Homework 1 - EEB590C

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EEB590C -Homework 1

Homework 1: Lectures 1-4

This assignment is due prior to class in week 6. You are to self-select and work in groups: 2-3 in a group. For the assignment below submit one R-script. Annotations via comments are highly encouraged. The script should run!

Assignment Instructions:

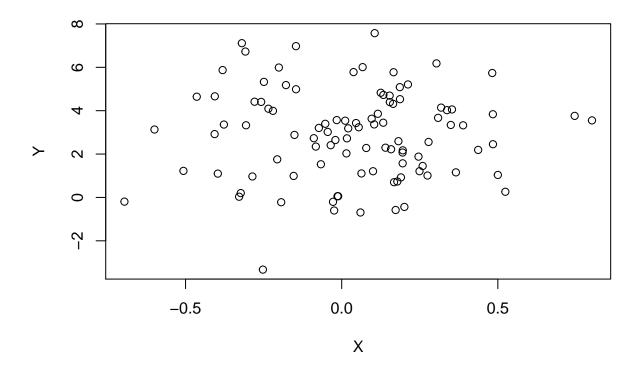
- 1: Select some form of linear model containing a single dependent variable (continuous) and at least 1 independent variable. Next, simulate two datasets: the first with no relationship between X & Y, and the second with some positive association between X & Y. Perform 100 simulations under each condition. Run the linear models on all datasets to confirm that on average, the patterns for condition 1 (no relationship) and condition 2 (some relationship) are met. (HINT: this requires determining an appropriate summary measure extracted from the linear model).
- 2: Devise a permutation procedure to evaluate the above linear model. Write code for this permutation procedure. Next, devise a SECOND implementation of the same permutation procedure (ie, code the procedure in a different manner). For a single dataset compare the two implementations for their computational performance. Summarize your findings via comments in the code (e.g., which approach was faster? Which components of the slower approach could be improved, etc.).

Homework Breakdown:

We selected lm as a linear model and we simulated two datasets: the first with no relationship between X amd Y, and the second with positive association between X and Y. Here we have the random uncorrelated data, sampling 100 datapoints with y and x from normal distributions.

```
# data set with no relationship between x & Y
random_corr_gen <- function(elements) {
    x1 <- rnorm(elements, mean = 0, sd = 0.3)
    y1 <- rnorm(elements, mean = 3, sd = 2)
    uncor_dataframe <- data.frame(x1, y1)
}
uncor_data <- random_corr_gen(100)
plot(uncor_data, main = "Uncorrelated Data", xlab = "X", ylab = "Y")</pre>
```

Uncorrelated Data



Here, we have the positively correlated, normally distributed, Y and X data generated using a correlation of 0.9.

```
# data set with positive association between x \ \ensuremath{\mathfrak{C}}\ Y
library(tidyverse)
## -- Attaching packages
                                                            ----- tidyverse 1.3.0 --
## v ggplot2 3.3.3
                        v purrr
                                   0.3.4
## v tibble 3.0.6
                        v dplyr
                                   1.0.4
## v tidyr
             1.1.2
                        v stringr 1.4.0
             1.4.0
## v readr
                        v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                      masks stats::lag()
pos_cor_gen <- function(elements, corr.val) {</pre>
    correlation_value <- corr.val</pre>
    x2 \leftarrow rnorm(elements, mean = 0, sd = 0.3)
    y2 <- (correlation_value) * (x2) + (rnorm(elements, mean = 1,</pre>
        sd = 0.2))
    cor_data <- data.frame(x2, y2)</pre>
    return(cor_data)
}
pos_cor_data <- pos_cor_gen(100, 0.9)</pre>
```

We then perform 100 simulations under each condition using the replicate function.

First we simulate 100 uncorrelated x and y dataframes and put it a list called uncor data sim.

```
# Random Uncorrelated Data List
uncor_data_sim <- replicate(100, random_corr_gen(100), simplify = FALSE)</pre>
```

Then we simulate 100 lists of the correlated data, called cor_data_sim.

```
# Random Correlated Data List
cor_data_sim <- replicate(100, pos_cor_gen(100, 0.9), simplify = FALSE)</pre>
```

We then run the linear model lm on the two datasets (uncorrelated and correlated) to confirm the typically the patterns for condition 1 (no relationship) and condition 2 (some relationship) are met.

Below is the linear model lm function applied to each list of x and y in the uncorrelated dataset. The summary of the linear model is saved to summary_ lm_uncor_tests .

```
# model 1 - uncorrelated
lm_uncor_tests <- lapply(uncor_data_sim, lm, formula = y1 ~ x1)
summary_lm_uncor_tests <- lapply(lm_uncor_tests, summary)
anova_lm_uncor_tests <- lapply(lm_uncor_tests, anova)</pre>
```

Of the 100 simulations, a grand total of ~ 97 simulations had a pvalue that was greater than 0.05, indicating that there is NOT a linear relationship between X and Y at a significance level of 0.05. Because we can't set a seed, the 97 simulations changes slightly every time, but remains about 90 simulations that have a pvalue greater than 0.05.

```
sum_pvalue_uncor_nonsig <- 0</pre>
sum_pvalue_uncor_sig <- 0</pre>
count_pvalue_uncor_nonsig <- 0</pre>
count_pvalue_uncor_sig <- 0</pre>
# sum up p-value for uncorrelated tests p-values less than
# 0.05 have a significant linear relationship p-values
# greater than 0.05 have a do not significant linear
# relationship
for (i in 1:length(anova_lm_uncor_tests)) {
    if (anova lm uncor tests[[i]][["Pr(>F)"]][1] > 0.05) {
        count_pvalue_uncor_nonsig <- count_pvalue_uncor_nonsig +</pre>
        sum_pvalue_uncor_nonsig <- sum_pvalue_uncor_nonsig +</pre>
            anova lm uncor tests[[i]][["Pr(>F)"]][1]
    } else {
        count_pvalue_uncor_sig <- count_pvalue_uncor_sig + 1</pre>
        # print(i)
        sum_pvalue_uncor_sig <- sum_pvalue_uncor_sig + anova_lm_uncor_tests[[i]][["Pr(>F)"]][1]
    }
}
average_pvalue_uncor_tests_nonsig <- sum_pvalue_uncor_nonsig/count_pvalue_uncor_nonsig
print(paste("Average pvalue greater than 0.05 for uncorrelated tests:",
    average pvalue uncor tests nonsig))
```

[1] "Average pvalue greater than 0.05 for uncorrelated tests: 0.541159480571145"

```
average_pvalue_uncor_tests_sig <- sum_pvalue_uncor_sig/count_pvalue_uncor_sig
print(paste("Average p-value less than 0.05 for uncorrelated tests:",
    average_pvalue_uncor_tests_sig))
## [1] "Average p-value less than 0.05 for uncorrelated tests: 0.0242839798485414"
average_pvalue_uncor_tests <- (sum_pvalue_uncor_nonsig + sum_pvalue_uncor_sig)/(count_pvalue_uncor_sig
    count_pvalue_uncor_nonsig)
print(paste("Average p-value for all uncorrelated tests:", average_pvalue_uncor_tests))
## [1] "Average p-value for all uncorrelated tests: 0.520484460542241"
# of 100 simulations, the count of that had a nonsignificant
# p-value
count_pvalue_uncor_nonsig
## [1] 96
# of 100 simulations, the count of that had a significant
# p-value
count_pvalue_uncor_sig
## [1] 4
Next is the linear model lm applied to each list of the positively correlated dataset.
# model 2 - positively correlated model
lm cor tests <- lapply(cor data sim, lm, formula = y2 ~ x2)</pre>
summary_lm_cor_tests <- lapply(lm_cor_tests, summary)</pre>
anova_lm_cor_tests <- lapply(lm_cor_tests, anova)</pre>
Of the 100 simulations, all 100 simulations have a pvalue that is less than 0.05, indicating that there is a
linear relationship between X and Y at a significance level of 0.05.
sum_pvalue_cor_nonsig <- 0</pre>
sum_pvalue_cor_sig <- 0</pre>
count_pvalue_cor_nonsig <- 0</pre>
count_pvalue_cor_sig <- 0</pre>
# sum up p-value for correlated tests p-values less than 0.05
# have a significant linear relationship p-values greater
# than 0.05 have a do not significant linear relationship
for (i in 1:length(anova lm cor tests)) {
    if (anova_lm_cor_tests[[i]][["Pr(>F)"]][1] > 0.05) {
        count_pvalue_cor_nonsig <- count_pvalue_cor_nonsig +</pre>
        sum_pvalue_cor_nonsig <- sum_pvalue_cor_nonsig + anova_lm_cor_tests[[i]][["Pr(>F)"]][1]
    } else {
        count_pvalue_cor_sig <- count_pvalue_cor_sig + 1</pre>
        sum_pvalue_cor_sig <- sum_pvalue_cor_sig + anova_lm_cor_tests[[i]][["Pr(>F)"]][1]
    }
}
average_pvalue_cor_tests_sig <- sum_pvalue_cor_sig/count_pvalue_cor_sig
print(paste("Average pvalue less than 0.05 for correlated tests:",
    average_pvalue_cor_tests_sig))
```

[1] "Average pvalue less than 0.05 for correlated tests: 1.32390585459262e-18"

```
average_pvalue_cor_tests_nonsig <- sum_pvalue_cor_nonsig/count_pvalue_cor_nonsig
print(paste("Average p-value greater than 0.05 for correlated tests:",
    average_pvalue_cor_tests_nonsig))
## [1] "Average p-value greater than 0.05 for correlated tests: NaN"
average_pvalue_cor_tests <- (sum_pvalue_cor_nonsig + sum_pvalue_cor_sig)/(count_pvalue_cor_sig +
    count_pvalue_cor_nonsig)
print(paste("Average p-value for all correlated tests:", average_pvalue_cor_tests))
## [1] "Average p-value for all correlated tests: 1.32390585459262e-18"
# of 100 simulations for the correlated data, the count of
# simulations with a nonsignificant p-value
count_pvalue_cor_nonsig
## [1] 0
# of 100 simulations, the count of simulations with a
# significant p-value
count_pvalue_cor_sig
## [1] 100
```

Question 2:

The first permutation procedure we used to evaluate the above linear model on the correlated data using the RRPP package.

```
# install.packages('RRPP')
library(RRPP)
ourdata <- rrpp.data.frame(pos_cor_data[, 2], pos_cor_data[,</pre>
    1])
model3 <- lm.rrpp(pos_cor_data[, 2] ~ pos_cor_data[, 1], iter = 999,</pre>
    print.progress = FALSE, data = ourdata)
anova(model3)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
                     Df
                             SS
                                    MS
                                           Rsq
                                                           Z Pr(>F)
## pos_cor_data[, 1] 1 8.6452 8.6452 0.67131 200.15 6.423 0.001 **
                     98 4.2329 0.0432 0.32869
## Residuals
## Total
                     99 12.8781
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Call: lm.rrpp(f1 = pos_cor_data[, 2] ~ pos_cor_data[, 1], iter = 999,
       data = ourdata, print.progress = FALSE)
```

Next, we devised a SECOND implementation of a permutation procedure. This time we will write a permutation from scratch for 999 iterations using a for loop. We set the observed data's f value to be one of the iterations.

```
pos_cor_lm <- anova(lm(pos_cor_data$y2 ~ pos_cor_data$x2))
f.obs <- pos_cor_lm$`F value`[[1]]
f.obs</pre>
```

[1] 200.1546

We then created a function for 999 permutations + our observed (1000 total). This function can later be called when comparing the time it takes for a for loop versus RRPP.

```
# Randomization function
permute_correlated_data <- function(correlated_data, permute_num,</pre>
    f.obs.reported) {
    f.rand.vec <- array(NA, (permute_num + 1))</pre>
    f.rand.vec[permute_num + 1] <- f.obs.reported</pre>
    for (i in 1:permute_num) {
        ### Shuffle Data
        permuted_cor_data <- sample(correlated_data$y2)</pre>
        ### Run analysis on random data
        permuted_pos_cor_lm <- anova(lm(permuted_cor_data ~ correlated_data$x2))</pre>
        f.rand.vec[i] <- permuted_pos_cor_lm$`F value`[[1]]</pre>
    } #end permute
    P.Ftest <- rank(f.rand.vec[permute_num + 1])/(permute_num +
        1)
    return(P.Ftest)
}
p_value_of_permuted_pos_data <- permute_correlated_data(pos_cor_data,</pre>
    999, f.obs)
p_value_of_permuted_pos_data
```

[1] 0.001

Below are the times of the two permutation methods. As you can see, RRPP is the superior method when simply comparing the time as well as ease of use. The time of RRPP permuting 999 iterations is reported in milliseconds (~ 156 milliseconds) while the permutation that was written out in a for loop yields results in terms of seconds (~ 1.866 seconds).

```
library(microbenchmark)
res <- microbenchmark(anova(lm.rrpp(pos_cor_data[, 2] ~ pos_cor_data[,
    1], iter = 999, print.progress = FALSE, data = ourdata)),
   times = 1) #using rrpp for permutation method
print(res)
## Unit: milliseconds
##
  anova(lm.rrpp(pos_cor_data[, 2] ~ pos_cor_data[, 1], iter = 999,
                                                                         print.progress = FALSE, data
                lq
                     mean median
                                       uq
                                               max neval
  173.582 173.582 173.582 173.582 173.582 173.582
res2 <- microbenchmark(permute_correlated_data(pos_cor_data,
   999, f.obs), times = 1)
print(res2) #second permutation method
```