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3. $E[k] = E[X]$, $X = X_1 + \dots + X_k \rightarrow$ Each X has the same distribution, so for any X , the probability that a head will appear is $p = .5$. So, the *expected* number of coin tosses you make to get the i th head after you have already gotten $i-1$ heads is $\frac{1}{p} = 2$. $E[X] = E[X_1] + \dots + E[X_k] \rightarrow$
 $E[X] = \frac{1}{p} + \dots + \frac{1}{p}$, k times. Meaning that $E[k] = \frac{k}{p}$. In this case, $p = .5$, $E[k] = \frac{k}{p} = 2k$.