COSE471 hw3

GAOZHONGSONG

TOTAL POINTS

20 / 20

QUESTION 1

1 Q1 3 / 3

✓ + 3 pts Correct

+ 0 pts Wrong

QUESTION 2

2 Q2 2 / 2

✓ + 2 pts Correct

+ 0 pts Wrong

QUESTION 3

3 Q3 1 / 1

✓ + 1 pts Correct

+ 0 pts Wrong

QUESTION 4

4 Q4 1 / 1

✓ + 1 pts Correct

+ 0 pts Wrong

QUESTION 5

5 Q5 2 / 2

✓ + 2 pts Correct

+ 0 pts Wrong

QUESTION 6

6 Q6 2 / 2

✓ + 2 pts Correct

+ 0 pts Wrong

QUESTION 7

7 Q7a 1 / 1

✓ + 1 pts Correct

+ 0 pts Wrong

QUESTION 8

8 Q7b 2 / 2

✓ + 2 pts Correct

+ 0 pts Wrong

QUESTION 9

9 Q8a 1 / 1

✓ + 1 pts Correct

+ 0 pts Wrong

QUESTION 10

10 Q8b 1 / 1

✓ + 1 pts Correct

+ 0 pts Wrong

QUESTION 11

11 Q8c 2 / 2

✓ + 2 pts Correct

+ 0 pts Wrong

QUESTION 12

12 Q8d 2 / 2

✓ + 2 pts Correct

+ 0 pts Wrong

In [7]:
```
training_data['SalePrice'].describe()
```

Out[7]:
```
count      2000.000000
mean     180775.897500
std       81581.671741
min        2489.000000
25%      128600.000000
50%      162000.000000
75%      213125.000000
max      747800.000000
Name: SalePrice, dtype: float64
```

Question 1

To check your understanding of the graph and summary statistics above, answer the following `True` or `False` questions:

1. The distribution of `SalePrice` in the training set is left-skew.
2. The mean of `SalePrice` in the training set is greater than the median.
3. At least 25% of the houses in the training set sold for more than $200,000.00.

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned each variable to `True` *or* `False`*.*

In [8]:
```
# These should be True or False
q1statement1 = False
q1statement2 = True
q1statement3 = True
```

In [9]:
```
ok.grade("q1");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------

Test summary
    Passed: 4
    Failed: 0
[oooooooooook] 100.0% passed
```

1 Q1 3 / 3

✓ + 3 pts Correct

+ 0 pts Wrong

There's certainly an association, and perhaps it's linear, but the spread is wider at larger values of both variables. Also, there are two particularly suspicious houses above 5000 square feet that look too inexpensive for their size.

Question 2

What are the Parcel Indentification Numbers for the two houses with `Gr_Liv_Area` greater than 5000 sqft?

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned `q2house1` *and* `q2house2` *to two integers that are in the range of PID values.*

In [19]:
```
# BEGIN YOUR CODE
# ------------------------
# Hint: You can answer this question in one line
q2house1, q2house2 = training_data.loc[training_data['Gr_Liv_Area'] > 5000]['PID']
# ------------------------
# END YOUR CODE
```

In [20]:
```
ok.grade("q2");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------
Test summary
    Passed: 5
    Failed: 0
[oooooooooook] 100.0% passed
```

2 Q2 2 / 2

✓ **+ 2 pts** **Correct**

+ 0 pts Wrong

Question 3

The codebook tells us how to manually inspect the houses using an online database called Beacon. These two houses are true outliers in this data set: they aren't the same time of entity as the rest. They were partial sales, priced far below market value. If you would like to inspect the valuations, follow the directions at the bottom of the codebook to access Beacon and look up houses by PID.

For this assignment, we will remove these outliers from the data. Write a function `remove_outliers` that removes outliers from a data set based off a threshold value of a variable. For example, `remove_outliers(training_data, 'Gr_Liv_Area', upper=5000)` should return a data frame with only observations that satisfy `Gr_Liv_Area` less than or equal to 5000.

The provided tests check that training_data was updated correctly, so that future analyses are not corrupted by a mistake. However, the provided tests do not check that you have implemented remove_outliers correctly so that it works with any data, variable, lower, and upper bound.

In [28]:
```
def remove_outliers(data, variable, lower=-np.inf, upper=np.inf):
    """
    Input:
      data (data frame): the table to be filtered
      variable (string): the column with numerical outliers
      lower (numeric): observations with values lower than this will be removed
      upper (numeric): observations with values higher than this will be removed

    Output:
      a winsorized data frame with outliers removed

    Note: This function should not change mutate the contents of data.
    """
    # BEGIN YOUR CODE
    # ------------------------
    return data.loc[(data[variable]<=upper) & (data[variable]>=lower)]
    # ------------------------
    # END YOUR CODE

training_data = remove_outliers(training_data, 'Gr_Liv_Area', upper=5000)
```

In [29]:
```
ok.grade("q3");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
Running tests

---------------------------------------------------------------------
Test summary
    Passed: 5
    Failed: 0
[oooooooooook] 100.0% passed
```

Part 2: Feature Engineering

In this section we will create a new feature out of existing ones through a simple data transformation.

Bathrooms

Let's create a groundbreaking new feature. Due to recent advances in Universal WC Enumeration Theory, we now know that Total Bathrooms can be calculated as:

$$\text{TotalBathrooms} = (\text{BsmtFullBath} + \text{FullBath}) + \frac{1}{2}(\text{BsmtHalfBath} + \text{HalfBath})$$

The actual proof is beyond the scope of this class, but we will use the result in our model.

Question 4

Write a function `add_total_bathrooms(data)` that returns a `copy of data` with an additional column called `TotalBathrooms` computed by the formula above.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

3 Q3 **1 / 1**

✓ **+ 1 pts** **Correct**

+ 0 pts Wrong

In [32]:
```
def add_total_bathrooms(data):
    """
    Input:
      data (data frame): a data frame containing at least 4 numeric columns
            Bsmt_Full_Bath, Full_Bath, Bsmt_Half_Bath, and Half_Bath
    """
    with_bathrooms = data.copy()
    bath_vars = ['Bsmt_Full_Bath', 'Full_Bath', 'Bsmt_Half_Bath', 'Half_Bath']
    weights = pd.Series([1, 1, 0.5, 0.5], index=bath_vars)
    with_bathrooms = with_bathrooms.fillna({var: 0 for var in bath_vars})
    # BEGIN YOUR CODE
    # ------------------------
    with_bathrooms['TotalBathrooms'] = with_bathrooms[bath_vars].dot(weights)
    # ------------------------
    # END YOUR CODE
    return with_bathrooms

training_data = add_total_bathrooms(training_data)
```

In [33]:
```
ok.grade("q4");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------

Test summary
    Passed: 4
    Failed: 0
[oooooooooook] 100.0% passed
```

Question 5

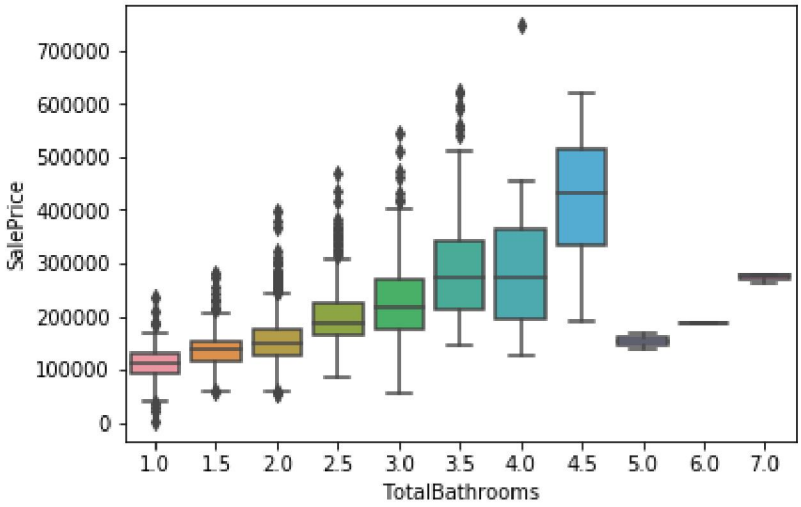
Create a visualization that clearly and succintly shows that `TotalBathrooms` is associated with `SalePrice`. Your visualization should avoid overplotting.

4 Q4 1 / 1

✓ **+ 1 pts** **Correct**

+ 0 pts Wrong

In [35]:
```
# BEGIN YOUR CODE
# ------------------------
sns.boxplot(x="TotalBathrooms", y="SalePrice", data=training_data);
# ------------------------
# END YOUR CODE
```



Part 3: Modeling

We've reached the point where we can specify a model. But first, we will load a fresh copy of the data, just in case our code above produced any undesired side-effects. Run the cell below to store a fresh copy of the data from `ames_train.csv` in a dataframe named `full_data`. We will also store the number of rows in `full_data` in the variable `full_data_len`.

In [36]:
```
# Load a fresh copy of the data and get its length
full_data = pd.read_csv("./data/ames_train.csv")
full_data_len = len(full_data)
full_data.head()
```

Out[36]:

	Order	PID	MS_SubClass	MS_Zoning	Lot_Frontage	Lot_Area	Street	Alley
0	1	526301100	20	RL	141.0	31770	Pave	NaN
1	2	526350040	20	RH	80.0	11622	Pave	NaN
2	3	526351010	20	RL	81.0	14267	Pave	NaN
3	4	526353030	20	RL	93.0	11160	Pave	NaN
4	5	527105010	60	RL	74.0	13830	Pave	NaN

5 rows × 82 columns

5 Q5 **2 / 2**

✓ **+ 2 pts** **Correct**

+ 0 pts Wrong

Question 6

Now, let's split the data set into a training set and test set. We will use the training set to fit our model's parameters, and we will use the test set to estimate how well our model will perform on unseen data drawn from the same distribution. If we used all the data to fit our model, we would not have a way to estimate model performance on unseen data.

"Don't we already have a test set in `ames_test.csv`?" you might wonder. The sale prices for `ames_test.csv` aren't provided, so we're constructing our own test set for which we know the outputs.

In the cell below, split the data in `full_data` into two DataFrames named `train` and `test`. Let `train` contain 80% of the data, and let `test` contain the remaining 20% of the data.

To do this, first create two NumPy arrays named `train_indices` and `test_indices`. `train_indices` should contain a *random* 80% of the indices in `full_data`, and `test_indices` should contain the remaining 20% of the indices. Then, use these arrays to index into `full_data` to create your final `train` and `test` DataFrames.

The provided tests check that you not only answered correctly, but ended up with the exact same train/test split as our reference implementation. Later testing is easier this way.

In [40]:
```
# This makes the train-test split in this section reproducible across different runs
# of the notebook. You do not need this line to run train_test_split in general
np.random.seed(1337)
shuffled_indices = np.random.permutation(full_data_len)

# Set train_indices to the first 80% of shuffled_indices and and test_indices to the re
st.
# BEGIN YOUR CODE
# ------------------------
train_indices = shuffled_indices[:int(len(shuffled_indices)*0.8)]
test_indices = shuffled_indices[int(len(shuffled_indices)*0.8):]
# ------------------------
# END YOUR CODE

# Create train and test` by indexing into `full_data` using
# `train_indices` and `test_indices`
# BEGIN YOUR CODE
# ------------------------
train = full_data.loc[train_indices]
test = full_data.loc[test_indices]
# ------------------------
# END YOUR CODE
```

In [41]:
```
ok.grade("q6");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------

Test summary
    Passed: 6
    Failed: 0
[oooooooooook] 100.0% passed
```

Reusable Pipeline

Throughout this assignment, you should notice that your data flows through a single processing pipeline several times. From a software engineering perspective, it's best to define functions/methods that can apply the pipeline to any dataset. We will now encapsulate our entire pipeline into a single function `process_data_gm`. gm is shorthand for "guided model". We select a handful of features to use from the many that are available.

In [42]:
```
def select_columns(data, *columns):
    """Select only columns passed as arguments."""
    return data.loc[:, columns]

def process_data_gm(data):
    """Process the data for a guided model."""
    data = remove_outliers(data, 'Gr_Liv_Area', upper=5000)

    # Transform Data, Select Features
    data = add_total_bathrooms(data)
    data = select_columns(data,
                          'SalePrice',
                          'Gr_Liv_Area',
                          'Garage_Area',
                          'TotalBathrooms',
                         )

    # Return predictors and response variables separately
    X = data.drop(['SalePrice'], axis = 1)
    y = data.loc[:, 'SalePrice']

    return X, y
```

Now, we can use `process_data_gm` to clean our data, select features, and add our `TotalBathrooms` feature all in one step! This function also splits our data into `X`, a matrix of features, and `y`, a vector of sale prices.

Run the cell below to feed our training and test data through the pipeline, generating `X_train`, `y_train`, `X_test`, and `y_test`.

6 Q6 2 / 2

✓ **+ 2 pts** **Correct**

+ 0 pts Wrong

In [43]:
```
# Pre-process our training and test data in exactly the same way
# Our functions make this very easy!
X_train, y_train = process_data_gm(train)
X_test, y_test = process_data_gm(test)
```

Fitting Our First Model

We are finally going to fit a model! The model we will fit can be written as follows:

$$\text{SalePrice} = \theta_0 + \theta_1 \cdot \text{Gr\_Liv\_Area} + \theta_2 \cdot \text{Garage\_Area} + \theta_3 \cdot \text{TotalBathrooms}$$

In vector notation, the same equation would be written:

$$y = \theta \cdot x$$

where y is the SalePrice, θ is a vector of all fitted weights, and x contains a 1 for the bias followed by each of the feature values.

Note: Notice that all of our variables are continuous, except for `TotalBathrooms`, which takes on discrete ordered values (0, 0.5, 1, 1.5, ...). In this homework, we'll treat `TotalBathrooms` as a continuous quantitative variable in our model, but this might not be the best choice. The next homework may revisit the issue.

Question 7a

We will use a `sklearn.linear_model.LinearRegression` (https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LinearRegression.html) object as our linear model. In the cell below, create a `LinearRegression` object and name it `linear_model`.

Hint: See the `fit_intercept` parameter and make sure it is set appropriately. The intercept of our model corresponds to θ_0 in the equation above.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [44]:
```
from sklearn import linear_model as lm

# BEGIN YOUR CODE
# ------------------------
linear_model = lm.LinearRegression(fit_intercept=True)
# ------------------------
# END YOUR CODE
```

In [45]:
```
ok.grade("q7a");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------------

Test summary
    Passed: 2
    Failed: 0
[oooooooooook] 100.0% passed
```

Question 7b

Now, remove the commenting and fill in the ellipses . . . below with `X_train`, `y_train`, `X_test`, or `y_test`.

With the ellipses filled in correctly, the code below should fit our linear model to the training data and generate the predicted sale prices for both the training and test datasets.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [47]:
```
# Uncomment the lines below and fill in the ... with X_train, y_train, X_test, or y_tes
t.
# BEGIN YOUR CODE
# ------------------------
linear_model.fit(X_train, y_train)
y_fitted = linear_model.predict(X_train)
y_predicted = linear_model.predict(X_test)
# ------------------------
# END YOUR CODE
```

In [48]:
```
ok.grade("q7b");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------------

Test summary
    Passed: 2
    Failed: 0
[oooooooooook] 100.0% passed
```

7 Q7a **1 / 1**

✓ **+ 1 pts** **Correct**

+ 0 pts Wrong

In [45]:
```
ok.grade("q7a");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------------

Test summary
    Passed: 2
    Failed: 0
[oooooooooook] 100.0% passed
```

Question 7b

Now, remove the commenting and fill in the ellipses . . . below with `X_train`, `y_train`, `X_test`, or `y_test`.

With the ellipses filled in correctly, the code below should fit our linear model to the training data and generate the predicted sale prices for both the training and test datasets.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [47]:
```
# Uncomment the lines below and fill in the ... with X_train, y_train, X_test, or y_tes
t.
# BEGIN YOUR CODE
# ------------------------
linear_model.fit(X_train, y_train)
y_fitted = linear_model.predict(X_train)
y_predicted = linear_model.predict(X_test)
# ------------------------
# END YOUR CODE
```

In [48]:
```
ok.grade("q7b");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------------

Test summary
    Passed: 2
    Failed: 0
[oooooooooook] 100.0% passed
```

8 Q7b **2 / 2**

✓ **+ 2 pts** **Correct**

+ 0 pts Wrong

Question 8a

Is our linear model any good at predicting house prices? Let's measure the quality of our model by calculating the Root-Mean-Square Error (RMSE) between our predicted house prices and the true prices stored in `SalePrice`.

$$\text{RMSE} = \sqrt{\frac{\sum_{\text{houses in test set}} (\text{actual price of house} - \text{predicted price of house})^2}{\text{\# of houses in data set}}}$$

In the cell below, write a function named `rmse` that calculates the RMSE of a model.

Hint: Make sure you are taking advantage of vectorized code. This question can be answered without any `for` statements.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [49]:
```
def rmse(actual, predicted):
    """
    Calculates RMSE from actual and predicted values
    Input:
      actual (1D array): vector of actual values
      predicted (1D array): vector of predicted/fitted values
    Output:
      a float, the root-mean square error
    """
    # BEGIN YOUR CODE
    # ------------------------
    numerator = ((actual-predicted)**2).sum()
    denominator = len(actual)
    return (numerator/denominator)**0.5
    # ------------------------
    # END YOUR CODE
```

In [50]:
```
ok.grade("q8a");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------

Test summary
    Passed: 2
    Failed: 0
[oooooooooo] 100.0% passed
```

9 Q8a **1 / 1**

✓ **+ 1 pts** **Correct**

+ 0 pts Wrong

Question 8b

Now use your `rmse` function to calculate the training error and test error in the cell below.

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned each variable to a non-negative number.

In [51]:
```
# BEGIN YOUR CODE
# ------------------------
training_error = rmse(y_train, y_fitted)
test_error = rmse(y_test, y_predicted)
# ------------------------
# END YOUR CODE
(training_error, test_error)
```

Out[51]: (46710.597505875856, 46146.642656826247)

In [52]:
```
ok.grade("q8b");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------------

Test summary
    Passed: 4
    Failed: 0
[oooooooooook] 100.0% passed
```

10 Q8b **1 / 1**

✓ **+ 1 pts** **Correct**

+ 0 pts Wrong

Question 8c

How much does including `TotalBathrooms` as a predictor reduce the RMSE of the model on the test set? That is, what's the difference between the RSME of a model that only includes `Gr_Liv_Area` and `Garage_Area` versus one that includes all three predictors?

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned the answer variable to a non-negative number.

In [53]:
```
# BEGIN YOUR CODE
# ------------------------
def process_data_gm_nb(data):
    data = remove_outliers(data, 'Gr_Liv_Area', upper=5000)
    data = add_total_bathrooms(data)
    data = select_columns(data, 'SalePrice', 'Gr_Liv_Area', 'Garage_Area',)
    X = data.drop(['SalePrice'], axis = 1)
    y = data.loc[:, 'SalePrice']
    return X, y

X_train_nb, y_train_nb = process_data_gm_nb(train)
X_test_nb, y_test_nb = process_data_gm_nb(test)

linear_model.fit(X_train_nb, y_train_nb)
y_fitted_nb = linear_model.predict(X_train_nb)
y_predicted_nb = linear_model.predict(X_test_nb)

test_error_no_bath = rmse(y_test, y_predicted_nb)
# ------------------------
# END YOUR CODE

test_error_difference = test_error_no_bath - test_error
test_error_difference
```

Out[53]:
```
2477.0084636470347
```

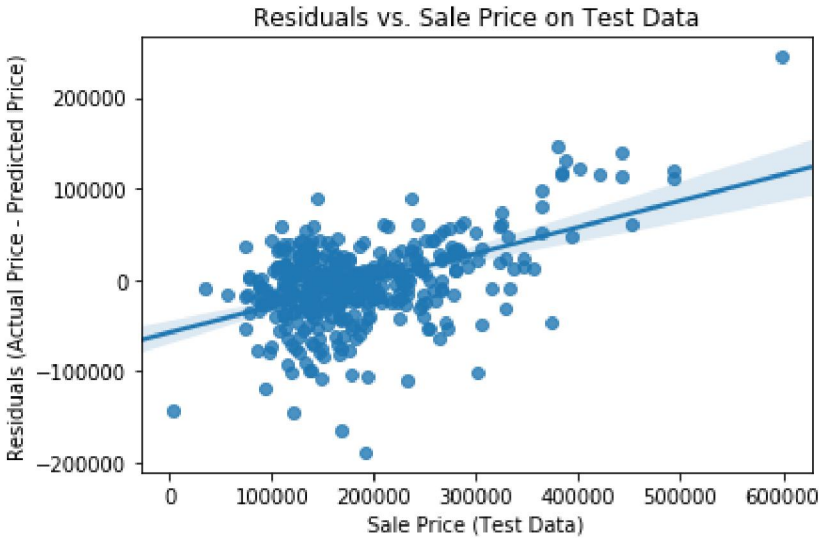
In [54]:
```
ok.grade("q8c");
```

```
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

Running tests

---------------------------------------------------------------------
Test summary
    Passed: 2
    Failed: 0
[oooooooooook] 100.0% passed
```

Residual Plots

One way of understanding the performance (and appropriateness) of a model is through a residual plot. Run the cell below to plot the actual sale prices against the residuals of the model for the test data.

In [55]:
```
residuals = y_test - y_predicted
ax = sns.regplot(y_test, residuals)
ax.set_xlabel('Sale Price (Test Data)')
ax.set_ylabel('Residuals (Actual Price - Predicted Price)')
ax.set_title("Residuals vs. Sale Price on Test Data");
```



Ideally, we would see a horizontal line of points at 0 (perfect prediction!). The next best thing would be a homogenous set of points centered at 0.

But alas, our simple model is probably too simple. The most expensive homes are systematically more expensive than our prediction.

Question 8d

What changes could you make to your linear model to improve its accuracy and lower the test error? Suggest at least two things you could try in the cell below, and carefully explain how each change could potentially improve your model's accuracy.

11 Q8c **2 / 2**

✓ **+ 2 pts** **Correct**

+ 0 pts Wrong

Answer: 1: Increase the model complexity by adding a useful feature while guaranteeing that it decreases bias more than it increases variance.
Adding a useful feature to the data reduces bias and increases model variance, since models with many parameters have many possible combinations of parameters and therefore have higher variance than models with few parameters. However, as complexity of the model goes up, the test error would first decrease then increase as the increased model variance outweighs the decreased model bias. Therefore, we need to strike a balance between model bias and variance.
2: Cross Validation
We can implement k-fold cross validation on our training data. We can split the training data into K equal sized partitions, using K-1 splits to train, last split as validation set. We would repeat this for K times and come up with average of K errors, the validation error. Finally we can pick the model with the lowest validation error. The repeated estimates can mitigate the variance of splits and help preventing overfitting of the training data. This can help improve the model's accuracy in predicting in our test data.
3: Regularization
If we add more useful features into the model, we can use regularizaition to penalize the large weighted features, in order to decrease the variance of the model.

Congratulations! You have completed HW3.

Make sure you have run all cells in your notebook in order before running the cell below, so that all images/graphs appear in the output.,

Please save before submitting!

Please generate pdf as follows and submit it to Gradescope.

File > Print Preview > Print > Save as pdf

12 Q8d **2 / 2**

✓ **+ 2 pts** **Correct**

+ 0 pts Wrong