Rings - 1 round

3v3

$$e^{-3i\gamma}\left(\cos^3(\beta) - i\sin^3(\beta)\right) + e^{i\gamma}\left(-3\sin^2(\beta)\cos(\beta) + 3i\sin(\beta)\cos^2(\beta)\right)$$

p = 0.99999999999678

3v2 1

4v4

$$e^{-4i\gamma} \left(\sin^4(\beta) + \cos^4(\beta) \right) - 2e^{4i\gamma} \sin^2(\beta) \cos^2(\beta) + 4i \sin(\beta) \cos^3(\beta) - 4\sin^2(\beta) \cos^2(\beta) - 4i \sin^3(\beta) \cos(\beta)$$

$$p = 0.5398544578511101$$

4v3 1

$$e^{-4i\gamma} \left(i\sin(\beta)\cos^3(\beta) - i\sin^3(\beta)\cos(\beta) \right) + e^{4i\gamma} \left(i\sin(\beta)\cos^3(\beta) - i\sin^3(\beta)\cos(\beta) \right)$$

+
$$\sin^4(\beta) + \cos^4(\beta) + 2i\sin(\beta)\cos^3(\beta) - 6\sin^2(\beta)\cos^2(\beta) - 2i\sin^3(\beta)\cos(\beta)$$

p = 0.5

4v2 2

$$-2e^{-4i\gamma}\sin^{2}(\beta)\cos^{2}(\beta) - 2e^{4i\gamma}\sin^{2}(\beta)\cos^{2}(\beta) + \sin^{4}(\beta) + \cos^{4}(\beta) + 4i\sin(\beta)\cos^{3}(\beta) - 2\sin^{2}(\beta)\cos^{2}(\beta) - 4i\sin^{3}(\beta)\cos(\beta)$$

4v1 1 1 1

$$e^{4i\gamma} \left(\sin^4(\beta) + \cos^4(\beta) \right) - 2e^{-4i\gamma} \sin^2(\beta) \cos^2(\beta) + 4i \sin(\beta) \cos^3(\beta) - 4\sin^2(\beta) \cos^2(\beta) - 4i \sin^3(\beta) \cos(\beta)$$

$$p = 0.5398544578511104$$

5v5

$$e^{-5i\gamma} \left(\cos^{5}(\beta) + i\sin^{5}(\beta)\right) + e^{3i\gamma} \left(-5\sin^{2}(\beta)\cos^{3}(\beta) - 5i\sin^{3}(\beta)\cos^{2}(\beta)\right) + e^{-i\gamma} \left(5i\sin(\beta)\cos^{4}(\beta) - 5\sin^{2}(\beta)\cos^{3}(\beta) - 5i\sin^{3}(\beta)\cos^{2}(\beta) + 5\sin^{4}(\beta)\cos(\beta)\right)$$

p = 0.4105035493177127

5v4 1

$$\begin{split} & e^{-5i\gamma} \left(\sin^4(\beta) \cos(\beta) + i \sin(\beta) \cos^4(\beta) \right) \\ & + e^{3i\gamma} \left(2i \sin(\beta) \cos^4(\beta) - 3 \sin^2(\beta) \cos^3(\beta) - 3i \sin^3(\beta) \cos^2(\beta) + 2 \sin^4(\beta) \cos(\beta) \right) \\ & + e^{-i\gamma} \left(i \sin^5(\beta) + \cos^5(\beta) + 2i \sin(\beta) \cos^4(\beta) - 7 \sin^2(\beta) \cos^3(\beta) - 7i \sin^3(\beta) \cos^2(\beta) + 2 \sin^4(\beta) \cos(\beta) \right) \end{split}$$

p = 0.3985485156786475

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\begin{split} &e^{-5i\gamma}\left(-\sin^2(\beta)\cos^3(\beta)-i\sin^3(\beta)\cos^2(\beta)\right)\\ &+e^{3i\gamma}\left(i\sin(\beta)\cos^4(\beta)-4\sin^2(\beta)\cos^3(\beta)-4i\sin^3(\beta)\cos^2(\beta)+\sin^4(\beta)\cos(\beta)\right)\\ &+e^{-i\gamma}\left(i\sin^5(\beta)+\cos^5(\beta)+4i\sin(\beta)\cos^4(\beta)-5\sin^2(\beta)\cos^3(\beta)-5i\sin^3(\beta)\cos^2(\beta)+4\sin^4(\beta)\cos(\beta)\right) \end{split}
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p = 0.5150158139390923

5v2 1 1 1

```
\begin{split} & e^{-5i\gamma} \left( -\sin^2(\beta)\cos^3(\beta) - i\sin^3(\beta)\cos^2(\beta) \right) \\ & + e^{-i\gamma} \left( 3i\sin(\beta)\cos^4(\beta) - 7\sin^2(\beta)\cos^3(\beta) - 7i\sin^3(\beta)\cos^2(\beta) + 3\sin^4(\beta)\cos(\beta) \right) \\ & + e^{3i\gamma} \left( i\sin^5(\beta) + \cos^5(\beta) + 2i\sin(\beta)\cos^4(\beta) - 2\sin^2(\beta)\cos^3(\beta) - 2i\sin^3(\beta)\cos^2(\beta) + 2\sin^4(\beta)\cos(\beta) \right) \end{split}
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p = 0.87890625000000002

6v6

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\begin{split} &e^{-6i\gamma} \left(\cos^6(\beta) - \sin^6(\beta)\right) - 2ie^{6i\gamma} \sin^3(\beta) \cos^3(\beta) \\ &+ e^{2i\gamma} \left( -9 \sin^2(\beta) \cos^4(\beta) - 12i \sin^3(\beta) \cos^3(\beta) + 9 \sin^4(\beta) \cos^2(\beta) \right) \\ &+ e^{-2i\gamma} \left( 6i \sin(\beta) \cos^5(\beta) - 6 \sin^2(\beta) \cos^4(\beta) - 6i \sin^3(\beta) \cos^3(\beta) + 6 \sin^4(\beta) \cos^2(\beta) + 6i \sin^5(\beta) \cos(\beta) \right) \end{split}
```

p = 0.30171820009611067

6v5 1

```
\begin{split} &e^{-6i\gamma} \left( i \sin(\beta) \cos^5(\beta) + i \sin^5(\beta) \cos(\beta) \right) + e^{6i\gamma} \left( \sin^4(\beta) \cos^2(\beta) - \sin^2(\beta) \cos^4(\beta) \right) \\ &+ e^{2i\gamma} \left( 3i \sin(\beta) \cos^5(\beta) - 6 \sin^2(\beta) \cos^4(\beta) - 12i \sin^3(\beta) \cos^3(\beta) + 6 \sin^4(\beta) \cos^2(\beta) + 3i \sin^5(\beta) \cos(\beta) \right) \\ &+ e^{-2i\gamma} \left( -\sin^6(\beta) + \cos^6(\beta) + 2i \sin(\beta) \cos^5(\beta) - 8 \sin^2(\beta) \cos^4(\beta) - 8i \sin^3(\beta) \cos^3(\beta) + 8 \sin^4(\beta) \cos^2(\beta) + 2i \sin^5(\beta) \cos(\beta) \right) \end{split}
```

p = 0.2621557189304736

6v4 2

```
\begin{split} &-2ie^{6i\gamma}\sin^{3}(\beta)\cos^{3}(\beta) + e^{-6i\gamma}\left(\sin^{4}(\beta)\cos^{2}(\beta) - \sin^{2}(\beta)\cos^{4}(\beta)\right) \\ &+ e^{2i\gamma}\left(2i\sin(\beta)\cos^{5}(\beta) - 9\sin^{2}(\beta)\cos^{4}(\beta) - 8i\sin^{3}(\beta)\cos^{3}(\beta) + 9\sin^{4}(\beta)\cos^{2}(\beta) + 2i\sin^{5}(\beta)\cos(\beta)\right) \\ &+ e^{-2i\gamma}\left(-\sin^{6}(\beta) + \cos^{6}(\beta) + 4i\sin(\beta)\cos^{5}(\beta) - 5\sin^{2}(\beta)\cos^{4}(\beta) \\ &- 10i\sin^{3}(\beta)\cos^{3}(\beta) + 5\sin^{4}(\beta)\cos^{2}(\beta) + 4i\sin^{5}(\beta)\cos(\beta)\right) \end{split}
```

p = 0.4260966260907454

6v3 1 1 1

```
\begin{split} &e^{6i\gamma} \left( i \sin(\beta) \cos^5(\beta) + i \sin^5(\beta) \cos(\beta) \right) + e^{-6i\gamma} \left( \sin^4(\beta) \cos^2(\beta) - \sin^2(\beta) \cos^4(\beta) \right) \\ &+ e^{-2i\gamma} \left( 3i \sin(\beta) \cos^5(\beta) - 6 \sin^2(\beta) \cos^4(\beta) - 12i \sin^3(\beta) \cos^3(\beta) + 6 \sin^4(\beta) \cos^2(\beta) \right) \\ &+ 3i \sin^5(\beta) \cos(\beta) \right) + e^{2i\gamma} \left( -\sin^6(\beta) + \cos^6(\beta) + 2i \sin(\beta) \cos^5(\beta) \right) \\ &- 8 \sin^2(\beta) \cos^4(\beta) - 8i \sin^3(\beta) \cos^3(\beta) + 8 \sin^4(\beta) \cos^2(\beta) + 2i \sin^5(\beta) \cos(\beta) \right) \end{split}
```

p = 0.26215571893047385

6v3 3

$$-2ie^{-6i\gamma}\sin^{3}(\beta)\cos^{3}(\beta) + e^{6i\gamma}\left(\sin^{4}(\beta)\cos^{2}(\beta) - \sin^{2}(\beta)\cos^{4}(\beta)\right) \\ + e^{2i\gamma}\left(2i\sin(\beta)\cos^{5}(\beta) - 6\sin^{2}(\beta)\cos^{4}(\beta) - 14i\sin^{3}(\beta)\cos^{3}(\beta) + 6\sin^{4}(\beta)\cos^{2}(\beta) + 2i\sin^{5}(\beta)\cos(\beta)\right) \\ + e^{-2i\gamma}\left(-\sin^{6}(\beta) + \cos^{6}(\beta) + 4i\sin(\beta)\cos^{5}(\beta) - 8\sin^{2}(\beta)\cos^{4}(\beta)\right) \\ - 4i\sin^{3}(\beta)\cos^{3}(\beta) + 8\sin^{4}(\beta)\cos^{2}(\beta) + 4i\sin^{5}(\beta)\cos(\beta)\right)$$

p = 0.375000000000000017

6v2 1 2 1

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-2ie^{6i\gamma}\sin^{3}(\beta)\cos^{3}(\beta) + e^{-6i\gamma}\left(\sin^{4}(\beta)\cos^{2}(\beta) - \sin^{2}(\beta)\cos^{4}(\beta)\right) \\ + e^{-2i\gamma}\left(2i\sin(\beta)\cos^{5}(\beta) - 6\sin^{2}(\beta)\cos^{4}(\beta) - 14i\sin^{3}(\beta)\cos^{3}(\beta) + 6\sin^{4}(\beta)\cos^{2}(\beta)\right) \\ + 2i\sin^{5}(\beta)\cos(\beta)\right) + e^{2i\gamma}\left(-\sin^{6}(\beta) + \cos^{6}(\beta) + 4i\sin(\beta)\cos^{5}(\beta)\right) \\ - 8\sin^{2}(\beta)\cos^{4}(\beta) - 4i\sin^{3}(\beta)\cos^{3}(\beta) + 8\sin^{4}(\beta)\cos^{2}(\beta) + 4i\sin^{5}(\beta)\cos(\beta)\right)
```

p = 0.3749999999999933

6v2 1 1 2

$$\begin{aligned} &-2ie^{-6i\gamma}\sin^{3}(\beta)\cos^{3}(\beta) + e^{6i\gamma}\left(\sin^{4}(\beta)\cos^{2}(\beta) - \sin^{2}(\beta)\cos^{4}(\beta)\right) \\ &+ e^{-2i\gamma}\left(2i\sin(\beta)\cos^{5}(\beta) - 9\sin^{2}(\beta)\cos^{4}(\beta) - 8i\sin^{3}(\beta)\cos^{3}(\beta) + 9\sin^{4}(\beta)\cos^{2}(\beta) + 2i\sin^{5}(\beta)\cos(\beta)\right) \\ &+ e^{2i\gamma}\left(-\sin^{6}(\beta) + \cos^{6}(\beta) + 4i\sin(\beta)\cos^{5}(\beta) - 5\sin^{2}(\beta)\cos^{4}(\beta) \\ &- 10i\sin^{3}(\beta)\cos^{3}(\beta) + 5\sin^{4}(\beta)\cos^{2}(\beta) + 4i\sin^{5}(\beta)\cos(\beta)\right) \end{aligned}$$

p = 0.4260966260907456

6v1 1 1 1 1 1

$$\begin{split} & e^{6i\gamma} \left(\cos^6(\beta) - \sin^6(\beta) \right) - 2i e^{-6i\gamma} \sin^3(\beta) \cos^3(\beta) \\ & + e^{-2i\gamma} \left(-9 \sin^2(\beta) \cos^4(\beta) - 12i \sin^3(\beta) \cos^3(\beta) + 9 \sin^4(\beta) \cos^2(\beta) \right) \\ & + e^{2i\gamma} \left(6i \sin(\beta) \cos^5(\beta) - 6 \sin^2(\beta) \cos^4(\beta) - 6i \sin^3(\beta) \cos^3(\beta) + 6 \sin^4(\beta) \cos^2(\beta) + 6i \sin^5(\beta) \cos(\beta) \right) \end{split}$$

p = 0.3017182000961104