

MATRICES

Q1 If $A = \begin{bmatrix} 2 & 3 \\ -1 & 4 \end{bmatrix}$, then $(A^T)^T$ is:

- (A) $\begin{bmatrix} 2 & -1 \\ 3 & 4 \end{bmatrix}$ (B) $\begin{bmatrix} 2 & 3 \\ -1 & 4 \end{bmatrix}$
 (C) $\begin{bmatrix} -1 & 2 \\ 4 & 3 \end{bmatrix}$ (D) None of these

Q2 If $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$, then A^T is:

- (A) $\begin{bmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{bmatrix}$ (B) $\begin{bmatrix} 1 & 2 \\ 4 & 5 \\ 3 & 6 \end{bmatrix}$
 (C) $\begin{bmatrix} 4 & 1 \\ 5 & 2 \\ 6 & 3 \end{bmatrix}$ (D) None of these

Q3 Let $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$. Find $(2A)^T$

- (A) $\begin{bmatrix} 2 & 6 \\ 4 & 8 \end{bmatrix}$ (B) $\begin{bmatrix} 2 & 4 \\ 6 & 8 \end{bmatrix}$
 (C) $\begin{bmatrix} 2 & 6 \\ 4 & 8 \end{bmatrix}$ (D) $\begin{bmatrix} 2 & 4 \\ 6 & 8 \end{bmatrix}$

Q4 For any two matrices A and B such that AB is defined, which is true?

- (A) $(AB)^T = A^T B^T$ (B) $(AB)^T = B^T A^T$
 (C) $(AB)^T = AB^T$ (D) $(AB)^T = BA^T$

Q5 The transpose of an upper triangular matrix is:

- (A) Diagonal
 (B) Lower triangular

(C) Skew-symmetric

(D) Symmetric

Q6 Which of the following is not true?

- (A) $(A^T)^T = A$ (B) $(AB)^T = A^T B^T$
 (C) $(A + B)^T = A^T + B^T$ (D) $(kA)^T = kA^T$

Q7 If $A^T = A$ and $B^T = -B$, then what is $(AB)^T$?

- (A) $B^T A^T = -BA$ (B) $B^T A^T = AB$
 (C) $A^T B^T = -AB$ (D) $B^T A^T = A^T B^T$

Q8 Let $A = BB^T + CC^T$, where

$$B = \begin{bmatrix} \cos \theta \\ \sin \theta \end{bmatrix}, C = \begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix}; \theta \in R. \text{ Then}$$

A is:

- (A) $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
 (B) $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
 (C) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
 (D) $\begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$

Q9 If $A = \begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix}$ and $A \text{ adj } A = AA^T$,

then $5a + b$ is equal to:

- (A) 13 (B) -1
 (C) 5 (D) 4



Answer Key

Q1 (B)
Q2 (A)
Q3 (A)
Q4 (B)
Q5 (B)

Q6 (B)
Q7 (A)
Q8 (C)
Q9 (C)



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Hints & Solutions

Note: scan the QR code to watch video solution

Q1 Text Solution:

We know that $(A^T)^T = A$.

So, the matrix remains the same. Hence, option B.

Video Solution:



Q2 Text Solution:

Transpose: Flip rows and columns

Row 1 \rightarrow Column 1: $[1, 2, 3] \rightarrow [1; 2; 3]$

Row 2 \rightarrow Column 2: $[4, 5, 6] \rightarrow [4; 5; 6]$

Video Solution:



Q3 Text Solution:

First compute $2A = \begin{bmatrix} 2 & 4 \\ 6 & 8 \end{bmatrix}$

Then transpose = same (since symmetric here)

Video Solution:



Q4 Text Solution:

Transpose of product rule:

$$(AB)^T = B^T A^T$$

Video Solution:



Q5 Text Solution:

Transpose flips rows and columns \rightarrow upper becomes lower triangular.

Video Solution:



Q6 Text Solution:

Correct is $(AB)^T = B^T A^T$, not $A^T B^T \rightarrow$ hence incorrect.

Video Solution:



Q7 Text Solution:

$$(AB)^T = B^T A^T = -BA = -BA$$

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**Q8 Text Solution:**

$$\begin{aligned}
A &= BB^T + CC^T \\
&= \begin{bmatrix} \cos \theta \\ \sin \theta \end{bmatrix} [\cos \theta \quad \sin \theta] + \begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix} [\sin \theta \quad -\cos \theta] \\
&= \begin{bmatrix} \cos^2 \theta & \cos \theta \cdot \sin \theta \\ \sin \theta \cdot \cos \theta & \sin^2 \theta \end{bmatrix} \\
&\quad + \begin{bmatrix} \sin^2 \theta & -\sin \theta \cdot \cos \theta \\ -\sin \theta \cdot \cos \theta & \cos^2 \theta \end{bmatrix} \\
&= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}
\end{aligned}$$

Video Solution:**Q9 Text Solution:**

Given, $A \cdot \text{adj } A = A \cdot A^T$

$$A = \begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix}, \text{adj } A = \begin{bmatrix} 2 & b \\ -3 & 5a \end{bmatrix},$$

$$A^T = \begin{bmatrix} 5a & 3 \\ -b & 2 \end{bmatrix}$$

$$A \cdot \text{adj } A = A \cdot A^T$$

$$\begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix} \begin{bmatrix} 2 & b \\ -3 & 5a \end{bmatrix} =$$

$$\begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix} \begin{bmatrix} 5a & 3 \\ -b & 2 \end{bmatrix}$$

$$\begin{bmatrix} 10a + 3b & 0 \\ 0 & 10a + 3b \end{bmatrix} =$$

$$\begin{bmatrix} 25a^2 + b^2 & 15a - 2b \\ 15a - 2b & 13 \end{bmatrix}$$

comparing both side, we get

$$15a - 2b = 0 \dots (i)$$

$$10a + 3b = 13 \dots (ii)$$

Solving two equation, we get the values of a & b

$$a = \frac{2}{5}, b = 3$$

Now,

$$5a + b = 5 \times \frac{2}{5} + 3 = 5$$

Video Solution: