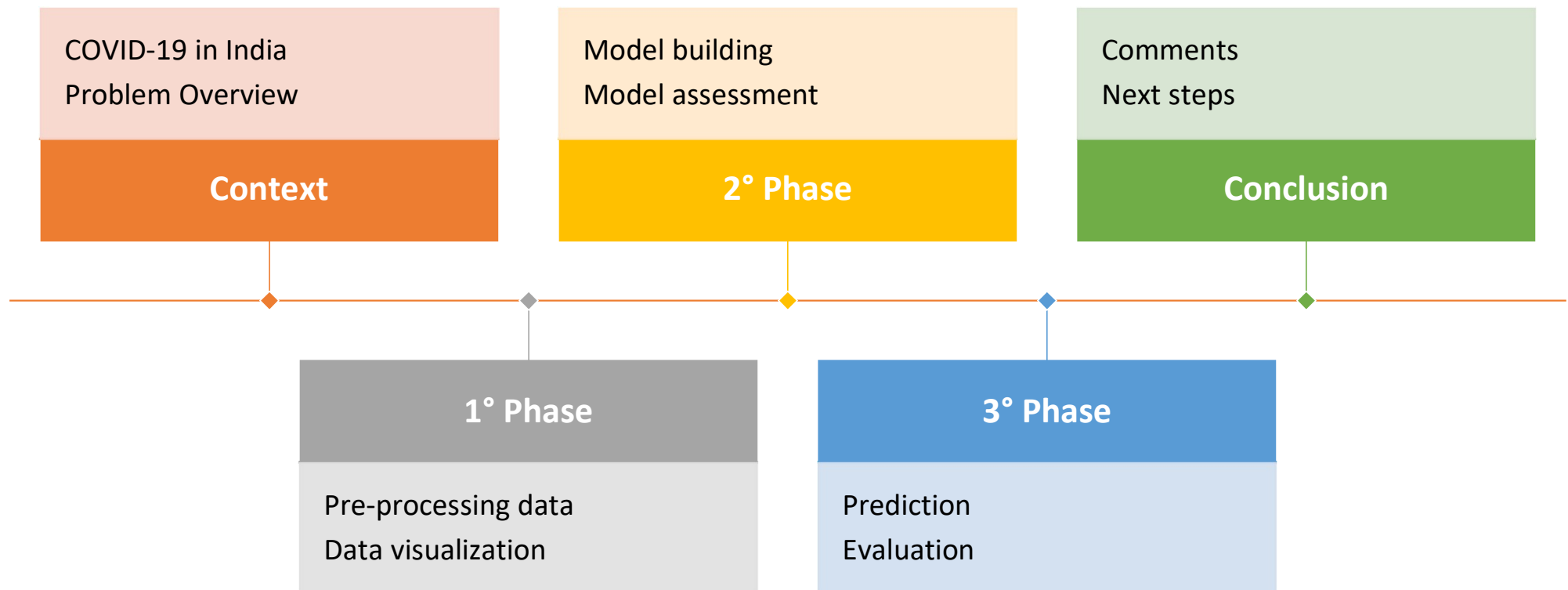




COVID-19 DIFFUSION IN CENTRAL INDIA

Michele Rispoli, Eros Fabrici, Dogan Demirbilek, Pietro Morichetti

Road Map of our Project



CONTEXT

- Covid-19 in Central India
- Problem Overview

Context

Covid-19 in India

- India is composed of 28 states, with 1.45 billion of people (24 times of italian population)
- First case reported on 30 January 2020, at this moment 4-th place in world
- OxCGRT gave a score of 100 at the end of June for the swift emergency policy

Problem Overview

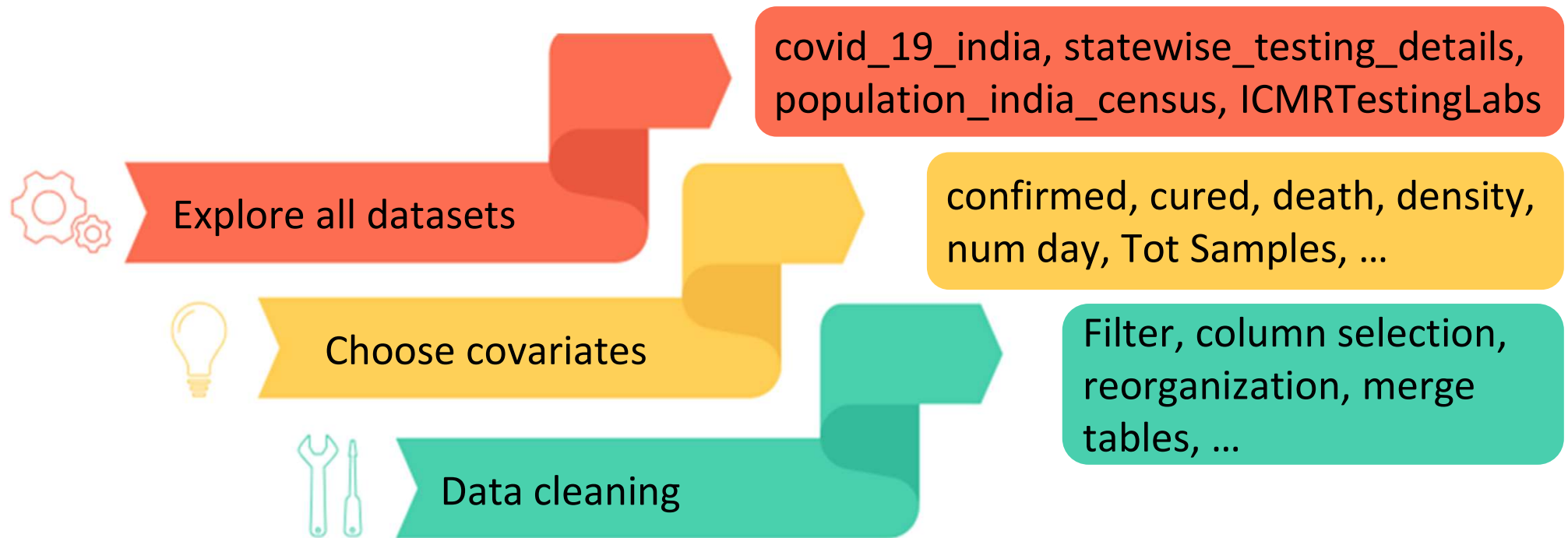
- Focus on central states of India
- Build a predictive model over the daily confirmed cases of the pandemic
- Build a predictive model over the cumulative confirmed cases of the pandemic



1° PHASE

- Pre-processing data
- Data visualization

1° Phase: Pre-processing data

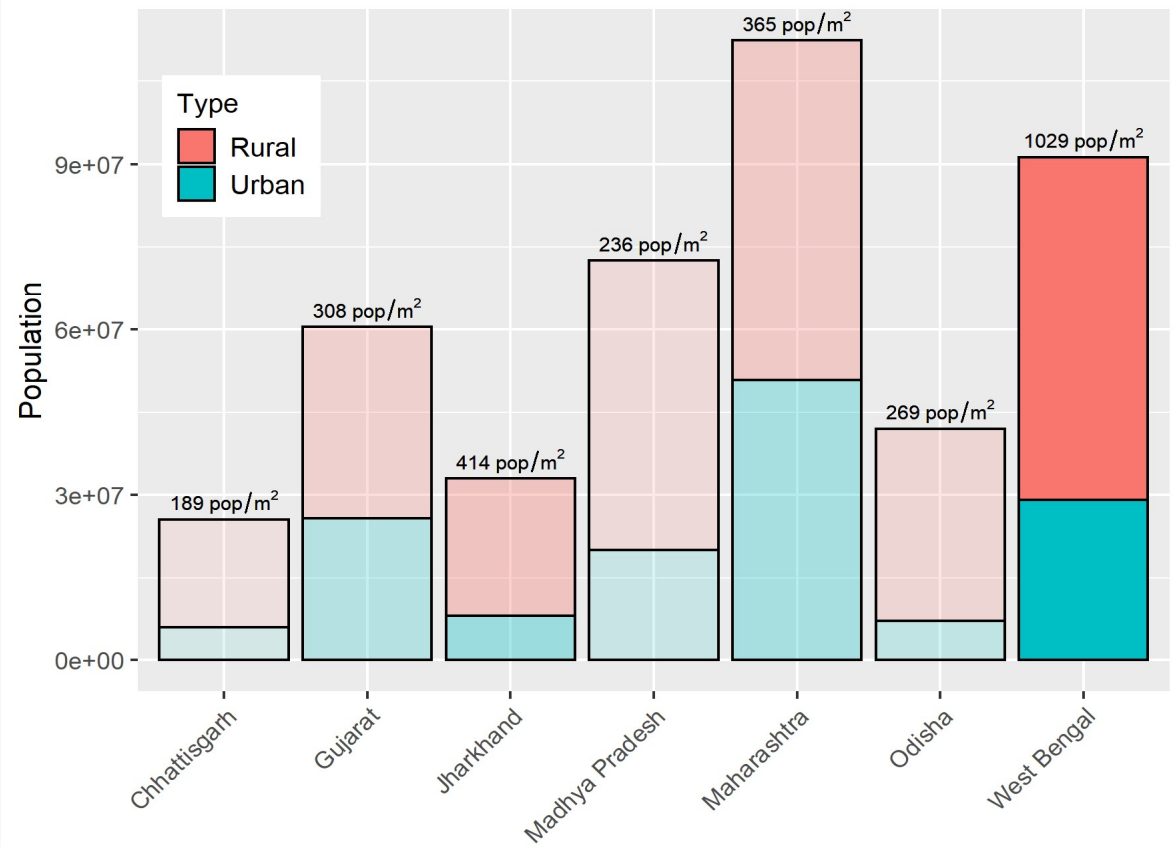


- * *These datasets are taken from Kaggle website*
- * *Some chosen covariates are used for data visualization and prediction*
- * *Last phase is valid for every kind of analysis*



1° Phase: Data visualization

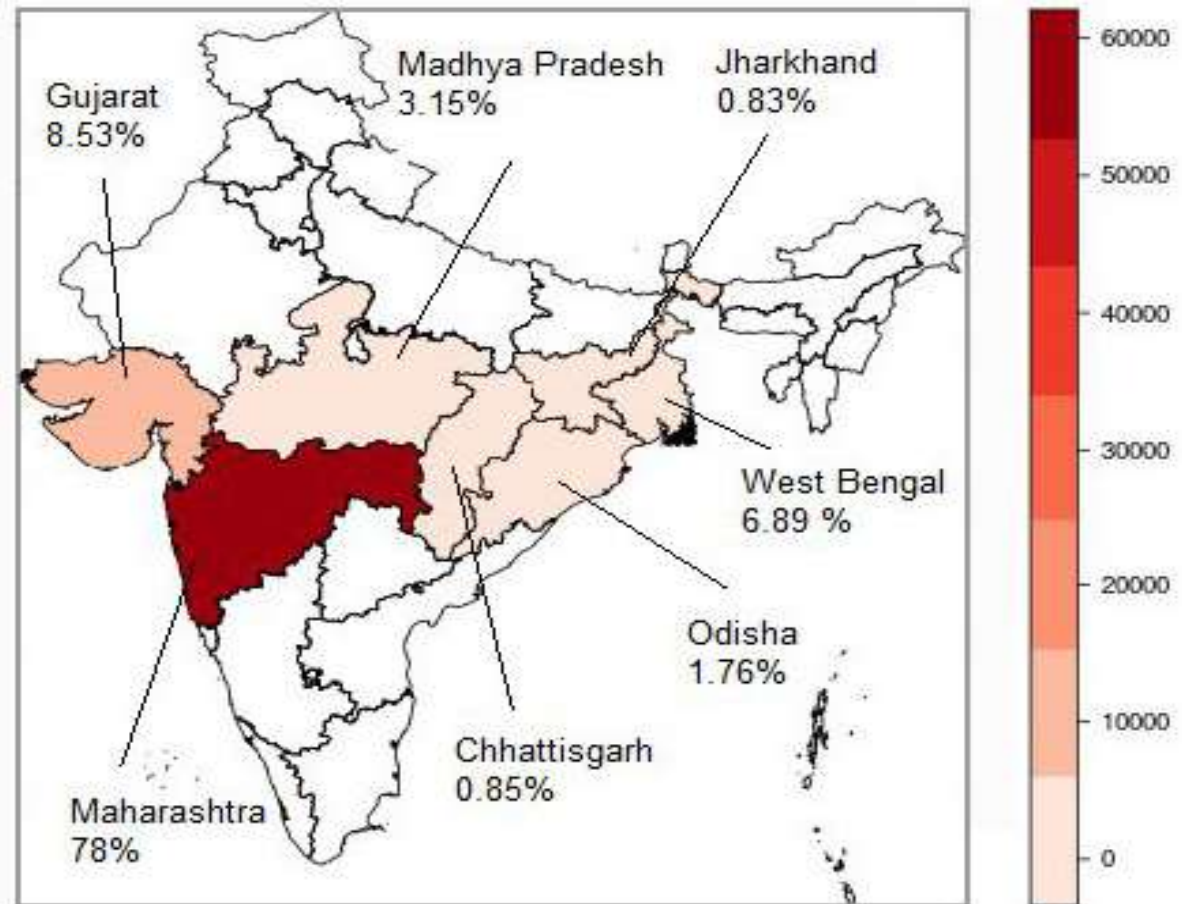
- Total population divided by rural and urban and density for each state
- Focus on Maharashtra and West Bengal, they are the most populous



1° Phase: Data visualization

Cumulative Analysis

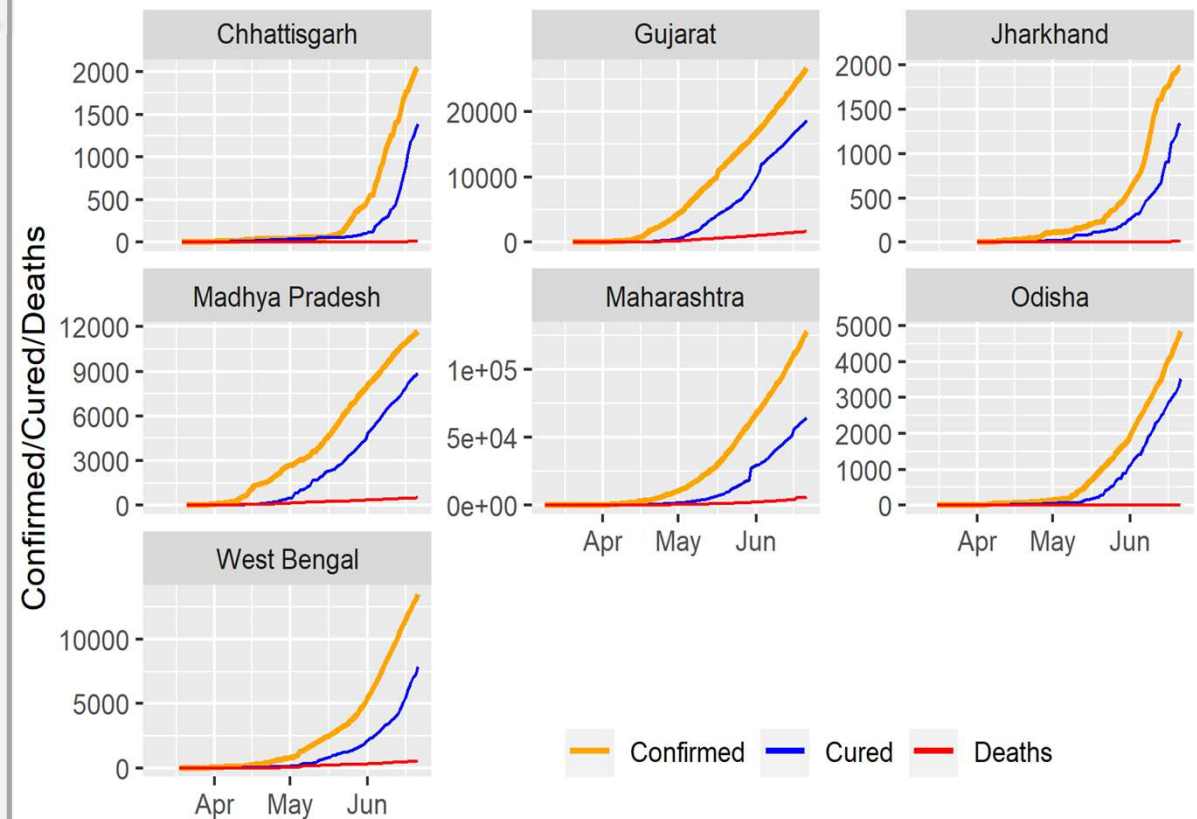
- Confirmed cases in each region, they are concentrated on Maharashtra.
- Also according the percentage scale, it is the most critical state



1° Phase: Data visualization

Cumulative Analysis

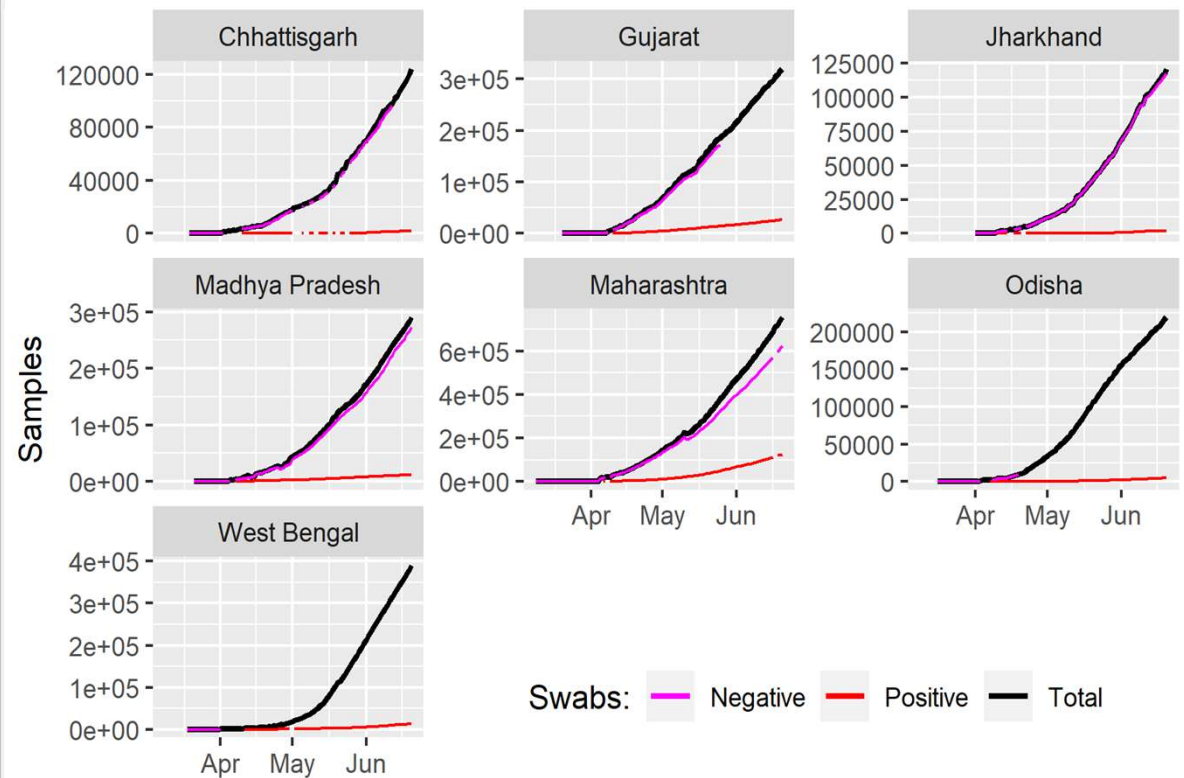
- Plot shows cumulative confirmed cases, cured and death trends
- Interesting note:
apparently Cured+Deaths
lags behind confirmed of
about 14 days



1° Phase: Data visualization

Cumulative Analysis

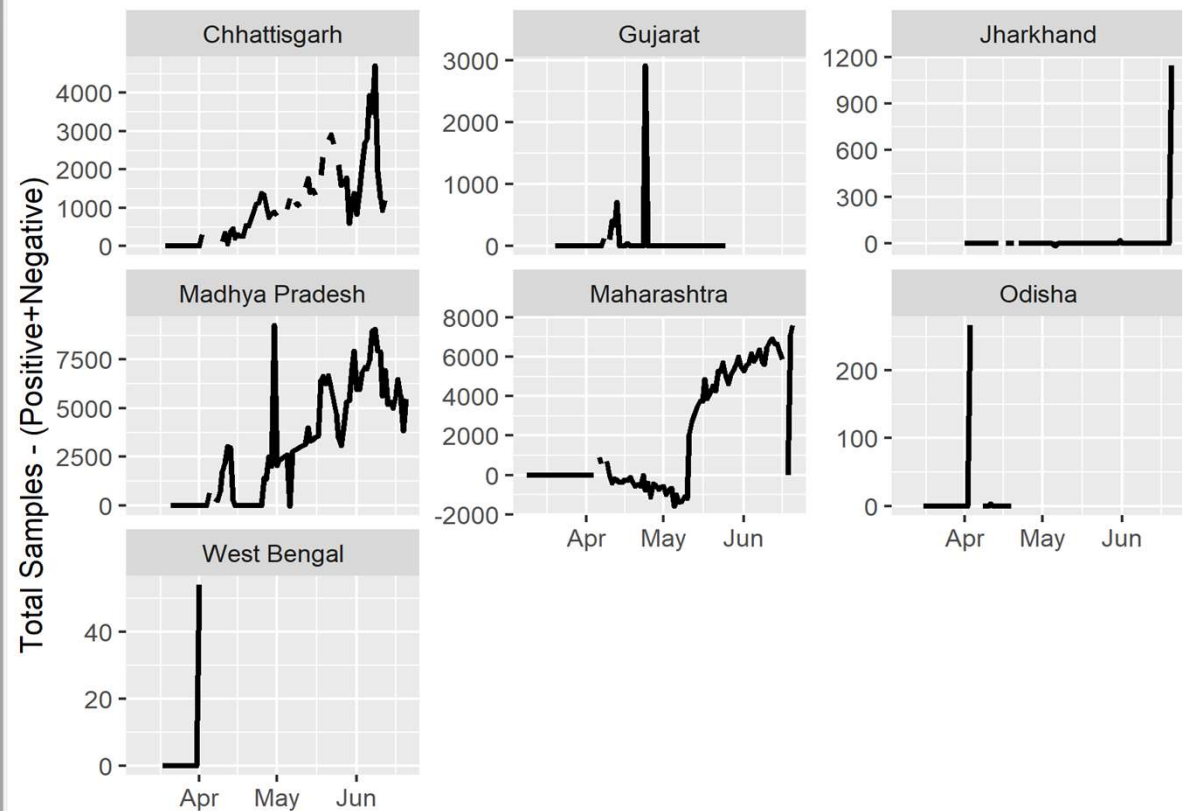
- Counting of test responses for each state
- Lots of missing data for positive/negative swabs



1° Phase: Data visualization

Cumulative Analysis

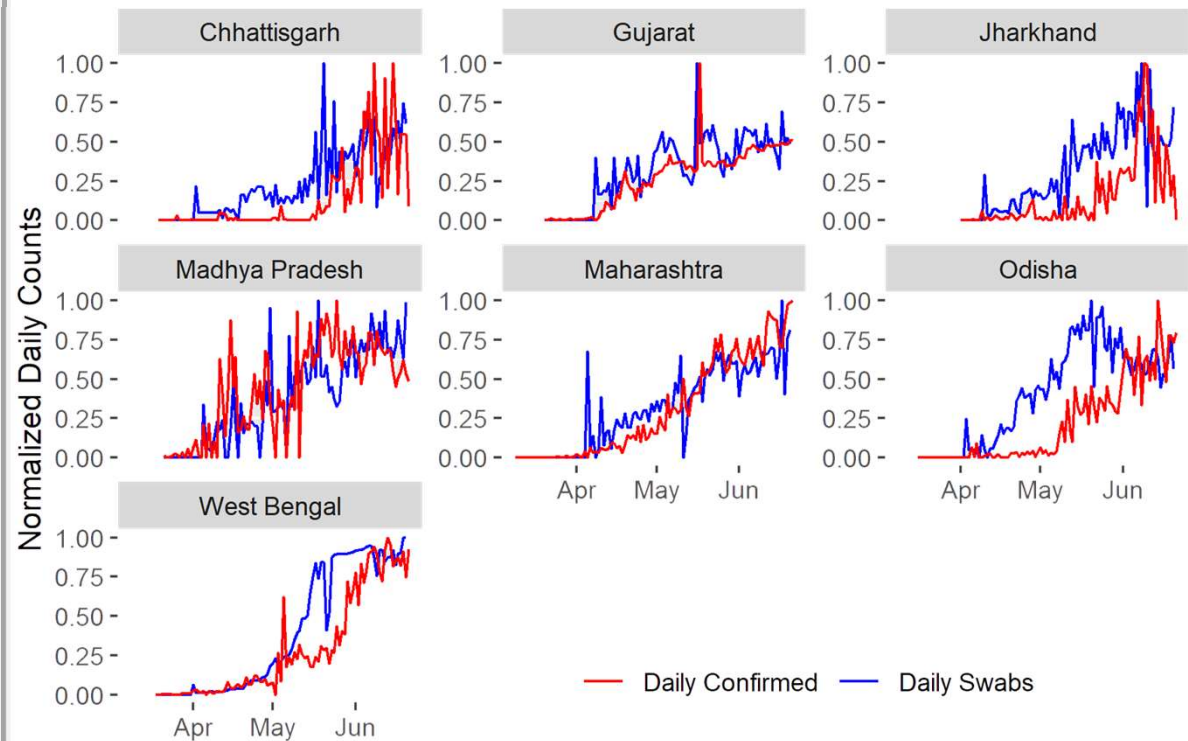
- Difference between the total swabs, and number of positive and negative
- Difference should be zero, so there is noise in data
- For some points we observed negative values (Maharashtra)



1° Phase: Data visualization

Daily Analysis

- Daily swabs vs daily confirmed
- Few irregular points where found in daily swabs count and also in daily confirmed cases
- Those points were handled setting them to zero



2° PHASE

- Model building
- Model assessment

2° Phase: Model Building

Daily Analysis

Excluded

- State specific constants (Population, Healthcare and Testing facilities)
- Positive and Negative swabs
- Cured and Deaths

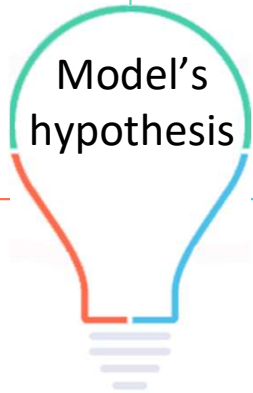
GLM poisson

- Integer values
- Range $[0, +\infty]$

Covariates

- Yesterday Tot samples
- Yesterday confirmed
- Num day
- Num day²

Model's hypothesis



$$\text{Daily Confirmed}_i \sim \text{Poisson}(\lambda_i)$$

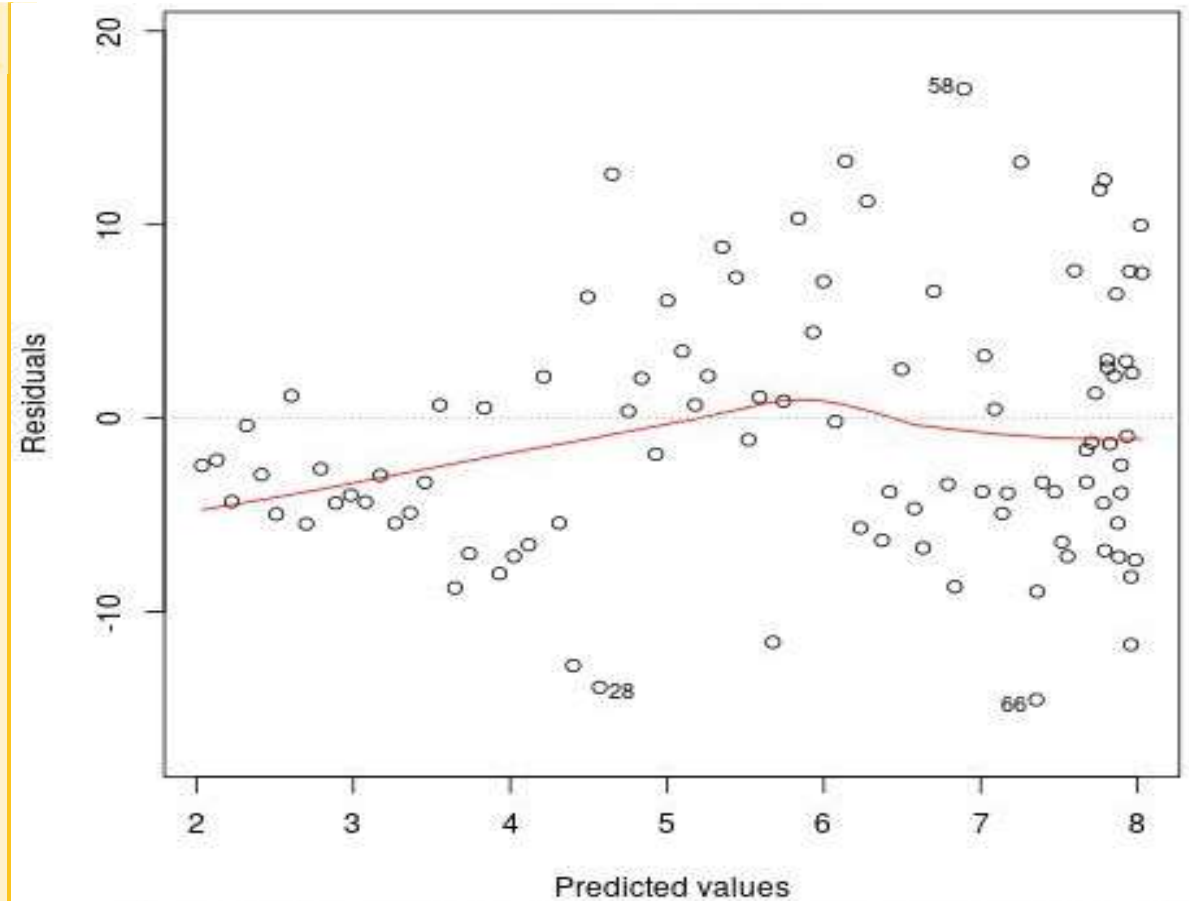
$$\log(\lambda_i) = \beta_0 + \beta_1 \cdot \text{Num Day}_i + \beta_2 \cdot \text{Num Day}_i^2 + \beta_3 \cdot \text{Yest Confirmed}_i + \beta_4 \cdot \text{Yest Tot Samples}_i$$



2° Phase: Model Assessment

Daily Analysis

- Scaled residuals vs fitted values plot (Maharashtra)
- We used the AER package for dispersion test over poisson model
- P-value is very close to zero and we reject the equidispersion null hypothesis
- We switched to **quasi-poisson** model



2° Phase: Model Assessment

Daily Analysis

- *Backward selection*: we discard the covariates with p-value over 0,05
- *F-Test*: p-value over 0,05 means pick the simplest model otherwise reject it

MODELS (Maharashtra)		RES DEV	F-TEST
M1	$\text{Num Day} + \text{Num Day}^2 + \text{Yest Confirmed} + \text{Tot Samples}$	4217	0,68
M2	$\text{Num Day} + \text{Num Day}^2 + \text{Yest Confirmed}$	4224	0,19
M3	$\text{Num Day} + \text{Yest Confirmed}$	4299	<<
M4	Yest Confirmed	42000	-

* F-test was performed considering sequential models (eg. M1~M2, M2~M3, ...)



2° Phase: Model Assessment

Daily Analysis

	Intercept	Num Day	Num Day ²	Yest Confirmed	Yest Tot Samples	RES DEV
Gujarat	X	X	X	X	X	1311
Chhattisgarh	-	-	-	X	X	650,07
Jharkhand	-	X	X	X	X	521,52
Odisha	-	-	X	X	-	573
Maharashtra	X	X	-	X	-	4373
West Bengal	-	X	X	-	X	1084,8
Madhya Pradesh	X	X	--	X	-	2948,9



2° Phase: Model Building

Cumulative Analysis

- One idea is extending daily models to cumulative cases, simply by summing them
- Second idea is using *tscout* package (i.e. modeling of count time series following glm), because it is a flexible class of models which can describe serial correlation in a parsimonious way



2° Phase: Model Building

Cumulative Analysis 2

Excluded

- State specific constants (Population, Healthcare and Testing facilities)
- Positive and Negative swabs

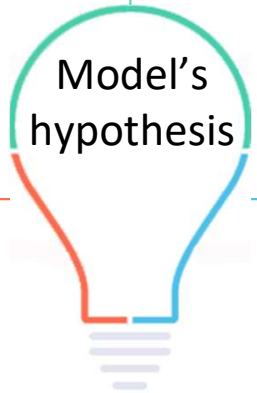
GLM poisson

- Cumulative count values
- Range $[0, +\infty]$

Covariates

- Previous confirmed cases
- Mean of past 14 confirmed cases
- Total Sample
- Previous daily confirmed cases
- Previous Cured and Deaths

Model's hypothesis



Legend

- λ_t : estimated mean condition on previous process history

$$Cumulative\ Confirmed_t \sim Poisson(\lambda_t)$$

$$\log(\lambda_t) = \beta_0 + \beta_1 \cdot Cumulative\ Confirmed_{t-1} + \alpha \cdot \log(\lambda_{t-14}) + \eta_i \cdot Cov_{i,t}$$

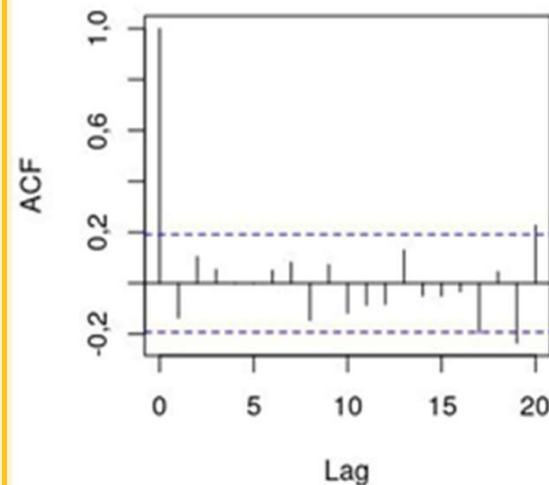


2° Phase: Model Assessment

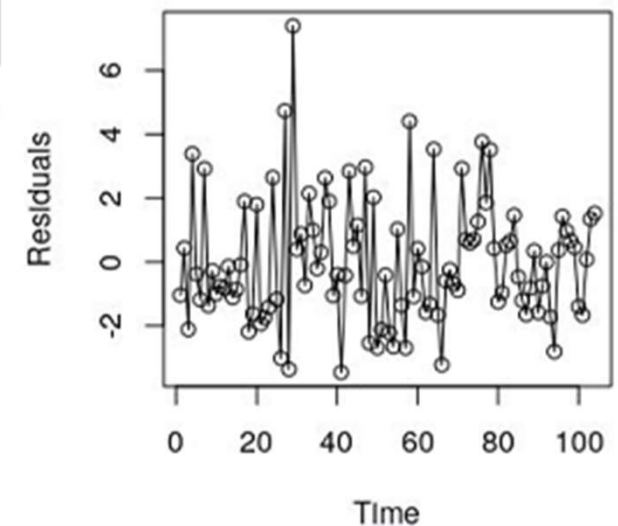
Cumulative Analysis 2

- Diagnostics ACF and Residuals (Maharashtra)
- To assess a model we checked the residuals and we tried to observe not auto-correlated, random residuals

ACF of Pearson residuals



Pearson residuals over time



2° Phase: Model Assessment

Cumulative Analysis 2

- We choose the model which has lowest MSE on both train and test sets
- Information criteria were excluded because of small and discording differences

MODELS (Maharashtra)		TOT MSE
M1	$\beta_0 + \beta_1 \cdot y_{t-1} + \alpha \cdot \lambda_{t-14} + \eta_1 \cdot \text{Tot Samples} + \eta_2 \cdot \text{Yest Daily Confirmed} + \eta_3 \cdot \text{Yest Cured} + \eta_4 \cdot \text{Yest Death}$	1247406
M2	$\beta_0 + \beta_1 \cdot y_{t-1} + \alpha \cdot \lambda_{t-14} + \eta_1 \cdot \text{Tot Samples} + \eta_2 \cdot \text{Yest Daily Confirmed} + \eta_3 \cdot \text{Yest Cured}$	151067
M3	$\beta_0 + \beta_1 \cdot y_{t-1} + \alpha \cdot \lambda_{t-14} + \eta_1 \cdot \text{Tot Samples} + \eta_2 \cdot \text{Yest Daily Confirmed}$	98448
M4	$\beta_0 + \beta_1 \cdot y_{t-1} + \alpha \cdot \lambda_{t-14} + \eta_1 \cdot \text{Tot Samples}$	86735



2° Phase: Model Assessment

Cumulative Analysis 2

	Yest Cured	Yest Death	Yest Daily Confirmed	Tot Samples	TOT MSE
Gujarat	-	-	X	X	9576
Chhattisgarh	-	-	-	X	13179
Jharkhand	X	-	X	X	2613
Odisha	-	-	X	X	425
Maharashtra	-	-	-	X	86736
West Bengal	X	X	X	X	9274
Madhya Pradesh	-	-	X	X	19415



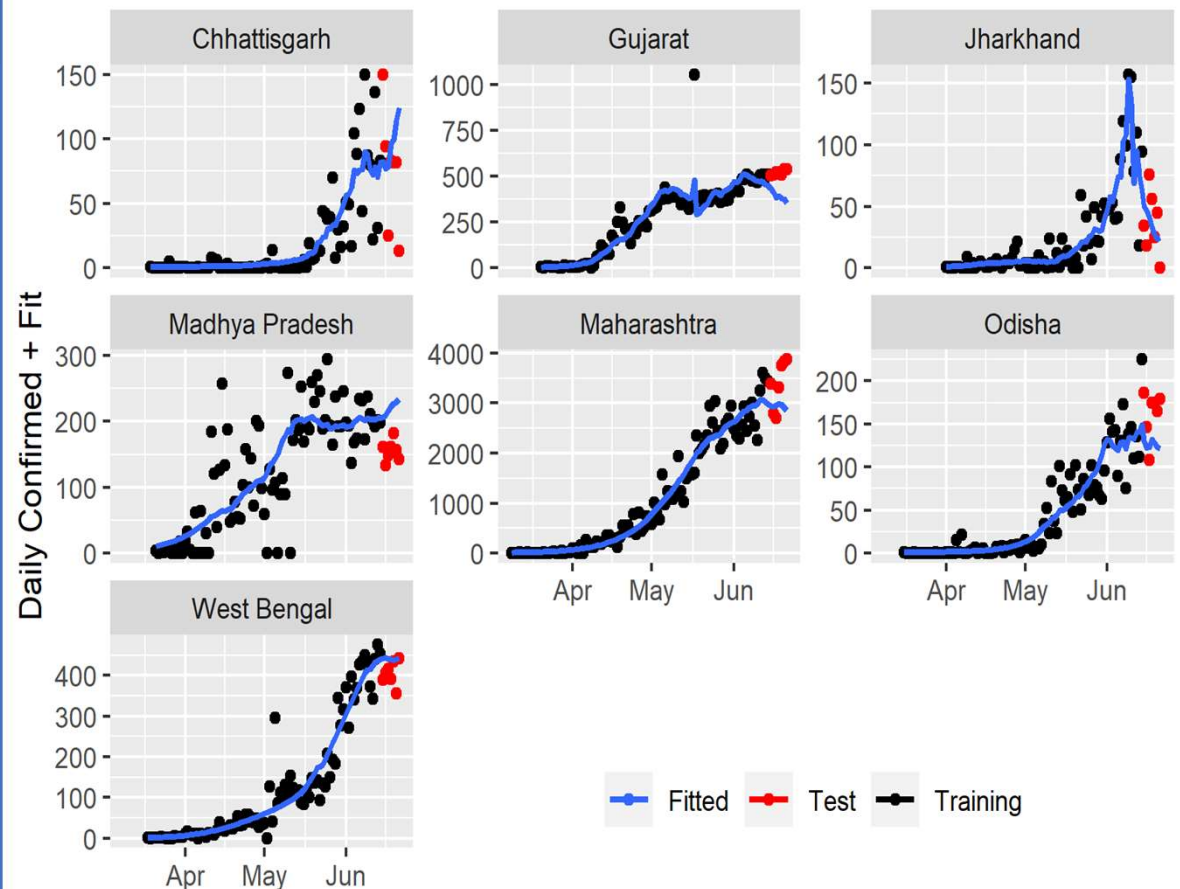
3° PHASE

- Prediction
- Evaluation

3° Phase: Prediction

Daily Analysis

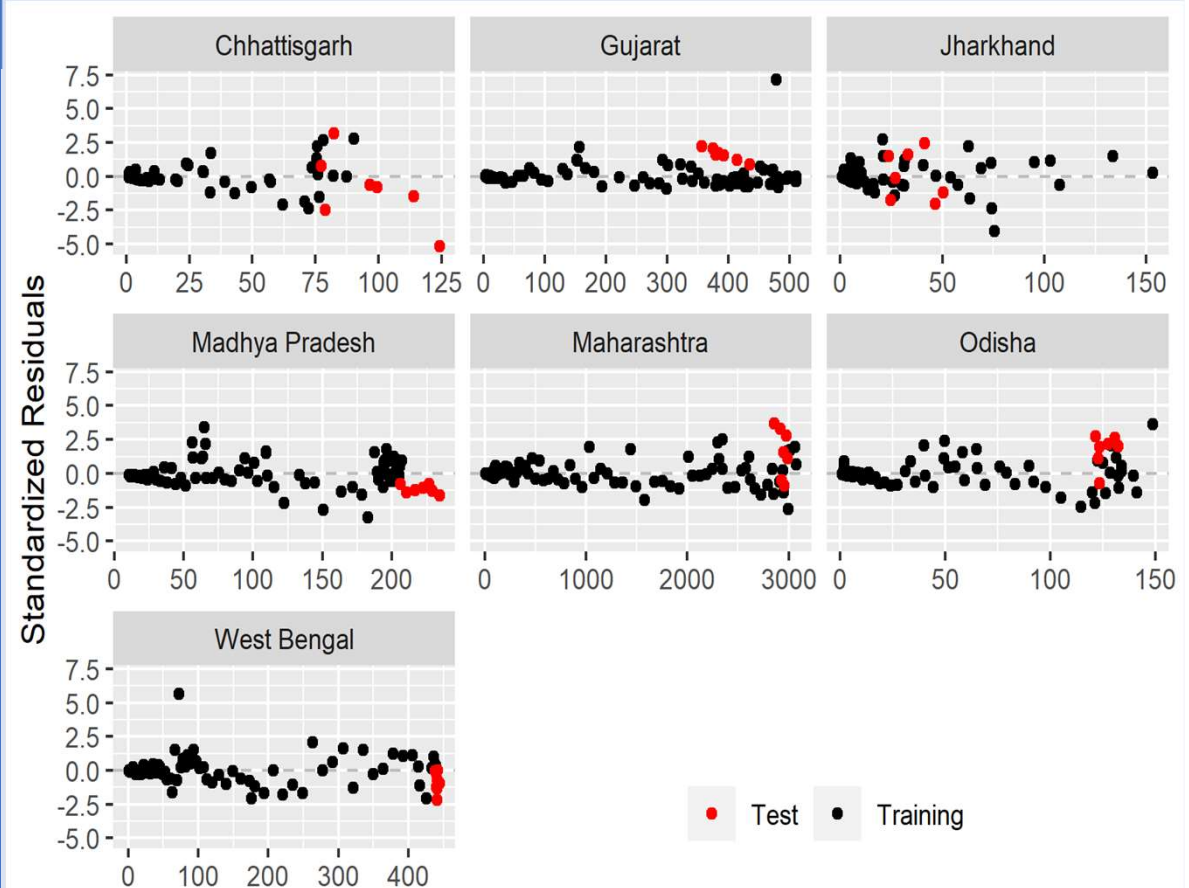
- Final predictive plot by using the selected models
- For some states the observations are very noisy
- Models fit well less noisy data



3° Phase: Evaluation

Daily Analysis

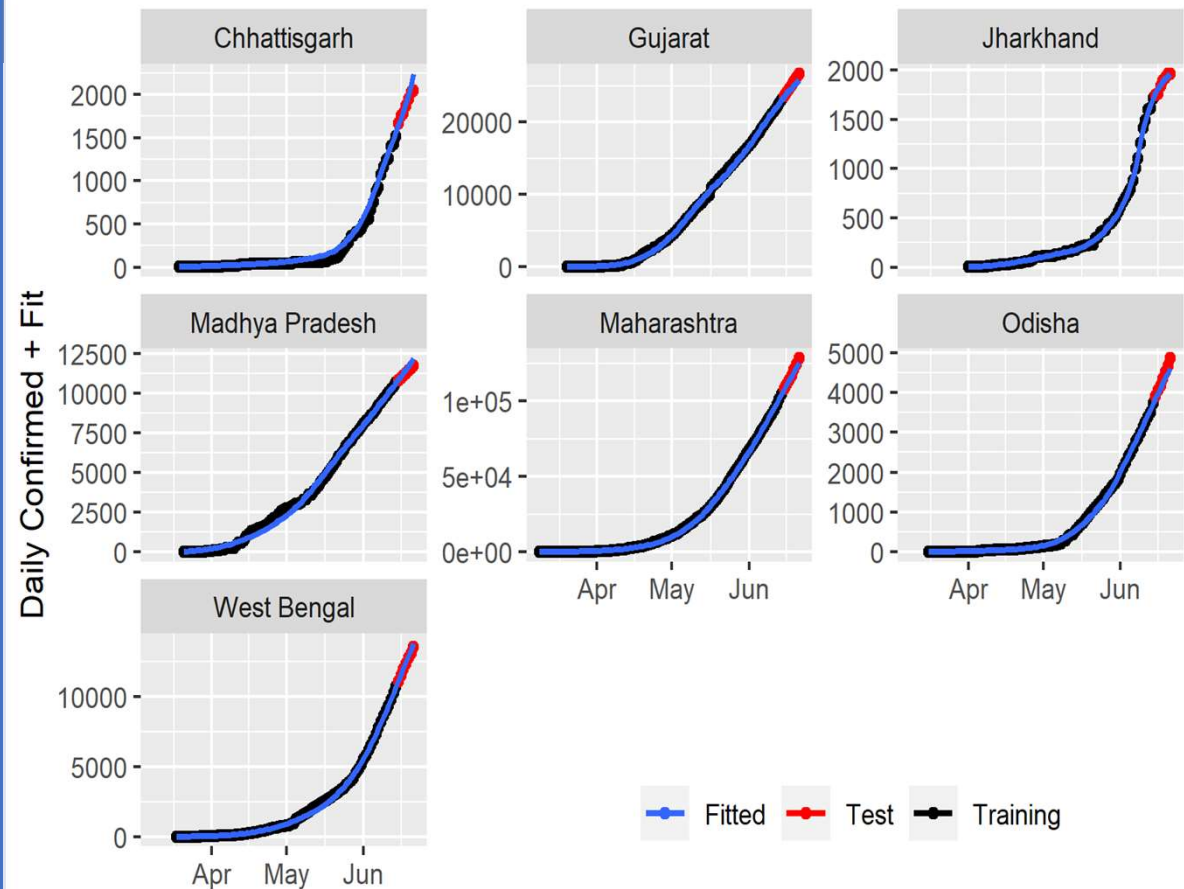
- Residuals plot for each state
- Residuals distributions show no systematic pattern
- Heteroskedasticity is observed but less than in Poisson case



3° Phase: Prediction

Cumulative Analysis 1

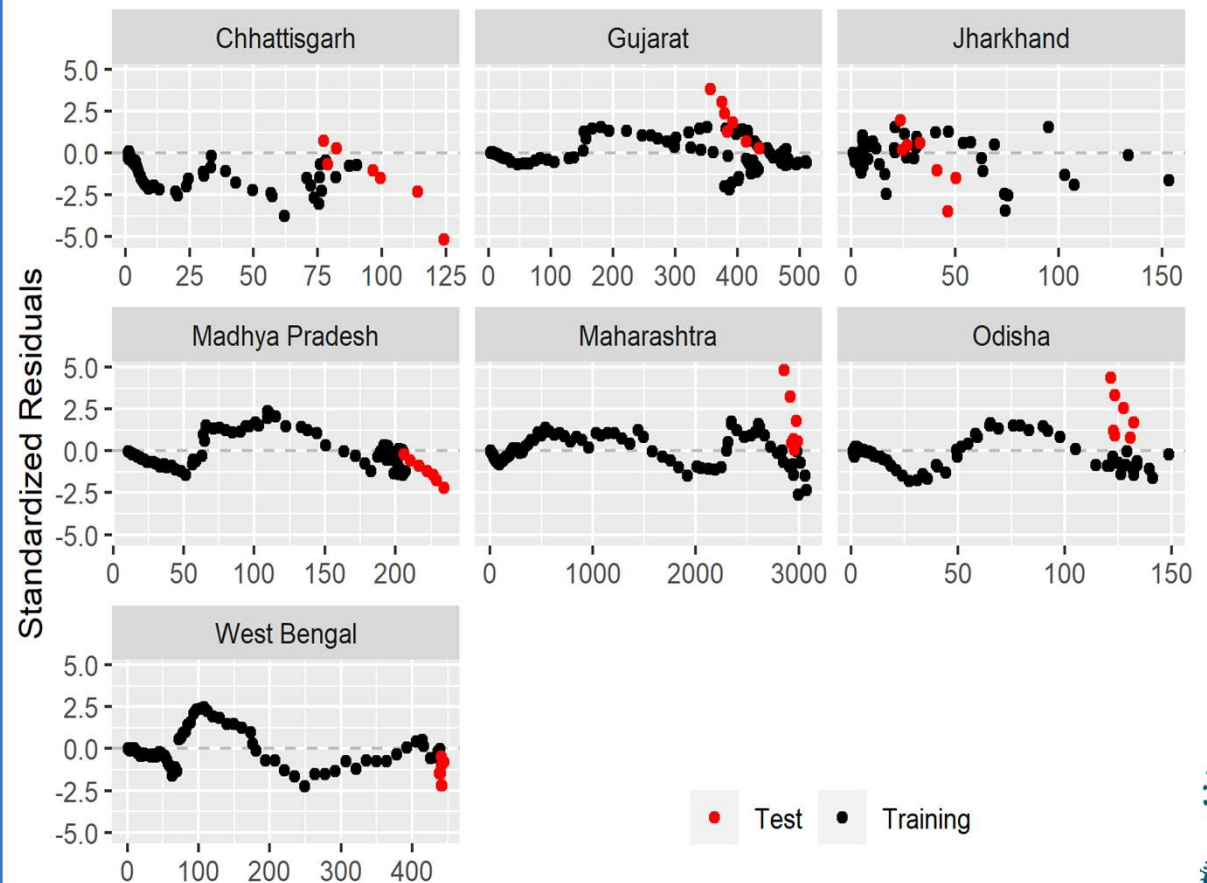
- Final cumulative predictive plot by using the Daily Model
- Apparently good fit on data



3° Phase: Evaluation

Cumulative Analysis 1

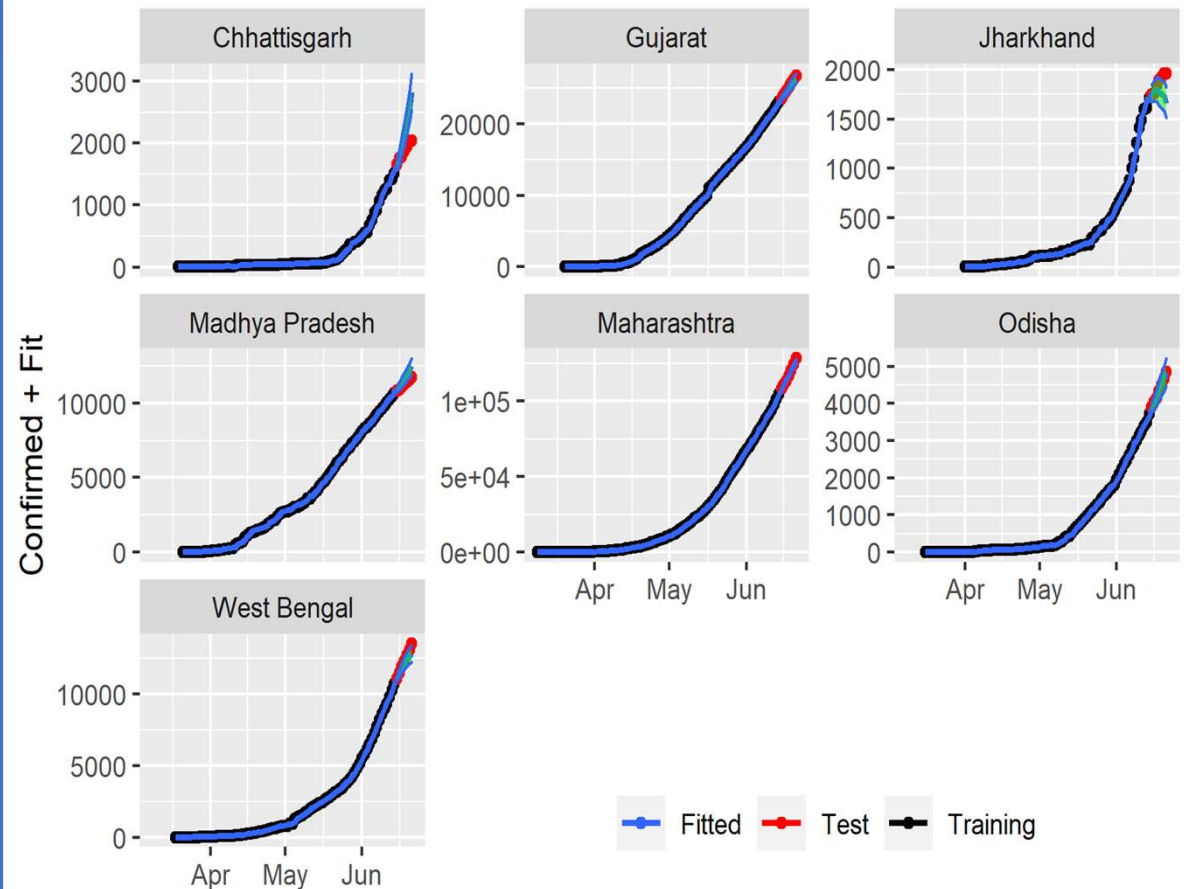
- Standardized residuals vs fitted values
- Residuals performance is not satisfying and shows systematic behaviour



3° Phase: Prediction

Cumulative Analysis 2

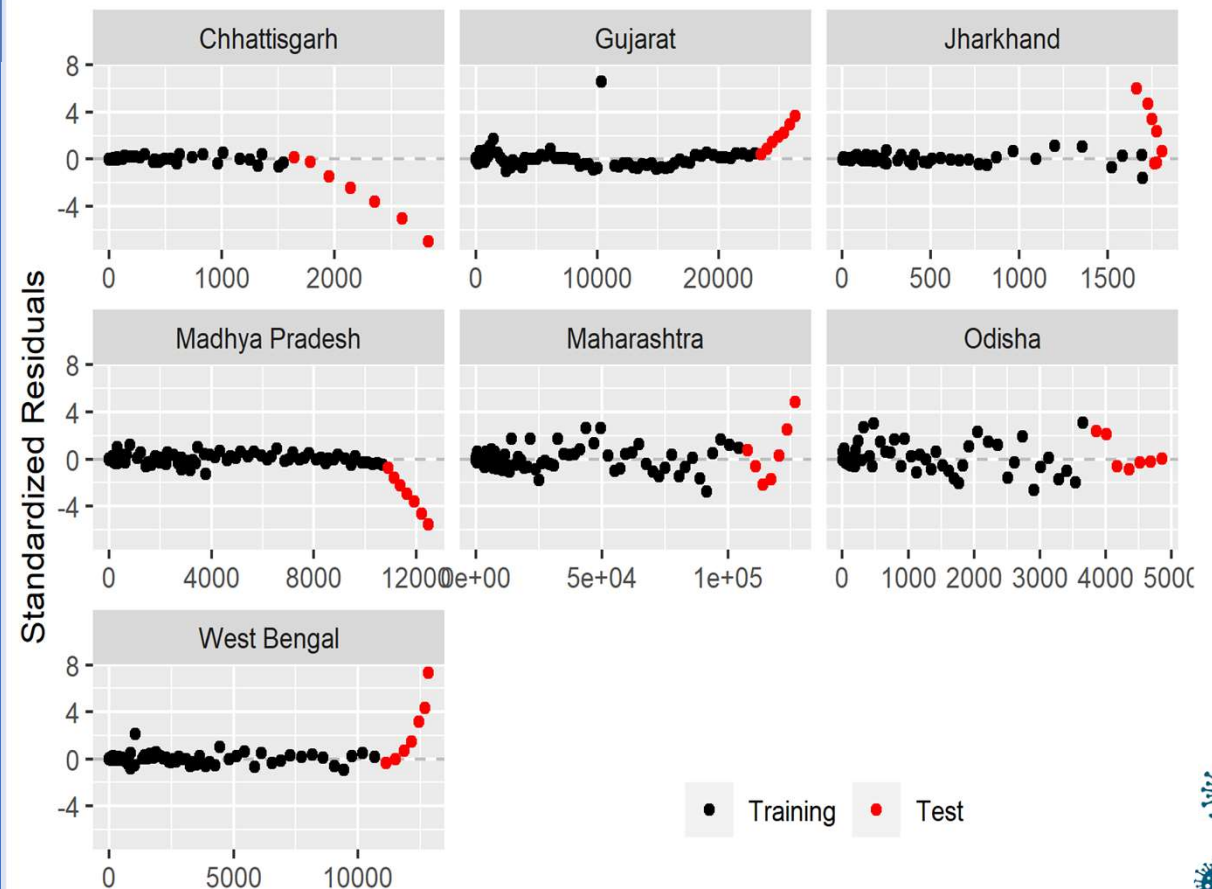
- Final predictive plot by using the selected models
- Chhattisgarh and Jharkhand show an aberrant behaviour on test data



3° Phase: Evaluation

Cumulative Analysis 2

- Standardized residuals vs predicted values
- Most of the states show a trending behaviour on test



CONCLUSION

- Comments
- Next steps

Conclusion: Comments



PROS

- Residuals distributions in daily models show no systematic pattern
- Gives acceptable predictions for spread and noisy data



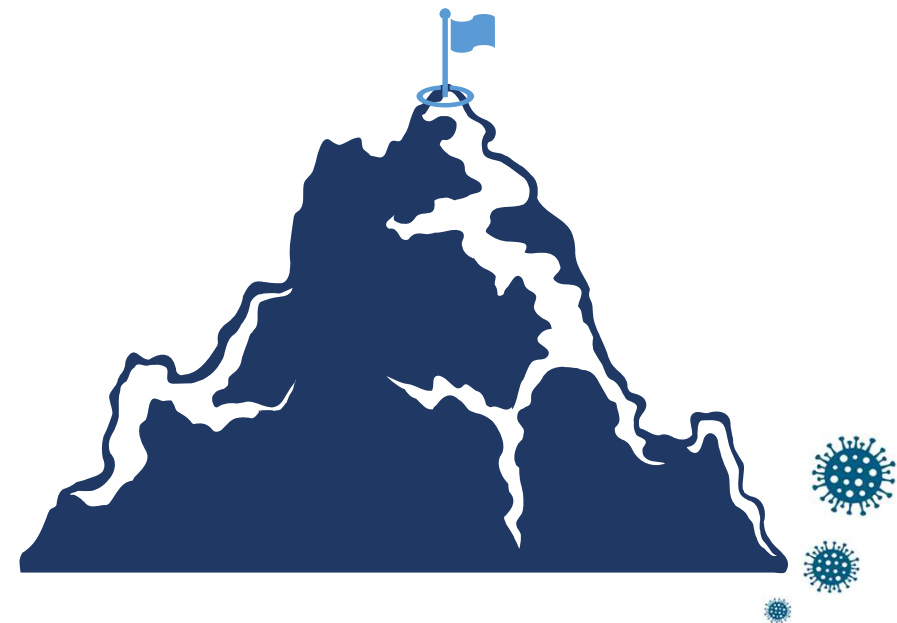
CONS

- Need to predict covariates for future predictions
- Cumulative prediction from daily model shows deterministic residuals pattern



Conclusion: Next steps

- Study can be extended by using multilevel / hierarchical model instead of choosing different models for each state
- Bayesian models can be considered to combine prior information with data
- Other models such as logistic or Gompertz Curve can be tried especially for cumulative part



References

- Leonardo Egidi, “Covid-19 spreading outbreak – Italy”, <https://www.leonardoegidi.com/covid-19>
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- Kaggle, “COVID-19 in India”, https://www.kaggle.com/sudalairajkumar/covid19-in-india?select=covid_19_india.csv





THANK YOU
FOR YOUR ATTENTION

Michele Rispoli, Eros Fabrici, Dogan Demirbilek, Pietro Morichetti