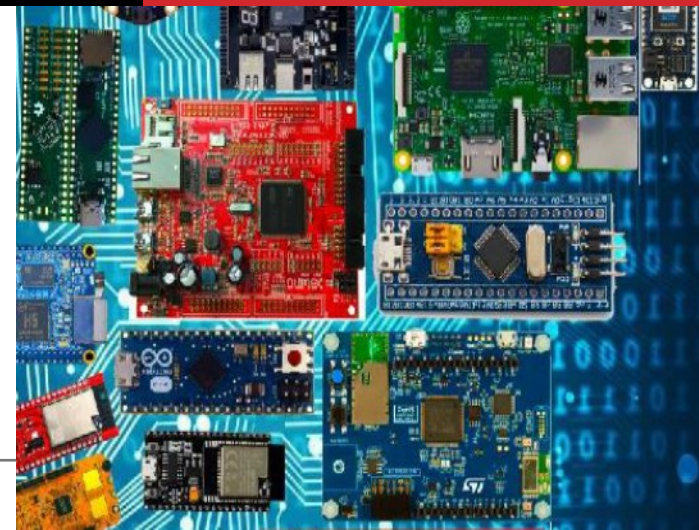


# VLSI & Embedded System

## TRANSISTORS TO LOGIC GATES

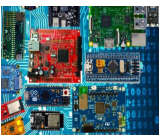
Dennis A. N. Gookyi





# CONTENTS

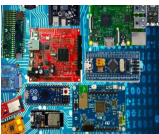
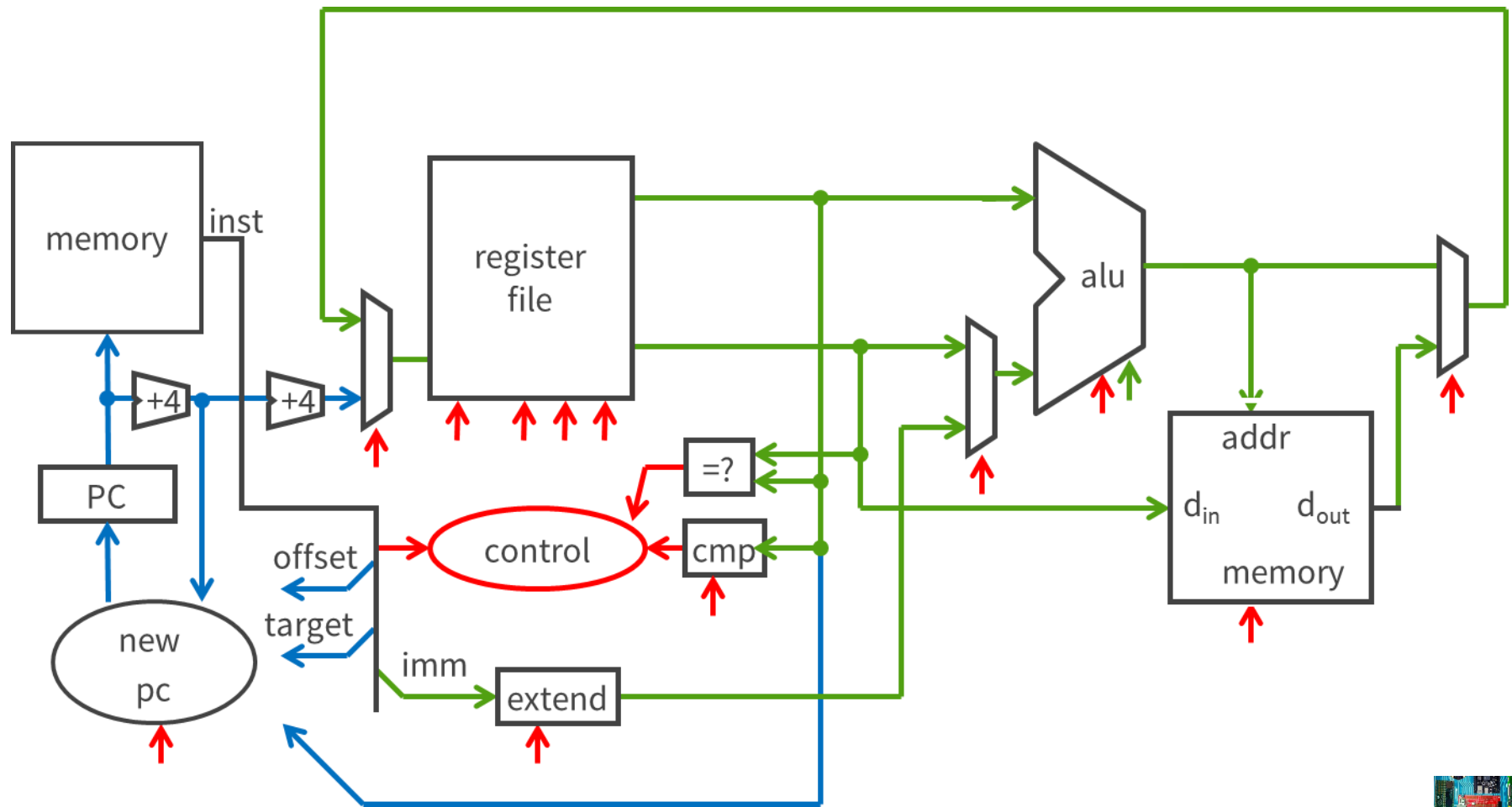
## ❖ TRANSISTORS TO LOGIC GATES





# BIG PICTURE: BUILDING A PROCESSOR

## ❖ Single cycle processor



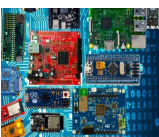


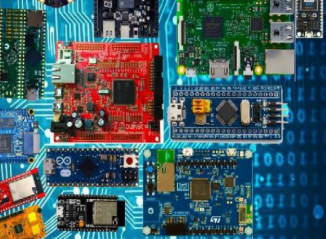
# WHAT IS THIS?

❖ How does it work?

```
#include <stdio.h>

int main() {
    printf("Hello world!\n");
    return 0;
}
```





# COMPILERS AND ASSEMBLERS

- ❖ From high level language to machine language

C

```
int x = 10;  
x = 2 * x + 15;
```

compiler

r0 = 0

RISC-V  
assembly  
language

```
addi r5, r0, 10 ← r5 = r0 + 10  
mulr r5, r5, 2 ← r5 = r5 * 2  
addi r5, r5, 15 ← r5 = r5 + 15
```

*Everything is a number!*

assembler

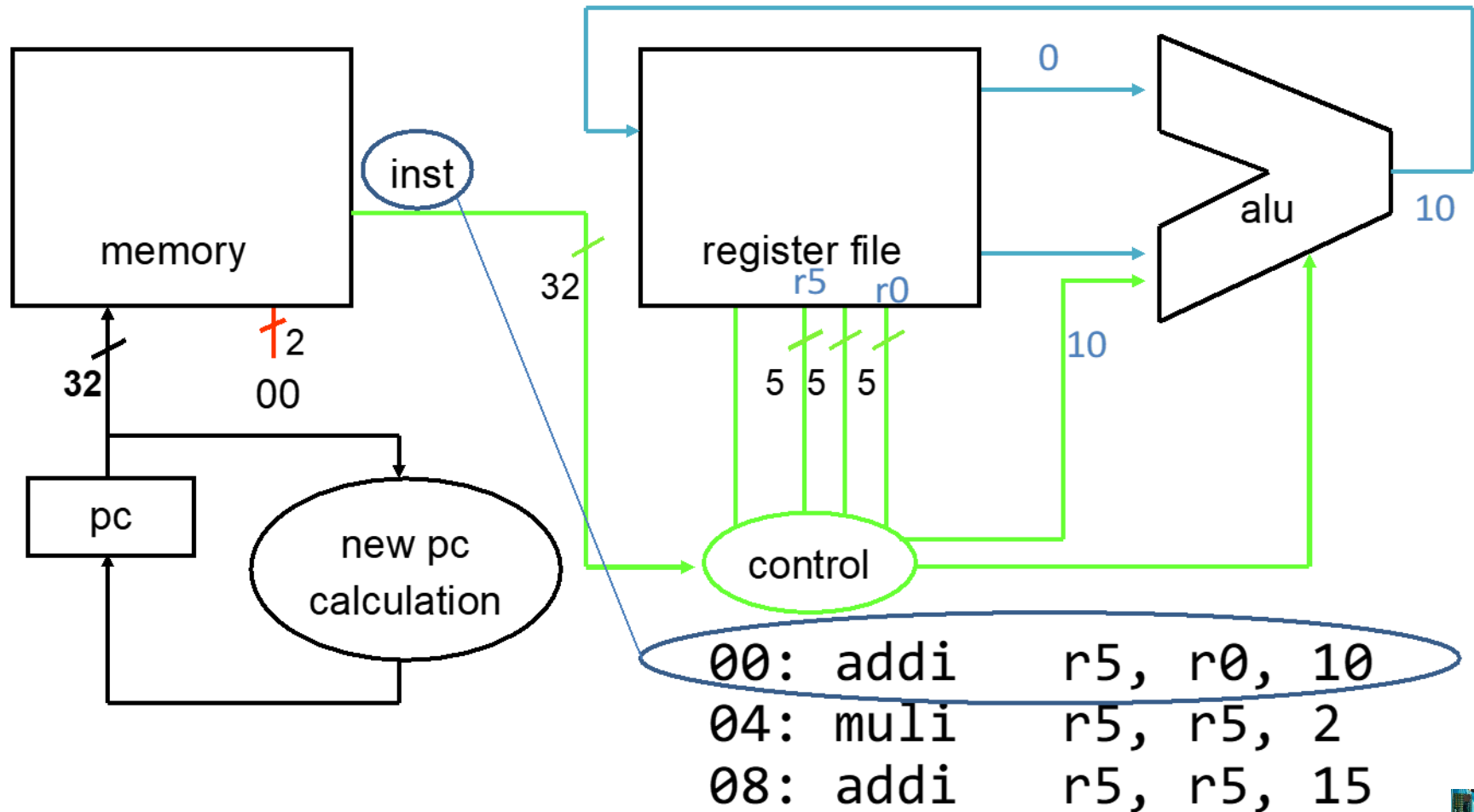
RISC-V  
machine  
language

10	r0	r5	op = addi
0000000001010	00000000000000101	00000000000000101	0010011
00000000000001001	00101001001001010010010011		
0000000001111	00101000000000101	00000000000000101	0010011
15	r5	r5	op = addi



# COMPILERS AND ASSEMBLERS

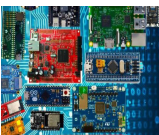
## ❖ How to design a simple process





# INSTRUCTION SET ARCHITECTURE (ISA)

- ❖ Abstract interface between hardware and the lowest level software
- ❖ User portion of the instruction set plus the operating system interfaces used by application programmers





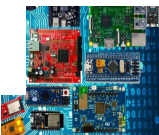
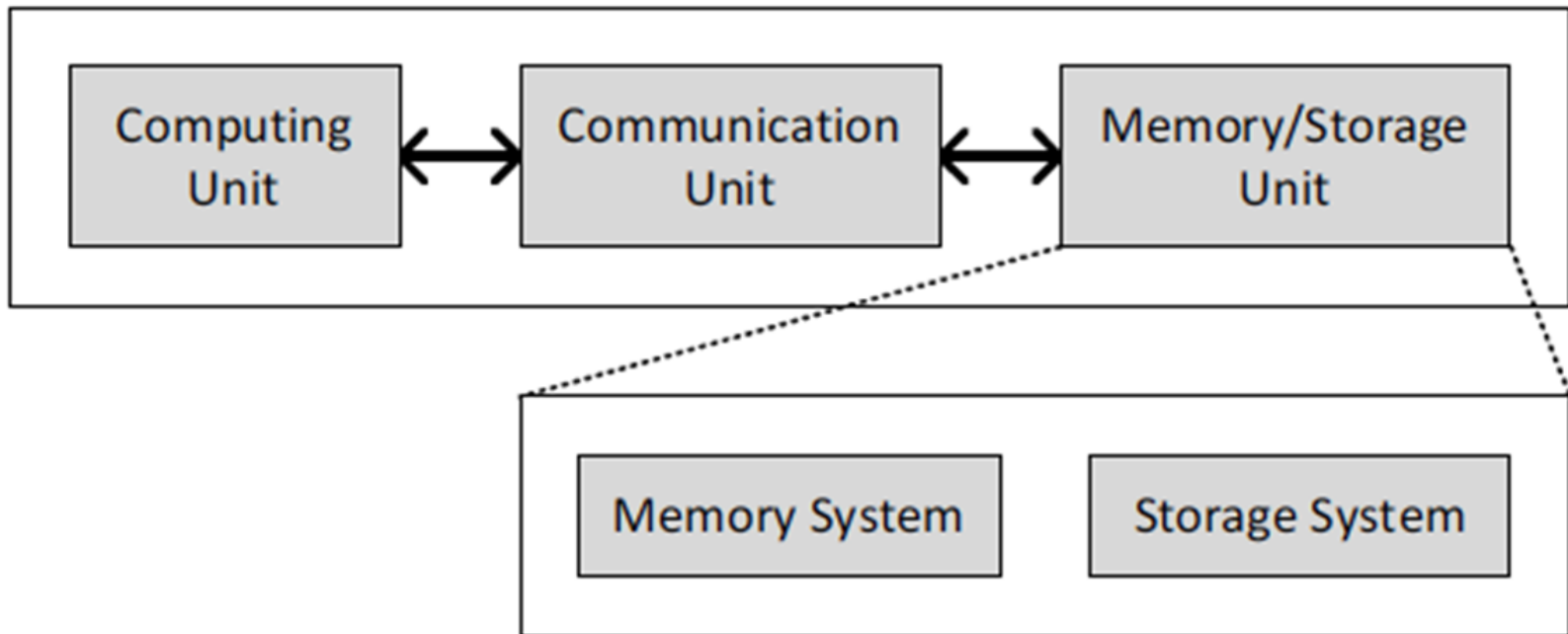


# BASIC COMPUTER SYSTEM

## ❖ Three key components

- Computation
- Communication
- Storage/memory

### Computing System

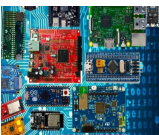
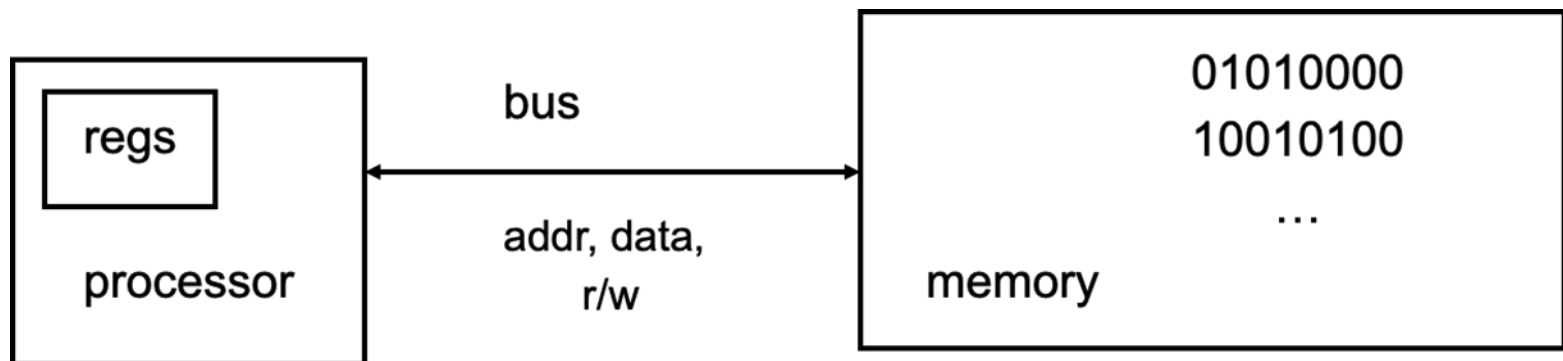


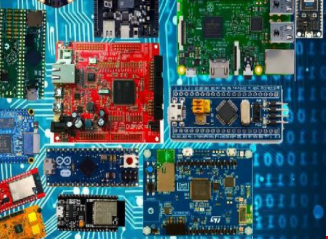




# BASIC COMPUTER SYSTEM

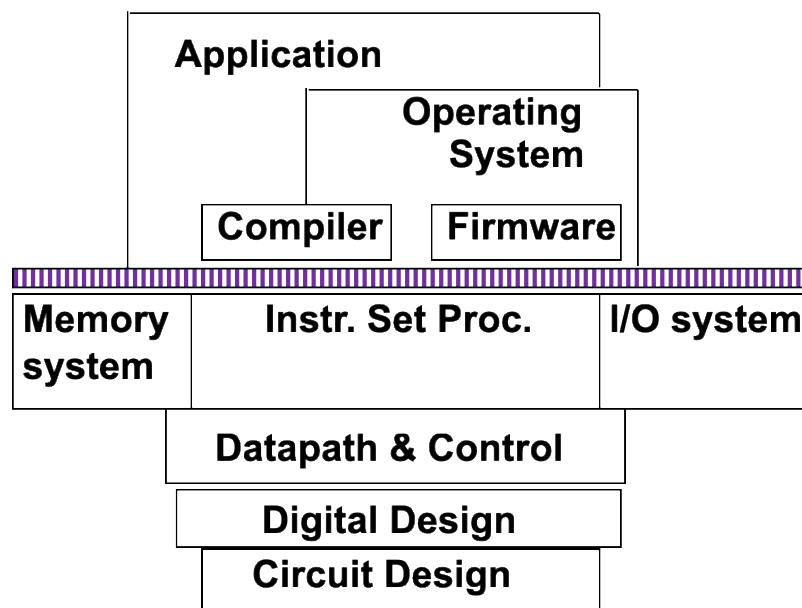
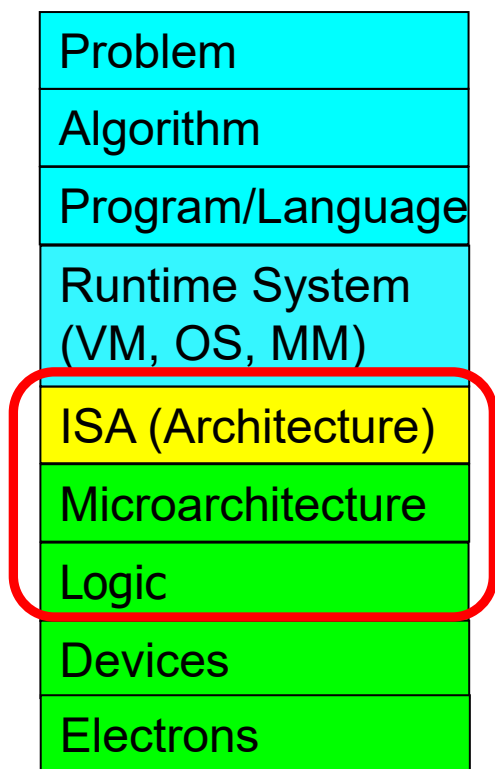
- ❖ A processor executes instructions
  - Processor has some internal state in storage elements (registers)
- ❖ A memory holds instructions and data
  - Von Neumann architecture: combined **inst** and **data**
- ❖ A bus connects the two





# OVERVIEW

❖ Covered in this course



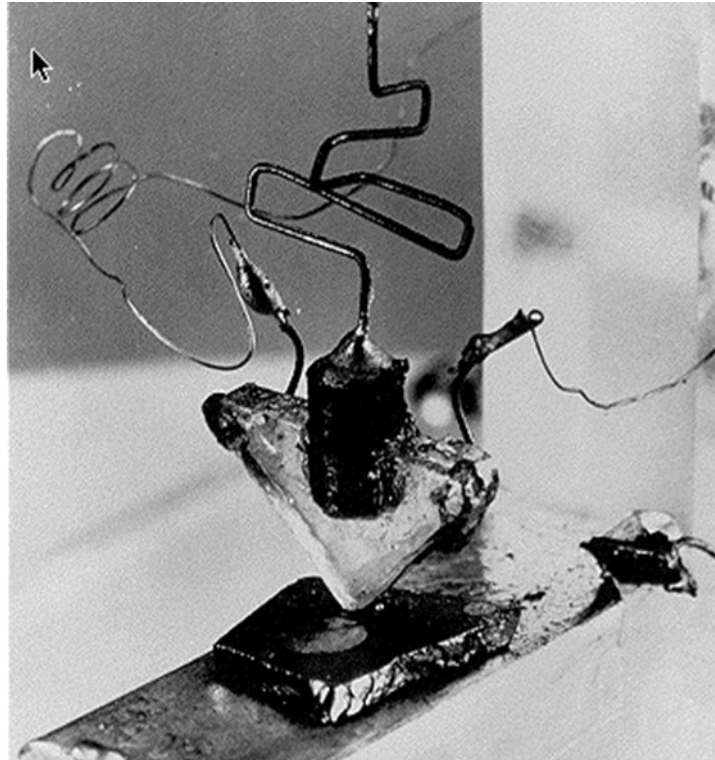
Instruction Set  
Architecture



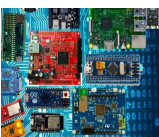


# WHERE DID IT BEGIN:

- ❖ Electrical Switch
  - On/Off
  - Binary
- ❖ Transistor



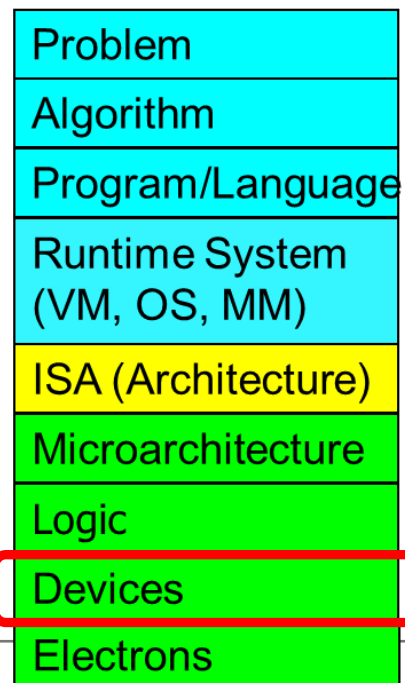
The first transistor on a workbench at AT&T Bell Labs in 1947

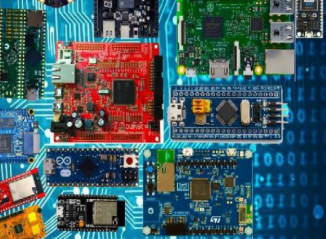




# TRANSISTORS

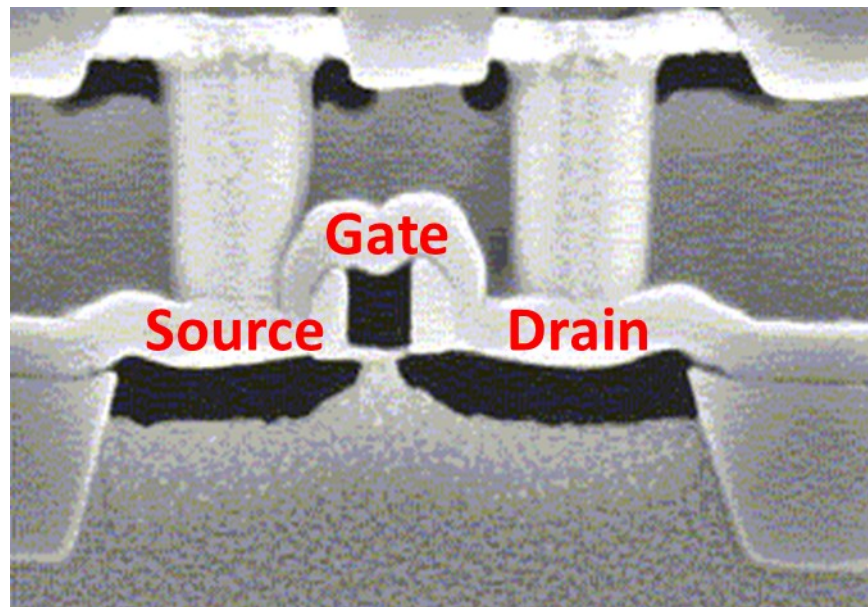
- ❖ Computers are built from very large numbers of very small (and relatively simple) structures: transistors
  - Intel 4004, in 1971, had 2300 MOS transistors
  - Intel's Pentium IV microprocessor, 2000, was made up of more than 42 Million MOS transistors
  - Apple's M2 Max, offered for sale in 2022, is made up of more than 67 Billion MOS transistors





# MOS TRANSISTOR

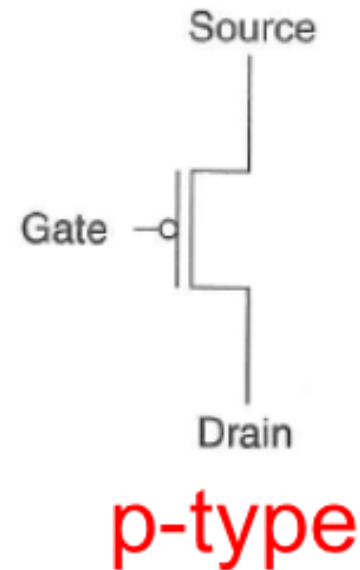
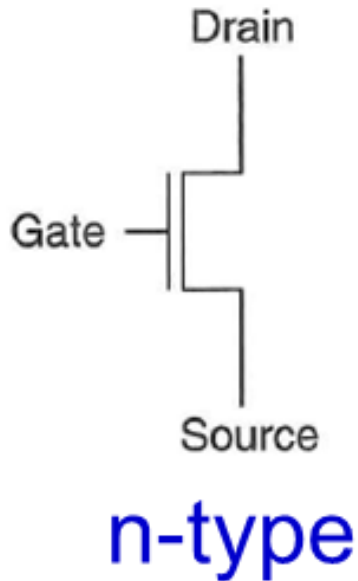
- ❖ By combining
  - Conductors (Metal)
  - Insulators (Oxide)
  - Semiconductors
- ❖ We get a Transistor (MOS)
- ❖ Why is this useful?
  - We can combine many of these to realize simple logic gates
- ❖ The electrical properties of metal-oxide semiconductors are well beyond the scope of what we want to understand in this course
  - They are below our lowest level of abstraction



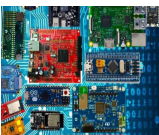


# MOS TRANSISTOR

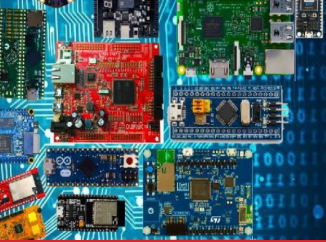
- ❖ There are two types of MOS transistors: n-type and p-type



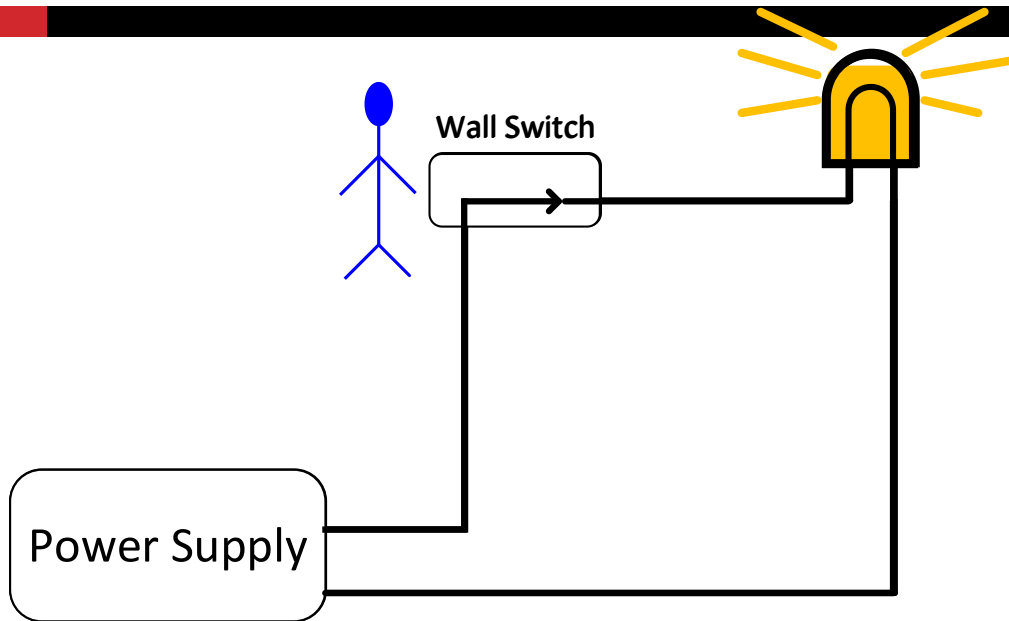
- ❖ They both operate “logically,” very similar to the way wall switches work



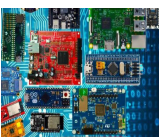




# MOS TRANSISTOR



- In order for the lamp to glow, **electrons must flow**
- In order for electrons to flow, there must be a **closed circuit** from the power supply to the lamp and back to the power supply
- The lamp can be **turned on and off** by simply manipulating the wall switch to make or break the closed circuit

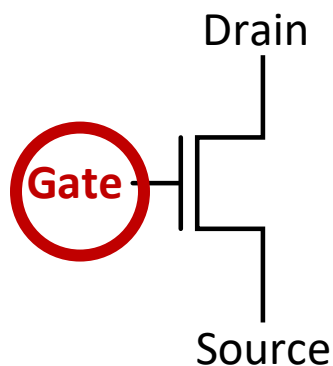






# MOS TRANSISTOR

- ❖ Instead of the wall switch, we could use an n-type or a p-type MOS transistor to make or break the closed circuit



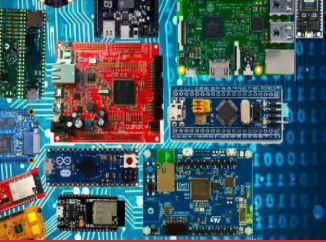
Schematic of an n-type MOS transistor

If the gate of an n-type transistor is supplied with a **high** voltage, the connection from source to drain acts like a **piece of wire** (i.e., the circuit is **closed**)

Depending on the technology, high voltage can range from 0.3V to 3

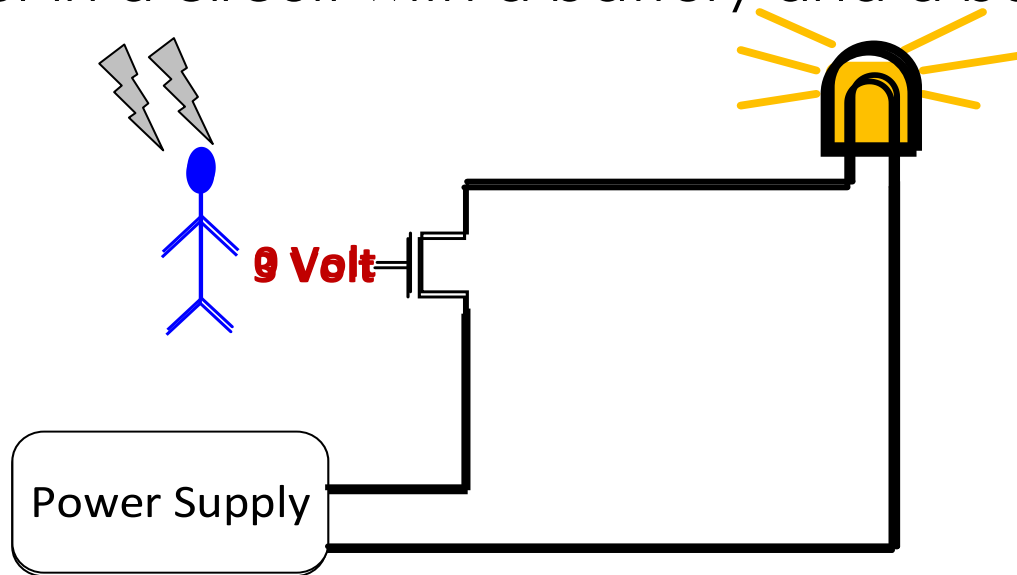
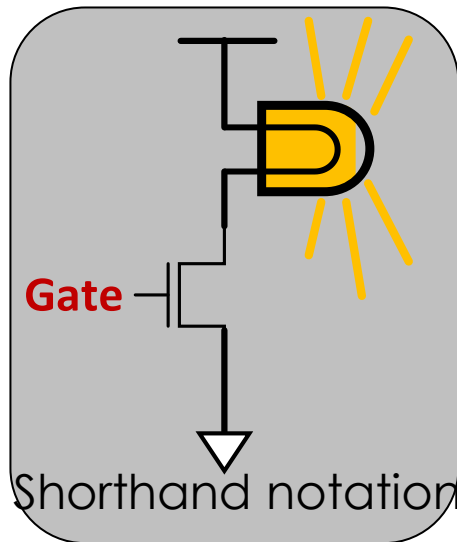
If the gate of the n-type transistor is supplied with **zero** voltage, the connection between the source and drain is **broken** (i.e., the circuit is **open**)





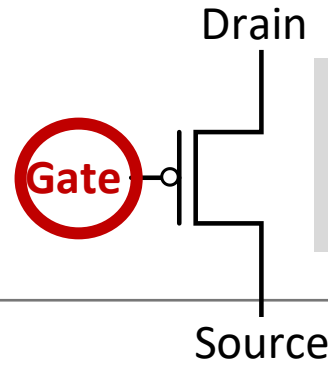
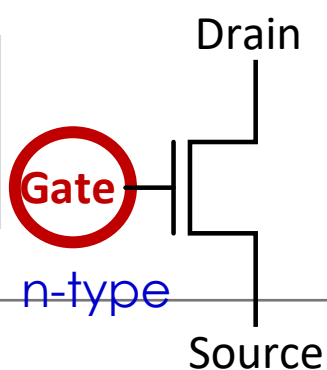
# MOS TRANSISTOR

- ❖ The n-type transistor in a circuit with a battery and a bulb

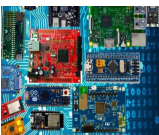


- ❖ The p-type transistor works in exactly the opposite fashion from the n-type transistor

The circuit is closed when the gate is supplied with 3V



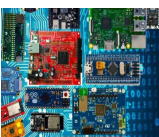
The circuit is closed when the gate is supplied with 0V





# LOGIC GATES

- ❖ We know how a MOS transistor works
  - How do we build logic structures out of MOS transistors?
    - We construct basic logical units out of individual MOS transistors
    - These logical units are called logic gates
    - They implement simple Boolean functions



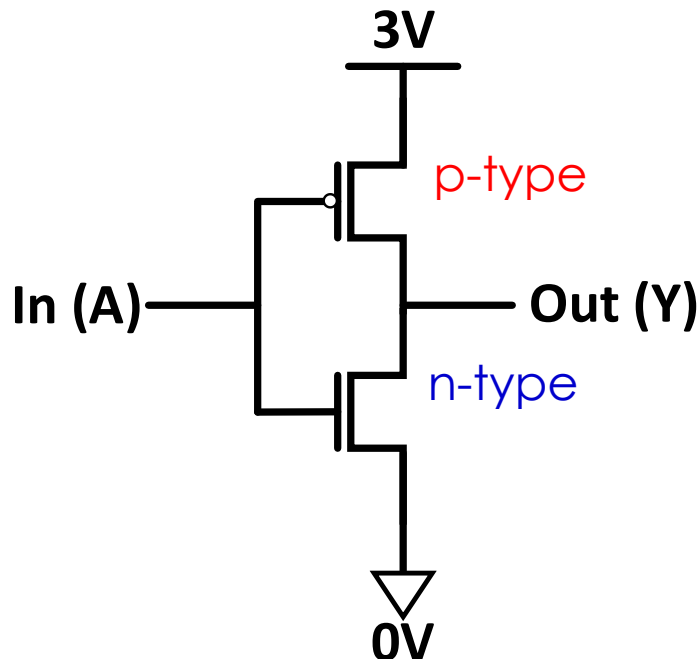


# LOGIC GATES

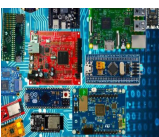
- ❖ Modern computers use both n-type and p-type transistors, i.e. Complementary MOS (CMOS) technology

**nMOS + pMOS = CMOS**

- ❖ The simplest logic structure that exists in a modern computer



What does this circuit do?

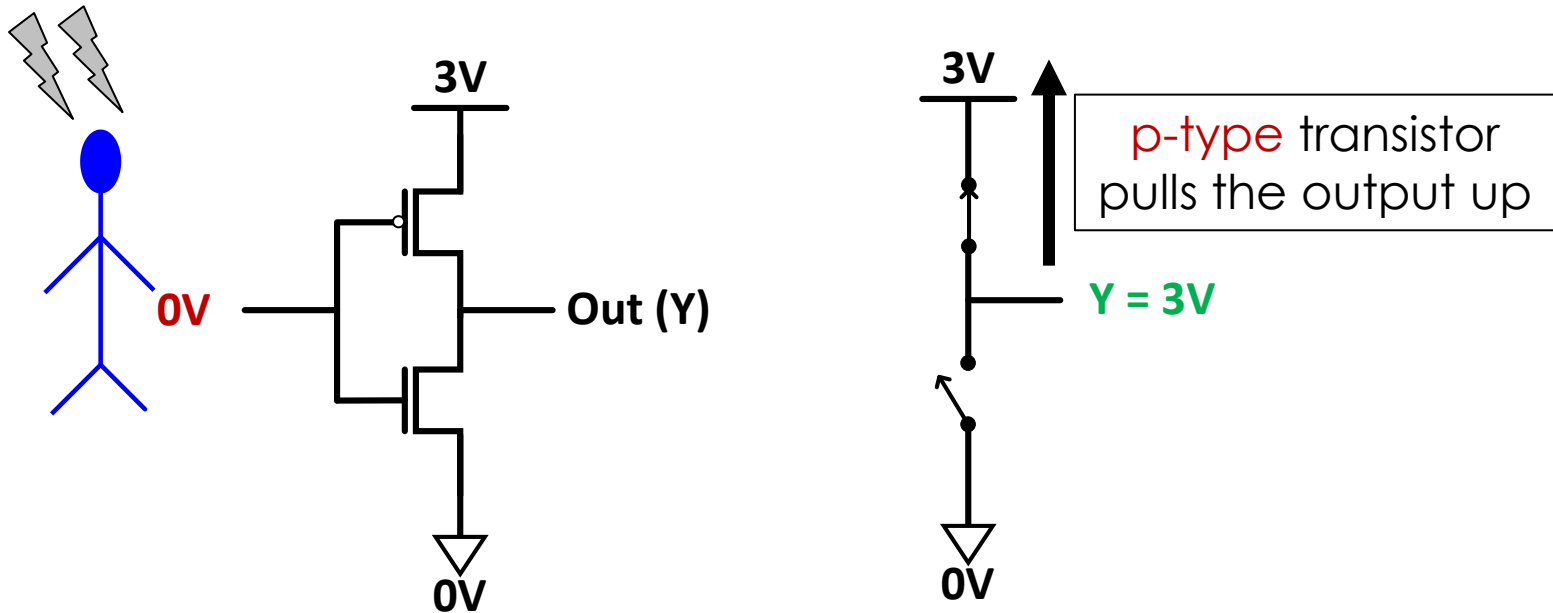




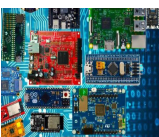
# LOGIC GATES

## ❖ Functionality of CMOS circuits

What happens when the input is connected to 0V?



**p-type** transistors are good at **pulling up** the voltage

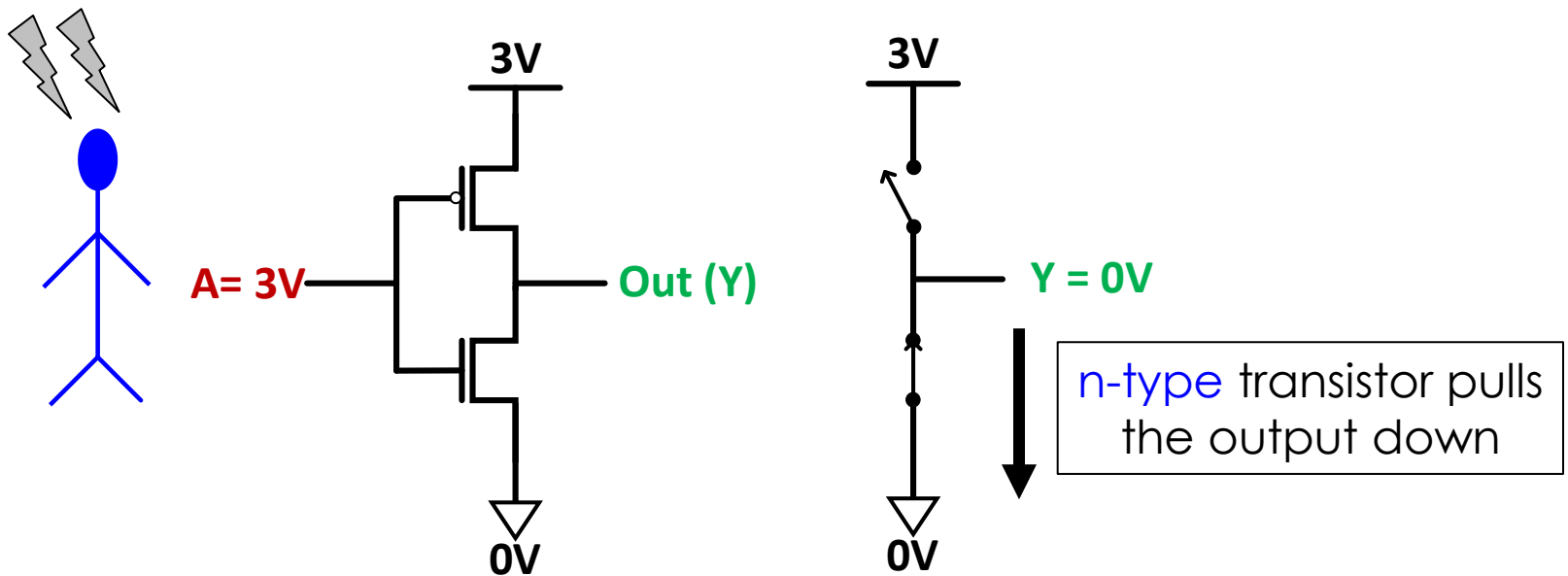




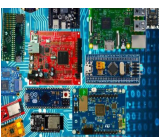
# LOGIC GATES

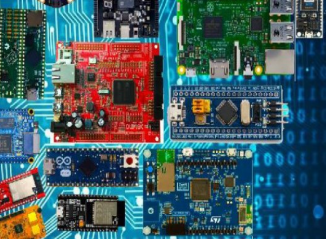
## ❖ Functionality of CMOS circuits

What happens when the input is connected to 3V?



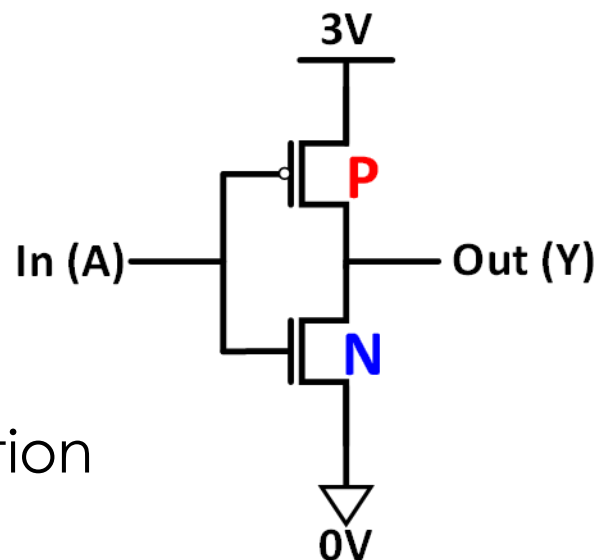
n-type transistors are good at pulling down the voltage





# LOGIC GATES

- ❖ Functionality of CMOS circuits
- ❖ This is actually the CMOS NOT Gate
- ❖ Why do we call it NOT?
  - If  $A = 0V$  then  $Y = 3V$
  - If  $A = 3V$  then  $Y = 0V$
- ❖ Digital circuit: one possible interpretation
  - Interpret  $0V$  as logical (binary) 0 value
  - Interpret  $3V$  as logical (binary) 1 value



A	P	N	Y
0	ON	OFF	1
1	OFF	ON	0

$$Y = \overline{A}$$

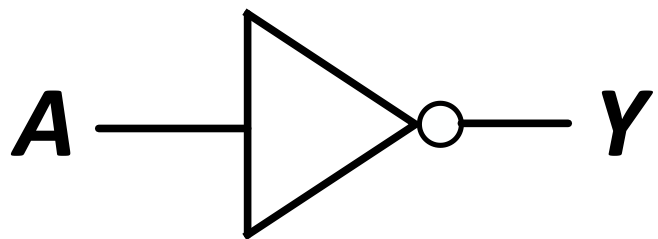
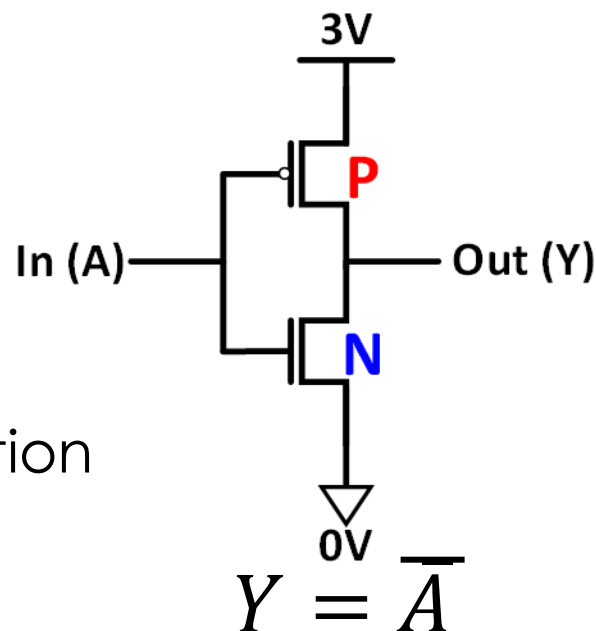






# LOGIC GATES

- ❖ Functionality of CMOS circuits
- ❖ This is actually the CMOS NOT Gate
- ❖ Why do we call it NOT?
  - If  $A = 0V$  then  $Y = 3V$
  - If  $A = 3V$  then  $Y = 0V$
- ❖ Digital circuit: one possible interpretation
  - Interpret  $0V$  as logical (binary) 0 value
  - Interpret  $3V$  as logical (binary) 1 value



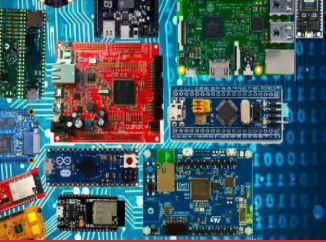
We call this a **NOT** gate  
or an **inverter**

(bubble indicates inversion)

**Truth table:** shows what is the logical output of the circuit for each possible input

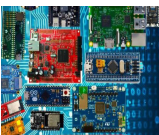
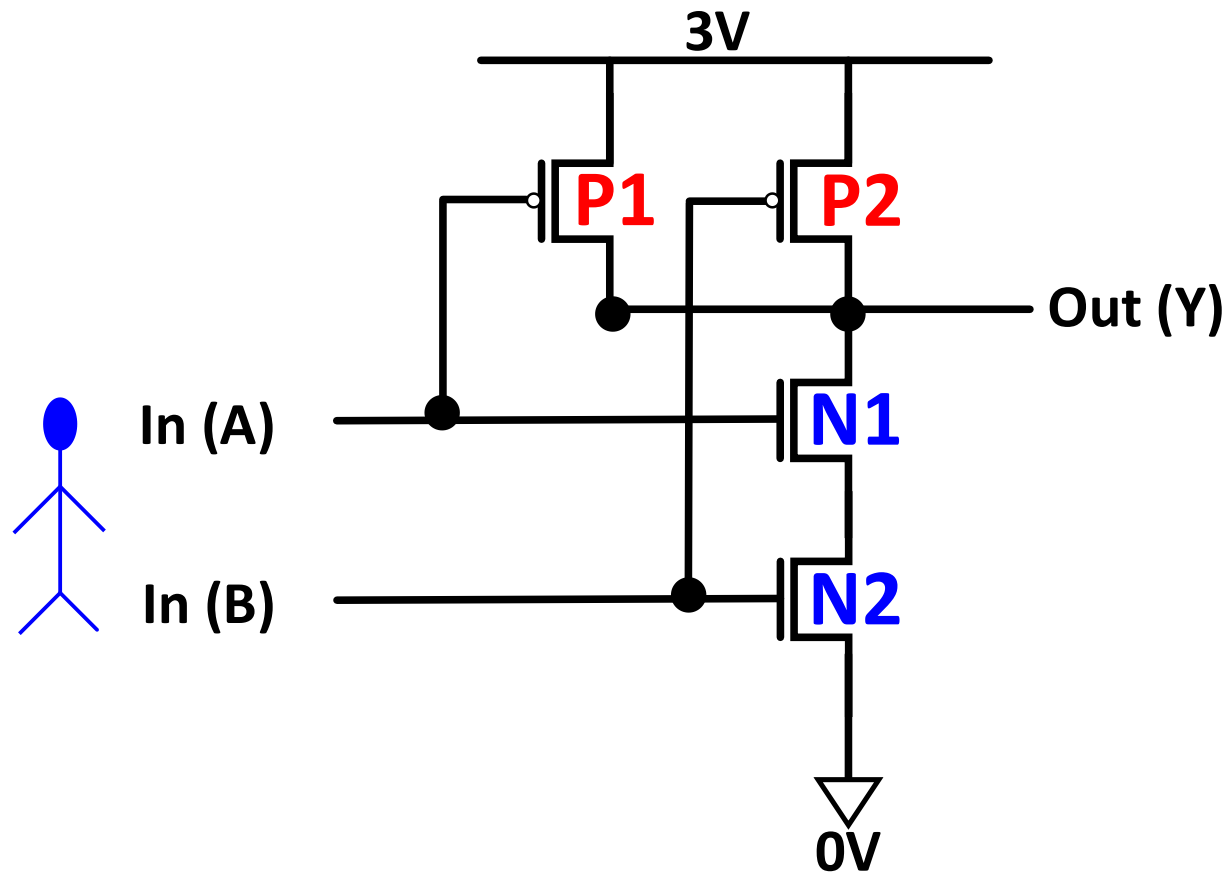
$A$	$Y$
0	1
1	0

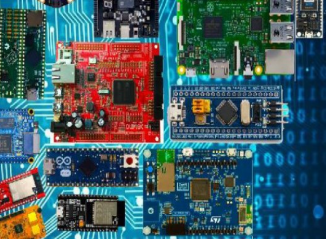




# LOGIC GATES

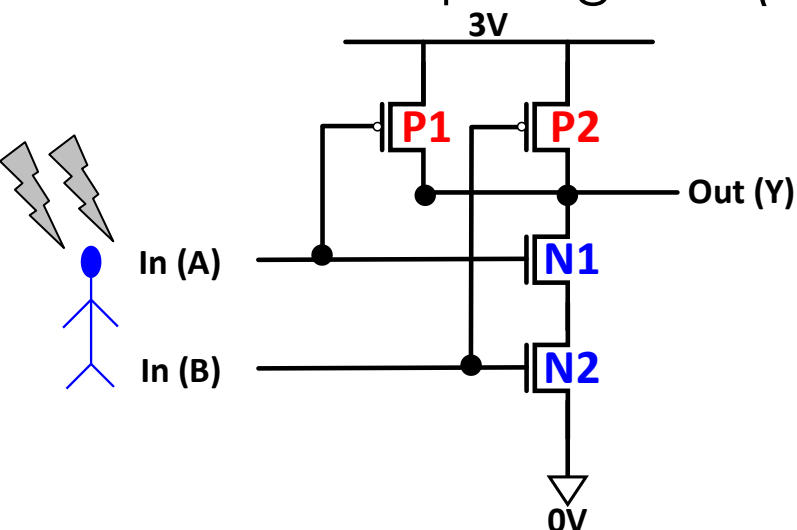
❖ More complex gates





# LOGIC GATES

- ❖ More complex gates (CMOS NAND gate)

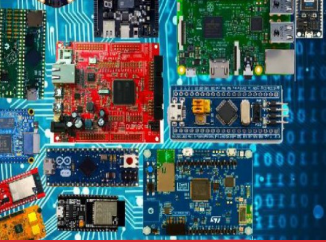


$$Y = \overline{A \cdot B} = \overline{AB}$$

A	B	P1	P2	N1	N2	Y
0	0	ON	ON	OFF	OFF	1
0	1	ON	OFF	OFF	ON	1
1	0	OFF	ON	ON	OFF	1
1	1	OFF	OFF	ON	ON	0

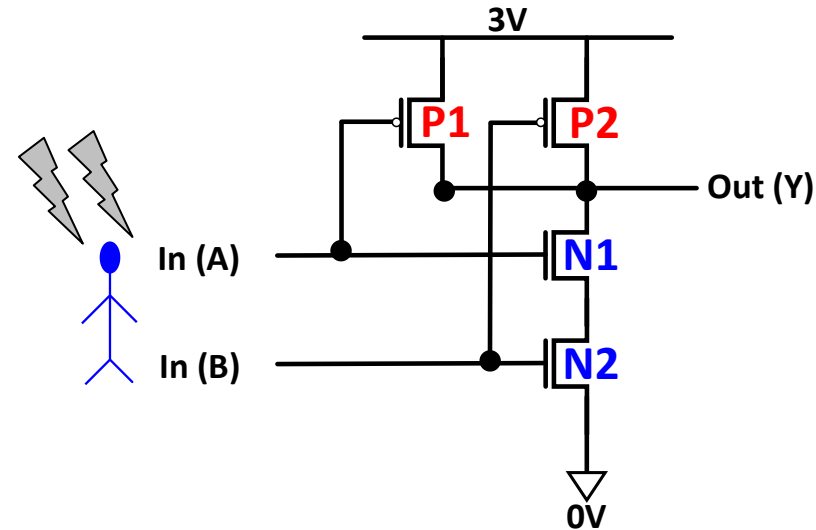
- ❖ P1 and P2 are in parallel; only one must be ON to pull up the output to 3V
- ❖ N1 and N2 are connected in series; both must be ON to pull down the output to 0V



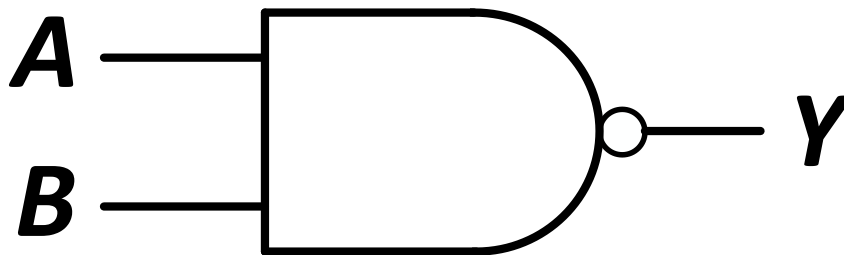


# LOGIC GATES

- ❖ More complex gates (CMOS NAND gate)

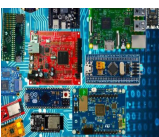


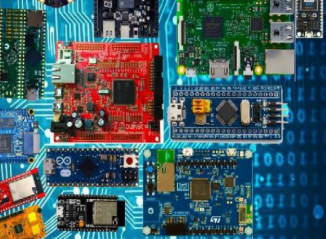
$$Y = \overline{A \cdot B} = \overline{AB}$$



A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

We call this a **NAND** gate  
(bubble indicates inversion)



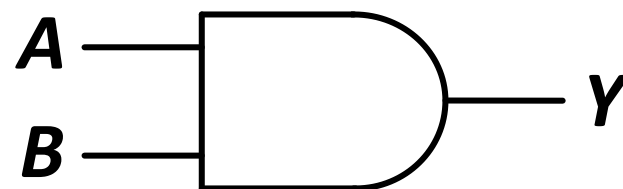


# LOGIC GATES

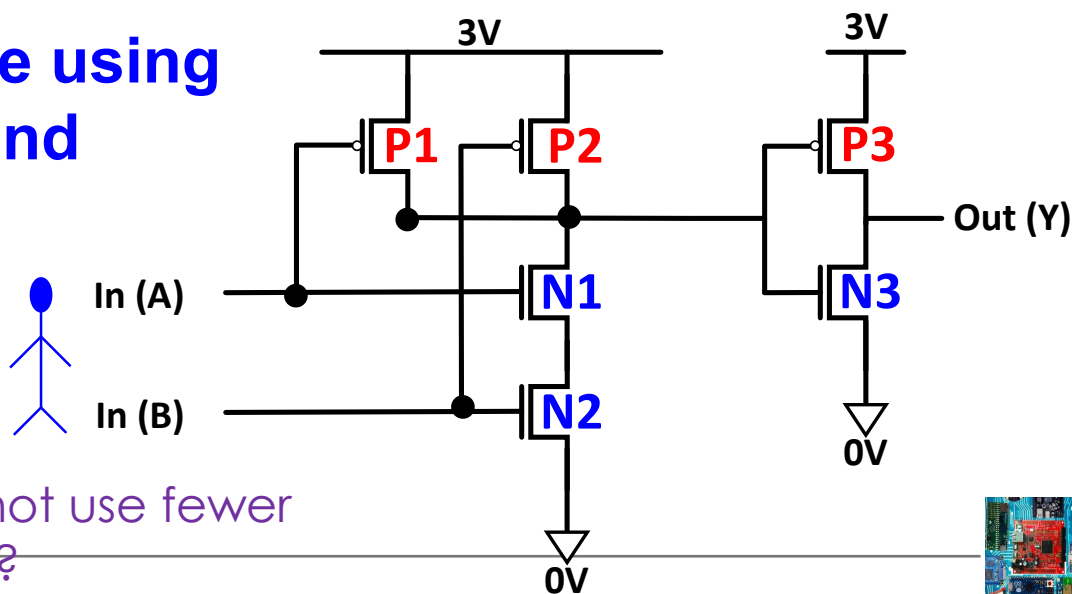
❖ More complex gates (CMOS AND gate)

$$Y = A \cdot B = AB$$

<i>A</i>	<i>B</i>	<i>Y</i>
0	0	0
0	1	0
1	0	0
1	1	1



We make an **AND** gate using  
one **NAND** gate and  
one **NOT** gate



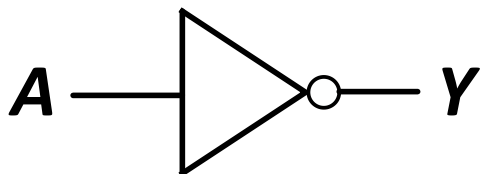
Food for thought: Can we not use fewer transistors for the AND gate?



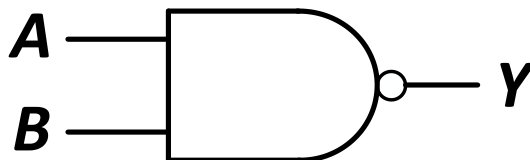


# LOGIC GATES

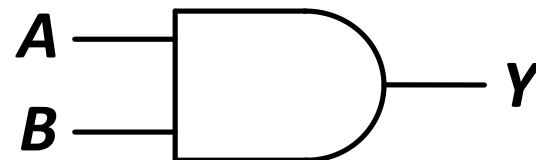
❖ CMOS NOT, NAND, AND gates



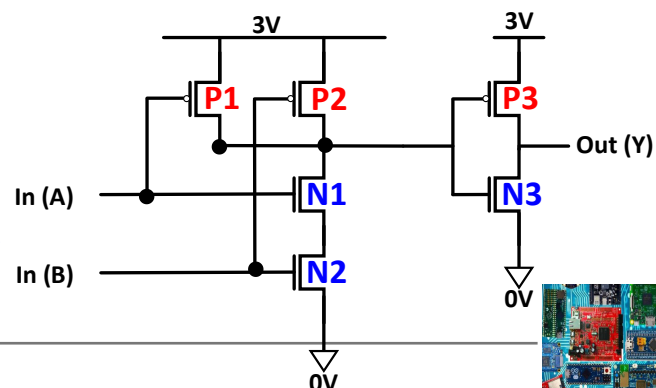
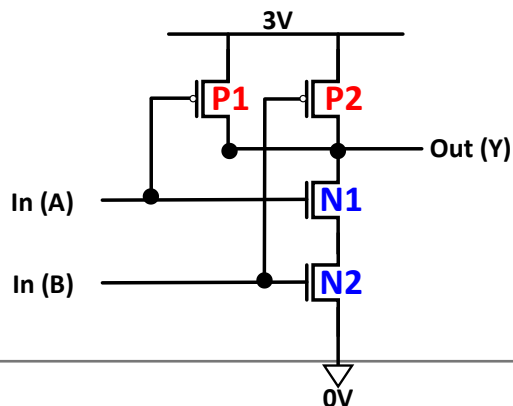
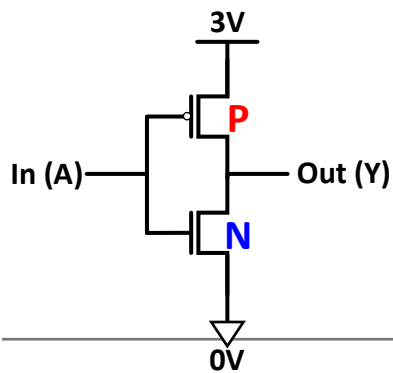
A	Y
0	1
1	0

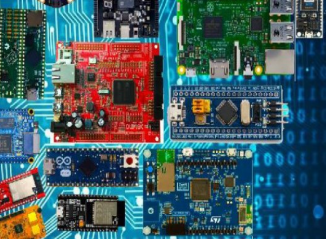


A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0



A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1





# MOORE'S LAW

- ❖ 1965
- ❖ # of transistors integrated on a die doubles every 18-24 months (i.e., grows exponentially with time)
- ❖ Amazingly visionary
  - ❑ 2300 transistors, 1 MHz clock (Intel 4004) - 1971
  - ❑ 16 Million transistors (Ultra Sparc III)
  - ❑ 42 Million transistors, 2 GHz clock (Intel Xeon) – 2001
  - ❑ 55 Million transistors, 3 GHz, 130nm technology, 250mm<sup>2</sup> die (Intel Pentium 4) – 2004
  - ❑ 290+ Million transistors, 3 GHz (Intel Core 2 Duo) – 2007
  - ❑ 721 Million transistors, 2 GHz (Nehalem) - 2009
  - ❑ 1.4 Billion transistors, 3.4 GHz Intel Haswell (Quad core) – 2013
  - ❑ 7.2 Billion transistors, 3-3.9 GHz Intel Broadwell (22-core) – 2016







# MOORE'S LAW

- ❖ # of transistors integrated on a die doubles every 18-24 months (i.e., grows exponentially with time)

