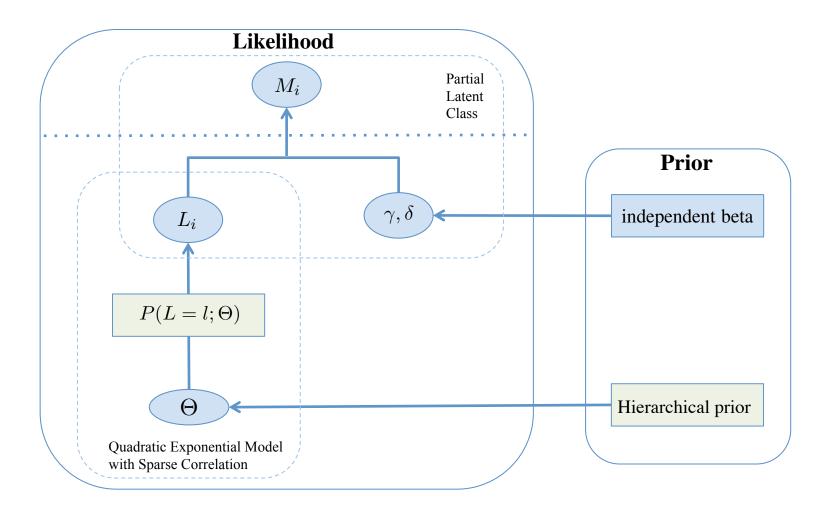
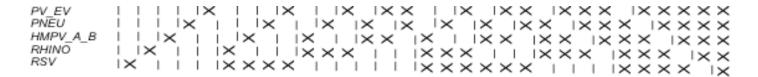
Model Hierarchy





Latent Variable



Regular Quadratic Exponential Model:

$$P(L=l;\Theta) = \exp\{\Theta_1^T l + \Theta_2^T u_2\}/A(\Theta)$$
 with
$$A(\Theta) = \sum_{l^* \in \{0,1\}^K} \exp\{\Theta^T l^*\}$$

 $\theta_{ik}^{(1)} = X_i^T \beta_k$, where X_i is the vector of covariates.

Sparse Correlation:

$$\Theta_2 = \theta_2 \cdot (I_1, \dots, I_{\binom{K}{2}})$$

Hierarchical Prior:

$$I_j \sim \text{Bernoulli}(p)$$

 $p \sim \text{Beta}(a, b)$



Simulation Study

5 candidate etiological pathogens.

BS are available for each of them.

500 cases and 1000 controls in each data set.

200 independent data sets simulated.

Two binary covariates: age and severity.

Simulation I-a:

- Allow multiple pathogen infect lung at the same time. Pr(2 or more) $\approx 0.35\,$
- All pathogens have SS measurements.
- Relatively low-quality data: SS TPR ≈ 0.1 BS TPR ≈ 0.6 BS FPR ≈ 0.45

Simulation I-b:

- Only pathogen D, E have SS measurements.

Simulation II:

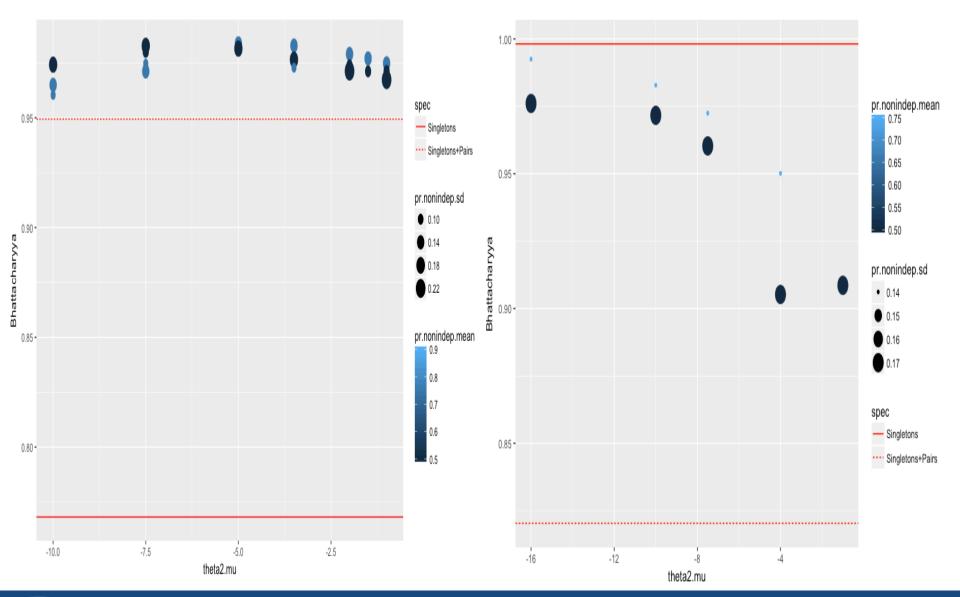
- Relatively high-quality data: SS TPR ≈ 0.8 BS TPR ≈ 0.9 BS FPR ≈ 0.1

Simulation III:

- Only single-pathogen infection is possible.



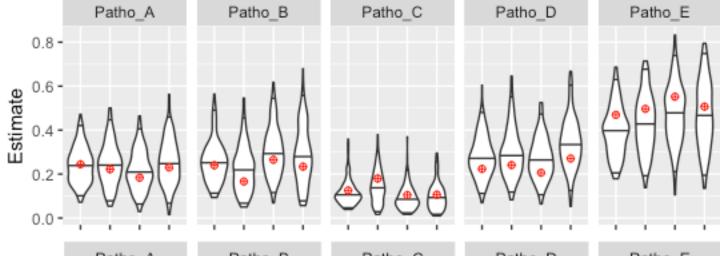
Simulation I-a and III vs. pLCM



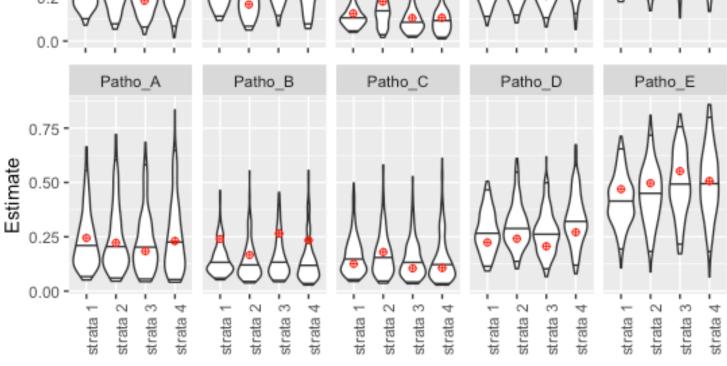


Simulation I-a vs. I-b

SS available for all five pathogens:

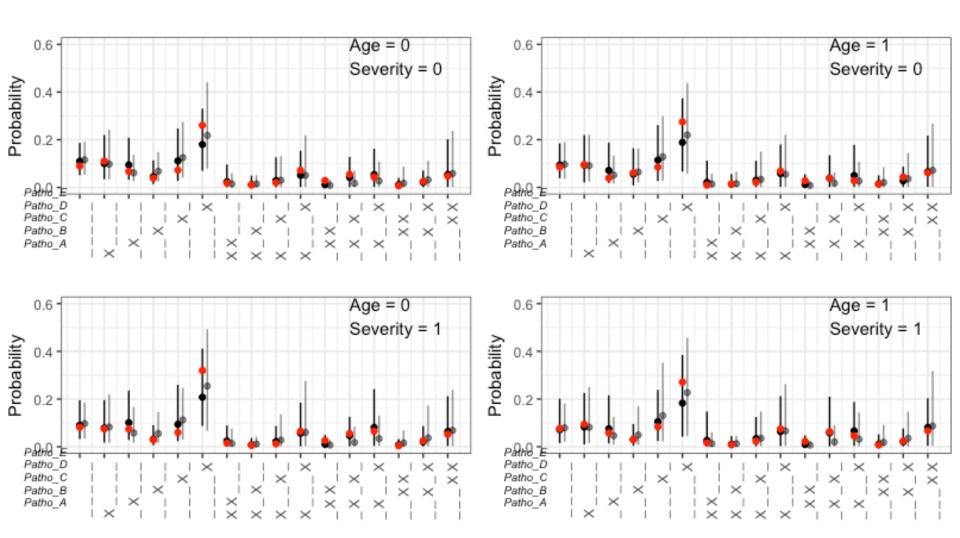


SS available for pathogen D and E only:





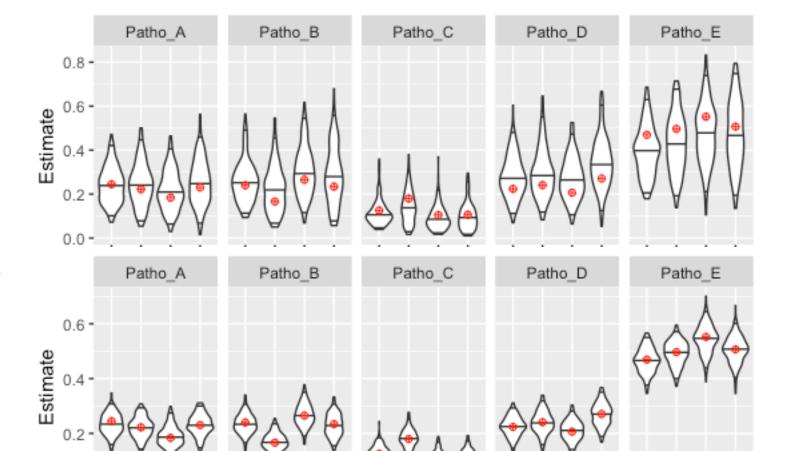
Simulation I-a vs. I-b





Simulation I-a vs. II

Low-quality data:



strata 3

strata 4

strata 1

strata 3

strata 2

strata 4

strata 2

strata 1

strata 3

strata 4

strata 2

strata 1

High-quality data:



strata 3

strata 4

strata 2

strata 1

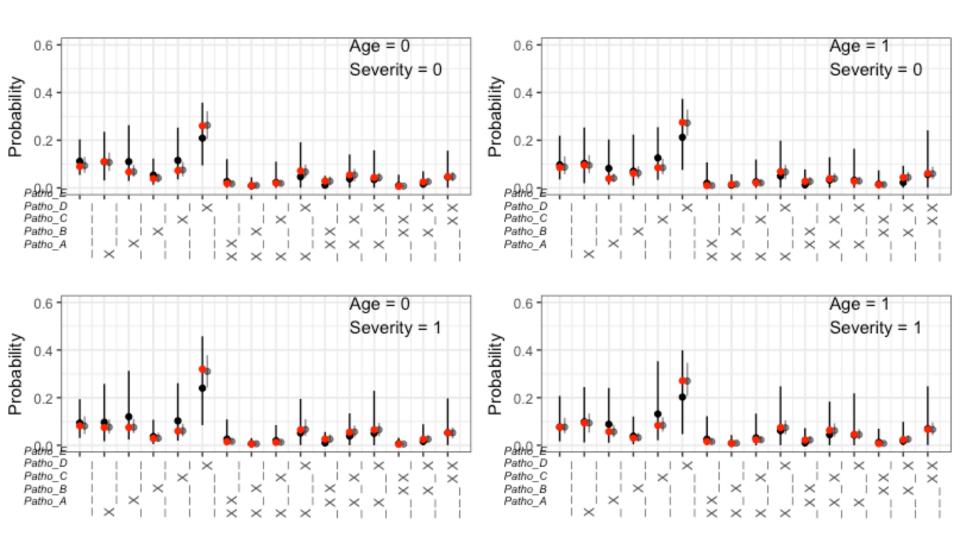
strata 2

strata 1

strata 3

strata 4

Simulation I-a vs. II





Appendix

```
PV EV
           PNEU
HMPV A B
           RHINO
RSV
\beta_0
     0.210 -0.282 -0.835 -0.205 1.068
\beta_{\text{age}}
     -0.1 -0.5 0.5
                        0.2 0.1
     -0.3 0.2
                 -0.2 -0.1 0.3
\beta_{\text{sev}}
     0.4 0.3
                 -0.4 0.2 -0.2
\beta_{\mathtt{a}:\mathtt{s}}
\Theta_2 = (-1.5, -1.5, -1.5, -1.5, 0.0, 0.0, -1.5, -1.5, -1.5)
Мıյ
   Γ11
      [2] [3] [4] [5]
00
   0.245 0.240 0.126 0.224 0.469
10
   0.222 0.166 0.180 0.241 0.497
0.1
   0.184 0.265 0.105 0.206 0.552
11
   0.230 0.234 0.106 0.271 0.507
Pr(s)
      [0]
           [1] [2] [3] [4] [5]
0.0
      0.090 0.550 0.329 0.031 0.000
10
     0.085 0.555 0.328 0.031 0.000
01
     0.081 0.558 0.329 0.032 0.000
     0.076 0.536 0.351 0.036 0.001
11
```

