

- 3) This algorithm could use recursion to consider the left and right ^{children}. Because every child of a min heap is larger than its parent, an algorithm proportional to $O(k)$ would need to stop iterating on a subtree once the value of the nodes become higher than x . Iterating through these values that are deeper in the tree become unnecessary, as we already know that we will not count any node in that subtree, so we can move on to the subtree directly "to the left" of the last node that was $< x$.

Pseudo Code:

let numLessThan = 0

let index = 0

def numLessThanX(minHeap, x, index):

Base cases

if the index > minHeap.length \rightarrow Break, to control the num of times we loop

if minHeap[index] $\geq x \rightarrow$ Break, as we know from the definition of a min heap that all children of this particular subtree will also break

Recursive step

if the two base cases are not satisfied

numLessThan++

Call numLessThan on left subtree \rightarrow Change value of index \rightarrow Increment by the value of the implementation of array

Call numLessThan on right subtree \rightarrow Change value of index

def atleastKItems(minHeap, k, x):

numLessThanX(minHeap, x, index)

return numLessThan $\geq k$