Dennis Kuzminer CSCI-UA 310-001 PS1

8.

a.

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Fib 3 Fib 4

Fib 1 Fib 2 Fib 2 Fib 3

Fib 0 Fib 1 Fib Fib 1 Fib 2

Fib 0 Fib 1 Fib 1 Fib 2

Fib 0 Fib 1
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b. Base case n = 0
    G(n)=2F(n+1)-1 \rightarrow 1=2(1)-1 \rightarrow 1=1
    Inductive step: Assume G(k)=2F(k+1)-1 holds for all n up to k. Prove k+1 also
    holds: G(k+1)=2F(k+2)-1 \rightarrow
    G(k)+G(k-1)+1=2F(k)+2F(k+1)-1 \rightarrow
    2F(k-1+1)-1+G(k)+1=2F(k)+2F(k+1)-1 \rightarrow
    G(k)+1=2F(k+1) \rightarrow
    G(k)=2F(k+1)-1 \rightarrow
    ∴G(n)=2F(n+1)-1 holds for all n\ge 0
c. int fib(int n) {
            int fib[] = new int[n+2];
            for(int i = 0; i \le n; i++) {
                    if(i == 0)  {
                             fib[i] = 0;
                     } else {
                             if(i == 1) {
                                      fib[i] = 1;
                             } else {
                                      fib[i] = fib[i-1] + fib[i-2];
                             }
                     }
            return fib[n];
```