

Matrices

Q1 If $A = \begin{bmatrix} 1 & 2 & 3 \\ 9 & 10 & 11 \end{bmatrix}$ and $B = \begin{bmatrix} 0 & 5 & 0 \\ 5 & 0 & 5 \end{bmatrix}$, then find $A + B$.

(A) $A + B = \begin{bmatrix} 1 & 7 & 3 \\ 11 & 10 & 16 \end{bmatrix}$ (B) $A + B = \begin{bmatrix} 1 & 7 & 3 \\ 14 & 11 & 13 \end{bmatrix}$

(C) $A + B = \begin{bmatrix} 1 & 7 & 3 \\ 14 & 10 & 16 \end{bmatrix}$ (D) $A + B = \begin{bmatrix} 1 & 5 & 3 \\ 14 & 10 & 16 \end{bmatrix}$

Q2 If $A + B = \begin{bmatrix} 6 & 7 \\ 5 & 0 \end{bmatrix}$ and $A = \begin{bmatrix} 2 & 5 \\ 1 & -1 \end{bmatrix}$. Find the matrix B.

(A) $B = \begin{bmatrix} 4 & 1 \\ 2 & 4 \end{bmatrix}$ (B) $B = \begin{bmatrix} 4 & 2 \\ 4 & 1 \end{bmatrix}$

(C) $B = \begin{bmatrix} 4 & 1 \\ 4 & 2 \end{bmatrix}$ (D) $B = \begin{bmatrix} 4 & 4 \\ 4 & 2 \end{bmatrix}$

Q3 Find AB if $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 5 \\ 3 & 2 \end{bmatrix}$

(A) $AB = \begin{bmatrix} 15 & 23 \\ 9 & 7 \end{bmatrix}$ (B) $AB = \begin{bmatrix} 9 & 7 \\ 23 & 15 \end{bmatrix}$

(C) $AB = \begin{bmatrix} 7 & 9 \\ 15 & 23 \end{bmatrix}$ (D) $AB = \begin{bmatrix} 7 & 9 \\ 23 & 15 \end{bmatrix}$

Q4 If A and B are matrices such that AB is defined, which of the following must be true?

(A) Number of columns in A = number of rows in B

(B) Number of rows in A = number of rows in B

(C) Number of columns in B = number of rows in A

(D) Number of rows in A = number of columns in B

Q5 If $A = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$, then what is A^3 equal to?

(A) $\begin{bmatrix} \cos 3\theta & \sin 3\theta \\ -\sin 3\theta & \cos 3\theta \end{bmatrix}$

(B) $\begin{bmatrix} \cos^3 \theta & \sin^3 \theta \\ -\sin^3 \theta & \cos^3 \theta \end{bmatrix}$

(C) $\begin{bmatrix} \cos 3\theta & -\sin 3\theta \\ \sin 3\theta & \cos 3\theta \end{bmatrix}$

(D) $\begin{bmatrix} \cos^3 \theta & -\sin^3 \theta \\ \sin^3 \theta & \cos^3 \theta \end{bmatrix}$

Q6 If $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$, then the value of A^4 is

(A) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ (B) $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$

(C) $\begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$ (D) $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$

Q7 Consider the following in respect of the matrix

$$A = \begin{pmatrix} -1 & 1 \\ 1 & -1 \end{pmatrix} :$$

1. $A^2 = -A$

2. $A^3 = 4A$

Which of the above is/are correct?

(A) 1 only

(B) 2 only

(C) Both 1 and 2

(D) Neither 1 or 2

Q8 If $X = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$, $B = \begin{bmatrix} 5 & 2 \\ -2 & 1 \end{bmatrix}$ and

$A = \begin{bmatrix} p & q \\ r & s \end{bmatrix}$ satisfy the equation $AX = B$, then

the matrix A is equal to

(A) $\begin{bmatrix} -7 & 26 \\ 1 & -5 \end{bmatrix}$

(B) $\begin{bmatrix} 7 & 26 \\ 4 & 17 \end{bmatrix}$



(C) $\begin{bmatrix} -7 & -4 \\ 26 & 13 \end{bmatrix}$

(D) $\begin{bmatrix} -7 & 26 \\ -6 & 23 \end{bmatrix}$

Q9 $A = \begin{bmatrix} x+y & y \\ 2x & x-y \end{bmatrix}$, $B = \begin{bmatrix} 2 \\ -1 \end{bmatrix}$ and

$C = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$

If $AB = C$, then what is A^2 equal to?

(A) $\begin{bmatrix} 6 & -10 \\ 4 & 26 \end{bmatrix}$

(B) $\begin{bmatrix} -10 & 5 \\ 4 & 24 \end{bmatrix}$

(C) $\begin{bmatrix} -5 & -6 \\ -4 & -20 \end{bmatrix}$

(D) $\begin{bmatrix} -5 & -7 \\ -5 & 20 \end{bmatrix}$

Q10 If $A = \begin{pmatrix} 4 & x+2 \\ 2x-3 & x+1 \end{pmatrix}$ is symmetric, then what is x equal to?

(A) 2

(B) 3

(C) -1

(D) 5



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Answer Key

Q1 C
Q2 B
Q3 C
Q4 A
Q5 A

Q6 A
Q7 B
Q8 A
Q9 A
Q10 D



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Hints & Solutions

Note: scan the QR code to watch video solution

Q1 Text Solution:

Given that, $A = \begin{bmatrix} 1 & 2 & 3 \\ 9 & 10 & 11 \end{bmatrix}$ and

$$B = \begin{bmatrix} 0 & 5 & 0 \\ 5 & 0 & 5 \end{bmatrix}$$

$$\begin{aligned} \text{Then } A + B &= \begin{bmatrix} 1+0 & 2+5 & 3+0 \\ 9+5 & 10+0 & 11+5 \end{bmatrix} \\ &= \begin{bmatrix} 1 & 7 & 3 \\ 14 & 10 & 16 \end{bmatrix} \end{aligned}$$

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Q2 Text Solution:

Given that, $A + B = \begin{bmatrix} 6 & 7 \\ 5 & 0 \end{bmatrix}$ and

$$A = \begin{bmatrix} 2 & 5 \\ 1 & -1 \end{bmatrix}$$

$$\Rightarrow B = (A + B) - A = \begin{bmatrix} 6 & 7 \\ 5 & 0 \end{bmatrix}$$

$$- \begin{bmatrix} 2 & 5 \\ 1 & -1 \end{bmatrix}$$

$$B = \begin{bmatrix} 4 & 2 \\ 4 & 1 \end{bmatrix}$$

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Q3 Text Solution:

Given that, $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 5 \\ 3 & 2 \end{bmatrix}$

$$\begin{aligned} \text{Then, } AB &= \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 1 & 5 \\ 3 & 2 \end{bmatrix} \\ &= \begin{bmatrix} 1 \times 1 + 2 \times 3 & 1 \times 5 + 2 \times 2 \\ 3 \times 1 + 4 \times 3 & 3 \times 5 + 4 \times 2 \end{bmatrix} \\ &= \begin{bmatrix} 7 & 9 \\ 15 & 23 \end{bmatrix} \end{aligned}$$

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Q4 Text Solution:

Matrix multiplication AB is defined only when the number of columns of A = number of rows of B .

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Q5 Text Solution:

$$A = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$$

$$\text{We know, } A^n = \begin{bmatrix} \cos n\theta & \sin n\theta \\ -\sin n\theta & \cos n\theta \end{bmatrix}$$

$$\therefore A^3 = \begin{bmatrix} \cos 3\theta & \sin 3\theta \\ -\sin 3\theta & \cos 3\theta \end{bmatrix}$$

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Q6 Text Solution:

$$A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$A^4 = A^2 \cdot A^2$$

$$= \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

Video Solution:**Q7 Text Solution:**

$$A = \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$A \cdot A = \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -2 \\ -2 & 2 \end{bmatrix} = -2 \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$A^2 = -2A$$

$$A^2, A = -2 \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$= -2 \begin{bmatrix} 2 & -2 \\ -2 & 2 \end{bmatrix} = 4 \begin{bmatrix} -1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$A^3 = 4A$$

$$\text{Hence } A^2 \neq -A, A^3 = 4A$$

Video Solution:**Q8 Text Solution:**

$$X = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}, B = \begin{bmatrix} 5 & 2 \\ -2 & 1 \end{bmatrix} \text{ and}$$

$$A = \begin{bmatrix} p & q \\ r & s \end{bmatrix}$$

Now, $AX = B$

$$\begin{bmatrix} p & q \\ r & s \end{bmatrix} \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix} = \begin{bmatrix} 5 & 2 \\ -2 & 1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 3p + q & -4p - q \\ 3r + s & -4r - s \end{bmatrix} = \begin{bmatrix} 5 & 2 \\ -2 & 1 \end{bmatrix}$$

$$3p + q = 5 \dots (i)$$

$$-4p - q = 2 \dots (ii)$$

$$3r + s = -2 \dots (iii)$$

$$-4r - s = 1 \dots (iv)$$

From equations (i) and (ii), we get $-p = 7$

$$\therefore p = -7$$

$$\Rightarrow q = 5 - 3(-7)$$

$$q = 26$$

From

(iii) and (iv),

$$-r = -1$$

$$\therefore r = 1$$

$$\Rightarrow s = -2 - 3 = -5$$

$$\therefore s = -5$$

$$\text{Hence, } A = \begin{bmatrix} p & q \\ r & s \end{bmatrix} = \begin{bmatrix} -7 & 26 \\ 1 & -5 \end{bmatrix}$$

\therefore Option (A) is correct

Video Solution:**Q9 Text Solution:**

$$A = \begin{bmatrix} x+y & y \\ 2x & x-y \end{bmatrix}$$

$$B = \begin{bmatrix} 2 \\ -1 \end{bmatrix} \text{ and } C = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$

Here $AB = C$

$$\therefore \begin{bmatrix} x+y & y \\ 2x & x-y \end{bmatrix} \begin{bmatrix} 2 \\ -1 \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$



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$$\Rightarrow \begin{bmatrix} 2(x+y) & -y \\ 4x & -x+y \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$

$$2x + y = 3 \dots (i)$$

$$3x + y = 2 \dots (ii)$$

From equations (i) and (ii), we get $x = -1$ and $y = 5$

$$\therefore A = \begin{bmatrix} 4 & 5 \\ -2 & -6 \end{bmatrix}$$

$$\text{Now, } A^2 = \begin{bmatrix} 4 & 5 \\ -2 & -6 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ -2 & -6 \end{bmatrix}$$

$$= \begin{bmatrix} 16 - 10 & 20 - 30 \\ -8 + 12 & -10 + 36 \end{bmatrix} = \begin{bmatrix} 6 & -10 \\ 4 & 26 \end{bmatrix}$$

\therefore Option (A) is correct.

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Q10 Text Solution:

$$\therefore A = A'$$

$$\Rightarrow \begin{pmatrix} 4 & x+2 \\ 2x-3 & x+1 \end{pmatrix} = \begin{pmatrix} 4 & 2x-3 \\ x+2 & x+1 \end{pmatrix}$$

$$\Rightarrow 2x - 3 = x + 2$$

$$\therefore x = 5$$

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