## Dennis Kuzminer CSCI-UA 310-001 PS3b

- 5. To see when a particular animal dies, we can
  - a. Construct a graph connecting all the animals [1...n], with edge weights of  $C_{\nu}$ . (Linear time). More specifically,
    - i. We have 2 states: the alive/just infected state and the contagious state.
    - ii. We can treat the alive/just infected state as a node  $a_i$  and the contagious state  $b_i$ , where  $i \in [1...n]$ .
    - iii. Then, connect  $a_i$  to  $b_i$  with an edge weight of  $C_v$ , showing the transition to contagion.
    - iv. Connect  $b_i$  to  $a_{i+1}$  with an edge of weight 0. This is because once an animal gets contagious, its neighbors will immediately become infected.
    - v. We can simplify this graph by just connecting all the animals [1...n], with edge weights of  $C_{\nu}$ .
  - b. Create some source node s that connects to all  $S \in [1...n]$ . Make the edge weights of these 0. (Less or perhaps equal to than linear time)
  - c. Run Dijstraka, so we see which animals will die.
    - i. Runs in O((|V| + |E|)log(|V|)); however, we assume each cage/animal is surrounded by at most 8 other animals/cages. We can restate the runtime:  $O((|V| + 8|V|)log(|V|)) \rightarrow O((9|V|)log(|V|)) \rightarrow O(nlog(n))$
  - d. Dijkstra tracks the shortest path to some node v using the array d[v]. Each entry in this array will be the sum of the weights  $(C_v)$ . Whatever d[v] is for some node, this will be the time of infection of this animal.
  - e. Death of an animal happens  $D_v$  after  $C_{v(aggregate)}$ , where  $C_{v(aggregate)} = d[v]$ .
  - f. Therefore, death of each animal happens  $d[v] + D_v$ .

Disclaimer: no animals were harmed in the solution of this exercise.