# CMU 15-418/618: Exam 2 Practice Exercises

# **Problem 1: Miscellaneous Short Answer Questions**

A.	The lock-free data structures discussed in lecture assumed a sequentially consistent address space. What new issues must be considered if a lock-free implementation is executed on a system with weaker memory consistency?
В.	What is the motivation for a content distribution network (CDN)? Why do Facebook images get served to your browser by a CDN but your main news feed is not?
C.	Give two reasons why an implementation of a web server might spawn more worker threads than cores present in the machine it is running on?

D.	If you replaced a highly contended lock with an atomic{} block to enable transactional implementation of mutual exclusion, do you think pessimistic or optimistic conflict detection would yield better performance?
E.	You get a job at Fitbit and your boss asks you to optimize some code to <b>improve the battery life</b> of their latest wearable product. You profile the code and find that most time is spent in the function getting_fit() which uses 10 arithmetic instructions to compute how much fitter the wearer is from his last 10 steps. You determine that it's possible to reduce the function to only 5 instructions if one of the instructions is a load from a precomputed lookup table stored in DRAM. You propose this solution to your boss and she shoots it down as a bad idea. Why? (Assume the table does not fit in the processor's cache, and that the Fitbit's memory system has infinite bandwidth and no latency.)
F.	Your new startup's codebase makes use of two data structures: a stack and a linked list. Both structures are implemented using a single (per structure) global lock to avoid data races. Your developers suggest there is time before product launch to reimplement one of the two structures in a lock-free manner to enable concurrency. Assuming both structures are equally important to the overall performance of the program and equally difficult to implement, which structure's reimplementation do you recommend that your team focus effort on, and why? (Hint: we are looking for an answer that considers the potential for performance improvement from a lock-free implementation.)

G.	You are responsible for designing the packet format for the interconnect for the new multi-core chip by Yinzer Processors. It has already been decided that the interconnect will use <b>cut-through flow control</b> . You design a packet format where the front of the packet (i.e., the first bits that arrive at a switch) contain the checksum, and the end of the packet contains the destination node address, and present it to your team, and get nasty looks from everyone. Why are they unhappy with your design?
H.	Consider a spin lock that uses <b>exponential back off</b> to reduce coherence traffic generated by threads
	waiting for the lock. How could this policy result in starvation? Briefly give one approach to avoiding starvation during lock acquisition while maintaining low traffic. (naming an alternative lock implementation is fine)
I.	Imagine you are designing a parallel machine with P processors to execute convolutions in parallel on a 2D array. (Recall each array element is updated to be a weighed combination of all neighboring values). Do you advocate for a mesh or torus interconnect for this system? Why? (Hint: think about performance/cost trade-offs)

J.	Consider the difference between store-and-forward and cut-through flow control in a chip interconnect. Although cut-through flow control will typically reduce packet transmission latency, its behavior degenerates to that of the store-and-forward scheme under high contention. Why?
K.	You and friend start a company called CMUTube that delivers high-quality video lectures to students around the world. Each day, your company makes all the lectures conducted at CMU available on a server and viewable on a mobile phone. Your friend is a L33t programmer and begins implementing his own video playback software in highly optimized ARM assembly. You recommend that he just use the high-level programming interfaces provided by iOS and Android for video playback. Even if your friend is the best programmer on the planet, why is his strategy misguided? (Hint: we are looking for an answer that addresses energy.)
L.	Could your company's service benefit from content distribution networks? Why or why not?

M.	Your job is to implement an iPhone app that continuously processes images from the camera. To provide a good experience, the app must run at a 30 fps. While developing the app, you always test it on a benchmark that contains 100 frames. After a few days of performance tuning the app consistently meets the performance requirement on this benchmark. Excited, you go to show your boss! She starts walking around the office with the app on, testing out how it works. After a few minutes of running the app, she comes back to your desk and says, "You're going to have to try harder, the app is not fast enough – it's not running at 30 frames per second". No changes have been made to the app. What happened?
N.	Given atomicCAS please implement a lock-free atomicOR below. (You do not need to worry about the ABA problem.) In this problem, have atomicCAS return the result AFTER the OR occurs.
	<pre>// atomically bitwise OR the value val with the current value in addr int atomicOR(int* addr, int val) {</pre>

}

O. Consider an application whose runtime on a single-core processor of type Core A consists of 80% deep neural network (DNN) evaluation and 20% graph processing. All the DNN work must complete before the graph processing work is started (graph processing depends on the DNN output, so they cannot be done in parallel). However, each stage itself is perfectly parallelizable. Imagine there are two possible cores, each with different performance characteristics on the DNN and graph processing workloads. The chart below gives the performance of Core B relative to core A on the two workloads (these are relative throughputs).

	Core Type	
	Core A	Core B
Resource Cost	1	1
Perf (throughput): DNN Eval	1	4
Perf (throughput): Graph Processing	1	0.5

If you had to design a multi-core processor for this workload that could have any mixture of cores so long as the total resource cost did not exceed 4, what mixture would you choose? **In your answer state (approximately) what speedup over a processor with one core of type A would you expect?** Hint: In each step of the problem its wise to parallelize work across all the chosen cores.

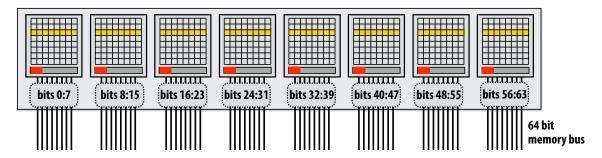
Math hint: consider a workload that spends 800 ms in DNN eval and 200 ms in graph processing on a single Core A. How much time would the computation take on a quad-core Core B processor?

Also, since the math in this problem isn't the cleanest... 200/2.5 = 80,  $200/3 \approx 67$ ,  $800/13 \approx 62$ 

P. (2 pts) Next year all CMU students will be required to take 15-418/618, which will generate increased load on the course website. To keep response times on the course website low, Tom Cortina suggests that we buy a bunch of high-end machines for webservers and keep them in the machine room at CMU. The 15-418/618 TAs, **observing the figure on the front page of this exam**, suggest an alternative way to design the website to meet this load. What is it?

### **Problem 2: Controlling DRAM**

Consider a DRAM DIMM with 8 chips (8-bit interface per chip) just like what we talked about in class and in exercise 6. Physical memory addresses are strided across the chips as in the figure below, so that 64 consecutive bits from the address space can be read in a single clock over the bus. The DRAM row size is 2 kilobits (256 bytes). There is only a single bank per chip. (We ignore banking in this problem.)



The memory controller processes requests with the following logic:

```
int active_row;  // stores active row
handle_64bit_request(void* addr) {
  int row, col;
  compute_row_col(addr, &row, &col);  // compute row/col from addr (0 cycles)
  if (row != active_row)
     activate_row(row);  // this operation takes 15 cycles
  transfer_column(col);  // this operation takes 1 cycle
}
```

Questions are on the next page...

Now consider the following C-program, which executes using 2 pthreads on a dual-core processor with a single shared cache.

```
struct ThreadArg {
  int threadId;
  double sum; // thread-local variable
           // assume this is very large
  int N;
  double* A; // pointer to shared array
};
// each thread processes one half of array A
void myfunc(void* targ) {
 ThreadArg* arg = (ThreadArg*)targ;
  arg -> sum = 0.f;
  int offset = arg->threadId * arg->N / 2;
  for (int i=0; i<arg->N / 2; i++)
   arg->sum += arg->A[offset + i];
/* main code */
ThreadArg args[2];
args[0].threadId = 0; args[1].threadId = 1;
args[0].A = args[1].A = new double[N];
// initialize args[].sum, args[].N, args[].A, and launch two pthreads here that run myfunc
// Then wait for threads to complete
print("%f\n", args[0].sum + args[1].sum);
```

- A. Assume that the two threads run at approximately the same speed, so the memory controller receives requests from the two threads in interleaved order: thread0\_req0, thread1\_req0, thread0\_req1, thread1\_req1, etc. Given this stream, what is the effective bandwidth of the memory system as observed by the processor (the rate at which it receives data)? Assume that:
  - The program is bandwidth bound so that the memory system always has a deep queue of requests to process.
  - The granularity of transfer between the memory controller and the cache is 64 bits. (e.g., 8-byte cache line size)
  - Note that array elements are DOUBLES (8 bytes).

B. Modify the program code to significantly improve the effective memory system bandwidth. What is the new bandwidth you observe?

C. Return to the original code given in this assignment (ignore your solution to part B), and assume that requests now arrive at the memory controller every ten cycles. For example...

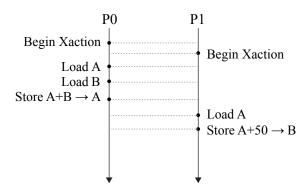
```
cycle 0: thread 0 req 0 cycle 10: thread 1 req 0 cycle 20: thread 0 req 1 cycle 30: thread 1 req 1 cycle 40: thread 0 req 2 cycle 50: thread 1 req 2 cycle 60: thread 0 req 3
```

Write (rough) pseudocode for a memory request scheduling algorithm that allowed the memory system to keep up with this request stream. Your implementation can assume there is an incoming request buffer called request\_buf that holds up to 4 requests. (The processor stalls if the request buffer is full.)

D. (TRICKY, YOU MAY WANT TO COME BACK TO THIS ONE) You add hardware multi-threading to your dual-core processor (2 threads-per core) and spawn four pthreads in your code. You assign contiguous blocks of the input array to each pthread. Assuming the request arrival rate stays the same (but now requests from four threads, rather than two, are interleaved), how would you change your solution in part C to keep up with the request stream? (you may modify the buffer size if need be). Is overall memory latency higher or lower than in part C? Why?

## **Problem 3: Transactional Memory**

A. Consider the following schedule of operations performed by processors P0 and P1.



Assume that at the start of the program A=0 and B=100 and that this system implements **lazy**, **optimistic** transactional memory.

Notice that the schedule above does not designate when the end of transactions occur. Fill in the table below for each possible schedule of transaction commits. Indicate whether P0 or P1 (or both) execute a rollback, and fill in the final values of A and B after **both transactions are complete**.

Important! For row 3, you may wish to state your assumptions about the details of the transactional memory implementation to justify your answer.

	P0 rollback (y/n)	P1 rollback (y/n)	A	В
P0 reaches end of transaction be-				
fore P1 (but after P1's performs				
loads/stores to A and B)				
P1 reaches end of transaction be-				
fore P0				
P0 reaches end of transaction be-				
fore P1 performs loads/stores to				
A and B)				

#### Problem 4: Paparazzi Camera

You are designing a heterogeneous multi-core processor to perform real-time "celebrity detection" on a future camera. The camera will continuously process low-resolution live video and snap a high-resolution picture whenever it identifies a subject in a database of 100 celebrities. Pseudocode for its behavior is below:

```
void process_video_frame(Image input_frame)
{
   Image face_image = detect_face(input_frame);
   for (int i=0; i<100; i++)
      if (match_face(face_image, database_face[i]))
        take_high_res_photo();
}</pre>
```

In order to not miss the shot, the camera MUST call take\_high\_res\_photo within 500 ms of the start of the original call to process\_video\_frame! To keep things simple:

- Assume the code loops through all 100 database images regardless of whether a match is found (e.g., we want to find all matches).
- The system has plenty of bandwidth for any number of cores.

Two types of cores are available to use in your chip. One is a fixed-function unit that accelerates detect\_face, the other is a general-purpose processor. The cost (in chip resources) of the cores and their performance (in ms) executing important functions in the pseudocode are given below:

Operation	Core Type	
	C1 (fixed-function) C2 (Programmable)	
Resource Cost	1	1
Perf (ms): detect_face	100	400
Perf (ms): match_face	N/A	20

A. Assume a video frame arrives exactly every 500 ms. **If you only use cores of type C2**, how many cores do you need to meet the performance requirement for the video stream? (You cannot change the algorithm, and please justify your answer).

B. Your team has just built a multi-core processor that contains a large number of cores of type C2. It achieves  $5.9\times$  speedup on the camera workload discussed above. Amdahl's Law says that the maximum speedup of the camera pipeline in this problem should be  $2400/400 = 6\times$ , so your team is happy. They are shocked when your boss demands a speedup of  $10\times$ . Your team is on the verge of quitting due "unreasonable demands". How do you argue to them that the goal is reasonable one if they consider all the possibilities in the above table? (Hint: What assumption are they making in their Amdahl's Law calculations, and why does it not hold?)

.

C. Now assume you can use both cores of types C1 and C2 in your design. How many of each core do you choose to minimize resource usage, while still meeting the same performance requirements as in part A? Does your new chip use more or fewer total resources than your solution in part A (by how much)?

D. Beyonce is about to release a new album, and your paparazzi customers want to follow her around all day. They request a camera that is more energy efficient. Energy efficiency is so important they are willing to relax their performance requirement and allow high-res photos to be taken within 1500 ms (not 500 ms) of a video frame arriving. You find that the primary consumer of power in your application is loading database faces from memory. Describe how you would change the pseudocode to **approximately double** the energy efficiency of the camera while still meeting the performance requirements. You should assume you use the same processor design as in part C (or part A for that matter), and that your processor has a cache that holds up to 4 database images.

#### **Problem 5: A Lock-Free Stack**

In class we discussed the following implementation of a lock-free stack of integers.

```
// CAS function prototype: update address with new_value if its contents
// match expected_value. Return value of addr (at start of operation).
Node* compare_and_swap(Node** addr, Node* expected_value, Node* new_value);
struct Node {
 Node* hello;
  int value;
struct Stack {
 Node∗ top;
void init(Stack* s) {
 s->top = NULL;
void push(Stack* s, Node* n) {
 while (1) {
   Node* old_top = s->top;
   n->next = old_top;
   if (compare_and_swap(&s->top, old_top, n) == old_top)
Node* pop(Stack* s) {
 while (1) {
   Node* top = s->top;
    if (top == NULL)
     return NULL;
   Node* new_top = top->next;
   if (compare_and_swap(&s->top, top, new_top) == top)
      return top;
}
```

A. We talked about how this implementation could fail due to the "ABA problem". What is the ABA problem? Describe a sequence of operations that causes it.

В.	Even though the above implementation is lock free, it does not mean it is free of contention. In a system with P processors, imagine a situation where all P processors are contending to pop from the stack. Describe a potential performance problem with the current implementation and describe one potential solution strategy. (A simple descriptive answer is fine.)

## **Problem 6: Deletion from a Binary Tree**

The code below, and continuing on the following two pages implements node deletion from a binary search tree. We have left space in the code for you to insert locks to ensure thread-safe access and high concurrency. You may assume functions lock(x) and unlock(x) exist (where x has type Lock). Your solution NEED ONLY consider the delete operation.

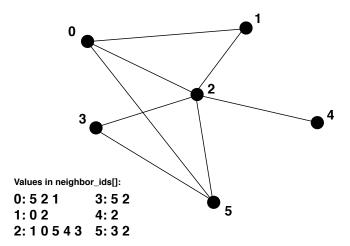
```
// opaque definition of a lock. You can call 'lock' and 'unlock' on
// instances of this type
struct Lock;

// definition of a binary search tree node. You may edit this structure.
struct Node {
   int value;
   Node* left;
   Node* right;
   Lock lock;
};
```

```
// Delete node containing value given by 'value'
// Note: For simplicity, assume that the value to be deleted is not the root node!!!
void delete_node(Node* root, int value) {
   Node** prev_link = NULL;
                                          // pointer to link to current node
   Node* cur = root;
                                          // current node during traversal
                                          // while node not found
   while (cur) {
      if (value == cur->value) {
                                          // found node to delete!
         // Case 1: Node is leaf, so just remove it, and update the parent node's pointer to
         // this node to point to NULL
         if (cur->left == NULL && cur->right == NULL) {
            *prev_link = NULL;
            free(cur);
            return;
         } else if ( cur->left == NULL ) {
            // Case 2: Node has one child. Make parent node point to this child
            *prev_link = cur->right;
            free(cur);
            return;
         } else if ( cur->right == NULL) {
            // *** ignore this case, symmetric with previous case ***
         } else {
            // Case 3: Node has two children. Move the next larger value in the tree into this
            // position. The subroutine delete_helper returns this value and executes the swap
            // by removing the node containing the next larger value. SEE NEXT PAGE \,
            /* We need to hold cur->lock the entire time we're in the tree subtree */
            cur->value = delete_helper(cur->right, &cur->right);
            return;
      } else if (value < cur->value) {
         // still searching, traverse left
         prev_link = &cur->left;
         cur = cur->left;
      } else {
         // still searching traverse right
         // *** ignore this case, symmetric with previous case ***
      }
  }
}
```

```
// The helper method removes the smallest node in the tree rooted at node {\sf n}.
// It returns the value of the smallest node.
int delete_helper(Node* n, Node** prev) {
   Node** prev_link = prev;
   NODE* cur = n;
   // search for the smallest value in the tree by always traversing left
  while (cur->left) {
      prev_link = &cur->left;
      cur = cur->left;
  }
   // this is the smallest value
   int value = cur->value;
   // remove the node with the smallest value
   if (cur->right == NULL) {
      // Case 1: Node is a leaf
      *prev_link = null;
      free(cur);
   } else {
     // Case 2: Node has a right child
      *prev_link = cur->right;
      free(cur);
  }
   return value;
}
```

### Problem 7: Updating a Graph



```
struct Graph_node {
   Lock lock;
   float value;
   int num_edges; // number of edges connecting to node (its degree)
   int* neighbor_ids; // array of indices of adjacent nodes
};

// a graph is a list of nodes, just like in assignment 3
Graph_node graph[MAX_NODES];
```

Consider the undirected graph representation shown in the code above. The figure shows an example graph. In the bottom-left of the figure are the values in neighbor\_ids for each node.

Your boss asks you to write a program that atomically updates each graph node's value field by setting it to the average of all the values of neighboring nodes. The program must obtain a lock on the current node and all adjacent nodes to perform the update. It does so as follows...

```
void update(int id) {
    Graph_node* n = &graph[id];
    LOCK(n->lock);
    for (int i=0; i<n->num_edges; i++)
        LOCK(graph[n->neighbor_ids[i]].lock);

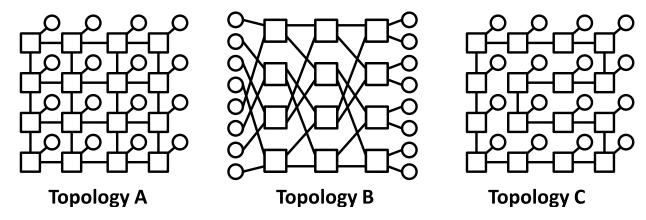
// now perform computation...
```

Question on the next page...

You run your update code in parallel on nodes 0 and 2 and deadlock occurs. Please provide a solution (a sketch in pseudocode is fine) to the deadlock problem that maintains high concurrency and limits the amount of extra work that is performed in the update function. **Hint: your solution may involve preprocessing of the graph data structure (if so, describe it).** 

### **Problem 8: Interconnection Networks**

A. The figure below shows four common network topologies (circles and squares represent network endpoints and routers respectively).

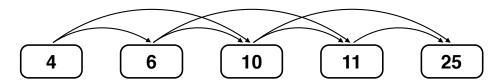


Identify each topology and fill in the table below. Express the bisection bandwidth in Gbit/s, assuming each link is 1 Gbit/s. Express the cost and latency in terms of the number of network nodes N, using Big O notation, e.g., O(logN)).

	Topology A	Topology B	Topology C
Topology Type/Name			
Direct or Indirect			
Blocking or Non-Blocking			
Bisection Bandwidth			
Cost			
Latency			

B. Briefly describe two advantages and two disadvantages of circuit-switched networks compared packet-based networks.	to
C. What common networking problem do virtual channels solve?	

### **Problem 9: Another Fine-Grained Locking Question**



Consider the semi-skip list structure pictured above. Each node maintains a pointer to the next node and the next-next node in the list. **The list must be kept in sorted order.** A node struct is given below.

```
struct Node {
  int value;
  Node* next;
  Node* skip; // note that skip == next->next
};
```

Please describe a thread-safe implementation of **node deletion** from this data structure. You may assume that deletion is the only operation the data structure supports. Please write C-like pseudocode.

To keep things simple, you can ignore edge-cases near the front and end of the list (assume that you're not deleting the first two or last two nodes in the list, and the node to delete is in the list). If you define local variables like curNode, prevNode, etc. just state your assumptions about them. However, please clearly state what per-node locks are held at the start of your process. E.g., "I start by holding locks on the first two nodes.". Full credit will only be given for solutions that maximize concurrency.

```
// delete node containing value
void delete_node(Node* head, int value) {
```

}

#### **Problem 10: Bringing Locality Back**

Justin Timberlake and Kanye West hear that Spark is all the rage and decide they are going to code up their own implementation to compete against that of the Apache project. Justin's first test runs the following Spark program, which creates four RDDs. The program takes Justin's lengthy (1 TB!) list of dancing tips and finds all misspelled words.

A. Understanding that the Spark RDD abstraction affords many possible implementations, Justin decides to keep things simple and implements his Spark runtime such that each RDD is implemented by a fully allocated array. This array is stored either in memory or on disk depending on the size of the RDD and available RAM. The array is allocated and populated at the time the RDD is created — as a result of executing the appropriate operator (map, flatmap, filter, etc.) on the input RDD.

Justin runs his program on a cluster with 10 computers, each of which has 100 GB of memory. The program gets correct results, but Justin is devastated because the program runs *incredibly slow*. He calls his friend Taylor Swift, ready to give up on the venture. Encouragingly, Taylor says, "shake it off Justin", just run your code on 40 computers. Justin does this and observes a speedup much greater than  $4 \times$  his original performance. Why is this the case?

B. With things looking good, Kanye runs off to write a new single "All of the Nodes" to use in the marketing for their product. At that moment, Taylor calls back, and says "Actually, Justin, I think you can schedule the computations much more efficiently and get very good performance with less memory and far fewer nodes." Describe how you would change how Justin schedules his Spark computations to improve memory efficiency and performance.

C. After hacking all night, the next day, Justin, Kanye, and Taylor run the optimized program on 10 nodes. The program runs for 1 hour, and then right before misspelled.count() returns, node 6 crashes. Kanye is irate! He runs onto the machine room floor, pushing Taylor aside and says, "Taylor, I have a single to release, and I don't have time to deal with rerunning your programs from scratch. Geez, I already made you famous." Taylor gives Kayne a stink eye and says, "Don't worry, it will be complete in just a few minutes." Approximately how long will it take after the crash for the program to complete? You should assume the .count() operation is essentially free. But please clearly state any assumptions about how the computation is scheduled in justifying your answer.

#### Problem 11: Two Box Blurs are Better Than One

An interesting fact is that repeatedly convolving an image with a box filter (a filter kernel with equal weights, such as the one often used in class) is equivalent to convolving the image with a Gaussian filter. Consider the program below, which runs two iterations of box blur.

```
float input[HEIGHT][WIDTH];
float temp[HEIGHT][WIDTH];
float output[HEIGHT][WIDTH];
float weight; // assume initialized to (1/FILTER_SIZE)^2
void convolve(float output[HEIGHT][WIDTH], float input[HEIGHT][WIDTH], float weight) {
  for (int j=0; j<HEIGHT; j++) {
    for (int i=0; i<WIDTH; i++) {</pre>
      float accum = 0.f;
      for (int jj=0; jj<FILTER_SIZE; jj++) {</pre>
        for (int ii=0; ii<FILTER_SIZE; ii++) {</pre>
           // ignore out-of-bounds accesses (assume indexing off the end of image is
           // handled by special case boundary code (not shown)
           // count as one math op (one multiply add)
           accum += weight * input[j-FILTER_SIZE/2+jj][i-FILTER_SIZE/2+ii];
        }
     output[j][i] = accum;
    }
  }
convolve(temp, input, weight);
convolve(output, temp, weight);
```

A. Assume the code above is run on a processor that can comfortably store FILTER\_SIZE\*WIDTH elements of an image in cache, so that when executing convolve each element in the input array is loaded from memory exactly once. What is the arithmetic intensity of the program, in units of math operations per element load?

Many times in class Prof. Kayvon emphasized the need to increase arithmetic intensity by exploiting producer-consumer locality. But sometimes it is tricky to do so. Consider an implementation that attempts to double arithmetic intensity of the program above by producing 2D chunks of output at a time. Specifically the loop nest would be changed to the following, **which now evaluates BOTH CONVOLUTIONS.** 

```
for (int j=0; j<HEIGHT; j+=CHUNK_SIZE) {</pre>
 for (int i=0; i<WIDTH; i+=CHUNK_SIZE) {</pre>
    float temp[...][...]; // you must compute the size of this allocation in 6B
    // compute required elements of temp here (via convolution on region of input)
    // Note how elements in the range temp[0][0] -- temp[FILTER_SIZE-1][FILTER_SIZE-1] are the temp
    // inputs needed to compute the top-left corner pixel of this chunk
    for (int chunkj=0; chunkj<CHUNK_SIZE; chunkj++) {</pre>
      for (int chunki=0; chunki<CHUNK_SIZE; chunki++) {</pre>
        int iidx = i + chunki;
        int jidx = j + chunkj;
        float accum = 0.f;
        for (int jj=0; jj<FILTER_SIZE; jj++) {</pre>
          for (int ii=0; ii<FILTER_SIZE; ii++) {</pre>
            accum += weight * temp[chunkj+jj][chunki+ii];
        output[jidx][iidx] = accum;
   }
 }
```

B. Give an expression for the number of elements in the temp allocation.

C. Assuming CHUNK\_SIZE is 8 and FILTER\_SIZE is 5, give an expression of the **total amount of arithmetic performed per pixel of output** in the code above. You do not need to reduce the expression to a numeric value.

D. Will the transformation given above improve or hurt performance if the original program from part A was <i>compute bound</i> for this FILTER_SIZE? Why?
E. Why might the chunking transformation described above he a readyl transformation in a mobile
E. Why might the chunking transformation described above be a useful transformation in a mobi processing setting regardless of whether or not it impacts performance?