

Dennis Kuzminer
CSCI-UA 310-001 PS3b

2. Using the fact that if all edge weights are non-negative integers bounded by a constant, then we can implement Dijkstra (with buckets) in time $O(nB + m)$, where B is the bound. Because all legal edges are irrelevant we will loop through the graph and assign all legal edges a value of 0. Then construct a reverse edge, which will be denoted as illegal, and assign all illegal edges a value of 1.

for each $v \in \text{Successor}(u)$ where $u \in V$:

$\text{wt}(u, v) \leftarrow 0$

$\text{wt}(v, u) \leftarrow 1$

Then, run Dijkstra with buckets algorithm, and return a subset of R (the result set) where the first element is s and the last element is t ($R[s, t]$) without changing the order of R .

This algorithm will run in $O(n + m)$ time, as the bound $B = 1$.