An Investigation of the Moments About a Horizontal Rigid Beam
IB Physics SL

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1   Experimental plan

1.1   Manipulated variable

The manipulated variable is the distance of the weights from the pivot point /m. In this lab, the manipulated variable will be changed by moving the position of the weights to the right. This change will be measured by the ruler that the weights are hanging from.

1.2   Responding variable

The responding variable is the amount of force that the spring balance measures /N. The responding variable will be measured using a spring balance.

1.3 Controlled variables

Condition	How to control it	Why it must be controlled
The position of the pivot and spring balance along the ruler.	Recording each trial with the pivot and the spring balance consistently positioned at the exact same location along the ruler.	Varying the position of these objects will change the distances between the pivot to the ruler's center of mass, the weights, and the spring balance. This will ultimately cause inconsistencies in the calculated torque values.
The number of weights suspended on the ruler.	Recording each trial with the same number of weights suspended from the ruler.	Varying the number of weights suspended on the ruler will cause the gravitational force of the weights to vary, affecting both calculations for net force and calculations for net torque.

Table 1: Controlled variables in the experiment

2 Background Information

2.1 Horizontal ruler requirement

If this experiment is to be physically conducted, then there is a need for the ruler or beam to be horizontal. This is because the torques acting on the beam only come from the the force component perpendicular to the beam, therefore using a horizontal beam would then simplify the analysis, as the calculation of the components of the forces perpendicular to the beam would not be required.

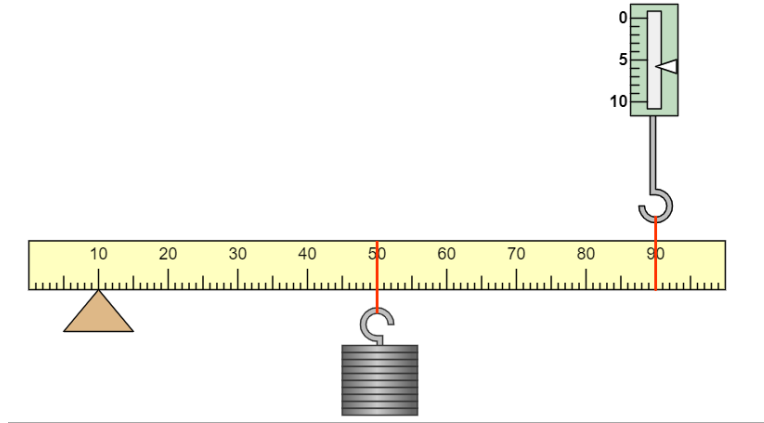What is meant by the beam/ruler to be horizontal is visually shown by the ruler in Figure 1.
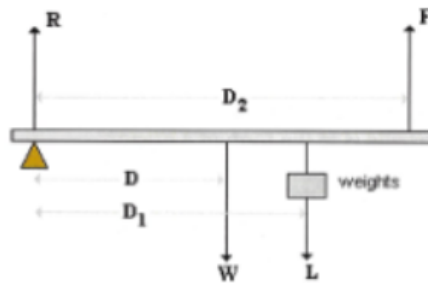
Figure 1: Horizontal beam/ruler in the apparatus of the investigation.

2.2 Conditions for static equilibrium and derivations of required equations

The following conditions need to be met for static equilibrium:

- The sum of all forces acting on the system must be equal to zero ($\sum F = 0$).

- The sum of all torques with respect to some point in the system must be equal to zero ($\sum \tau = 0$).

Four forces act on the beam: W, L, F, and R.
- R = the force exerted by the support pivot on the beam.
- W = the weight of the beam.
- L = the load placed on the beam.
- F = the force exerted by the spring balance on the beam.

Figure 2: Apparatus labelled with variables along with descriptions of forces acting in the system

With reference to the variables in Figure 2, we can derive the following equations.

3

Forces acting on the beam

$$\sum F = 0$$
$$\vec{R} + \vec{L} + \vec{F} = 0$$

Torques acting on the beam relative to support pivot (orange triangle in Figure 2)

Assigning clockwise spin as the positive direction

$$\sum \tau = 0$$
$$\left(\left| \vec{W} \right| \cdot D \right) + \left(\left| \vec{L} \right| \cdot D_1 \right) - \left(\left| \vec{F} \right| \cdot D_2 \right) = 0$$

3 Raw data

3.1 Determination of uncertainty in force measured by spring balance

Setting the weights the 0.801m along the ruler, as shown in Figure 3, the range of the force measured by the spring balance is 0.5N, with a minimum value of 9.2N and a maximum value of 9.7N.
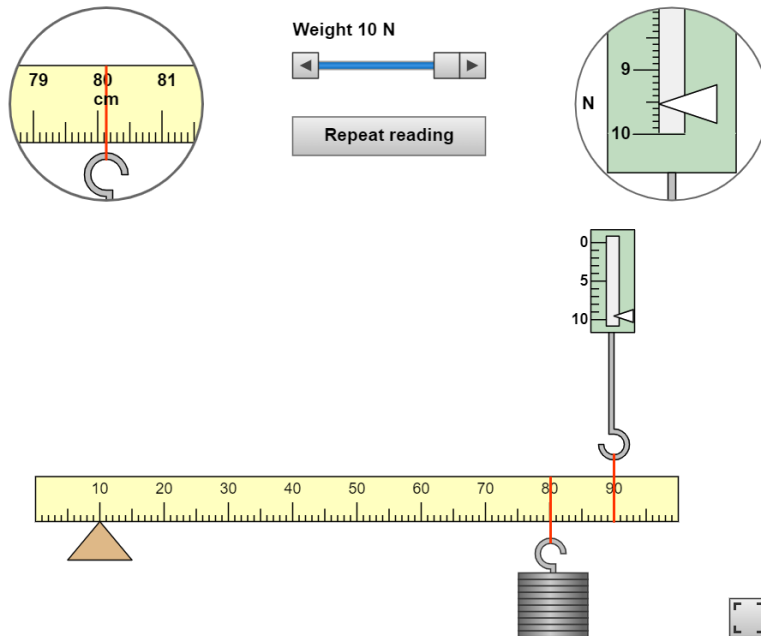

Figure 3: Positioning of weight in apparatus for uncertainty calculation of spring balance

Therefore, by dividing this range by 2, the uncertainty of the force probe is determined to be 0.3N.

3.2 Collected raw data

Table 2: Table of Position of weights along ruler with respective values of Force measured by spring scale

Position of weights along ruler /m (Δm $\pm$ 0.001m)	Force measured by spring scale /N (Δm $\pm$ 0.5N)
0.200	2.0
0.210	2.1
0.220	2.3
0.230	2.4
0.240	2.5
0.250	2.6
0.260	2.8
0.270	2.9
0.280	3.0
0.290	3.1
0.300	3.2
0.310	3.4
0.320	3.5
0.330	3.6
0.340	3.8
0.350	3.9
0.360	4.0
0.370	4.2
0.380	4.3
0.390	4.4
0.400	4.5
0.410	4.6
0.420	4.8
0.430	4.9
0.440	5.0
0.450	5.2
0.460	5.2
0.470	5.4
0.480	5.5
0.490	5.6
0.500	5.8
0.510	5.9
0.520	6.0
0.530	6.2
0.540	6.3
0.550	6.5
0.560	6.7

0.570	6.6
0.580	6.8
0.590	6.8
0.600	7.1
0.610	7.2
0.620	7.3
0.630	7.4
0.640	7.6
0.650	7.7
0.660	7.8
0.670	7.9
0.680	8.0
0.690	8.2
0.700	8.3
0.710	8.4
0.720	8.6
0.730	8.7
0.740	8.8
0.750	8.9
0.760	9.1
0.770	9.2
0.780	9.3
0.790	9.5
0.800	9.6
0.810	9.7
0.820	9.8
0.830	10.0

4   Processed data

Taking the trial with the weight positioned at 0.200m along the ruler, we can determine the predicted force of the spring balance for this trial.

Because the force applied by the pivot point is unknown but the weight of the ruler is known (1.5N), then only the torque equation defined earlier (shown below) can be used to solve for the predicted force of the spring balance.

$$\left(\left|\vec{W}\right| \cdot D\right) + \left(\left|\vec{L}\right| \cdot D_1\right) - \left(\left|\vec{F}\right| \cdot D_2\right) = 0$$
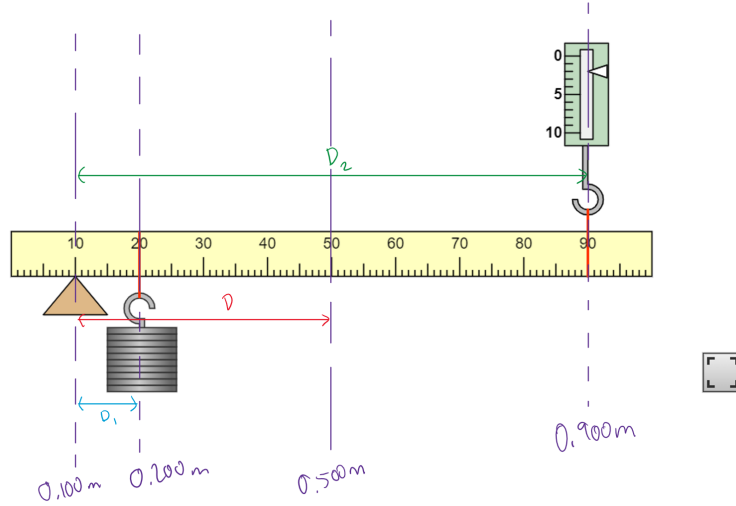
Figure 4: Reference for distance and positions of objects along ruler

The calculation for the predicated force of the spring balance given that the weight is positioned at 0.200m along the ruler is shown below, with distance values originating from Figure 4

$$\left(\left|\vec{W}\right| \cdot D\right) + \left(\left|\vec{L}\right| \cdot D_1\right) - \left(\left|\vec{F}\right| \cdot D_2\right) = 0$$

where $\left|\vec{W}\right| =$ the magnitude of the weight of the ruler /N

$\left|\vec{L}\right| =$ the magnitude of the weight of the weights suspended on the ruler /N

$\left|\vec{F}\right| =$ the magnitude of the force applied onto the ruler by the

spring balance /N

$D =$ the distance between the pivot and the ruler's centre of mass /m

$D_1 =$ the distance between the pivot point and the weights /m

$D_2 =$ the distance between the pivot point and the spring balance /m

$$\left(\left|\vec{F}\right| \cdot D_2\right) = \left(\left|\vec{W}\right| \cdot D\right) + \left(\left|\vec{L}\right| \cdot D_1\right)$$

Given that $\left|\vec{W}\right| = 1.5\text{N}$

$$\left|\vec{L}\right| = 10\text{N}$$

$$D_2 = 0.900\text{m} - 0.100\text{m} = 0.800\text{m}$$

$$D = 0.500\text{m} - 0.100\text{m} = 0.400\text{m}$$

$$D_1 = 0.200\text{m} - 0.100\text{m} = 0.100\text{m}$$

$$(0.800\text{m}) \cdot \left|\vec{F}\right| = (0.400\text{m})(1.5\text{N}) + (0.100\text{m})(10\text{N})$$

$$\left|\vec{F}\right| = 2.0\text{N}$$

Continuing with these calculations, the graph in Figure 5 shows the trend of the predicted force of the spring balance with respect to the distance between the weights and the pivot point.
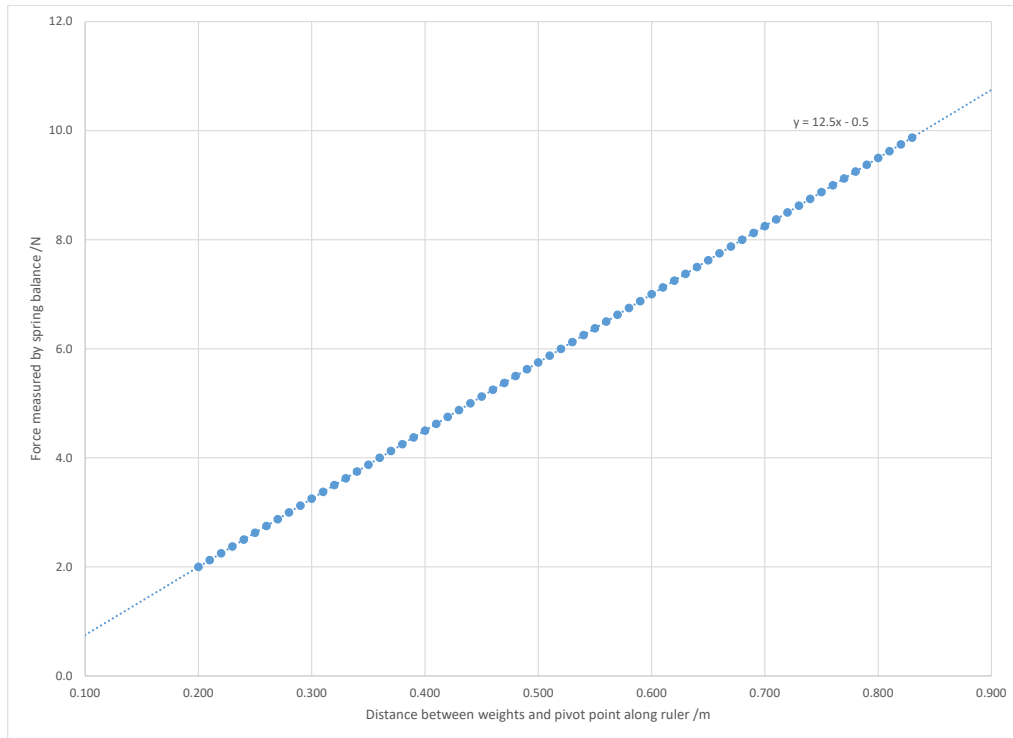

Figure 5: Force measured by spring balance /N versus Distance between weights and pivot point along ruler /m

5   Analysis