

3. To see if there is a k -alternating path, we can
- Making k copies of the graph ($G^{(0)}, G^{(1)} \dots G^{(k-1)}, G^{(k)}$) connected by k edges with each edge that connects two graphs alternating between black and white.
 - Particularly, connect two such copies, i and $i+1$, iff an edge from i to $i+1$ (using the same connections as in the original graph) changes the current path color (alternates). This will make the “new” connections to the graph alternate in color.
 - Run Dijkstra from some node in $G^{(0)}$ to some node in $G^{(k)}$. Record whether Dijkstra has found a path.
 - Run Dijkstra again from some node in $G^{(0)}$ to some node in $G^{(k)}$; however, the starting node this time should have a different color than the starting node in step c. Record whether Dijkstra has found a path. This is to check whether there is a k -alternating path but starting on the opposite color of $G^{(0)}$.
 - If Dijkstra has found a path on either of these, then there exists a k -alternating path.

In this case, because we are making k (with k times as many edges and vertices) copies of the graph, the time complexity of this algorithm is $O((k|V| + k|E|)\log(k|V|))$. Although, we are running Dijkstra twice that should not impact time complexity.