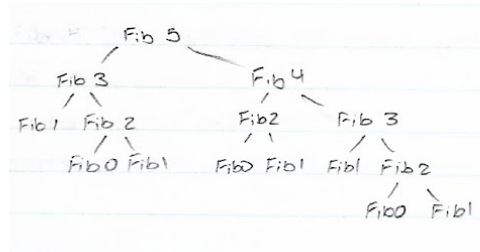


8.

a.



b. Base case $n = 0$

$$G(n) = 2F(n+1) - 1 \rightarrow 1 = 2(1) - 1 \rightarrow 1 = 1$$

Inductive step: Assume $G(k) = 2F(k+1) - 1$ holds for all n up to k . Prove $k+1$ also

$$\text{holds: } G(k+1) = 2F(k+2) - 1 \rightarrow$$

$$G(k) + G(k-1) + 1 = 2F(k) + 2F(k+1) - 1 \rightarrow$$

$$2F(k-1+1) - 1 + G(k) + 1 = 2F(k) + 2F(k+1) - 1 \rightarrow$$

$$G(k) + 1 = 2F(k+1) \rightarrow$$

$$G(k) = 2F(k+1) - 1 \rightarrow$$

$$\therefore G(n) = 2F(n+1) - 1 \text{ holds for all } n \geq 0$$

c. `int fib(int n) {`

`int fib[] = new int[n+2];`

`for(int i = 0; i <= n; i++) {`

`if(i == 0) {`

`fib[i] = 0;`

`} else {`

`if(i == 1) {`

`fib[i] = 1;`

`} else {`

`fib[i] = fib[i-1] + fib[i-2];`

`}`

`}`

`}`

`return fib[n];`

`}`