

Relations and Functions

Q1 If $A = \{1, 2, 3\}$ and $R_1 = \{(1, 2), (3, 2), (1, 3)\}$, $R_2 = \{(1, 3), (3, 6), (2, 1), (1, 2)\}$ then:

- (A) R_1 is a relation and R_2 is not a relation on A
- (B) R_1 and R_2 both are relation on A
- (C) R_1 and R_2 both are not relation on A
- (D) None of these

Q2 Let R be a relation in the set N given by $R = \{(a, b) : a = b - 2, b > 6\}$. Then

- (A) (8, 7) R
- (B) (6, 8) R
- (C) (3, 8) R
- (D) (2, 4) R

Q3 If $R = \{(x, y) : x, y \in W, 2x + y = 5\}$. Then

- (A) $R = \{(\frac{5}{2}, 0), (2, 1), (\frac{3}{2}, 2), (\frac{1}{2}, 4), (0, 5)\}$
- (B) $R = \{(\frac{5}{2}, 0), (2, 1), (\frac{3}{2}, 2), (\frac{1}{2}, 4)\}$
- (C) $R = \{(0, 5), (1, 3), (2, 1)\}$
- (D) $R = \{(1, 2), (3, 1), (5, 0)\}$

Q4 The relation R defined on the set of natural numbers as $\{(a, b) : a \text{ differs from } b \text{ by } 3\}$, is given by

- (A) $\{(1, 4), (2, 5), (3, 6), \dots\}$
- (B) $\{(4, 1), (5, 2), (6, 3), \dots\}$
- (C) $\{(1, 3), (2, 6), (3, 9), \dots\}$
- (D) None of the above

Q5 Let $n(A) = m$ and $n(B) = n$. Then, the total number of non-empty relations that can be defined from A to B is

- (A) mn
- (B) $nm - 1$
- (C) $mn - 1$
- (D) $2mn - 1$

Q6 Two finite sets A and B have m and n elements respectively. If the total number of relation from A to B is 64, then the possible values of m and n can be

- (A) 1 and 5
- (B) 2 and 4
- (C) 2 and 3
- (D) 1 and 4

Q7 If a relation R is defined on the set Z of integers as follows $(a, b) \in R \Leftrightarrow a^2 + b^2 = 25$, then domain (R) is equal to

- (A) $\{3, 4, 5\}$
- (B) $\{0, 3, 4, 5\}$
- (C) $\{0, \pm 3, \pm 4, \pm 5\}$
- (D) None of these

Q8 Consider set $A = \{-1, 0, 1, 2, 3\}$ and $B = \{1, 2, 4, 5, 0\}$. $R = \{(a, b) : b - a = 1, a \in A, b \in B\}$, then domain of relation R is

- (A) $\{0, 1, 3\}$
- (B) $\{-1, 0, 1, 3\}$
- (C) $\{1, 2, 4, 0\}$
- (D) $\{1, 2, 4, 5, 0\}$

Q9 Let R be a relation in N defined by $R = \{(1 + x, 1 + x^2) : x \leq 5, x \in N\}$. Which of the following is false?

- (A) $R = \{(2, 2), (3, 5), (4, 10), (5, 17), (6, 25)\}$
- (B) Domain of R = $\{2, 3, 4, 5, 6\}$
- (C) Range of R = $\{2, 5, 10, 17, 26\}$
- (D) None of these

Q10 Let A be the set of first ten natural numbers and let R be a relation on A defined by $(x, y) \in R \Leftrightarrow x + 2y = 10$, i.e., $R = \{(x, y) : x \in A, y \in A \text{ and } x + 2y = 10\}$. Then the domain and range of R is

- (A) $\{2, 4, 6, 8\}, \{4, 3, 2, 1\}$ respectively
- (B) $\{4, 3, 2, 1\}, \{2, 4, 6, 8\}$ respectively
- (C) $\{1, 2, 3, 4\}, \{1, 2, 3, 4\}$ respectively
- (D) None of these



Answer Key

Q1 A
Q2 B
Q3 C
Q4 B
Q5 D

Q6 C
Q7 C
Q8 B
Q9 A
Q10 A



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Hints & Solutions

Note: scan the QR code to watch video solution

Q1 Text Solution:

$$A \times A =$$

$$\{(1, 1), (1, 2), (1, 3), (2, 1), (2, 2), (2, 3), (3, 1), (3, 2), (3, 3)\}$$

$\therefore R_1 \subset A \times A \therefore R_1$ is a relation on A.

As $(3, 6) \in R_2$ but $6 \notin A \therefore R_2 \not\subset A \times A$

$\therefore R_2$ is a relation on A.

Video Solution:



Q2 Text Solution:

Given, $R = \{(a, b) : a = b - 2, b > 6\}$

Since, $b > 6$, so $(2, 4) \notin R$

Also, $(3, 8) \notin R$ as $3 \neq 8 - 2$

and $(8, 7) \notin R$ as $8 \neq 7 - 2$

Now, for $(6, 8)$, we have

$8 > 6$ and $6 = 8 - 2$, which is true

$\therefore (6, 8) \in R$

Video Solution:



Q3 Text Solution:

For $x = 0, 2 \times 0 + y = 5 \Rightarrow y = 5 \in W$

For $x = 1, 2 \times 1 + y = 5 \Rightarrow y = 3 \in W$

For $x = 2, 2 \times 2 + y = 5 \Rightarrow y = 1 \in W$

For $x = 3, 2 \times 3 + y = 5 \Rightarrow y = -1 \notin W$

We stop here as for $x > 3$, y is not a whole number

$\therefore R = \{(0, 5), (1, 3), (2, 1)\}$

Video Solution:



Q4 Text Solution:

Given, $R = \{(a, b) : a - b = 3\} = \{(4, 1), (5, 2), (6, 3), \dots\}$

Video Solution:



Q5 Text Solution:

Given, $n(A) = m$ and $n(B) = n$

\therefore Total number of relations from A to B $= 2^{mn}$

\therefore Total number of non-empty relations from A to B $= 2^{mn} - 1$

Video Solution:



Q6 Text Solution:

Clearly, $n(A \times B) = n(A) \times n(B) = mn$

\therefore Total number of relation from A to B $= 2^{mn}$

Thus, we have $2^{mn} = 64 = 2^6$

$\Rightarrow mn = 6$

Hence, possible value of m and n are 2 and 3, respectively.

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**Q7 Text Solution:**

We have, $(a, b) \in R \Leftrightarrow a^2 + b^2 = 25$

$$\Rightarrow b = \pm\sqrt{25 - a^2}$$

Clearly, $a = 0 \Rightarrow b = \pm 5$

$$a = \pm 3 \Rightarrow b = \pm 4$$

$$a = \pm 4 \Rightarrow b = \pm 3$$

$$\text{and } a = \pm 5 \Rightarrow b = 0$$

Hence, domain $(R) = \{0, \pm 3, \pm 4, \pm 5\}$.

Video Solution:**Q8 Text Solution:**

$$\text{For } a = -1, b - (-1) = 1 \Rightarrow b = 0$$

$$\in B \quad \therefore (-1, 0) \in R$$

$$\text{For } a = 0, b - 0 = 1 \Rightarrow b = 1 \in B$$

$$\therefore (0, 1) \in R$$

$$\text{For } a = 1, b - 1 = 1 \Rightarrow b = 2 \in B$$

$$\therefore (1, 2) \in R$$

$$\text{For } a = 2, b - 2 = 1 \Rightarrow b = 3 \notin B$$

$$\therefore (2, 3) \notin R$$

$$\text{For } a = 3, b - 3 = 1 \Rightarrow b = 4 \in B$$

$$\therefore (3, 4) \in R$$

$$\therefore R = \{(-1, 0), (0, 1), (1, 2), (3, 4)\}$$

$$\therefore \text{Domain of } R = \{-1, 0, 1, 3\}$$

Video Solution:**Q9 Text Solution:**

$$\text{For } x = 1, 1 + x = 2 \text{ and } 1 + x^2 = 2$$

$$\therefore (2, 2) \in R$$

$$\text{For } x = 2, 1 + x = 3 \text{ and } 1 + x^2 = 5$$

$$\therefore (3, 5) \in R$$

$$\text{For } x = 3, 1 + x = 4 \text{ and } 1 + x^2 = 10$$

$$\therefore (4, 10) \in R$$

$$\text{For } x = 4, 1 + x = 5 \text{ and } 1 + x^2 = 17$$

$$\therefore (5, 17) \in R$$

$$\text{For } x = 5, 1 + x = 6 \text{ and } 1 + x^2 = 26$$

$$\therefore (6, 26) \in R$$

$$\therefore R$$

$$= \{(2, 2), (3, 5), (4, 10), (5, 17), (6, 26)\}$$

$$\Rightarrow \text{Domain of } R = \{2, 3, 4, 5, 6\}$$

$$\text{Range of } R = \{2, 5, 10, 17, 26\}$$

Video Solution:**Q10 Text Solution:**

$$\text{For } x = 1, 1 + 2y = 10 \Rightarrow y = \frac{9}{2} \notin A$$

$$\therefore (1, \frac{9}{2}) \notin R$$

$$\text{For } x = 2, 2 + 2y = 10 \Rightarrow y = 4 \in A$$

$$\therefore (2, 4) \in R$$

$$\text{For } x = 3, 3 + 2y = 10 \Rightarrow y = \frac{7}{2} \notin A$$

$$\therefore (3, \frac{7}{2}) \notin R$$

$$\text{For } x = 4, 4 + 2y = 10 \Rightarrow y = 3 \in A$$

$$\therefore (4, 3) \in R$$

$$\text{For } x = 5, 5 + 2y = 10 \Rightarrow y = \frac{5}{2} \notin A$$

$$\therefore (5, \frac{5}{2}) \notin R$$

$$\text{For } x = 6, 6 + 2y = 10 \Rightarrow y = 2 \in A$$

$$\therefore (6, 2) \in R$$

$$\text{For } x = 7, 7 + 2y = 10 \Rightarrow y = \frac{3}{2} \notin A$$

$$\therefore (7, \frac{3}{2}) \notin R$$



For $x = 8$, $8 + 2y = 10 \Rightarrow y = 1 \in A$

$\therefore (8, 1) \in R$

For $x = 9$, $9 + 2y = 10 \Rightarrow y = \frac{1}{2} \notin A$

$\therefore (9, \frac{1}{2}) \notin R$

For $x = 10$, $10 + 2y = 10 \Rightarrow y = 0$

$\notin A \therefore (10, 0) \notin R$

$\therefore R = \{(2, 4), (4, 3), (6, 2), (8, 1)\}$

\Rightarrow Domain of $R = \{2, 4, 6, 8\}$

Range of $R = \{4, 3, 2, 1\}$

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