

CS 575

Software Testing and Analysis

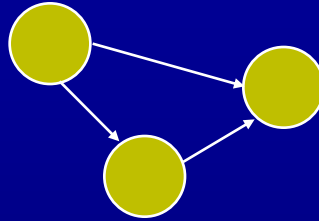
Test Coverage and Logic

Slightly modified versions of the textbook slides by Ammann & Offutt

Types of models

- **Graphs**

- E.g., prime path coverage



- **Logical expressions**

- E.g, clause coverage

(not X or not Y) and A and B

- **Input space**

- E.g., pair-wise coverage

A: {0, 1, >1}

B: {600, 700, 800}

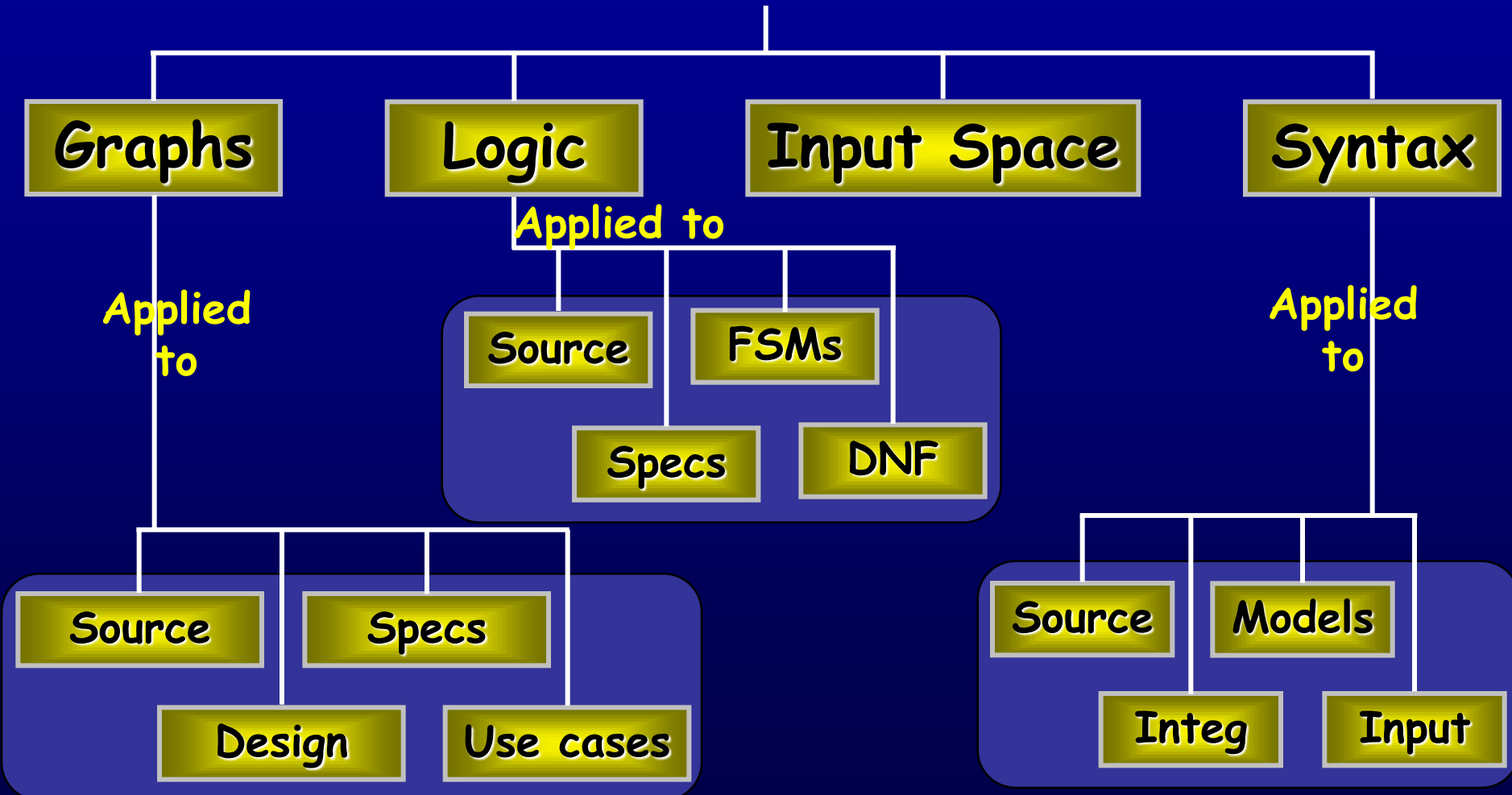
C: {swe, cs, isa, infs}

- **Syntax-based (grammars)**

- E.g., production coverage

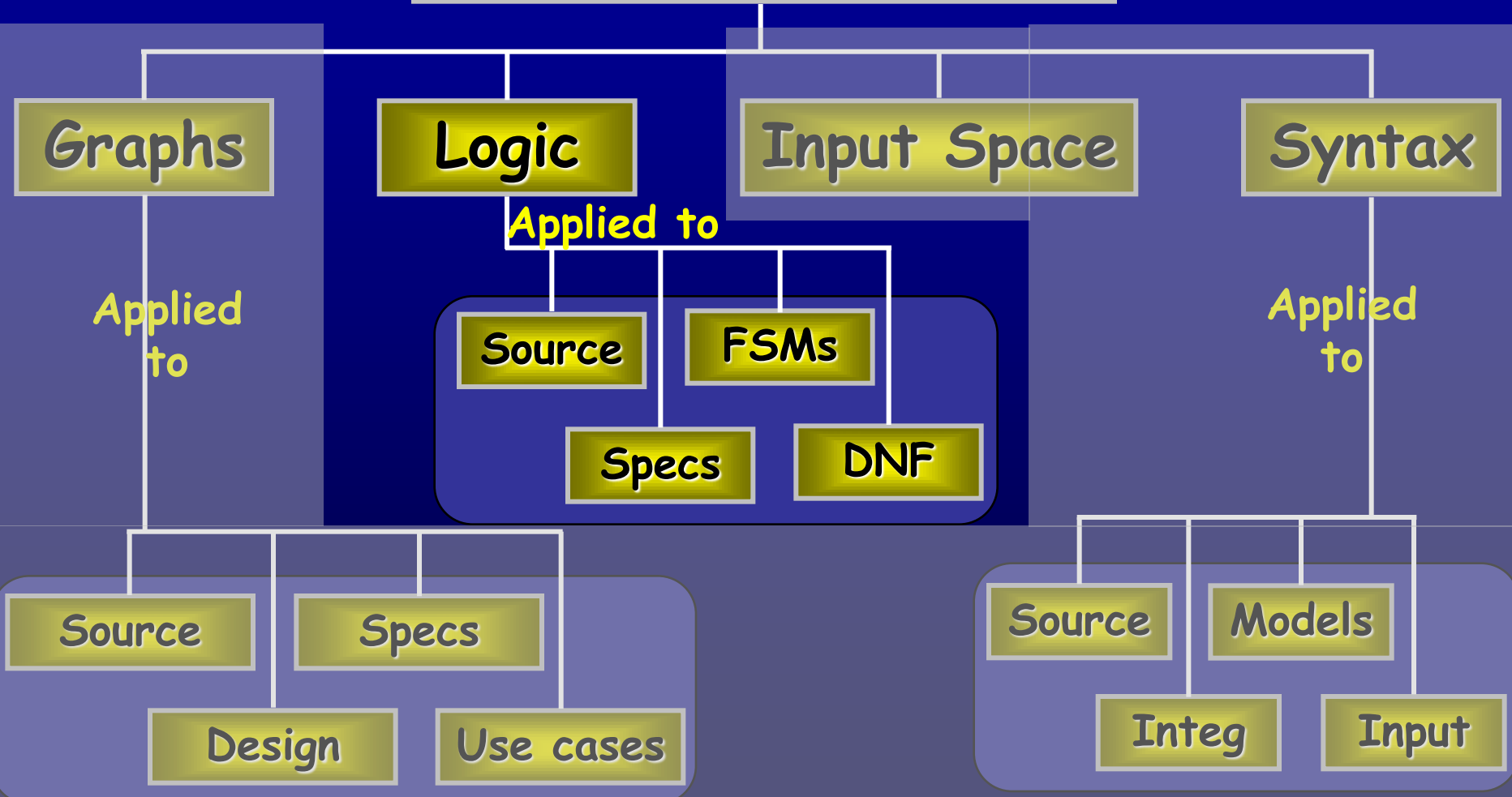
```
if (x > y)
    z = x - y;
else
    z = 2 * x;
```

Derivation of models



Ch. 3 : Logic Coverage

Four Structures for Modeling Software



Covering Logic Expressions (3.1)

- **Logic expressions show up in many situations**
- **Covering logic expressions is required by the US Federal Aviation Administration for safety critical software**
- **Tests are intended to choose some subset of the total number of truth assignments to the expressions**

Logic Predicates and Clauses

- A *predicate* is an expression that evaluates to a **boolean** value
- Predicates can contain
 - **boolean variables**
 - non-boolean variables that contain $>$, $<$, $==$, $>=$, $<=$, $!=$
 - boolean **function** calls
- Internal structure is created by logical operators
 - \neg – the *negation* operator
 - \wedge – the *and* operator
 - \vee – the *or* operator
 - \rightarrow – the *implication* operator
 - \oplus – the *exclusive or* operator
 - \leftrightarrow – the *equivalence* operator
- A *clause* is a predicate with no logical operators

Examples

- $(a < b) \vee f(z) \wedge D \wedge (m \geq n * o)$
- **Four clauses:**
 - $(a < b)$ – relational expression
 - $f(z)$ – boolean-valued function
 - D – boolean variable
 - $(m \geq n * o)$ – relational expression
- **Sources of predicates**
 - Decisions in programs
 - Guards in finite state machines
 - Decisions in UML activity graphs
 - Requirements, both formal and informal
 - SQL queries

Predicates Derived from Decisions in Programs

- Most predicates have only a **few clauses**
 - 88.5% have 1 clauses
 - 9.5% have 2 clauses
 - 1.35% have 3 clauses
 - Only .65% have 4 or more !

*from a study of 63 open
source programs,
>400,000 predicates*

Testing and Covering Predicates

- We use predicates in testing as follows :
 - Developing a model of the software as one or more predicates
 - Requiring tests to satisfy some combination of clauses
- Abbreviations:
 - P is the set of predicates
 - p is a single predicate in P
 - C is the set of clauses in P
 - C_p is the set of clauses in predicate p
 - c is a single clause in C

Predicate and Clause Coverage

- The first (and simplest) two criteria require that each predicate and each clause be evaluated to both true and false

Predicate Coverage (PC) : For each p in P , TR contains two requirements: p evaluates to true, and p evaluates to false.

- When predicates come from conditions on edges, this is equivalent to edge coverage
- PC does not evaluate all the clauses, so ...

Clause Coverage (CC) : For each c in C , TR contains two requirements: c evaluates to true, and c evaluates to false.

Predicate Coverage Example

$$((a < b) \vee D) \wedge (m \geq n * o)$$

predicate coverage

Predicate = true

$$\begin{aligned} & a = 5, b = 10, D = \text{true}, m = 1, n = 1, o = 1 \\ & = (5 < 10) \vee \text{true} \wedge (1 \geq 1 * 1) \\ & = \text{true} \vee \text{true} \wedge \text{TRUE} \\ & = \text{true} \end{aligned}$$

Predicate = false

$$\begin{aligned} & a = 10, b = 5, D = \text{false}, m = 1, n = 1, o = 1 \\ & = (10 < 5) \vee \text{false} \wedge (1 \geq 1 * 1) \\ & = \text{false} \vee \text{false} \wedge \text{TRUE} \\ & = \text{false} \end{aligned}$$

Clause Coverage Example

$$((a < b) \vee D) \wedge (m \geq n * o)$$

Clause coverage

<u>$(a < b) = \text{true}$</u>	<u>$(a < b) = \text{false}$</u>	<u>$D = \text{true}$</u>	<u>$D = \text{false}$</u>
$a = 5, b = 10$	$a = 10, b = 5$	$D = \text{true}$	$D = \text{false}$

<u>$m \geq n * o = \text{true}$</u>	<u>$m \geq n * o = \text{false}$</u>
$m = 1, n = 1, o = 1$	$m = 1, n = 2, o = 2$

Two tests

- 1) $a = 5, b = 10, D = \text{true}, m = 1, n = 1, o = 1$
2) $a = 10, b = 5, D = \text{false}, m = 1, n = 2, o = 2$

true cases

false cases

Problems with PC and CC

- **PC does not fully exercise all the clauses, especially in the presence of short circuit evaluation**
- **CC does not always ensure PC**
 - That is, we can satisfy CC without causing the predicate to be both true and false
 - This is definitely not what we want !
- **The simplest solution is to test all combinations ...**

Combinatorial Coverage

- CoC requires every possible combination
- Sometimes called Multiple Condition Coverage

Combinatorial Coverage (CoC) : For each \underline{p} in \underline{P} , TR has test requirements for the clauses in $\underline{C_p}$ to evaluate to each possible combination of truth values.

	$a < b$	D	$m \geq n * o$	$((a < b) \vee D) \wedge (m \geq n * o)$
1	T	T	T	T
2	T	T	F	F
3	T	F	T	T
4	T	F	F	F
5	F	T	T	T
6	F	T	F	F
7	F	F	T	F
8	F	F	F	F

Combinatorial Coverage

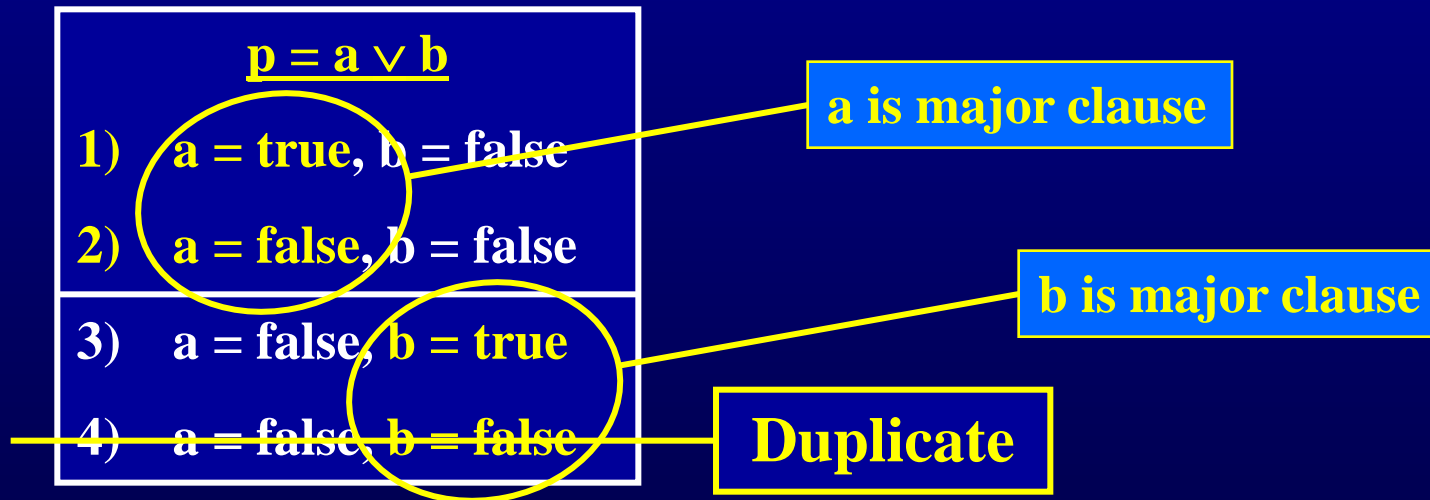
- This is simple, neat, clean, and comprehensive ...
- But quite expensive!
- 2^N tests, where N is the number of clauses
 - Impractical for predicates with more than 3 or 4 clauses
- The literature has lots of suggestions – some confusing
- The general idea is simple:

Test each clause independently from the other clauses

- Getting the details right is hard
- What exactly does “independently” mean ?
- The book presents this idea as “*making clauses active*” ...

Active Clause Coverage

Active Clause Coverage (ACC) : For each p in P and each major clause ci in Cp , choose minor clauses $cj, j \neq i$, so that ci determines p . TR has two requirements for each ci : ci evaluates to true and ci evaluates to false.



Active Clause Coverage

- This is a form of **MCDC**, which is required by the FAA for safety critical software
- **$N+1$** tests are sufficient for coverage, where **N** is the number of clauses
- **Ambiguity** : Do the minor clauses have to have the **same values** when the major clause is true and false?

Resolving the Ambiguity

$$\underline{p = a \vee (b \wedge c)}$$

Major clause : **a**

a = true, **b** = false, **c** = true

a = false, **b** = false, **c** = false

Is this allowed ?

- Separate criteria defined to avoid ambiguity
 - Minor clauses **do not** need to be the same
 - General Active Clause Coverage (GACC)
 - Minor clauses **do** need to be the same
 - Restricted Active Clause Coverage (RACC)

Exercise

```
for(n = 0;  
    n < max_size && (c = getc( yyin )) != EOF && c != '\n';  
    n++)  
    buf[n] = (char) c;
```

- Devise a set of test cases that satisfy the GACC and RACC criteria with respect to the loop condition
- Hint: There exist 3 clauses. So, 4 test cases should be sufficient to satisfy GACC and RACC

Adopted from the textbook slides by Pezze & Young

Exercise

```
for(n = 0;  
    n < max_size && (c = getc( yyin )) != EOF && c != '\n';  
    n++)  
    buf[n] = (char) c;
```

- Entries marked with "-" normally can be either of true or false to satisfy GACC. However, we should set them to true for satisfying RACC.

Test Case	$n < \text{max_size}$	$(c = \text{getc}(yyin)) \neq \text{EOF}$	$c \neq '\backslash n'$	Outcome
(1)	<u>false</u>	-	-	false
(2)	true	<u>false</u>	-	false
(3)	true	true	<u>false</u>	false
(4)	<u>true</u>	<u>true</u>	<u>true</u>	true



Test Case	$n < \text{max_size}$	$(c = \text{getc}(yyin)) \neq \text{EOF}$	$c \neq '\backslash n'$	Outcome
(1)	<u>false</u>	true	true	false
(2)	true	<u>false</u>	true	false
(3)	true	true	<u>false</u>	false
(4)	<u>true</u>	<u>true</u>	<u>true</u>	true

Correlated Active Clause Coverage

Correlated Active Clause Coverage (CACC) : For each p in P and each major clause c_i in C_p , choose minor clauses $c_j, j \neq i$, so that c_i determines p . TR has two requirements for each c_i : c_i evaluates to true and c_i evaluates to false. The values chosen for the minor clauses c_j must cause p to be true for one value of the major clause c_i and false for the other, that is, it is required that $p(c_i = \text{true}) \neq p(c_i = \text{false})$.

- A more recent interpretation
- **Implicitly** allows minor clauses to have different values
- **Explicitly** satisfies (**subsumes**) predicate coverage

CACC and RACC

	a	b	c	$a \wedge (b \vee c)$
1	T	T	T	T
2	T	T	F	T
3	T	F	T	T
4	T	F	F	F
5	F	T	T	F
6	F	T	F	F
7	F	F	T	F
8	F	F	F	F

major clause

$P_a : b = \text{true} \text{ or } c = \text{true}$

CACC can be satisfied by choosing any of rows 1, 2, 3 AND any of rows 5, 6, 7 – a total of nine pairs

	a	b	c	$a \wedge (b \vee c)$
1	T	T	T	T
2	T	T	F	T
3	T	F	T	T
4	T	F	F	F
5	F	T	T	F
6	F	T	F	F
7	F	F	T	F
8	F	F	F	F

RACC can only be satisfied by row pairs (1, 5), (2, 6), or (3, 7)

Only three pairs

Exercise by Paul Amman

- Devise a set of test cases that satisfy the CACC and RACC criteria with respect to the predicate

	a	b	c	P	P ₂
1	T	T	T		T
2	T	T		T	T
3	T		T		T
4	T			T	
5		T	T	T	T
6		T			T
7			T	T	T
8				T	

$P = \bar{a}b + a\bar{c} + \bar{a}c$

All pairs of p in Pa

- $Pa = T, a = T: 1, 2, 3$
- $Pa = T, a = F: 5, 6, 7$
- All Pairs:
 $(1,5) (2,5) (3,5)$
 $(1,6) (2,6) (3,6)$
 $(1,7) (2,7) (3,7)$
- Satisfies GACC

	a	b	c	P	P ₂
1	T	T	T		T
2	T	T		T	T
3	T		T		T
4	T			T	
5		T	T	T	T
6		T			T
7			T	T	T
8				T	

$P = \bar{a}b + a\bar{c} + \bar{a}c$

Pairs that satisfy CACC

- $Pa = T, a = T$: 1, 2, 3
- $Pa = T, a = F$: 5, 6 7
- All Pairs where P changes:
~~(1,5)~~ ~~(2,5)~~ ~~(3,5)~~
~~(1,6)~~ ~~(2,6)~~ ~~(3,6)~~
~~(1,7)~~ ~~(2,7)~~ ~~(3,7)~~

	a	b	c	P	P ₂
1	T	T	T		T
2	T	T		T	T
3	T		T		T
4	T			T	
5		T	T	T	T
6		T			T
7			T	T	T
8				T	

$P = \bar{a}b + a\bar{c} + \bar{a}c$

Pairs that satisfy RACC

- $Pa = T, a = T$: 1, 2, 3
- $Pa = T, a = F$: 5, 6, 7
- All Pairs where minor clauses remain the same:

~~(1,5)~~ ~~(2,5)~~ ~~(3,5)~~

~~(1,6)~~ ~~(2,6)~~ ~~(3,6)~~

~~(1,7)~~ ~~(2,7)~~ ~~(3,7)~~

	a	b	c	P	P ₂
1	T	T	T		T
2	T	T		T	T
3	T		T		T
4	T			T	
5		T	T	T	T
6		T			T
7			T	T	T
8				T	

$P = \bar{a}b + a\bar{c} + \bar{a}c$