

# Denis Ostroushko - HW1

## Problem 1

Table 1: All Potentially Confounding Variables Stratified by Treatment Group

|                              | Control Group    | Treatment Group  | SMD   |
|------------------------------|------------------|------------------|-------|
| N                            | 406              | 184              |       |
| Pre-term Pregnancy = Yes (%) | 53 (13.1)        | 18 ( 9.8)        | 0.103 |
| Birthweight (mean (SD))      | 3180.82 (727.49) | 3259.16 (574.17) | 0.120 |
| Clinic (%)                   |                  |                  | 0.150 |
| KY                           | 103 (25.4)       | 45 (24.5)        |       |
| MN                           | 123 (30.3)       | 58 (31.5)        |       |
| MS                           | 96 (23.6)        | 52 (28.3)        |       |
| NY                           | 84 (20.7)        | 29 (15.8)        |       |
| Age (mean (SD))              | 25.91 (5.52)     | 25.99 (5.60)     | 0.015 |
| Black = Yes (%)              | 180 (44.3)       | 82 (44.6)        | 0.005 |
| White = Yes (%)              | 118 (29.1)       | 27 (14.7)        | 0.354 |
| Nat.Am = Yes (%)             | 117 (28.8)       | 80 (43.5)        | 0.309 |
| Asian = Yes (%)              | 4 ( 1.0)         | 0 ( 0.0)         | 0.141 |
| Hisp (%)                     |                  |                  | 0.655 |
| No                           | 159 (39.2)       | 99 (53.8)        |       |
| Yes                          | 178 (43.8)       | 85 (46.2)        |       |
| NA                           | 69 (17.0)        | 0 ( 0.0)         |       |
| Education (%)                |                  |                  | 0.032 |
| 8-12 yrs                     | 238 (58.6)       | 107 (58.2)       |       |
| LT 8 yrs                     | 76 (18.7)        | 33 (17.9)        |       |
| MT 12 yrs                    | 92 (22.7)        | 44 (23.9)        |       |
| Public Assistance = Yes (%)  | 309 (76.1)       | 136 (73.9)       | 0.051 |
| Hypertension = Y (%)         | 9 ( 2.2)         | 6 ( 3.3)         | 0.064 |
| Diabetes = Yes (%)           | 8 ( 2.0)         | 9 ( 4.9)         | 0.161 |
| BL.Diab.Type (%)             |                  |                  | 0.191 |
| Type I                       | 1 ( 0.2)         | 4 ( 2.2)         |       |
| Type II                      | 7 ( 1.7)         | 5 ( 2.7)         |       |
| NA                           | 398 (98.0)       | 175 (95.1)       |       |
| BMI (mean (SD))              | 27.49 (6.89)     | 28.04 (7.95)     | 0.074 |
| Use.Tob (%)                  |                  |                  | 0.106 |
| No                           | 353 (86.9)       | 165 (89.7)       |       |
| Yes                          | 44 (10.8)        | 17 ( 9.2)        |       |
| NA                           | 9 ( 2.2)         | 2 ( 1.1)         |       |
| BL.Cig.Day (mean (SD))       | 0.82 (3.09)      | 0.90 (3.43)      | 0.025 |
| Use.Alc (%)                  |                  |                  | 0.090 |

|  |                |                |       |
|--|----------------|----------------|-------|
| No   | 389 (95.8)     | 178 (96.7)     |       |
| Yes  | 8 ( 2.0)       | 4 ( 2.2)       |       |
| NA   | 9 ( 2.2)       | 2 ( 1.1)       |       |
| BL.Drks.Day (mean (SD))                        | 0.04 (0.40)    | 0.03 (0.38)    | 0.013 |
| Drug.Add = NA (%)                              | 10 ( 2.5)      | 2 ( 1.1)       | 0.104 |
| Prev.preg = Yes (%)                            | 303 (74.6)     | 133 (72.3)     | 0.053 |
| N.prev.preg (mean (SD))                        | 1.87 (1.82)    | 1.67 (1.73)    | 0.114 |
| Live.PTB = Yes (%)                             | 43 (10.6)      | 9 ( 4.9)       | 0.215 |
| Any.stillbirth = Yes (%)                       | 6 ( 1.5)       | 2 ( 1.1)       | 0.035 |
| Spont.ab = Yes (%)                             | 94 (23.2)      | 52 (28.3)      | 0.117 |
| Induced.ab = Yes (%)                           | 67 (16.5)      | 8 ( 4.3)       | 0.406 |
| Any previous adverse birthing events = Yes (%) | 169 (41.6)     | 62 (33.7)      | 0.164 |
| N.living.kids (mean (SD))                      | 1.87 (1.82)    | 1.67 (1.73)    | 0.114 |
| N.qualifying.teeth (mean (SD))                 | 14.33 (6.67)   | 14.41 (6.92)   | 0.011 |
| BL.GE (mean (SD))                              | 1.42 (0.39)    | 1.49 (0.42)    | 0.173 |
| BL..BOP (mean (SD))                            | 69.12 (17.04)  | 70.08 (16.99)  | 0.057 |
| BL.PD.avg (mean (SD))                          | 2.84 (0.53)    | 2.87 (0.59)    | 0.064 |
| BL..PD.4 (mean (SD))                           | 24.80 (15.94)  | 25.67 (15.48)  | 0.055 |
| BL..PD.5 (mean (SD))                           | 9.95 (13.41)   | 10.09 (13.98)  | 0.010 |
| BL.CAL.avg (mean (SD))                         | 1.37 (0.66)    | 1.50 (0.78)    | 0.176 |
| BL..CAL.2 (mean (SD))                          | 41.29 (25.27)  | 46.10 (27.47)  | 0.183 |
| BL..CAL.3 (mean (SD))                          | 14.03 (16.05)  | 16.91 (17.80)  | 0.170 |
| BL.Calc.I (mean (SD))                          | 1.13 (0.62)    | 1.17 (0.61)    | 0.066 |
| BL.PI.I (mean (SD))                            | 1.23 (0.48)    | 1.28 (0.49)    | 0.111 |
| Birth.outcome (%)                              |                |                | 0.271 |
| Elective abortion                              | 1 ( 0.2)       | 1 ( 0.5)       |       |
| Live birth                                     | 391 (96.3)     | 183 (99.5)     |       |
| Non-live birth                                 | 14 ( 3.4)      | 0 ( 0.0)       |       |
| GA.at.outcome (mean (SD))                      | 269.18 (26.50) | 272.29 (17.48) | 0.139 |
| Preg.ended (mean (SD))                         | 0.13 (0.34)    | 0.10 (0.30)    | 0.103 |

## Problem 2

For the purpose of this problem, we need to impute categorical variables with mode values, and continuous variables with medians.

I identified Birthweight, N.prev.preg, Race\_ethnicity, and Use.Tob as variables that are subject to imputation.

### Unadjusted Treatment effect for reduction in pre-term pregnancies

- Unadjusted Average Treatment Effect (ATE) is the difference in proportions of pre-term pregnancies
- Control group experienced 13.1% of pre-term pregnancies
- Treatment group experienced 9.8% of pre-term pregnancies
- Average Treatment Effect is the difference between two means, which is -3.3

- Variance of the difference for two independent random variables is the sum of their variances, which works out to be  $7.59 \times 10^{-4}$ . Therefore, standard error for the test is 0.0276
- In order to see if the the proportion decreased for the treatment group, compared with the control group, we perform a one sided z-test:
- 5% percentile of a standard normal is -1.65
- test statistic is  $\frac{0.0327-0}{0.027} = -1.18$
- Since the test statistic is does not fall below the cutoff, we conclude that there are no statistically significant differences in the proportion of pre-term pregnancies between the control and treatment groups
- Conclusion:
  - Treatment effect: -0.033
  - Standard error 0.028
  - 95% Confidence interval: (-0.087, 0.021)

### **Unadjusted Treatment effect for increase in infant birthweights**

- Unadjusted Average Treatment Effect (ATE) is the difference is average birthweights between the two groups
- Control group showed average birthweight of 3181.5
- Treatment group showed average birthweight of 3259.2
- Average Treatment Effect is the difference between two means, which is 77.7
- Variance of the difference for two independent random variables is the sum of their variances, which works out to be 3085.7. Therefore, standard error for the test is 55.55
- In order to see if the the proportion decreased for the treatment group, compared with the control group, we perform a one sided z-test:
- 95% percentile of a standard normal is 1.65
- test statistic is  $\frac{78.33922-55.63465}{0.027} = 1.408101$
- Since the test statistic is does not fall above the cutoff, we conclude that there are no statistically significant differences in the proportion of pre-term pregnancies between the control and treatment groups
- Conclusion:

- Treatment effect: 77.68
- Standard error 55.549
- 95% Confidence interval: (-31.196, 186.557)

## Problem 3

### average (causal) treatment effect for pre-term pregnancy rates

In order to estimate potential outcomes  $Y^1$  and  $Y^0$  for each patient we fit the following regression model:

```
pregnancy_model <-
  glm(
    `Preg.ended...37.wk` ~
      Group + Race_ethnicity + Public.Asstce + Use.Tob + N.prev.preg +
      Live.PTB + BL.GE + BL..BOP + BL..PD.4 + BL..CAL.3,

    data = modeling_data,
    family = "binomial"
  )
```

Using this model, we obtain  $E[Y^1] = 0.11$  and  $E[Y^0] = 0.13$ .

Therefore, the average causal treatment effect is -0.02

Using a bootstrap procedure with 5000 replications, we obtain a standard error for the average causal treatment effect of 0.03

Therefore, using regression models and bootstrap procedure we obtain:

- Average causal treatment effect: -0.02
- Standard error of the average causal treatment effect: 0.03
- 95% Confidence interval: (-0.07, 0.04)

### average (causal) treatment effect for average birthweights

In order to estimate potential outcomes  $Y^1$  and  $Y^0$  for each patient we fit the following regression model:

```

borthweight_model <-
  lm(
    Birthweight ~
    Group *(Race_ethnicity + Public.Asstce + Use.Tob +
            N.prev.preg + Live.PTB + BL.GE + BL..BOP +
            BL..PD.4 + BL..CAL.3),

    data = modeling_data
  )

```

Using this model, we obtain  $E[Y^1] = 3266.27$  and  $E[Y^0] = 3186.97$ .

Therefore, the average causal treatment effect is 79.3

Using a bootstrap procedure with 5000 replications, we obtain a standard error for the average causal treatment effect of 56.93

Therefore, using regression models and bootstrap procedure we obtain:

- Average causal treatment effect: 79.3
- Standard error of the average causal treatment effect: 56.93
- 95% Confidence interval: (-31.71, 190.31)