

Mathematics

Determinants

Q1 For a 2×2 matrix $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$, the determinant $|A|$ is calculated as
 (A) $ad + bc$ (B) $ac - bd$
 (C) $ad - bc$ (D) $bc - ad$

Q2 The value of the determinant of the matrix

$$A = \begin{bmatrix} 2 & -1 \\ 3 & -5 \end{bmatrix} \text{ is equal to}$$

- (A) 7 (B) -7
 (C) -8 (D) 8

Q3 The value of the determinant of the matrix $A = \begin{bmatrix} 1 & 2 \\ -5 & 1 \end{bmatrix}$ is equal to

- (A) -5 (B) 5
 (C) 10 (D) -10

Q4 The value of $\begin{vmatrix} \sin \theta & -\cos \theta \\ \cos \theta & \sin \theta \end{vmatrix}$ is equal to

- (A) 0 (B) -1
 (C) 1 (D) 2

Q5 If $\begin{vmatrix} k & -2 \\ 5 & 7 \end{vmatrix} = \begin{vmatrix} 1 & -1 \\ 2 & 3 \end{vmatrix}$, then k is

- (A) $\frac{5}{7}$ (B) $-\frac{5}{7}$
 (C) $-\frac{3}{2}$ (D) $\frac{3}{2}$

Q6 The value of the determinant $\begin{vmatrix} 6 & 7 & 8 \\ 18 & 21 & 24 \\ 5 & -6 & 2 \end{vmatrix}$

is

- (A) 0 (B) 4
 (C) -4 (D) 1

Q7 The value of the determinant $\begin{vmatrix} 14 & 8 & 11 \\ 6 & 5 & 6 \\ 8 & 3 & 5 \end{vmatrix}$ is

- (A) 0 (B) 5
 (C) 15 (D) 75

Q8 If $\begin{vmatrix} \alpha & 3 & 4 \\ 1 & 2 & 1 \\ 1 & 4 & 1 \end{vmatrix} = 0$, then the value of α is

- (A) 1 (B) 2
 (C) 3 (D) 4

Q9 If $A = \begin{bmatrix} 2 & -5 \\ 3 & 7 \end{bmatrix}$, then the value of $|2A|$ is equal to

- (A) 117 (B) 116
 (C) 115 (D) 118

Q10 If $|A| = 20$, then the value of $|3A|$ is equal to (order of matrix A is 3)

- (A) 680 (B) 580
 (C) 640 (D) 540



Answer Key

Q1 C
Q2 B
Q3 A
Q4 C
Q5 B

Q6 A
Q7 A
Q8 D
Q9 B
Q10 D



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Hints & Solutions

Note: scan the QR code to watch video solution

Q1 Text Solution:

This is the standard formula for a 2×2 determinant.

i.e. $|A| = ad - bc$

Video Solution:



Q2 Text Solution:

$$\begin{aligned}|A| &= \begin{vmatrix} 2 & -1 \\ 3 & -5 \end{vmatrix} \\ &= 2 \times (-5) - (-1) \times (3) \\ &= -10 + 3 \\ &= -7\end{aligned}$$

Video Solution:



Q3 Text Solution:

Determinant of a matrix whose order is 1×1 is the element of matrix itself.

i.e. If $A = [a]$ then $|A| = a$

\therefore Determinant of the given matrix $A = -5$

Video Solution:



Q4 Text Solution:

$$\begin{vmatrix} \sin \theta & -\cos \theta \\ \cos \theta & \sin \theta \end{vmatrix} = \sin^2 \theta - (-\cos^2 \theta)$$

$$\begin{aligned}&= \sin^2 \theta + \cos^2 \theta \\ &= 1\end{aligned}$$

Video Solution:



Q5 Text Solution:

$$\begin{aligned}\begin{vmatrix} k & -2 \\ 5 & 7 \end{vmatrix} &= \begin{vmatrix} 1 & -1 \\ 2 & 3 \end{vmatrix} \\ \Rightarrow 7k - (5)(-2) &= 1 \times 3 - (2)(-1) \\ \Rightarrow 7k + 10 &= 3 + 2 \\ \Rightarrow 7k &= -5 \\ \Rightarrow k &= \frac{-5}{7}\end{aligned}$$

Video Solution:



Q6 Text Solution:

$$\begin{aligned}\begin{vmatrix} 6 & 7 & 8 \\ 18 & 21 & 24 \\ 5 & -6 & 2 \end{vmatrix} &= 6 \begin{vmatrix} 21 & 24 \\ -6 & 2 \end{vmatrix} - 7 \begin{vmatrix} 18 & 24 \\ 5 & 2 \end{vmatrix} \\ &+ 8 \begin{vmatrix} 18 & 21 \\ 5 & -6 \end{vmatrix} \\ &= 6[42 + 144] - 7(36 - 120) \\ &+ 8(-108 - 105) \\ &= 1116 - 7(-84) + 8 \times (-213) \\ &= 1116 + 588 - 1704 \\ &= 1704 - 1704 = 0\end{aligned}$$

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Q7 Text Solution:

$$\begin{vmatrix} 14 & 8 & 11 \\ 6 & 5 & 6 \\ 8 & 3 & 5 \end{vmatrix} = 14 \begin{vmatrix} 5 & 6 \\ 3 & 5 \end{vmatrix} - 8 \begin{vmatrix} 6 & 6 \\ 8 & 5 \end{vmatrix}$$

$$+ 11 \begin{vmatrix} 6 & 5 \\ 8 & 3 \end{vmatrix}$$

$$= 14(25 - 18) - 8(30 - 48)$$

$$+ 11(18 - 40)$$

$$= 14 \times 7 - 8 \times (-18) + 11(-22)$$

$$= 98 + 144 - 242$$

$$= 242 - 242 = 0$$

Video Solution:



Q8 Text Solution:

$$\begin{vmatrix} \alpha & 3 & 4 \\ 1 & 2 & 1 \\ 1 & 4 & 1 \end{vmatrix} = 0$$

$$\Rightarrow \alpha(2 - 4) - 3(1 - 1) + 4(4 - 2) = 0$$

$$\Rightarrow -2\alpha + 8 = 0$$

$$\Rightarrow \alpha = 4$$

Video Solution:



Q9 Text Solution:

$$|A| = \begin{vmatrix} 2 & -5 \\ 3 & 7 \end{vmatrix} = 14 - (-15) = 14$$

$$+ 15 = 29$$

As $|kA| = k^n |A|$ where n is order of A

$$\therefore |2A| = 2^2 |A| = 4 \times 29 = 116$$

Video Solution:



Q10 Text Solution:

As $|kA| = k^n |A|$ where n is order of A

$$\therefore |3A| = 3^3 |A| = 27 \times 20 = 540$$

Video Solution:



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