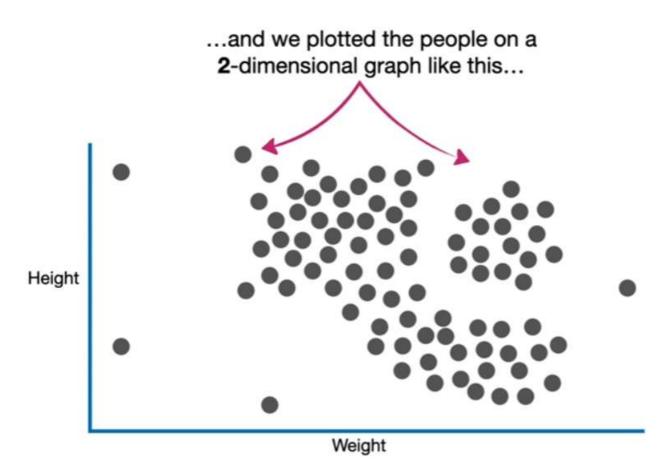
DB SCAN

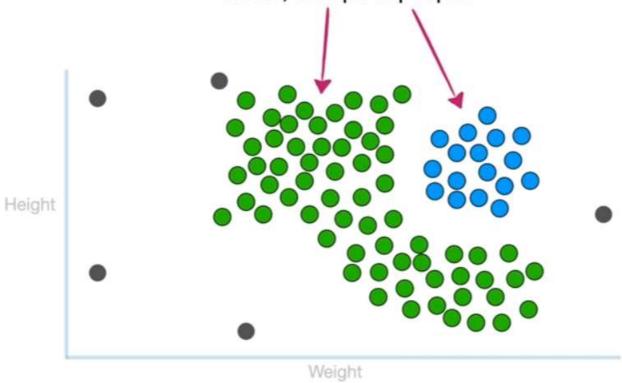
Some slides were adapted/taken from various sources, including Prof. Andrew Ng's Coursera Lectures, Stanford University, Prof. Kilian Q. Weinberger's lectures on Machine Learning, Cornell University, Prof. Sudeshna Sarkar's Lecture on Machine Learning, IIT Kharagpur, Prof. Bing Liu's lecture, University of Illinois at Chicago (UIC), University of Buffalo, CS231n: Convolutional Neural Networks for Visual Recognition lectures, Stanford University, Dr. Luis Serrano, Prof. Alexander Ihler, Dr. Josh Starmer and many more. We thankfully acknowledge them. Students are requested to use this material for their study only and NOT to distribute it.

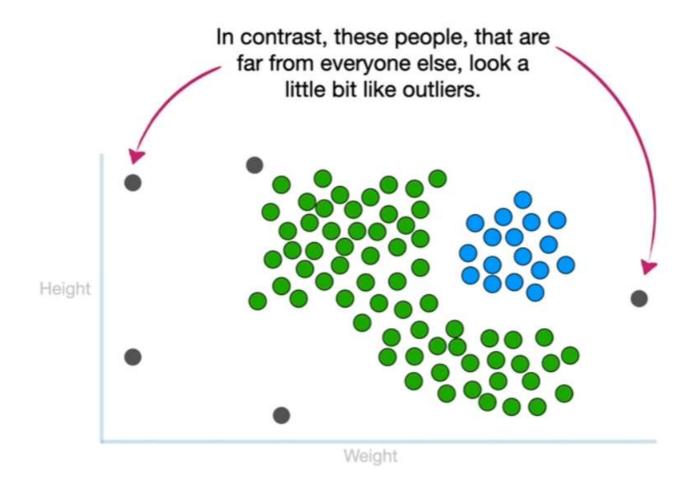
Now, imagine we collected **Weight** and **Height** measurements from a bunch of people...

*	Weight	Height
Person 1	56	150
Person 2	62	170
Person 3	71	168

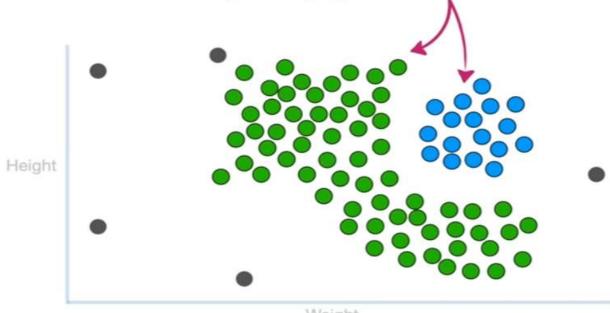


...by identifying two different, but relatively dense, clumps of people.



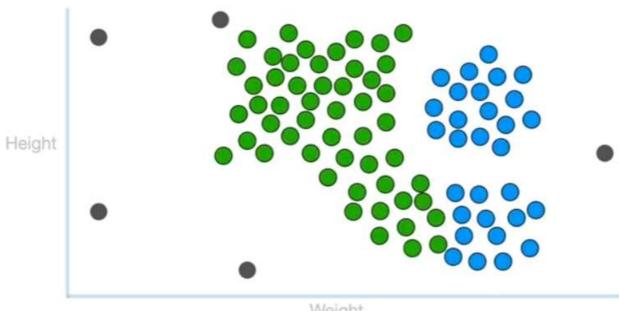


...a relatively standard clustering method like, **k-means clustering**, might have difficultly identifying these two clusters.

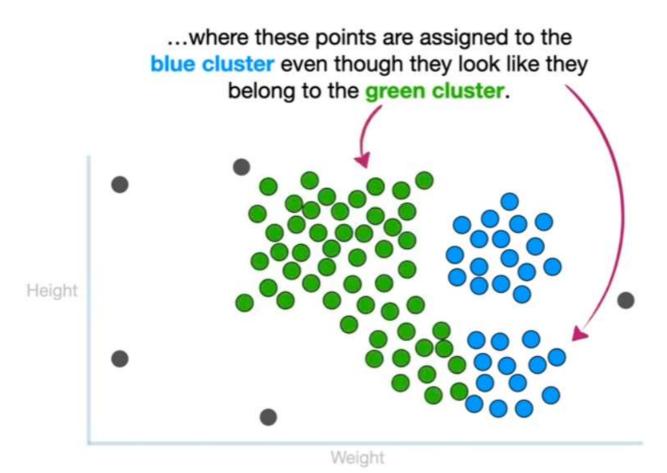


Weight

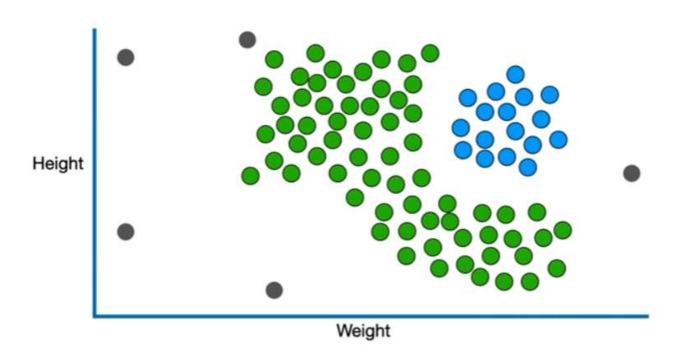
Instead, because of the nesting, a simple clustering method might get something weird like this...



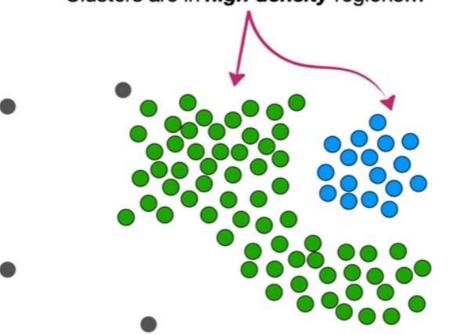
Weight

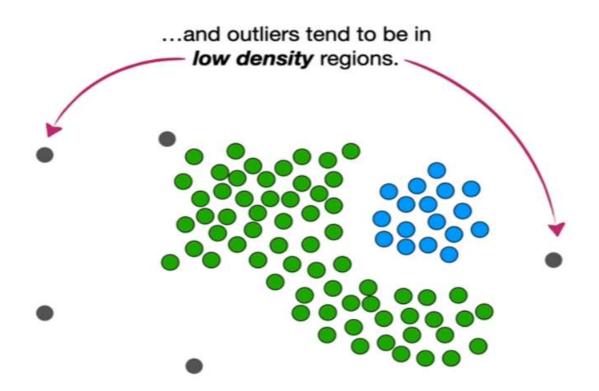


DBSCAN

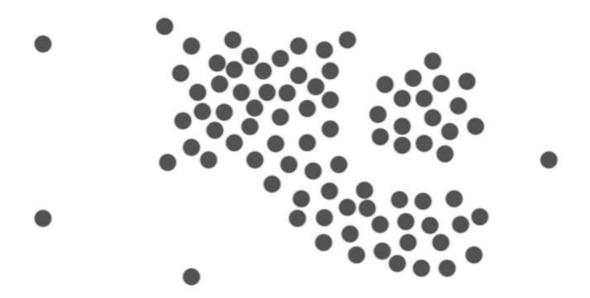


Clusters are in *high density* regions...

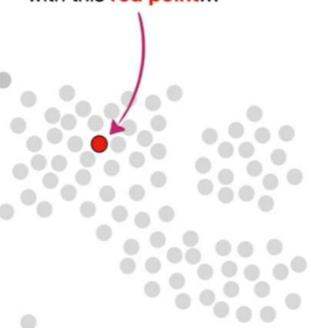




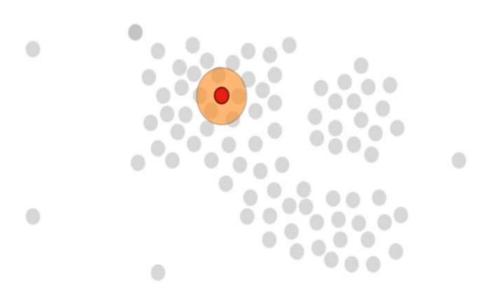
...the first thing we can do is count the number of points close to each point.



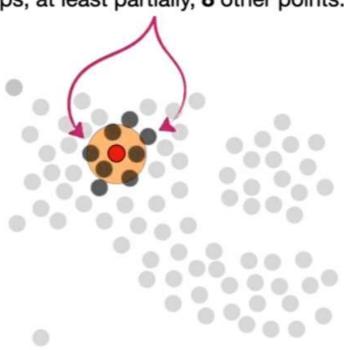
For example, if we start with this red point...



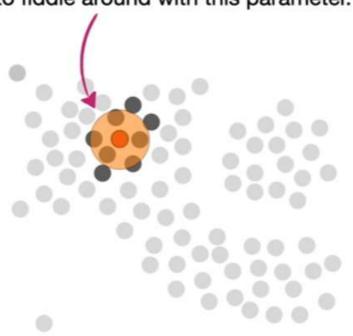
...then we see that the orange circle overlaps, at least partially, 8 other points.

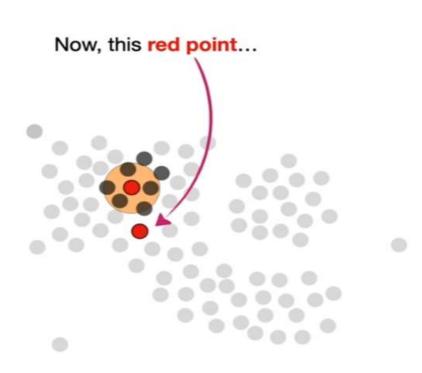


...then we see that the orange circle overlaps, at least partially, 8 other points.

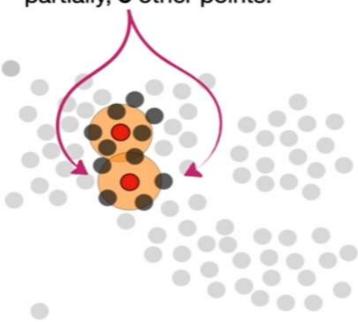


NOTE: The radius of the **orange circle** is user defined, so when using **DBSCAN**, you may need to fiddle around with this parameter.

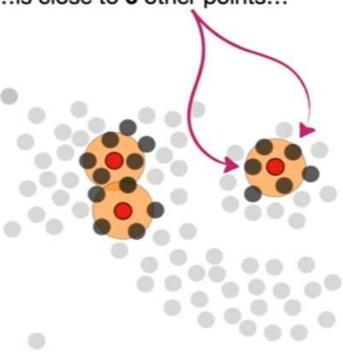


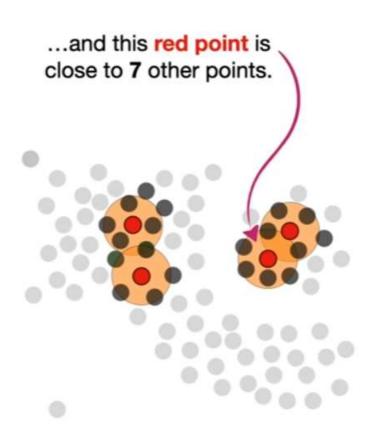


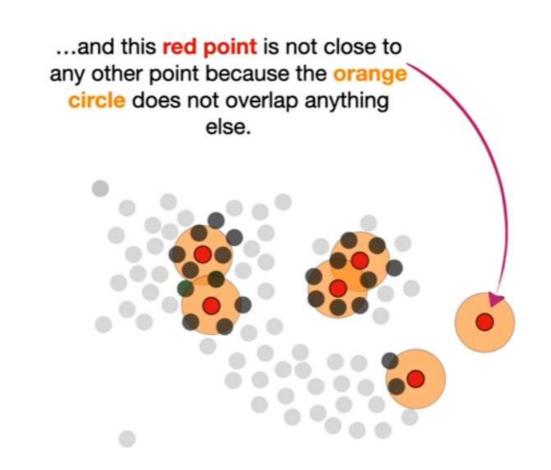
...is close to **5** other points because the **orange circle** overlaps, at least partially, **5** other points.



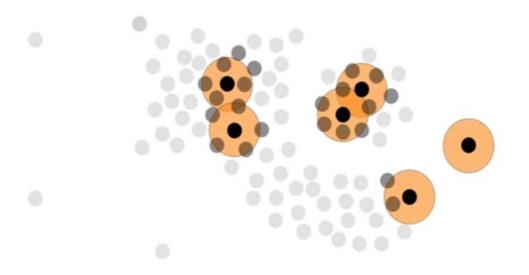
...is close to 6 other points...



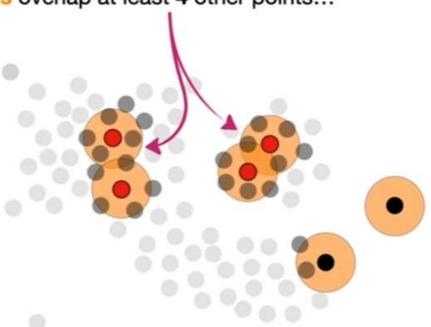


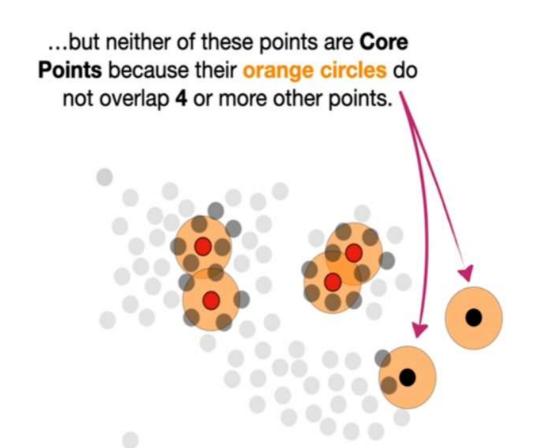


NOTE: The number of close points for a Core Point is user defined, so, when using DBSCAN, you might need to fiddle with this parameter as well.

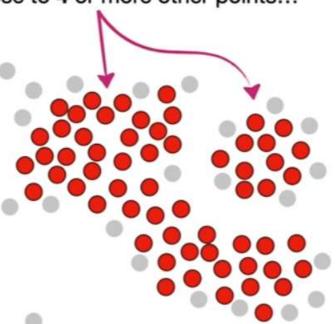


Anyway, these 4 points are some of the Core Points, because their orange circles overlap at least 4 other points...



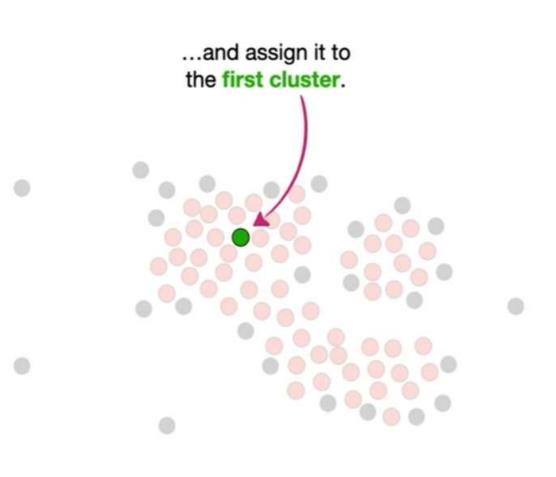


Ultimately, we can call all of these red points Core Points because they are all close to 4 or more other points...



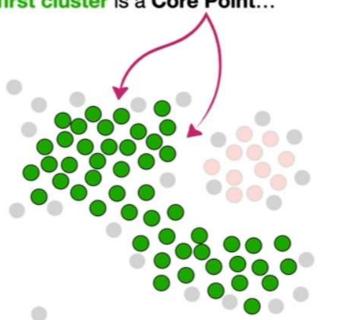
...and the remaining points are Non-Core.

Now we randomly pick a Core Point...



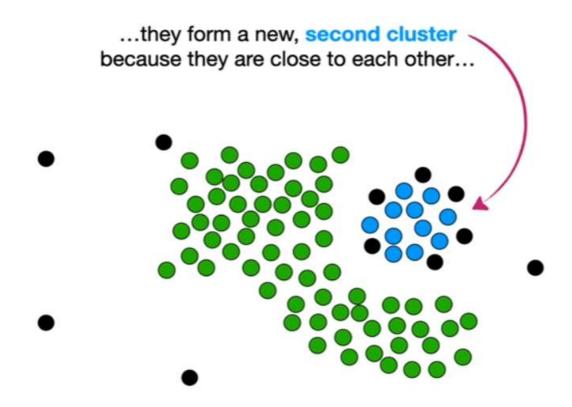
Next, the Core Points that are close to the first cluster, meaning they overlap the orange circle...

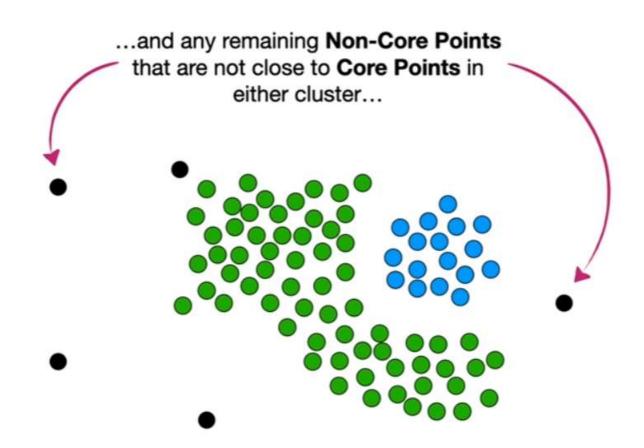
NOTE: At this point, every single point in the first cluster is a Core Point...



Non-Core Point

Non-Core Point





Density based Clustering

- Why Density-Based Clustering methods?
 - Discover clusters of arbitrary shape.
 - Clusters Dense regions of objects separated by regions of low density
 - DBSCAN the first density based clustering
 - OPTICS density based cluster-ordering
 - DENCLUE a general density-based description of cluster and clustering

DBSCAN:

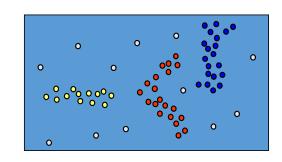
Density Based Spatial Clustering of Applications with Noise

- Proposed by Ester, Kriegel, Sander, and Xu (KDD96)
- Relies on a density-based notion of cluster: A cluster is defined as a maximal set of density-connected points.
- Discovers clusters of arbitrary shape in spatial databases with noise

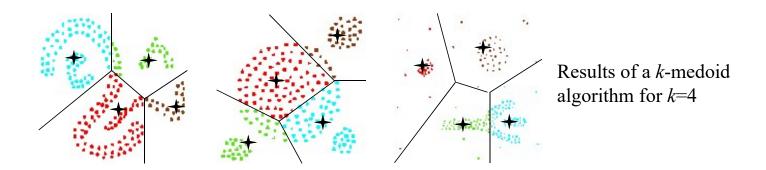
Density based Clustering

* Basic Idea:

Clusters are dense regions in the data space, separated by regions of lower object density

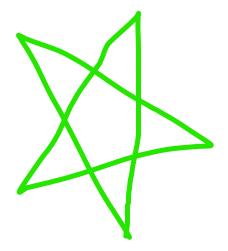


Why Density-Based Clustering?



Different density-based approaches exist. Here we discuss the ideas underlying the DBSCAN algorithm

Density based Clustering Basic Concept



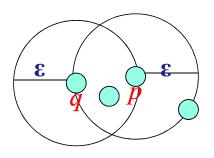
- Intuition for the formalization of the basic idea
 - For any point in a cluster, the local point density around that point has to exceed some threshold
 - The set of points from one cluster is spatially connected
- Local point density at a point p defined by two parameters
 - e radius for the neighborhood of point p: $N_e(p) := \{q \text{ in data set } D \mid dist(p, q) \leq e\}$
 - MinPts minimum number of points in the given neighborhood N(p)

ε-Neighborhood

• ε-Neighborhood – Objects within a radius of ε from an object.

$$N_{\varepsilon}(p): \{q \mid d(p,q) \leq \varepsilon\}$$

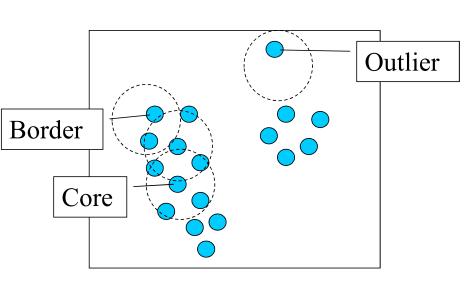
• "High density" - E-Neighborhood of an object contains at least *MinPts* of objects.



 ϵ -Neighborhood of p ϵ -Neighborhood of qDensity of p is "high" (MinPts = 4)

Density of q is "low" (MinPts = 4)

Core Point, Border Point, Outlier



 $\varepsilon = 1$ unit, MinPts = 5

Given ε and *MinPts*, categorize the objects into three exclusive groups.

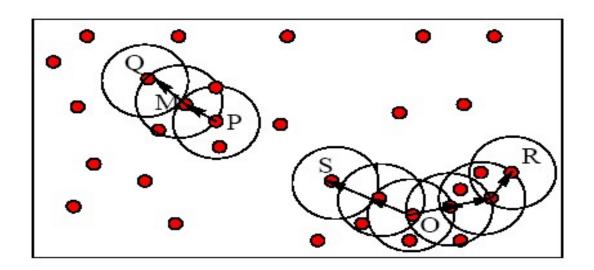
A point is a core point if it has more than a specified number of points (MinPts) within Eps. These are points that are at the interior of a cluster.

A border point has fewer than MinPts within Eps, but is in the neighborhood of a core point.

A noise point is any point that is not a core point nor a border point.

Example:

M, P, O, and R are core objects since each is in an Eps neighborhood containing at least 3 points



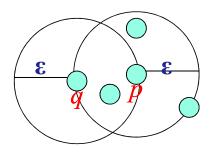
Minpts = 3

Eps=radius of the circles

Density Reachability

Directly density-reachable

An object q is directly density-reachable from object p if p is a core object and q is in p's ε -neighborhood.

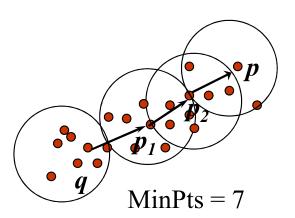


MinPts = 4

- q is directly density-reachable from p
- p is not directly density- reachable from q?
- Density-reachability is asymmetric.

Density Reachability

- Density-Reachable (directly and indirectly):
 - A point p is directly density-reachable from p2;
 - p2 is directly density-reachable from p1;
 - p1 is directly density-reachable from q;
 - $p \leftarrow p2 \leftarrow p1 \leftarrow q$ form a chain.



- p is (indirectly) density-reachable from q
- q is not density- reachable from p?

Density Reachability



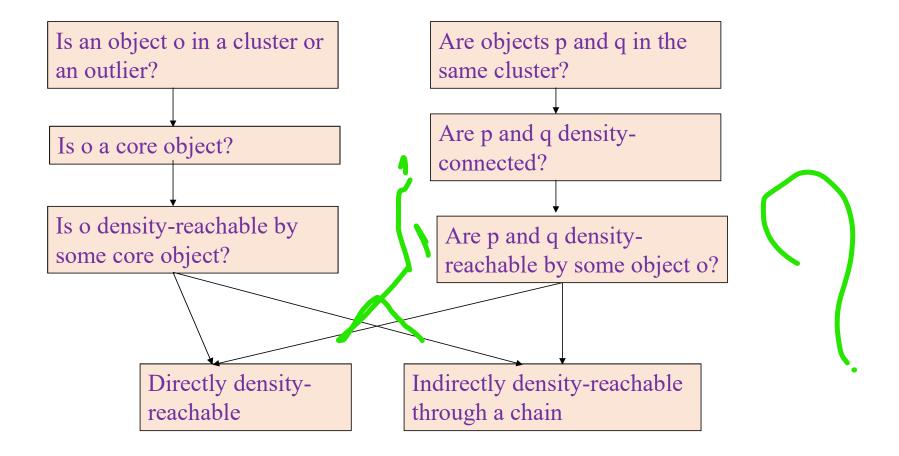
- Density-reachable is not symmetric
 - not good enough to describe clusters
- Density-Connected
 - A pair of points p and q are density-connected if they are commonly density-reachable from a point o.



Formal Description of Cluster

- Given a data set D, parameter ε and threshold MinPts.
- A cluster C is a subset of objects satisfying two criteria:
 - Connected: \forall p,q \in C: p and q are density-connected.
 - *Maximal*: \forall p,q: if p \in C and q is <u>density-reachable from p</u> (where p is the core object), then q \in C. (avoid redundancy)

Review of Concepts



DBSCAN Algorithm

```
Input: The data set D

Parameter: ε, MinPts

For each object p in D

if p is a core object and not processed then

C = retrieve all objects density-reachable from p

mark all objects in C as processed

report C as a cluster

else mark p as outlier

end if

End For
```

DBSCAN: The Algorithm

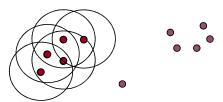
- Arbitrary select a point *p*
- Retrieve all points density-reachable from p wrt Eps and MinPts.
- If *p* is a core point, a cluster is formed.



- If *p* is a border point, no points are density-reachable from *p* and DBSCAN visits the next point of the database.
- Continue the process until all of the points have been processed.

DBSCAN Algorithm: Example

- Parameter
 - e = 2 cm
 - MinPts = 3



```
for each o Î D do

if o is not yet classified then

if o is a core-object then

collect all objects density-reachable
from o

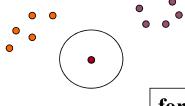
and assign them to a new cluster.

else

assign o to NOISE
```

DBSCAN Algorithm: Example

- Parameter
 - ε = 2 cm
 - *MinPts* = 3



```
for each o Î D do

if o is not yet classified then

if o is a core-object then

collect all objects density-reachable
from o

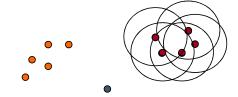
and assign them to a new cluster.

else

assign o to NOISE
```

DBSCAN Algorithm: Example

- Parameter
 - ε = 2 cm
 - *MinPts* = 3



```
for each o Î D do

if o is not yet classified then

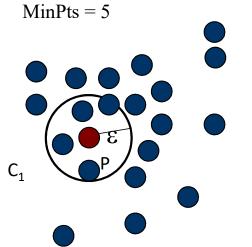
if o is a core-object then

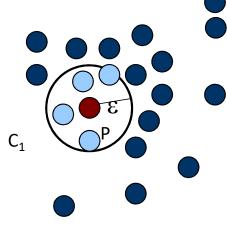
collect all objects density-reachable
from o

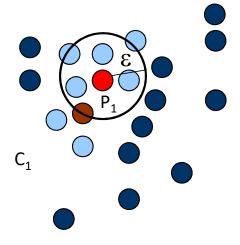
and assign them to a new cluster.

else

assign o to NOISE
```

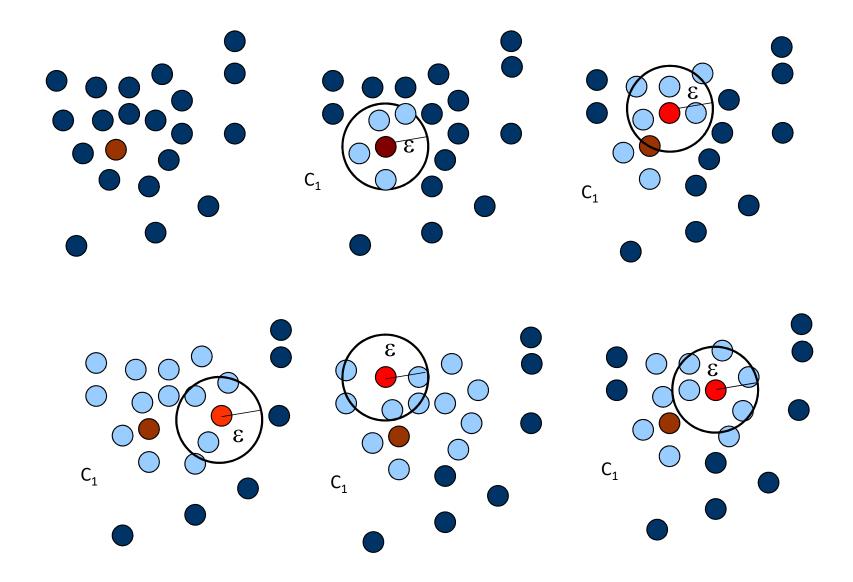




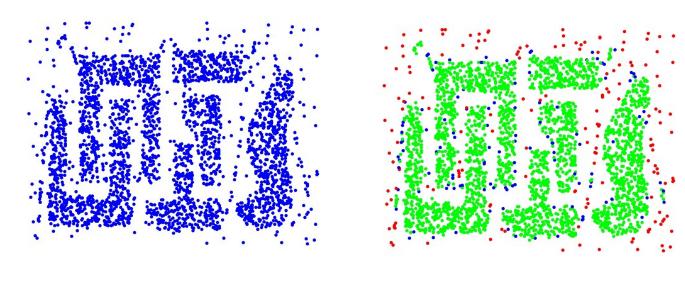


- 1. Check the ε-neighborhood of p;
- 2. If p has less than MinPts neighbors then mark p as outlier and continue with the next object
- 3. Otherwise mark p as processed and put all the neighbors in cluster C

- 1. Check the unprocessed objects in C
- 2. If no core object, return C
- 3. Otherwise, randomly pick up one core object p₁, mark p₁ as processed, and put all unprocessed neighbors of p₁ in cluster C



Example

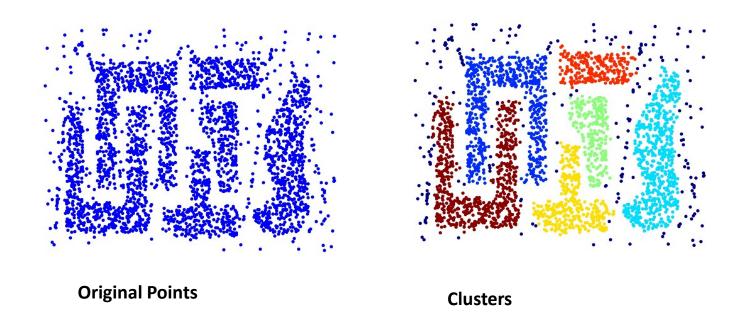


Original Points

Point types: core, border and outliers

 ϵ = 10, MinPts = 4

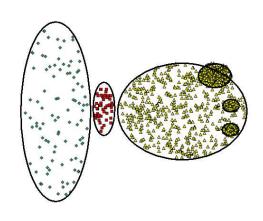
When DBSCAN Works Well



- Resistant to Noise
- Can handle clusters of different shapes and sizes

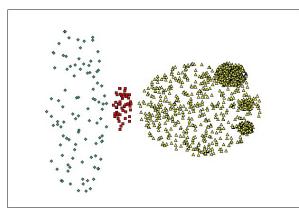
Continue...

When DBSCAN Does NOT Work Well

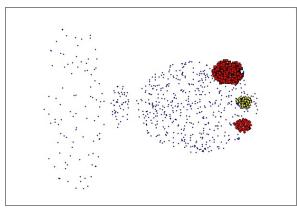


Original Points

- Cannot handle Varying densities
- sensitive to parameters

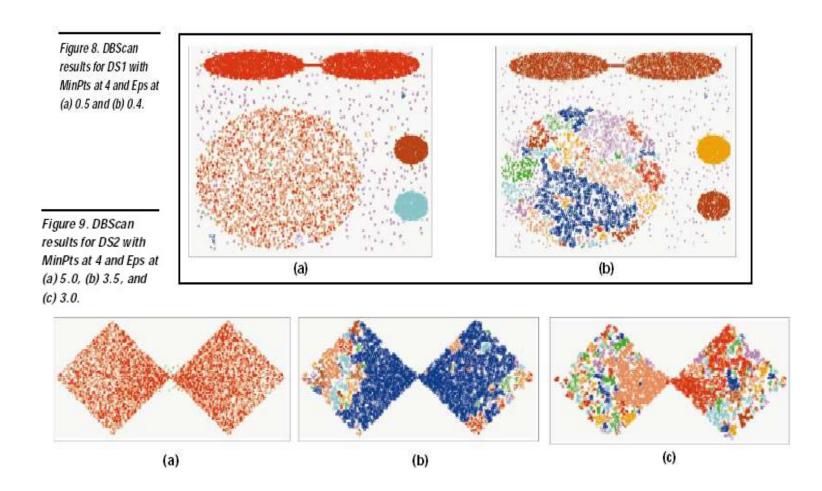


(MinPts=4, Eps=9.92).



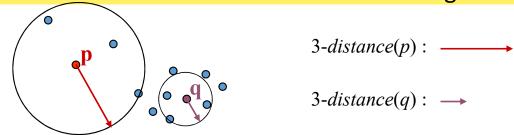
(MinPts=4, Eps=9.75)

DBSCAN: Sensitive to Parameters



Determining the Parameters arepsilon and MinPts

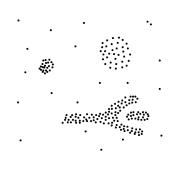
- Cluster: Point density higher than specified by ε and *MinPts*
- Idea: use the point density of the least dense cluster in the data set as parameters but how to determine this?
- Heuristic: look at the distances to the *k*-nearest neighbors

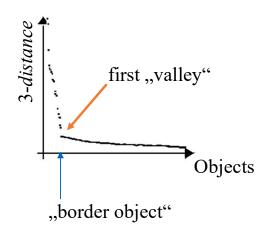


- Function *k-distance*(*p*): distance from *p* to the its *k*-nearest neighbor
- *k-distance plot: k-*distances of all objects, sorted in decreasing order

Determining the Parameters arepsilon and MinPts

• Example *k*-distance plot

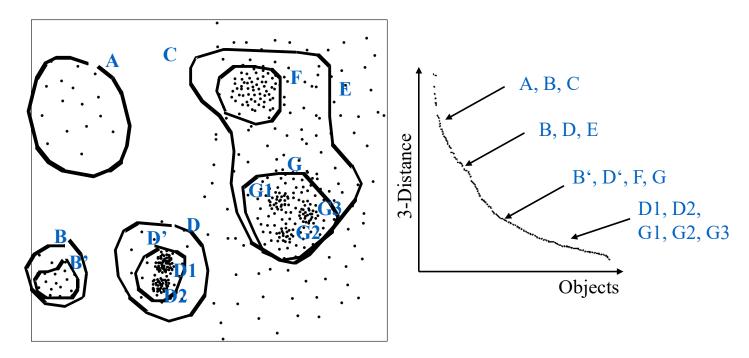




- Heuristic method:
 - Fix a value for *MinPts* (default: $2 \times d 1$)
 - User selects "border object" o from the MinPts-distance plot; ε is set to MinPts-distance(ο)

Determining the Parameters arepsilon and MinPts

• Problematic example



Density Based Clustering: Discussion

- Advantages
 - Clusters can have arbitrary shape and size
 - Number of clusters is determined automatically
 - Can separate clusters from surrounding noise
 - Can be supported by spatial index structures
- Disadvantages
 - Input parameters may be difficult to determine
 - In some situations very sensitive to input parameter setting