$$\frac{\Gamma \vdash A \quad \Gamma \vdash v \Leftarrow A \quad \Gamma \vdash w \Leftarrow A}{\Gamma \vdash \mathbf{eq} \, A \, v \, w} \quad \text{De_wfT_EQ}$$

$$\frac{\Gamma \vdash A \quad \Gamma, x : A \vdash B}{\Gamma \vdash \Pi x : A . \, B} \quad \text{De_wfT_PI}$$

$$\frac{\Gamma \vdash A \quad \Gamma, x : A \vdash B \quad x \in B \, ok}{\Gamma \vdash \forall x : A . \, B} \quad \text{De_wfT_Forall}$$

 $\Gamma \vdash A \equiv B$ Declarative type equivalence

$$\begin{array}{c} \hline \Gamma \vdash 1 \equiv 1 \\ \hline \Gamma \vdash A_1 \equiv A_2 \quad \Gamma, x : A_1 \vdash B_1 \equiv B_2 \\ \hline \Gamma \vdash \Pi x : A_1. B_1 \equiv \Pi x : A_2. B_2 \\ \hline \Gamma \vdash A_1 \equiv A_2 \quad \Gamma, x : A_1 \vdash B_1 \equiv B_2 \\ \hline \Gamma \vdash A_1 \equiv A_2 \quad \Gamma, x : A_1 \vdash B_1 \equiv B_2 \\ \hline \Gamma \vdash A_1 \equiv A_2 \quad \Gamma \vdash v_1 \equiv v_2 \Leftarrow A_1 \quad \Gamma \vdash w_1 \equiv w_2 \Leftarrow A_1 \\ \hline \Gamma \vdash A_1 \equiv A_2 \quad \Gamma \vdash v_1 \equiv v_2 \Leftarrow A_1 \quad \Gamma \vdash w_1 \equiv w_2 \Leftarrow A_1 \\ \hline \Gamma \vdash eq A_1 v_1 w_1 \equiv eq A_2 v_2 w_2 \\ \hline \hline \Gamma \vdash v \equiv w \Rightarrow A \quad Declarative inferring equivalence \\ \hline \Gamma \vdash v \lor v' \Rightarrow A \quad \Gamma \vdash w \lor w' \Rightarrow A \quad \Gamma \vdash v' \equiv_n w' \Rightarrow A \\ \hline \Gamma \vdash v \equiv w \Rightarrow A \quad Declarative checking equivalence \\ \hline \Gamma \vdash v \lor v' \Leftrightarrow A \quad \Gamma \vdash w \lor w' \Leftrightarrow A \quad \Gamma \vdash v' \equiv_n w' \Leftrightarrow A \\ \hline \Gamma \vdash v \equiv w \Leftrightarrow A \quad Declarative checking equivalence \\ \hline \Gamma \vdash v \lor v' \Leftrightarrow A \quad \Gamma \vdash w \lor w' \Leftrightarrow A \quad \Gamma \vdash v' \equiv_n w' \Leftrightarrow A \\ \hline \hline \Gamma \vdash v \equiv w \Leftrightarrow A \quad Declarative checking equivalence for terms in WHNF \\ \hline \hline \Gamma \vdash v \equiv_n w \Leftrightarrow A \quad Declarative checking equivalence for terms in WHNF \\ \hline \hline \Gamma \vdash v \equiv_n w \Leftrightarrow A \quad Declarative checking equivalence for terms in WHNF \\ \hline \hline \Gamma \vdash v \equiv_n w \Leftrightarrow A \quad Declarative checking equivalence for terms in WHNF \\ \hline \hline \Gamma \vdash v \equiv_n w \Leftrightarrow A \quad Declarative checking equivalence for terms in WHNF \\ \hline \hline \Gamma \vdash v \equiv_n w \Leftrightarrow B \quad \Gamma \vdash B \leqslant A \quad De_equivnChe_Forall \\ \hline \hline \Gamma \vdash v \equiv_n w \Rightarrow A \quad De_equivnChe_Forall \\ \hline \hline \Gamma \vdash v \equiv_n w \Rightarrow A \quad De_equivnChe_Subt \\ \hline \hline \Gamma \vdash v \equiv_n w \Rightarrow A \quad De_equivnInf_Var \\ \hline \hline \Gamma \vdash v \equiv_n w \Rightarrow A \quad De_equivnInf_Unit \\ \hline \hline \Gamma \vdash A \equiv A' \quad \Gamma \vdash v \equiv_n v' \Leftrightarrow A \quad De_equivnInf_Ann \\ \hline \hline \Gamma \vdash A \equiv A' \quad \Gamma \vdash v \equiv_n v' \Leftrightarrow A \quad De_equivnInf_Ann \\ \hline \hline \Gamma \vdash A \equiv A' \quad \Gamma \vdash v \equiv_n v' \Leftrightarrow A \quad De_equivnInf_Ann \\ \hline \hline \Gamma \vdash A \equiv A' \quad \Gamma \vdash v \equiv_n v' \Leftrightarrow A \quad De_equivnInf_Ann \\ \hline \hline \Gamma \vdash A \equiv A' \quad \Gamma \vdash v \equiv_n v' \Leftrightarrow A \quad De_equivnInf_Ann \\ \hline \hline \Gamma \vdash A \equiv_n f_2 \Rightarrow A \quad \Gamma \vdash A \trianglelefteq \Pi x : B.C \quad \Gamma \vdash v_1 \equiv v_2 \Leftrightarrow B \quad De_equivnInf_App \\ \hline \hline \Gamma \vdash f_1 \equiv_n f_2 \Rightarrow a \quad \Gamma \vdash f_2 v_2 \Rightarrow [v_1/x]C \quad De_equivnInf_App \\ \hline \hline \hline \Gamma \vdash f_1 \equiv_n f_2 v_2 \Rightarrow_1 [v_1/x]C \quad De_equivnInf_App \\ \hline \hline \hline \hline \Gamma \vdash f_1 \equiv_n f_2 v_2 \Rightarrow_2 [v_1/x]C \quad De_equivnInf_App \\ \hline \hline \hline \hline \hline \Gamma \vdash f_1 \equiv_n f_2 v_2 \Rightarrow_2 [v_1/x]C \quad De_equivnInf_App \\ \hline \hline \hline \hline \hline \Gamma \vdash f_1 \equiv_n f_2 v_2 \Rightarrow_2 [v_1/x]C \quad De_equivnInf_App \\ \hline \Gamma \vdash f_1 \equiv_n f_2 v_2 \Rightarrow_2 [v_1/x]C \quad De_equivnInf_App \\ \hline \hline \hline \hline \hline \hline$$

 $\Gamma \vdash A \leq B$ Declarative subtyping