# Logistic Regression Capstone Project - Part 3

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# **Project Description**

The logistic regression tool that you have developed allows you to run a logistic regression with an individual predictor and summarize the model's performance. Using this tool, investigate the performance of other predictors to determine which predictors appear to be the most informative.

# **Data Dictionary**

Field	Description					
annual_inc	The self-reported annual income provided by the borrower during registration, in \$1000s					
application_type	Indicates whether the loan is an individual application or a joint application with two co-borrowers					
collections_12_mths_ex_med	Number of collections in 12 months excluding medical collections					
delinq_2yrs	The number of 30+ days past-due incidences of delinquency in the borrower's credit file for the past 2 years					
dti	A ratio calculated using the borrower's total monthly debt payments on the total debt obligations, excluding mortgage and the requested LC loan, divided by the borrower's self-reported monthly income.					
home_ownership	The home ownership status provided by the borrower during registration. Our values are: RENT, OWN, MORTGAGE, OTHER.					
inq_last_6mths	The number of inquiries in past 6 months (excluding auto and mortgage inquiries)					
loan_status	Current status of the loan					
open_acc	The number of open credit lines in the borrower's credit file.					
pub_rec	Number of derogatory public records					
term	The number of payments on the loan. Values are in months and can be either 36 or 60.					
verification_status	Indicates if income was verified by LC, not verified, or if the income source was verified					

## **Summary**

Using alpha (significance value) at 0.05, features are annual income, delinquency, inquiry, opened credit lines, number of public records, 60 mths term and verified status are most informative

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### **Import Libraries**

```
In [1]: import numpy as np
        from numpy import count_nonzero, median, mean
        import pandas as pd
        import matplotlib.pyplot as plt
        import seaborn as sns
        import random
        import datetime
        from datetime import datetime, timedelta, date
        import statsmodels.api as sm
        import statsmodels.formula.api as smf
        from statsmodels.formula.api import ols
        import scipy
        from scipy import stats
        from scipy.stats.mstats import normaltest # D'Agostino K^2 Test
        from scipy.stats import boxcox
        from collections import Counter
        import sklearn
        from sklearn.preprocessing import StandardScaler, MinMaxScaler, LabelEncoder, OneHo
        from sklearn.model_selection import KFold, StratifiedKFold, GridSearchCV, Randomize
        from sklearn.model_selection import train_test_split, cross_validate
        from sklearn.metrics import accuracy_score, auc, classification_report, confusion_m
        from sklearn.metrics import precision_score, recall_score, ConfusionMatrixDisplay,
        from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
        from sklearn.feature_selection import f_regression, f_classif, chi2, RFE, RFECV
        from sklearn.feature_selection import mutual_info_regression, mutual_info_classif
        from sklearn.feature_selection import VarianceThreshold, GenericUnivariateSelect
        from sklearn.feature_selection import SelectFromModel, SelectKBest, SelectPercentil
        from sklearn.linear_model import LogisticRegression, LogisticRegressionCV
        from sklearn.neighbors import KNeighborsClassifier
        from sklearn.naive_bayes import GaussianNB, MultinomialNB, BernoulliNB, Categorical
        import imblearn
        from imblearn.under_sampling import RandomUnderSampler, CondensedNearestNeighbour
```

```
from imblearn.under_sampling import EditedNearestNeighbours, TomekLinks
from imblearn.over_sampling import SMOTE
from imblearn.combine import SMOTEENN, SMOTETomek
import feature_engine
from feature_engine.selection import DropConstantFeatures, DropDuplicateFeatures
from feature engine.selection import DropCorrelatedFeatures, SmartCorrelatedSelecti
from feature_engine.selection import SelectBySingleFeaturePerformance
import pycaret
from pycaret.classification import *
%matplotlib inline
#sets the default autosave frequency in seconds
%autosave 60
sns.set_style('dark')
sns.set(font_scale=1.2)
plt.rc('axes', titlesize=9)
plt.rc('axes', labelsize=14)
plt.rc('xtick', labelsize=12)
plt.rc('ytick', labelsize=12)
import warnings
warnings.filterwarnings('ignore')
# This module lets us save our models once we fit them.
# import pickle
pd.set_option('display.max_columns',None)
#pd.set_option('display.max_rows', None)
pd.set_option('display.width', 1000)
pd.set_option('display.float_format','{:.2f}'.format)
random.seed(0)
np.random.seed(0)
np.set_printoptions(suppress=True)
```

Autosaving every 60 seconds

#### **Quick Data Glance**

```
In [2]: df = pd.read_csv("calibdata1.csv")
In [3]: df.head()
```

```
annualinc collections deling ing openacc
                                                      dti pubrec individual mortgage
Out[3]:
        0
              205.00
                             0
                                    0
                                        2
                                                28 23.72
                                                               0
                                                                         1
                                                                                   1
                                                                                        (
               36.00
                             0
                                         0
                                                 8 22.77
                                                               0
                                                                         1
                                                                                   0
        1
                                    0
        2
               48.00
                             0
                                    0
                                        1
                                                10 13.68
                                                               0
                                                                         1
                                                                                   0
        3
               40.00
                             0
                                    0
                                        0
                                                11
                                                     8.37
                                                               0
                                                                         1
                                                                                        (
        4
                             0
                                    0
                                                               0
                                                                         1
                                                                                   0
               83.00
                                        0
                                                18 23.50
In [4]: df.info()
      <class 'pandas.core.frame.DataFrame'>
      RangeIndex: 49986 entries, 0 to 49985
      Data columns (total 16 columns):
       #
           Column
                              Non-Null Count Dtype
      ---
           ____
                              -----
       0
           annualinc
                              49986 non-null float64
           collections
                              49986 non-null int64
       2
           deling
                              49986 non-null int64
       3
           inq
                              49986 non-null int64
       4
           openacc
                              49986 non-null int64
       5
           dti
                              49986 non-null float64
       6
           pubrec
                              49986 non-null int64
       7
                              49986 non-null int64
           individual
       8
           mortgage
                              49986 non-null int64
       9
           rent
                              49986 non-null int64
       10 own
                              49986 non-null int64
       11 other
                              49986 non-null int64
       12 term60mths
                              49986 non-null int64
       13 vstatusverified
                              49986 non-null int64
       14 vstatusnotverified 49986 non-null int64
       15 lstatus
                              49986 non-null int64
      dtypes: float64(2), int64(14)
      memory usage: 6.1 MB
In [5]: df.dtypes.value_counts()
Out[5]: int64
                   14
        float64
                   2
        dtype: int64
```

In [6]: # Descriptive Statistical Analysis
 df.describe(include="all")

Out[6]:		annualinc	collections	delinq	inq	openacc	dti	pubrec	individual
	count	49986.00	49986.00	49986.00	49986.00	49986.00	49986.00	49986.00	49986.00
	mean	76.31	0.01	0.32	0.70	11.59	17.99	0.19	1.00
	std	62.81	0.13	0.87	1.01	5.29	8.22	0.67	0.02
	min	6.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00
	25%	47.00	0.00	0.00	0.00	8.00	11.83	0.00	1.00
	50%	65.00	0.00	0.00	0.00	11.00	17.53	0.00	1.00
	75%	90.00	0.00	0.00	1.00	14.00	23.66	0.00	1.00
	max	8253.00	5.00	27.00	33.00	58.00	39.99	63.00	1.00

In [7]: df.lstatus.value\_counts(normalize=True)

Out[7]: 0 0.93 1 0.07

Name: 1status, dtype: float64

In [8]: df.shape

Out[8]: (49986, 16)

In [9]: df.columns

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#### Create a small dataset

In [10]: df = df.sample(frac=0.25)

In [11]: df.reset\_index(drop=True, inplace=True)

In [12]: df.head()

Out[12]:		annualinc	collections	delinq	inq	openacc	dti	pubrec	individual	mortgage	ren
	0	50.00	0	0	0	7	16.83	0	1	1	(
	1	68.00	0	0	1	12	16.01	0	1	0	
	2	80.00	0	0	0	12	20.28	0	1	0	
	3	62.00	0	0	0	8	17.50	0	1	1	(
	4	97.30	0	0	1	10	12.14	0	1	0	

```
In [13]: df.shape
Out[13]: (12496, 16)
In [14]: df.lstatus.value_counts()
             11619
Out[14]: 0
        Name: lstatus, dtype: int64
        ______
        Logistic Regression (StatsModel)
In [15]: df.columns
Out[15]: Index(['annualinc', 'collections', 'deling', 'ing', 'openacc', 'dti', 'pubrec', 'i
        ndividual', 'mortgage', 'rent', 'own', 'other', 'term60mths', 'vstatusverified',
        'vstatusnotverified', 'lstatus'], dtype='object')
In [16]: df.shape
Out[16]: (12496, 16)
In [17]: X = df.iloc[:,0:15]
        y = df.iloc[:,15]
In [18]: X.values, y.values
Out[18]: (array([[ 50.,
                        0., 0., ...,
                                       0.,
                                             0.,
                                                  0.],
                        0., 0., ...,
                                                  1.],
                [ 68.,
                                       0.,
                                             0.,
                [ 80.,
                        0.,
                            0., ...,
                                       0.,
                                             0.,
                                                  1.],
                . . . ,
                [ 96.,
                        0.,
                            0., ...,
                                       1.,
                                             1.,
                                                  0.],
                [115.,
                        0.,
                            0., ...,
                                       0.,
                                             1.,
                                                  0.],
                        0., 1., ...,
                                       1.,
                                             0.,
                                                  0.]]),
         array([0, 0, 0, ..., 0, 0, 0], dtype=int64))
In [19]: X = sm.add_constant(X)
In [20]: logreg = sm.Logit(y, X).fit(maxiter=1000)
       Warning: Maximum number of iterations has been exceeded.
               Current function value: 0.246207
               Iterations: 1000
```

In [21]: logreg.summary()

Dep. Variable:	Istatus	No. Observations:	12496
Model:	Logit	Df Residuals:	12481
Method:	MLE	Df Model:	14
Date:	Tue, 25 Jul 2023	Pseudo R-squ.:	0.03110
Time:	19:31:57	Log-Likelihood:	-3076.6
converged:	False	LL-Null:	-3175.4
Covariance Type:	nonrobust	LLR p-value:	1.764e-34

	coef		z	P> z	[0.025	0.975]
const	-24.4125	2.15e+06	-1.14e-05	1.000	-4.22e+06	4.21e+06
annualinc	-0.0065	0.001	-5.814	0.000	-0.009	-0.004
collections	-0.1110	0.283	-0.392	0.695	-0.666	0.444
delinq	0.1004	0.038	2.627	0.009	0.025	0.175
inq	0.2913	0.031	9.514	0.000	0.231	0.351
openacc	-0.0158	0.008	-2.081	0.037	-0.031	-0.001
dti	-0.0004	0.005	-0.090	0.928	-0.010	0.009
pubrec	-0.1840	0.079	-2.321	0.020	-0.339	-0.029
individual	20.8911	3.44e+04	0.001	1.000	-6.73e+04	6.74e+04
mortgage	1.3124	2.15e+06	6.1e-07	1.000	-4.22e+06	4.22e+06
rent	1.5444	2.15e+06	7.18e-07	1.000	-4.22e+06	4.22e+06
own	1.4197	2.15e+06	6.6e-07	1.000	-4.22e+06	4.22e+06
other	-28.6890	1.31e+07	-2.19e-06	1.000	-2.57e+07	2.57e+07
term60mths	0.3798	0.078	4.897	0.000	0.228	0.532
vstatusverified	-0.3736	0.085	-4.375	0.000	-0.541	-0.206
vstatusnotverified	-0.2266	0.090	-2.519	0.012	-0.403	-0.050

#### **Explain the Statistics**

Model: OLS: Ordinary Least Squares: One way to create a linear regression model. Minimize the dependent samples so you can estimate the unknown samples when creating a linear regression model.

Method: Least Squares: Fit data to the model by minimizing the residual samples

R-squared: Measure of how well the regression line approximates the data points. If .5 then that is a sign that half of the observed variation can be explained by the models inputs. 1

would be perfectly correlated.

Adj, R-squared: Reflects the fit of the model. Values range from 0 to 1, where higher values indicate a good fit.

F-statistic: Measures how significantly the data points fit into the regression model by measuring variation of sample means.

Prob (F-statistic): Probability that the null hypothesis for the full model is true. Closer to zero the better the samples approach the model.

Log-Likelihood: The conditional probability that the observed data fits the model

AIC : Adjusts the log-likelihood based on the number of observations and complexity of the model. It focuses on the data points that best describe the data.

Df Residuals : Degrees of freedom of the residuals which is the difference between predicted values and the measured data.

BIC: We want a low BIC. It focuses on the shortest description of the data like AIC.

Df Model: Number of parameters in the model

Coefficient Constant: Is your Y intercept. If both dependent and independent coefficients are zero then the expected output would equal the constant coefficient.

Independent Coefficient: Represents the change of the independent variable per unit.

Standard Error: Accuracy of the coefficients

P>|t|: The P Value. A P Value less than .05 is considered statistically significant.

[.025 - .975]: Confidence Interval: Represents the range in which coefficients are likely to fall.

Omnibus : (D'Angostino's test) : Establishes whether the samples come from a normally distributed population.

Durbin-Watson: Test to see if the errors are not independent. Used to find repeating patterns that may be obstructed by noise. Its value lies between 0 and 4. If greater than 2 this is a sign that relationships between two variables are going in opposite directions (negatively correlated). If less than 2 variables are positively correlated.

Prob(Omnibus): Probability of Omnibus

Jarque-Bera: Tests whether the samples match a normal distribution. It never has a negative number and the further it gets from zero signals the data doesn't have a normal distribution.

Skew: Measure of the asymmetry of the probability distribution. Negative skew indicates the tail is longer on the left and the concentration of the data is on the right. Positive indicates

the tail is longer on the right. 0 indicates that the tails are balanced.

Prob(JB): The probability of Jarque-Bera

Kurtosis: Describes the shape of a probability distribution with a focus on the tails and not the peak. If the value is high that is a sign that there are more outliers. If the value is less than 3 that means there are fewer outliers. A value of 3 points towards a normal distribution. Values greater than 3 indicate more outliers.

Condition Number: Represents whether samples are highly related in our regression model. A large number indicates strong multicollinearity which means that independent variables are highly correlated with each other. This causes problems because a small number of samples are so dramatically different from others that results are corrupted.

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# **Train Test Split**

We've prepared our data and we're ready to model. There's one last step before we can begin. We must split the data into features and target variable, and into training data and test data. We do this using the train\_test\_split() function. We'll put 25% of the data into our test set, and use the remaining 75% to train the model.

Notice below that we include the argument stratify=y. If our master data has a class split of 80/20, stratifying ensures that this proportion is maintained in both the training and test data. =y tells the function that it should use the class ratio found in the y variable (our target).

The less data you have overall, and the greater your class imbalance, the more important it is to stratify when you split the data. If we didn't stratify, then the function would split the data randomly, and we could get an unlucky split that doesn't get any of the minority class in the test data, which means we wouldn't be able to effectively evaluate our model. Worst of all, we might not even realize what went wrong without doing some detective work.

Lastly, we set a random seed so we and others can reproduce our work.

```
In [22]: df.shape
Out[22]: (12496, 16)
In [23]: X = df.iloc[:,0:15]
y = df.iloc[:,15]
In [24]: Counter(y)
Out[24]: Counter({0: 11619, 1: 877})
```

```
In [25]: X.values, y.values
Out[25]: (array([[ 50.,
                        0., 0., ...,
                                        0.,
                                              0.,
                                                   0.1,
                                                   1.],
                [ 68., 0., 0., ...,
                                        0.,
                                              0.,
                [ 80., 0., 0., ...,
                                        0.,
                                              0.,
                                                   1.],
                [ 96., 0., 0., ...,
                                                   0.],
                                        1.,
                                              1.,
                [115., 0., 0., ...,
                                        0.,
                                              1.,
                                                   0.1,
                [ 70., 0., 1., ...,
                                              0., 0.]]),
                                        1.,
         array([0, 0, 0, ..., 0, 0, 0], dtype=int64))
In [26]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_sta
In [27]: X_train.shape, X_test.shape, y_train.shape, y_test.shape
Out[27]: ((9996, 15), (2500, 15), (9996,), (2500,))
In [28]: Counter(y_train), Counter(y_test)
Out[28]: (Counter({0: 9294, 1: 702}), Counter({0: 2325, 1: 175}))
```

# Logistic Regression (Scikit Learn)

#### **Logistic Regression model assumptions**

- Outcome variable is categorical
- Observations are independent of each other
- No severe multicollinearity among X variables
- No extreme outliers
- Linear relationship between each X variable and the logit of the outcome variable
- Sufficiently large sample size

Let's build our model using **LogisticRegression** from the Scikit-learn package. This function implements logistic regression and can use different numerical optimizers to find parameters, including 'newton-cg', 'lbfgs', 'liblinear', 'sag', 'saga' solvers. You can find extensive information about the pros and cons of these optimizers if you search it in the internet.

The version of Logistic Regression in Scikit-learn, support regularization. Regularization is a technique used to solve the overfitting problem of machine learning models. **C** parameter indicates **inverse of regularization strength** which must be a positive float. Smaller values specify stronger regularization.

# **Hyperparameter Tuning**

#### RandomSearchCV

Randomised grid search is very useful in finding near-optimal hyper parameters for any machine learning models.

Rules of thumb: with 60 iterations, 95% of the time, best 5% sets of parameters can be found, regardless of grid size.

```
In [29]: logreg = LogisticRegression(max_iter=1000, random_state=0)
In [30]: parameters = { 'solver' : ['newton-cg', 'lbfgs', 'liblinear', 'sag', 'saga'],
                         'penalty' : ['none', 'l1', 'l2', 'elasticnet'],
                         'C': [0.001, 0.01, 0.1, 1, 10, 100, 1000]
                      }
In [31]: | scoring = {'accuracy', 'precision', 'recall', 'f1', 'roc_auc'}
In [32]: lr_randm = RandomizedSearchCV(estimator=logreg, param_distributions = parameters, c
                                     n_jobs=-1, scoring=scoring, refit='roc_auc', random_stat
In [33]: %%time
         lr_randm.fit(X_train, y_train)
        CPU times: total: 3.12 s
        Wall time: 1min 49s
Out[33]: RandomizedSearchCV(cv=5,
                            estimator=LogisticRegression(max_iter=1000, random_state=0),
                            n_iter=50, n_jobs=-1,
                            param_distributions={'C': [0.001, 0.01, 0.1, 1, 10, 100,
                                                        1000],
                                                  'penalty': ['none', 'l1', 'l2',
                                                              'elasticnet'],
                                                  'solver': ['newton-cg', 'lbfgs',
                                                             'liblinear', 'sag',
                                                             'saga']},
                             random_state=0, refit='roc_auc',
                             scoring={'accuracy', 'recall', 'f1', 'precision', 'roc_auc'})
In [34]: lr_randm.best_estimator_
Out[34]: LogisticRegression(C=0.1, max iter=1000, random state=0, solver='newton-cg')
In [35]: lr_randm.best_score_
Out[35]: 0.6249028742849245
In [36]: lr_randm.best_params_
Out[36]: {'solver': 'newton-cg', 'penalty': 'l2', 'C': 0.1}
In [37]: def make_results(model_name:str, model_object, metric:str):
```

```
Arguments:
       model_name (string): what you want the model to be called in the output tab
       model object: a fit GridSearchCV object
       metric (string): precision, recall, f1, accuracy, or auc
   Returns a pandas df with the F1, recall, precision, accuracy, and auc scores
   for the model with the best mean 'metric' score across all validation folds.
   # Create dictionary that maps input metric to actual metric name in GridSearchC
   metric_dict = {
                 'precision': 'mean_test_precision',
                 'recall': 'mean_test_recall',
                 'f1': 'mean_test_f1',
                 'accuracy': 'mean_test_accuracy',
                 'roc_auc' : 'mean_test_roc_auc'
                 }
   # Get all the results from the CV and put them in a df
   cv_results = pd.DataFrame(model_object.cv_results_)
   # Isolate the row of the df with the max(metric) score
   best_estimator_results = cv_results.iloc[cv_results[metric_dict[metric]].idxmax
   # Extract Accuracy, precision, recall, and f1 score from that row
   f1 = best_estimator_results.mean_test_f1
   recall = best_estimator_results.mean_test_recall
   precision = best_estimator_results.mean_test_precision
   accuracy = best_estimator_results.mean_test_accuracy
   roc_auc = best_estimator_results.mean_test_roc_auc
   # Create table of results
   table = pd.DataFrame()
   table = table.append({'Model': model_name,
                        'Precision': precision,
                        'Recall': recall,
                        'F1': f1,
                        'Accuracy': accuracy,
                        'ROC-AUC' : roc_auc
                        },
                        ignore_index=True
   return table
lr_cv_results = make_results('Logistic Regression', lr_randm, 'roc_auc')
```

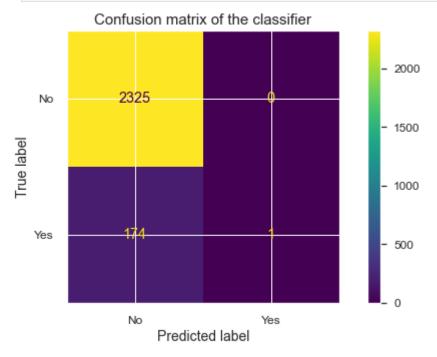
```
In [38]: # Get all CV scores
         lr_cv_results
```

```
Out[38]:
                       Model Precision Recall
                                                 F1 Accuracy ROC-AUC
                                           0.00 0.00
          0 Logistic Regression
                                   0.00
                                                          0.93
                                                                    0.62
```

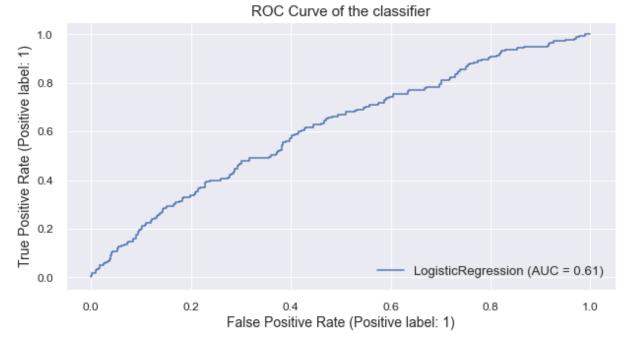
#### **Logistic Regression model**

```
In [39]: logreg = LogisticRegression( penalty='12', C=0.1, max_iter=1000, random_state=0, so
In [40]: logreg.fit(X_train,y_train)
Out[40]: LogisticRegression(C=0.1, max_iter=1000, random_state=0)
In [41]: logreg_pred = logreg.predict(X_test)
In [42]: logreg_pred[0:5]
Out[42]: array([0, 0, 0, 0, 0], dtype=int64)
In [43]: logreg.coef_
Out[43]: array([[-0.00645173, -0.02134201, 0.11508702, 0.30393628, -0.00959703,
                  0.00177016, -0.20658222, 0.11102757, -0.14985665, 0.10313881,
                 -0.00774341, 0.
                                     , 0.36816719, -0.32598921, -0.20154292]])
In [44]: logreg.intercept_
Out[44]: array([-2.33298616])
In [45]: logreg.score(X_train, y_train)
Out[45]: 0.929671868747499
In [46]: logreg.score(X_test, y_test)
Out[46]: 0.9304
         Logistic Model Evaluation
In [47]: print(classification_report(y_test,logreg_pred))
                     precision recall f1-score
                                                    support
                          0.93
                                    1.00
                                             0.96
                                                       2325
                          1.00
                                    0.01
                                             0.01
                                                        175
                                             0.93
                                                       2500
           accuracy
                          0.97
                                    0.50
                                             0.49
                                                       2500
          macro avg
       weighted avg
                          0.94
                                    0.93
                                             0.90
                                                       2500
In [48]: cm = confusion_matrix(y_test,logreg_pred)
Out[48]: array([[2325,
                         1]], dtype=int64)
                [ 174,
In [49]: fig, ax = plt.subplots(figsize=(10,5))
```

```
ConfusionMatrixDisplay.from_estimator(estimator=logreg, X=X_test, y=y_test, ax=ax, ax.set_title('Confusion matrix of the classifier', size=15)
plt.show()
```







Estimate the generalization error of a machine learning model

#### using Cross-Validation Schemes

```
In [51]: # K-Fold Cross-Validation
         kf = KFold(n_splits=5, shuffle=True, random_state=0)
In [52]: # estimate generalization error
         clf = cross_validate(estimator=logreg,
                           X=X_train,
                           y=y_train,
                           scoring='roc_auc',
                           return_train_score=True,
                           cv=kf)
In [53]: # mean test set roc-auc
         clf["test_score"].mean()
Out[53]: 0.6218615472715501
In [54]: # mean train set roc-auc
         clf["train_score"].mean()
Out[54]: 0.6383161789183376
In [55]: Irtable = pd.DataFrame()
         lrtable = lrtable.append({'Model': "Logistic Regression",
                               'F1': f1_score(y_test, logreg_pred),
                               'Recall': recall_score(y_test, logreg_pred),
                               'Precision': precision_score(y_test, logreg_pred),
                               'Accuracy': accuracy_score(y_test, logreg_pred),
                               'ROC-AUC': roc_auc_score(y_test, logreg_pred)
                             },
                               ignore_index=True)
         lrtable
Out[55]:
                     Model
                             F1 Recall Precision Accuracy ROC-AUC
         0 Logistic Regression 0.01
                                  0.01
                                           1.00
                                                    0.93
                                                             0.50
         ______
         Python code done by Dennis Lam
 In [ ]:
```