Master's Thesis

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Analyzing the Information Content of Multiple Views of an Object in Object Detection with Neural Networks

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Abstract

english abstract

Zusammenfassung

deutscher abstract

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Chapter 1

Introduction

1.1 Overview

1.2 Motivation

Chapter 2

Related Work

Chapter 3

Fundamentals

This chapter covers the fundamentals necessary to understand the methods presented and their application. It is divided into a section on neural networks and one on the used software and frameworks. The former starts with the principle of a neural network. It continues with an explanation of the required steps to train the network and ends with an overview of Convolutional Neural Networks, which are networks that are more suited for image processing. The latter explains which software and frameworks support building and training a model.

3.1 Artificial Neural Networks

This section examines the types of neural networks that are important for this work. Furthermore, it explains how these types are build in order to manage the wanted use case.

3.1.1 Overview

Artificial neural networks are vaguely inspired by the biological neural networks that constitute animal brains for recognizing patterns. Its task is being an universal approximator for any unknown function $f(x) = y$ where x is the input and y the output. There are two conditions that need to be fulfilled. One is the relation of x and y and the other is the presence of numerical data. So every data like images, text or time series must be translated. The complexity of the approximated function depends on the use case but usually it is highly non-linear. General use cases for neural networks embrace classification, clustering and regression.

Classification means the network divides given data like images into categories by recognizing patterns. This is the task used in this work. The correct category of each input is given as an additional label. Therefore, the network learns the correlation between data and labels. Kind of an downside here is that every input must be labeled by human knowledge beforehand. This kind of learning is called supervised learning, because each predicted category by the network needs to be compared with the ground truth label. Use cases are for example the classification of cars in images or even the

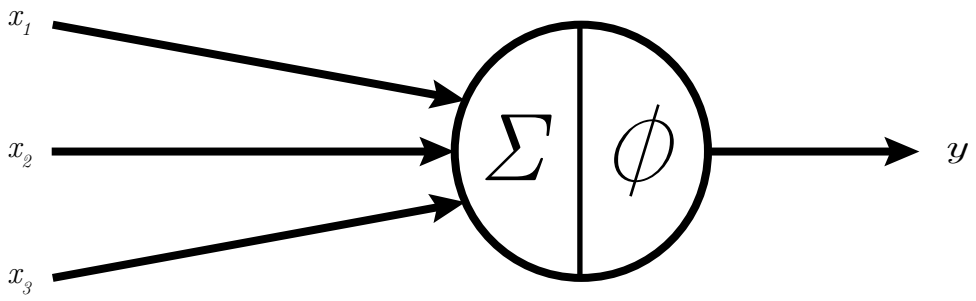


Figure 3.1: Model of a neuron. The inputs x_i are summed up and put into the activation function ϕ whose result is the neuron's output y.

type of car in an image or whether an email is spam. Again, it all depends on the wanted use case and given data.

Clustering divides data into clusters or groups, respectively, but without requiring labels. Therefore, this learning type is called unsupervised learning. So it is kind of an classification task with a dynamic category creation. Use cases are comparing data to each other and finding similarities or anomalies. Because unlabeled data occurs way more often than labeled data in real wold examples, a network can train on a broader range of related data and probably gets more accurate than a classification one.

Regression is the prediction of a future event by establishing correlations between past events and future events. A simple use case is the prediction of a price of a house given its size and the size-price data pairs of different houses. A more advanced use case is the prediction of hardware breakdowns by establishing correlations of already known data.

3.1.2 Multilayer Perceptron

This section starts with an explanation of a single computational neuron and its development to become a perceptron and ends with an overview of the multilayer perceptron architecture.

3.1.2.1 Pereptron

McCulloch and Pitts[1] were the first who defined a computational model of a neuron that corresponds to the functionality of one in neurobiology. This neuron has several logical inputs which can either be true or false and a logical output. Therefore, this neuron works as a linear classifier separating two categories where only one is the correct one. This is called binary classification. A schematic of this model can be seen in Fig. 3.2.

Because numerical values are required for later operations, every logical value is transformed to 0 if it is false or 1 if it is true. After summing up the inputs, a threshold

Table 3.1: Truth Tables of Logical Operations

(a) Logical AND

x_1	x_2	x_3	Thresh	Output
0	0		2	0
0	1		2	0
1	0		2	0
1	1		2	1
0	1	1	3	0
1	1	1	3	1

(b) Logical OR

x_1	x_2	x_3	Thresh	Output
0	0		1	0
0	1		1	1
1	0		1	1
1	1		1	1
0	0	0	1	0
0	0	1	1	1

(c) Logical XOR

x_1	x_2	x_3	Output
0	0		0
0	1		1
1	0		1
1	1		0
0	1	1	0
1	1	1	1

(d) Logical XNOR

x_1	x_2	x_3	Output
0	0		1
0	1		0
1	0		0
1	1		1
0	1	1	0
1	1	1	1

activation function is applied. In a mathematical sense

$$y = \phi\left(\sum_{i}^{n} x_i\right) \tag{3.1}$$

describes this operation where n is the amount of inputs, x_i a single input and ϕ the used activation function, in this case the threshold activation function. Plots of several activation functions including their equations are shown in Fig. 3.5. That means, if a given threshold is reached the output of the perceptron is 1 and 0 otherwise. This corresponds to the neurobiological spike of a neuron. The truth tables for the logical AND and OR operations are shown in Fig. 3.2a and Fig. 3.2b, respectively. The first one outputs true if all inputs are true. The second one outputs true if at least one input is true. It can be seen, that by changing the threshold value a different logical operation can be represented. For two inputs a threshold of 2 represents the logical AND operation. If the number of inputs are changed, a related change of the threshold still models the same operation. In this example the number of inputs is changed to 3 whereas the threshold must be changed to 3. The same procedure is valid for the logical OR operation. But here the threshold value is always 1 regardless of the amount of inputs and therefore differs to other logical operations. One limitation of this neuron type is its inability to represent exclusive logical operations like XOR and XNOR[2], whose truth tables are shown in Fig. 3.2c and Fig. 3.2d, respectively. The first one outputs true if the inputs are different. The second one outputs true if all inputs are identical which

equals an inverted XOR operation. It can easily be seen, that no threshold value can be found for meeting the requirements. For example, in the first case if the threshold is at 1 the first three combinations of inputs could be covered. If all inputs are false the threshold value is not reached and therefore the neuron outputs a 0. If the inputs differ from each other, the threshold value is reached which outputs a 1. But as soon as the fourth one needs to be classified the threshold value is no longer valid. The sum of the inputs equals two which exceeds the threshold and would output a logical true like in the OR case. But according to the truth table a logical false should be outputted. The reasons for this misbehavior are the neuron's limitation to binary values and a threshold activation function and therefore the classification of only two categories.

Donald Hebb states "When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased."[3] on how neurons learn. This means, that if a neuron repeatedly and persistently stimulates a immediately subsequent neuron, i.e. the more often two wired neurons are active, their synaptic efficacy increases. This is known as the Hebbian Theory. Hebb summarizes this with his famous quote "neurons that fire together, wire together".

Frank Rosenblatt developed the first perceptron[4]. Considering the Hebbian Theory the original McCulloch-Pitts-Neuron needs to be modified by adding associated weights for the inputs in order to simulate the strength of a synapse. Thus, Theorem 3.1 changes to

$$y = \phi\left(\sum_{i}^{n} x_i \cdot w_i\right) \tag{3.2}$$

by considering the weights w_i. Furthermore, the perceptron allows the usage of real-valued inputs and weights and uses the Heaviside step function as the activation function. According to Fig. 3.5b the Heaviside function outputs 0 if its parameter is negative and 1 otherwise. Therefore, its difference to the threshold activation function is just an offset of the threshold or bias, respectively. Adapting Fig. 3.1 to this results in Fig. **??**. There is an input with the value 1 which is weighted by the bias. Thus, when multiplied representing the bias. This result is part of the weighted sum of the inputs which is fed to an activation function whose result is the output of the perceptron. Combining this with Theorem 3.2 yields

$$y = \phi\left(x_1 \cdot w_1 + x_2 \cdot w_2 + \ldots + x_n \cdot w_n + b\right) \tag{3.3}$$

$$= \phi\left(\left(\sum_{i}^{n} x_i \cdot w_i\right) + b\right) \tag{3.4}$$

where x_i are the inputs, w_i the weights, b the bias and ϕ the Heaviside activation function.

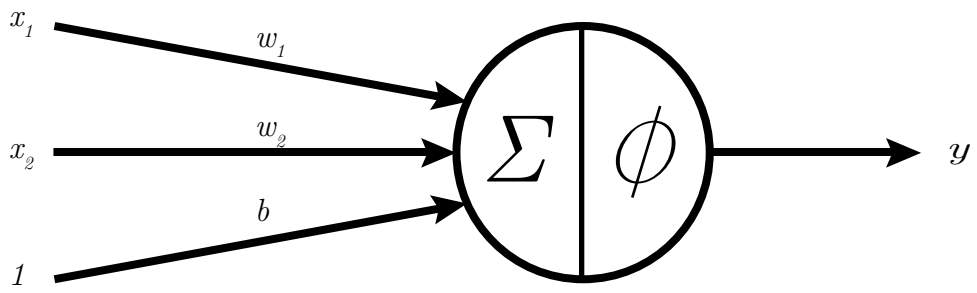


Figure 3.2: Model of a perceptron. The inputs x_i are weighted by w_i and are summed up with the bias b. This sum is put into the activation function ϕ whose result is the perceptron's output y.

Let's write the inputs and weights as vectors of

$$\boldsymbol{x} = \begin{pmatrix} x_1 & x_2 & \cdots & x_n \end{pmatrix}^T \tag{3.5}$$

$$\boldsymbol{w} = \begin{pmatrix} w_1 & w_2 & \cdots & w_n \end{pmatrix}^T \tag{3.6}$$

for simplicity. Inserting this in Theorem 3.3 results in

$$y = \phi\left(\boldsymbol{x} \cdot \boldsymbol{w^T} + b\right) \tag{3.7}$$

with the same parameters as before. However, this model still works as a linear classifier and thus is unable to represent logical exclusive functions. This can be solved by concatenating multiple perceptrons and building a multilayer artificial network.

3.1.2.2 Multilayer Perceptron

A multilayer perceptron consists of multiple perceptrons divided in layers and solves complex tasks[5]. It is an universal approximator for every function[6] regardless of the activation functions used[7]. Because of the multiple layers and the non-linear activation functions non-linearity is introduced into the network. Thus, it can distinguish data that is not linearly separable as most real world data is.

There are at least three layers. Each layer contains several perceptrons that are not connected to each other. However, every perceptron is connected to every perceptron of its subsequent layer. This type of connection is called fully-connected network. Because the data flow within the network is only in one direction and does not contain circles, the architecture is called feedforward neural network. A visualization of this is shown in Fig. 3.3. Although the weights and biases are not displayed for clarity, they still exist and follow the same principle as with a single perceptron. Like the single perceptrons every node in the networks still holds its activation, a single numerical value. In this kind of network architecture perceptrons are often referred to as nodes.

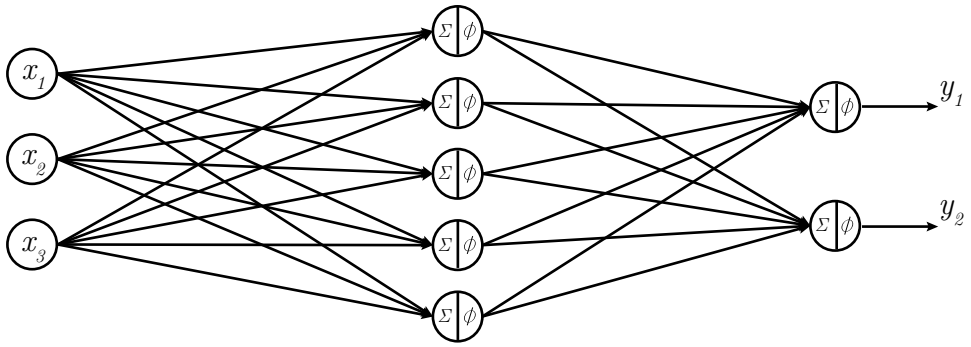


Figure 3.3: Multilayer perceptron with three layers. Each layer consists of multiple perceptrons. The input layer transfers real world data into the network. The output layer makes the computations of the network interpretable for humans. The layers inbetween, the hidden layers, perform calculations and feed forward the network data. Each connection between nodes has a weight, that is not displayed for clarity. Also every node has its own bias.

The input layer serves as an interface for the data. It does not perform any calculations and just passes the data to the next layer. The number of nodes in this layer depends on the data and how it can be divided. If the real world data is an image, for example, the number of nodes should be equal to the number of pixels, so that every node can hold the intensity value of one pixel.

The output layer is responsible for transferring the network data to the outside so that it can be interpreted and worked with. The number of nodes in this layer depends on the expected results. If kinds of animals need to be detected in an image, every output node would represent a single kind or category, respectively. Let's say there are three kinds of animals possible, then there need to be three output nodes. In theory the node representing the correct kind of animal holds a one and every other a zero, if the values are squashed within this range.

Every layer between the input and the output layer is a hidden layer. They have no direct connection to the outside, neither to the input nor the output, hence, their name. Their task is to transfer the input information to the output by performing calculations. With at least one hidden layer every continuous function can be approximated. So, the network models the function

$$f(\boldsymbol{x}) = \boldsymbol{y} \tag{3.8}$$

where

$$\boldsymbol{x} = (x_0, x_1, \cdots, x_n) \tag{3.9}$$

$$\boldsymbol{y} = (y_0, y_1, \cdots, y_m) \tag{3.10}$$

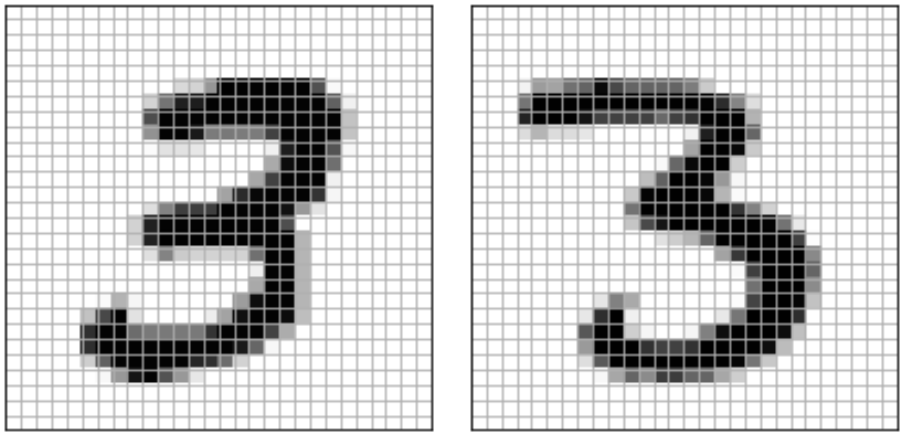


Figure 3.4: Handwritten Digits from the MNIST Digit Dataset. Represented as a 28×28 pixel matrix. Each cell represents a pixel.

are the input vector with n elements and output vector with m elements, respectively. Every element represents the activation of a neuron in the input layer or output layer, respectively.

Let's take again an image as an example. The task is to classify a handwritten digit from the MNIST dataset[8]. The digit can be seen in Fig. 3.4. Each grid cell represents a pixel. Now it is evidently that the intensity data of every pixel is relevant for classifying the digit. Thus, every pixel needs an associated node in the input layer of the network. This real world data is transferred into the network by flattening the intensity values of the image matrix to a vector. Therefore, the vector contains $28 \cdot 28 = 784$ elements which equals the number of input nodes. With the correct weights and biases the network knows which nodes are active for a certain digit. This means, that if in another image more or less the same pixels or nodes, respectively, have high intensities or activations, the same number needs to be classified. The downside of the flattening is, that every relation of pixels like position is lost, which means a loss in overall information. The consequence of this is, that if a digit has no similar position and shape like the digits the networks knows, the classification fails. If, for example, a digit the network classified correctly is not centered anymore and downscaled to take up only have its original size, completely different neurons are active. And, thus, the network cannot find any correlation to the original image or its knowledge of how digits look and returns a wrong classification result. Another severe downside is the huge number of parameters. If the image gets larger, the number of input neurons naturally needs to be adapted. Due to

this, additional weights and biases are introduced to the network, because every input neuron is connected to every node of its subsequent layer. This extends the finding of the optimal weights and biases and needs plenty of resources. A better solution is provided by convolutional neural networks that are covered in Section 3.1.3.

3.1.2.3 Training

Thus far optimal weights and biases were assumed.

Expressing the activation of every node with Theorem 3.3 would get very complex with only a few nodes. Hence, a matrix notation is the way to go in the long run. First, for every layer a vector is build

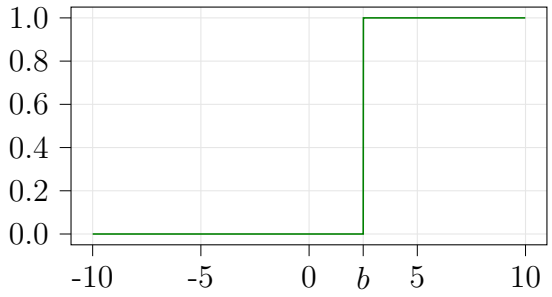
3.1.2.4 Improving Performance

3.1.3 Convolutional Neural Networks

Convolutional neural networks are suited for image processing tasks, because they perform better than the multilayer perceptrons architecture regarding accuracy and the number of parameters[8][9]. The reason for the first one is most likely that they are invariant regarding the position of an object within an image. Convolutional neural networks do not have a as strict separation in multiple layers as multilayer perceptrons do. They rather have a pool of several layers which can be arbitrarily connected to fulfill one's needs.

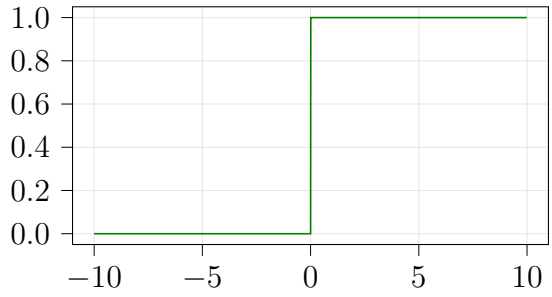
3.1.3.1 Convolutional Layer

The most important layer is the convolutional layer. As the name suggests it performs a convolution with a filter matrix of arbitrary size on an input matrix of arbitrary size. Let's say the input matrix is an image $\boldsymbol{X} \in \mathbb{R}^{m \times n}$. The filter matrix $\boldsymbol{K} \in \mathbb{R}^{i \times j}$ contains $i \cdot j$ weights of the network. The filter is now slid across the image and performs a dot product within its window. Fig. 3.6 illustrates the following operation. In reference to the figure the kernel covers the four elements in the top right corner of the input image. Hence, the dot product multiplication for this setup yields $5 \cdot 1 + 4 \cdot -1 + 1 \cdot -1 + 3 \cdot 1 = 3$. This result is stored in a new matrix at its corresponding place. At the end, this matrix will hold all values of the convolution operation. After each calculation of the dot product, the filter matrix moves. The corresponding step size is called stride. A stride of 1 moves the filter one pixel or element, respectively. There can be a different stride along the x-axis and y-axis. When the filter has moved across the whole input, the resulting matrix is completely filled up like the one in the figure. This resulting matrix is called a feature map, because the convolution extracted features from its input. Doing this operation the feature map is always smaller than the input. Sometimes this is not desirable, because this means a loss in information. If multiple convolutions are performed, the feature map constantly shrinks until no feature can be extracted



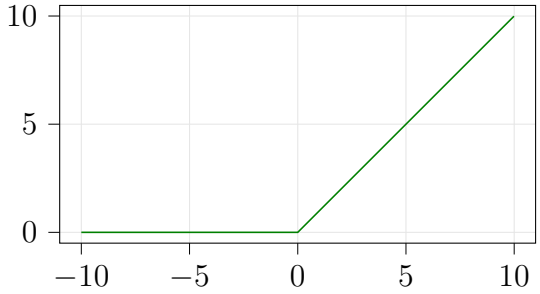
$$\phi(x) = \begin{cases} 1 & x \geq \text{Bias } b \\ 0 & x < \text{Bias } b \end{cases}$$

(a) Threshold



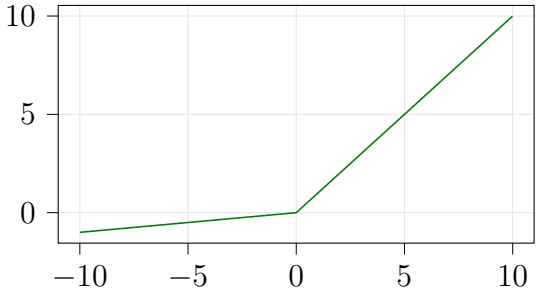
$$\phi(x) = \begin{cases} 1 & x \geq 0 \\ 0 & x < 0 \end{cases}$$

(b) Heaviside



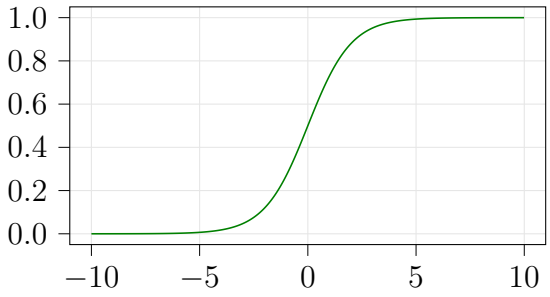
$$\phi(x) = \begin{cases} x & x \geq 0 \\ 0 & x < 0 \end{cases}$$

(c) Rectified Linear Unit



$$\phi(x) = \begin{cases} x & x \geq 0 \\ x \cdot \text{Slope } s & x < 0 \end{cases}$$

(d) Leaky Rectified Linear Unit



$$\phi(x) = \frac{1}{1 + \exp(-x)}$$

(e) Sigmoid

Figure 3.5: Plots and equations of common used activation functions. Where the Bias b is the threshold value and s adds a small slope. Usually, the latter is very small.

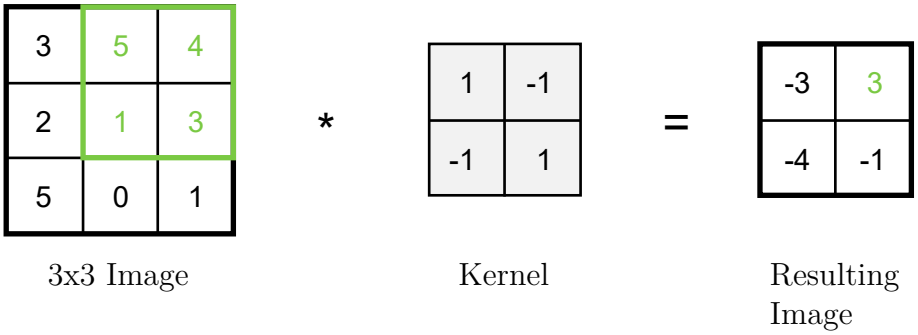


Figure 3.6: Convolution of an image and a kernel. The 2×2 kernel is sled across the 3×3 image and performs a dot product multiplication within its window each time. Here, the kernel moves with a stride of 1, which results in the shown image on the right, the so called feature map.

anymore or only rough ones. Thus, a padding p can be applied to the input. This means surrounding the input with p rounds of zeros like it is illustrated in Fig. 3.7 with $p = 1$. The convolution operates like usual, just on a larger input. In practical terms, there are two common conventions for convolutions: valid and same. The first defines that no padding is applied and therefore a kind of valid convolution is performed, because only the real input is minded. This means that the feature map has a size of $\boldsymbol{F} \in \mathbb{R}^{m-i+1 \times n-j+1}$. The latter means, that the size of the feature map equals the one of the input. How much padding p needs to be applied can be calculated by comparing each matrix shapes and using

$$m = m + 2p - i + 1 \tag{3.11}$$

$$p = \frac{i-1}{2} \tag{3.12}$$

as a general equation. However, this only covers the padding height. If the image or filter are not symmetrical, the padding along the width needs to be calculated as well by replacing m with n and i with j. Another remark is, that in computer vision filter sizes usually are odd. There can be two reasons for this. First, the filter has a center which helps to tell where exactly the filter points to. Second, the padding p is even. Otherwise, it needs to be rounded up for a correct mathematical representation, but only used on two sides of the image like it is shown in the figure with the help of transparency. Only the padding at the right and at the bottom are taken into account for creating a filter matrix with the same shape of the original input.

The kernel in the figure would find top-left to bottom-right diagonal features, because those are the pixels weighted most. Like this but with slightly larger kernels and different weights more complex features can be found. It is also possible to perform multiple different convolutions on the same input for finding different features. They are stored as a matrix, where every feature represents the depth of the feature map. This whole

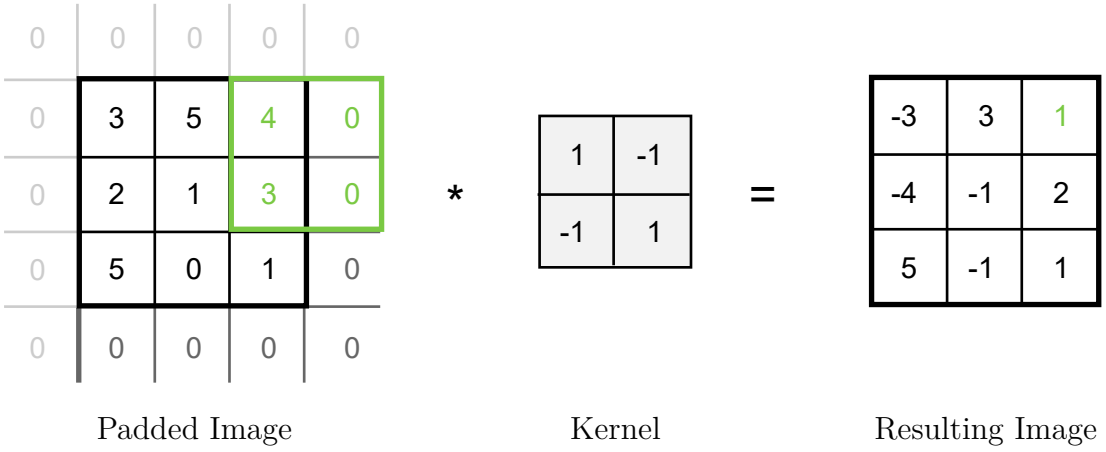


Figure 3.7: Convolution of a padded image with a 2×2 kernel. The 3×3 image is surrounded with zeros for inducing its size to the feature map. However, the convolution operates like usual, just on a larger input. If the amount padding is odd, a padding at the right and at the bottom is preferred.

process solves the limitation to a fixed position of features of the multilayer perceptrons architecture. Even if, for example, a digit covers only have the image, all features are found, because the kernel is moved over the image and not single neurons are responsible for single pixels. Furthermore, because features are found by a moving filter, convolutional neural networks need way less weights and biases due to the possibility of reusing them. The accuracy compared to multilayer perceptron networks is improved by concatenating several convolutions. That means a convolution is performed on the feature map of an earlier convolution. First, rough features like edges are found, and the deeper it gets into the network, the finer the features get.

3.1.3.2 Pooling Layer

3.1.3.3 Fully-Connected Layer

3.2 Software

This section focuses on explaining which software and frameworks are used for implementing the network and generating the dataset.

Chapter 4

Methods

Chapter 5

Results

Chapter 6

Discussion

6.1 Conclusions

6.2 Outlook

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