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★ Course / Unit 8: Linear Optimization / Assignment 8

(3)



### **Even' Star Organic Farm (OPTIONAL)**

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# IMPORTANT NOTE: This problem is optional, and will not count towards your grade. We have created this problem to give you extra practice with the topics covered in this unit.

Even' star organic farm (OPTIONAL)

Even' Star Organic Farm was founded in 1997 by Brett Grohsgal, a former chef in Washington DC. The company owns a 104-acre farm in southern Maryland, and grows and sells organic produce. For more information, see <a href="Even' Star's Facebook page">Even' Star's Facebook page</a>. This problem describes the business issues faced by Brett, and the data is based on actual observations.

Brett has decided to grow eight different types of produce: large tomatoes, small tomatoes, watermelon, okra, basil, cucumbers, sweet potatoes, and winter squash. He distributes his produce through three different channels: Restaurants, Community-Supported Agriculture, and Farmers' Markets.

Initially, he sold exclusively to restuarants. He knows of 20 restaurants that will buy his produce from his connections as a former chef. As his farm expanded, he also started selling his produce at a local farmers' market, where he can command a higher price. Recently, he has also started selling through Community Supported Agriculture (CSA), a program in which individuals pay a \$400 subscription price to get a box of produce each week for 15 weeks. He currently knows of 90 individuals who are interested in buying his produce through the CSA program.

Brett has a limited amount of produce that he can sell each season, and he needs to decide how much produce to sell through each channel (restaurants, CSA, or farmers' markets).

#### Problem 1.1 - Formulating the Problem

0 points possible (ungraded)

Let's formulate Brett's problem as a linear optimization problem. The spreadsheet <u>EvenStarFarm.ods</u> for LibreOffice or OpenOffice, and <u>EvenStarFarm.xlsx</u> for Microsoft Excel, contains the data for the problem, and has set up the decision variables and objective for you.

The **decision variables** in our problem are the number of cases of each type of produce to sell in each channel (there are 24 decision variables). They are highlighted in yellow in the spreadsheet.

Brett's **objective** is to maximize total profit (total revenue minus total cost). In the spreadsheet EvenStarFarm, the objective is highlighted in blue.

To compute the total revenue, we multiply the number of cases of each type of produce distributed in each channel by the price that Brett sells it for. The price of a case of each type of produce in each of the different channels is listed in cells C6:E13 of the spreadsheet.

The total cost is composed of two parts: a variable cost per client, and an entry cost for being in the particular channel. The entry costs are listed in cells B20:D20.

To compute the total variable cost for each restaurant client, we use the information that each restaurant client will buy 119 cases of produce during the season. So, the total number of restaurant clients served in a season can be computed as the total number of cases sold to restaurants, divided by 119. (Note that the number of restuarant clients Brett gives produce to could be fractional (like 16.57). This is a simplification we'll make for this problem, so please ignore the fact that this number should be integer. We'll see next week how you can add integer restrictions to an optimization model.)

To compute the total variable cost for CSA clients, we need to know that each CSA customer will buy \$400 worth of produce during the season. So, the total number of CSA clients served can be computed by dividing the total dollar amount sent to CSA customers by \$400. (Note that the number of CSA clients Brett gives produce to could be fractional (like 16.57). This is a simplification we'll make for this problem, so please ignore the fact that this number should be integer. We'll see next week how you can add integer restrictions to an optimization model.)

There is no variable cost for farmers' market clients.

() B19*S	UM(B26:B33)
B19/1	19
B19*( ✓	SUM(B26:B33)/119)
O SUM(	B26:B33)/119
estuarant c	cost per restaurant client is located in cell B19. We need to multiply this by the total number of lients, which can be computed by summing the total number of cases sent to restaurant clients, by 119, or SUM(B26:B33)/119. So the correct answer is B19*(SUM(B26:B33)/119).
Submit	You have used 0 of 1 attempt
<b>1</b> Answe	rs are displayed within the problem
	he data and variables in the spreadsheet EvenStarFarm.
~	SUMPRODUCT(C26:C33;D6:D13)/400)  PRODUCT(C26:C33:D6:D13)/400
SUMF	SUMPRODUCT(C26:C33;D6:D13)/400) PRODUCT(C26:C33;D6:D13)/400 SUMPRODUCT(C26:C33;D6:D13)
SUMF	PRODUCT(C26:C33;D6:D13)/400 SUMPRODUCT(C26:C33;D6:D13)
SUMF C19*S C19/4 Explanation The variable CSA custom	PRODUCT(C26:C33;D6:D13)/400 SUMPRODUCT(C26:C33;D6:D13)
SUMF C19*S C19/4 Explanation The variable CSA custom	PRODUCT(C26:C33;D6:D13)/400  SUMPRODUCT(C26:C33;D6:D13)  00  cost per CSA client is given in cell C19. We need to multiply this by the total dollar amount sent to ers, divided by \$400, which is computed is LibreOffice as SUMPRODUCT(C26:C33;D6:D13)/400.
SUMF C19*S C19/4 Explanation The variable CSA custom To the total Submit	PRODUCT(C26:C33;D6:D13)/400 SUMPRODUCT(C26:C33;D6:D13)  Cost per CSA client is given in cell C19. We need to multiply this by the total dollar amount sent to ers, divided by \$400, which is computed is LibreOffice as SUMPRODUCT(C26:C33;D6:D13)/400. variable cost is C19*(SUMPRODUCT(C26:C33;D6:D13)/400).
SUMF C19*S C19/4 Explanation The variable CSA custom So the total Submit  Answer	PRODUCT(C26:C33;D6:D13)/400  SUMPRODUCT(C26:C33;D6:D13)  Cost per CSA client is given in cell C19. We need to multiply this by the total dollar amount sent to ers, divided by \$400, which is computed is LibreOffice as SUMPRODUCT(C26:C33;D6:D13)/400. variable cost is C19*(SUMPRODUCT(C26:C33;D6:D13)/400).  You have used 0 of 1 attempt

<b>~</b>	
B26:D26 0	
B26:D26 0	
SUM(B26:D26)	36
SUM(B26:D26)	36
SUM(B26:D26)	36
han or equal to zero, and nore than the total numb	nts to restrict the total number of cases sold to each client (B26:D26) to be greater we need to make sure that the total number of cases sold (SUM(B26:D26)) is no eer produced, B6.  Constraints for each type of produce.
Submit You have use	ed 0 of 2 attempts
Answers are display	ed within the problem
constraint(s) captures thi	, the number of cases sold at the farmers' market can't be more than 600. Which s restriction?
SUM(D26:D33) = 6	500
D26:D33 600	
○ SUM(D26:D33)	600
Culta mait	of cases sold at the farmers' market, SUM(D26:D33) to be less than or equal to 600. ed 0 of 1 attempt
Answers are display	ed within the problem
Problem 1.5 - Form	ulating the Problem
0 points possible (ungraded) Brett knows that at most	

<b>*</b>		
SUM(B26:B33)/119 = 20		
O B26:B33/119 20		
B26:B33/119 = 20		
Explanation We first need to compute the total number of restaurant clients. We saw while this is SUM(B26:B33)/119. This should be less than or equal to 20.	computing the objective that	
Submit You have used 0 of 1 attempt		
Answers are displayed within the problem		
Problem 1.6 - Formulating the Problem		
Dipoints possible (ungraded) Brett knows that at most 90 CSA customers will buy his produce. Which consti Testriction? HINT: Each CSA customer buys \$400 worth of produce.	raint(s) captures this	
O SUM(C26:C33;D6:D13)/400 90		
SUMPRODUCT(C26:C33;D6:D13)/400 90		
SUM(C26:C33)/400 90		
Explanation We first need to compute the total number of CSA clients. We saw while composite SUMPRODUCT(C26:C33;D6:D13)/400. This should be less than or equal to 90 Add all of these constraints to your model in LibreOffice (or in the spreadsheet is a list of all of the constraints you should be adding:		
) Brett can't sell negative cases, and he can't sell more cases than he produce	es, for each type of produce.	
2) The number of cases sold at the farmer's market can't be more than 600.		
3) Brett can't sell produce to more than 20 restaurants.		
4) Brett can't sell produce to more than 90 CSA customers.		
Submit You have used 0 of 1 attempt		
Answers are displayed within the problem		
Problem 2.1 - Solving the Model		

0 points possible (ungraded)

Solve your model, and answer the following questions about the solution:

Explanation	
After solving the proble You should have added Large Tomato Limit: SU Small Tomato Limit: SUM Watermelon Limit: SUM Okra Limit: SUM(B29:D2 Basil Limit: SUM(B30:D2 Cucumbers Limit: SUM( Sweet Potatoes Limit: SUM Farmers' Market Limit: SU Restaurant Limit: SUM( CSA Limit: SUMPRODU	M(B27:D27) <= 608 I(B28:D28) <= 167 29) <= 76 30) <= 72 (B31:D31) <= 251 SUM(B32:D32) <= 107 JM(B33:D33) <= 133 SUM(D26:D33) <= 600
Submit You have u	used 0 of 6 attempts
• Answers are displa	ayed within the problem
Explanation The decision variable c	Answer: 0 orresponding to large tomatoes and CSA has value 0 in the solution.
	used 0 of 3 attempts
Submit You have u	ased 0 of 3 attempts
Tou Have C	ayed within the problem
• Answers are displaced and the control of the cont	ayed within the problem  lving the Model
• Answers are displaced points possible (ungrade	ayed within the problem  Iving the Model  ed)
Answers are displaced on the composition of the com	ayed within the problem  ving the Model  ed) termelon are given to farmer's market customers?

	Answer: 65.88
xplanation	
we look at the constraint for C	SA customers, we see that the left-hand side of the constraint has value technically sell produce to 66 customers (65 will get \$400 worth of produce, h of produce).
Submit You have used 0 of 3	3 attempts
• Answers are displayed with	in the problem
Problem 3.1 - Sensitivity	Analysis
200 more cases of produce to the	00 to trade in his truck for a larger truck. This would allow him to transport ne farmers' market (for a total of 800 cases). Should he do it? HINT: Adjust the ve it, and compare the increase in objective function value to the cost of
Yes, he should buy the lar	ger truck.
No, he shouldn't buy the la	arger truck.
Explanation  f you increase the right hand side e-solve the model, the new objection in the solution in the second	le of the constraint for farmers' market cases to 800 (increase by 200) and ective value is \$50,181.76. Compared to the old objective value of \$49,956.39 0,181.76 - \$49,956.39 = \$225.37. Since this is less than the cost of the truck,
Explanation  f you increase the right hand side solve the model, the new objection is an increase in profit of \$5	le of the constraint for farmers' market cases to 800 (increase by 200) and ective value is \$50,181.76. Compared to the old objective value of \$49,956.39 0,181.76 - \$49,956.39 = \$225.37. Since this is less than the cost of the truck,
Explanation  f you increase the right hand side re-solve the model, the new objection is an increase in profit of \$5 ne shouldn't buy the larger truck	le of the constraint for farmers' market cases to 800 (increase by 200) and ective value is \$50,181.76. Compared to the old objective value of \$49,956.39 0,181.76 - \$49,956.39 = \$225.37. Since this is less than the cost of the truck,
Explanation  f you increase the right hand side-solve the model, the new objection is an increase in profit of \$5 ne shouldn't buy the larger truck  Submit  You have used 0 of 1	le of the constraint for farmers' market cases to 800 (increase by 200) and ective value is \$50,181.76. Compared to the old objective value of \$49,956.39 0,181.76 - \$49,956.39 = \$225.37. Since this is less than the cost of the truck, attempt
Explanation  f you increase the right hand side re-solve the model, the new objection is an increase in profit of \$5 ne shouldn't buy the larger truck and the shouldn't buy the larger truck.  Submit  You have used 0 of 10 points possible (ungraded) One of Brett's workers has offered	le of the constraint for farmers' market cases to 800 (increase by 200) and ective value is \$50,181.76. Compared to the old objective value of \$49,956.39 0,181.76 - \$49,956.39 = \$225.37. Since this is less than the cost of the truck, attempt
Explanation  If you increase the right hand side e-solve the model, the new objective is an increase in profit of \$5 are shouldn't buy the larger truck of Submit  You have used 0 of 10 are points possible (ungraded) one of Brett's workers has offerearmer's market (for a total of 80 are points possible).	le of the constraint for farmers' market cases to 800 (increase by 200) and ective value is \$50,181.76. Compared to the old objective value of \$49,956.39 0,181.76 - \$49,956.39 = \$225.37. Since this is less than the cost of the truck, attempt  in the problem  / Analysis  ed to use his truck to help Brett transport 200 more cases of produce to the 0 cases). Which of the following choices would increase Brett's profit? Select

\$225.37. Thus Brett should hire the worker, and pay him \$150, since that will give him an additional profit of \$225.37 - \$150.00 = \$75.37. Submit You have used 0 of 2 attempts Answers are displayed within the problem Problem 3.3 - Sensitivity Analysis 0 points possible (ungraded) Now suppose that Brett has found 10 more customers who would like to join the CSA program, for a total of 100 potential CSA customers. Should he sell produce to these customers? If you have changed any values in the constraints, change them back to their original values before answering this question (600 cases at the farmers' market). Yes, adding all of these extra customers will increase his profit. Yes, adding some of these extra customers will increase his profit. No, he shouldn't sell produce to any of these customers. Explanation Since the constraint for CSA customers is not binding (we sell to 65.88 customers, when we know of 90) it is not beneficial to add 10 more CSA customers. Submit You have used 0 of 1 attempt Answers are displayed within the problem Problem 3.4 - Sensitivity Analysis 0 points possible (ungraded) Now suppose that Brett has purchased 5 additional acres of land, which allows him to produce 10 additional cases of one of his vegetables. Which vegetable should he plant on these 5 additional acres? If you have changed any values in the constraints, change them back to their original values before answering this question (600 cases at the farmers' market, and 90 potential CSA customers). Assume for this problem that the production cost is the same for all types of produce. For your reference, here is a list of the number of cases of each type of produce that Brett currently produces: 406 cases of Large Tomatoes, 608 cases of Small Tomatoes, 167 cases of Watermelon, 76 cases of Okra, 72 cases of Basil, 251 cases of Cucumbers, 107 cases of Sweet Potatoes, and 133 cases of Winter Squash. Tomatoes (large) Tomatoes (small) Watermelon Okra Basil Cucumber

Swee	et Potatoes	
O Winte	ter Squash	
-	ease the total number of cases of each type of produce one at a increase in the objective function value. Thus, Brett should pla	
Culomit		
Submit	You have used 0 of 2 attempts	
	ers are displayed within the problem	
<b>1</b> Answe		
Answer Acknowl This proble	ers are displayed within the problem	
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