# 3 Pythagorean expectation and the NBA

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## Pythagorean Expectation and the NBA

The NBA is the most popular basketball league in the world, and consists of 30 teams playing an 82 game regular season followed by playoffs to determine the champion. In terms of scale, this data looks much more like MLB data than the IPL data we just looked at.

Basketball resembles cricket in one way - the scores are much higher than in baseball. However, the points difference between winning and losing teams tend to be relatively small.

Let's see what we find this time. We follow the same procedure.

```
# Load the packages
options(warn = -1)
library("readxl", quietly = TRUE)
library("tidyverse", quietly = TRUE)
library("dplyr",quietly = TRUE)
library("ggplot2",quietly = TRUE)
# Now we import the data, which comes in the form of
# a list of games played in the 2018 season.
# We print out the list of variables names in the dataframe
# Load the data and see what it looks like
NBA = read.csv('NBA Games.csv')
head(NBA)
##
                               TEAM_NAME
              CITY
                                             TEAM_ID GAME_ID NICKNAME
## 1 Oklahoma City Oklahoma City Thunder 1610612760 11300001
                                                               Thunder
## 2
           Chicago
                           Chicago Bulls 1610612741 11300002
                                                                 Bulls
## 3
                          Indiana Pacers 1610612754 11300002
           Indiana
                                                                Pacers
## 4
       New Orleans
                    New Orleans Pelicans 1610612740 11300003 Pelicans
## 5
           Houston
                         Houston Rockets 1610612745 11300003 Rockets
## 6
      Golden State Golden State Warriors 1610612744 11300004 Warriors
##
          STATE YEAR_FOUNDED SEASON_ID TEAM_ABBREVIATION GAME_DATE
                                                      OKC 10/5/2013
## 1
       Oklahoma
                                 12013
                        1967
```

12013

12013

1966

1976

## 2

## 3

Illinois

Indiana

CHI 10/5/2013

IND 10/5/2013

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```
2002
                                   12013
## 4
     Louisiana
                                                         NOP 10/5/2013
## 5
                          1967
                                   12013
          Texas
                                                         HOU 10/5/2013
## 6 California
                          1946
                                   12013
                                                         GSW 10/5/2013
##
         MATCHUP WL MIN PTS PTSAGN FGM FGA FG_PCT FG3M FG3A FG3_PCT FTM FTA
                   W 241
                           95
                                  NA
                                       36
                                           74 0.486
                                                         2
                                                              14
                                                                   0.143
                                                                           21
                                                                               28
## 1
       OKC @ FBU
       CHI @ IND
                   W 239
                          82
                                       28
                                                                           23
## 2
                                  76
                                           74
                                               0.378
                                                         3
                                                              10
                                                                   0.300
                                                                               30
## 3 IND vs. CHI
                   L 240
                          76
                                 82
                                       27
                                           82
                                               0.329
                                                         5
                                                              17
                                                                   0.294
                                                                           17
                                                                               23
                   W 239 116
       NOP @ HOU
                                 115
                                       42
                                           86
                                               0.488
                                                                               40
                                                              10
                                                                   0.400
                   L 240 115
## 5 HOU vs. NOP
                                 116
                                       39
                                           68
                                               0.574
                                                         8
                                                              22
                                                                   0.364
                                                                               38
## 6
       GSW @ LAL
                   L 241
                           95
                                 104
                                       35
                                           88
                                               0.398
                                                         5
                                                              21
                                                                   0.238
                                                                               28
     FT PCT OREB DREB REB AST STL BLK TOV PF PLUS MINUS home not.paired
      0.750
                         52
                             22
                                  9
                                       8
                                          20 26
                                                         13
                                                                Α
## 1
               18
                    34
                                                                          999
                                                          6
      0.767
                         56
                             20
                                  5
                                          23 25
                                                                Α
                                                                            0
## 2
               17
                    39
                                      10
## 3
      0.739
                         38
                             15
                                 12
                                          15 23
                                                         -6
                                                                Η
                                                                            0
               11
                    27
                                       8
      0.700
               12
                    21
                         33
                             17
                                 12
                                          15 32
                                                                            0
## 4
                                                          1
                                                                Α
## 5
      0.763
                5
                    30
                         35
                             24
                                  9
                                       4
                                          22 27
                                                         -1
                                                                Η
                                                                            0
## 6
      0.714
                    38
                        52
                             21
                                 13
                                       5
                                          23 31
                                                         -9
                                                                Α
                                                                            0
               14
tail(NBA)
##
                 CITY
                                 TEAM NAME
                                               TEAM_ID
                                                           GAME ID NICKNAME
## 18411
           Cleveland Cleveland Cavaliers 1610612739 1621900005 Cavaliers
                        Memphis Grizzlies 1610612763 1621900005 Grizzlies
## 18412
              Memphis
## 18413 San Antonio
                        San Antonio Spurs 1610612759 1621900006
                                                                        Spurs
                                 Utah Jazz 1610612762 1621900006
## 18414
                 Utah
                                                                          Jazz
## 18415
                                                     NA
                                                                 NA
## 18416
                                                     NA
##
              STATE YEAR FOUNDED SEASON ID TEAM ABBREVIATION GAME DATE
                                       22019
                                                            CLE 7/3/2019
## 18411
               Ohio
                             1970
## 18412 Tennessee
                             1995
                                       22019
                                                            MEM 7/3/2019
                                                            SAS
                                                                7/3/2019
## 18413
              Texas
                             1976
                                       22019
## 18414
               Utah
                             1974
                                       22019
                                                            UTA 7/3/2019
## 18415
                               NA
                                          NA
## 18416
                               NA
                                          NA
              MATCHUP WL MIN PTS PTSAGN FGM FGA FG_PCT FG3M FG3A FG3_PCT FTM
##
## 18411
           CLE @ MEM
                       L 201
                               68
                                       81
                                           22
                                               60 0.367
                                                             10
                                                                  35
                                                                       0.286
                                                                               14
                                               74 0.419
## 18412 MEM vs. CLE
                       W 199
                               81
                                       68
                                           31
                                                             10
                                                                  28
                                                                       0.357
                                                                                9
                                               70
                                                             7
## 18413
           SAS @ UTA
                       L 200
                               81
                                       84
                                           29
                                                    0.414
                                                                  17
                                                                       0.412
                                                                               16
                                           30
                                               74
## 18414 UTA vs. SAS
                       W 199
                               84
                                       81
                                                    0.405
                                                                  31
                                                                       0.355
                                                                               13
                                                             11
## 18415
                           NA
                               NA
                                       NA
                                          NA
                                               NA
                                                       NA
                                                            NA
                                                                  NA
                                                                           NA
                                                                               NA
## 18416
                               NA
                                       NA
                                           NA
                                               NA
                           NA
                                                       NA
                                                            NA
                                                                  NA
                                                                           NA
                                                                               NA
         FTA FT PCT OREB DREB REB AST STL BLK TOV PF PLUS MINUS home
## 18411
          19
               0.737
                        3
                             26
                                 29
                                      15
                                           9
                                               3
                                                   17 12
                                                               -13.0
                                                                        Α
## 18412
               0.692
                                 47
                                      19
                                           8
                                               5
                                                                13.0
                                                                        Η
          13
                        11
                             36
                                                   14 19
## 18413
               0.615
                         9
                             29
                                 38
                                      12
                                           5
                                               3
                                                   11 14
                                                                -7.2
                                                                        Α
          26
```

```
## 18414 19 0.684
                                               15 25
                                                             5.8
                      13
                           31
                               44 15
                                        6
                                             5
                                                                    Η
## 18415
          NA
                               NA
                                   NA
                                                              NA
                 NA
                      NA
                           NA
                                       NA
                                           NA
                                                NA NA
## 18416 NA
                      NA
                                                              NA
                 NA
                           NA
                               NA
                                   NA
                                       NA
                                           NA
                                                NA NA
         not.paired
## 18411
## 18412
                  0
## 18413
                  0
## 18414
                  0
## 18415
                 NA
                636
## 18416
# The data consists of games played between 2013 and 2019.
# An important difference from the baseball and cricket data
# is that here each game appears in two rows, one for each team.
# Each pair of rows are mirror images of each other.
# The season is identified by the column SEASON_ID
# Pre-season games have the prefix "1" before the year,
# regular season games have the prefix "2"
# and postseason games have the prefix "4".
# We are going to look at the 2018 regular season and therefore
# want games with the prefix "2"
# We can use the command "summary()" to obtain descriptive statistics for our variable
NBAR18 = NBA %>% filter(SEASON ID == 22018)
NBAR18 %>% summary()
##
              CITY
                                         TEAM_NAME
                                                         TEAM_ID
## Los Angeles :
                   92
                        Los Angeles Lakers
                                                             :1.611e+09
                                                 92
                                                      Min.
##
   Memphis
                   92
                        Memphis Grizzlies
                                                 92
                                                      1st Qu.:1.611e+09
## Atlanta
                   91
                        Atlanta Hawks
                                                 91
                                                      Median :1.611e+09
## Golden State:
                   90
                        Golden State Warriors:
                                                 90
                                                      Mean
                                                             :1.611e+09
## Miami
                   90
                        Miami Heat
                                                 90
                                                      3rd Qu.:1.611e+09
##
    Sacramento
                   90
                        Sacramento Kings
                                                 90
                                                             :1.611e+09
##
    (Other)
                :2015
                        (Other)
                                              :2015
##
       GAME_ID
                             NICKNAME
                                                 STATE
                                                             YEAR_FOUNDED
## Min.
           :2.180e+07
                        Grizzlies:
                                    92
                                          California: 272
                                                            Min.
                                                                  :1946
    1st Qu.:2.180e+07
                                    92
                                                    : 264
                                                            1st Qu.:1949
                        Lakers
                                         Texas
## Median :2.180e+07
                        Hawks
                                    91
                                         Florida
                                                    : 177
                                                            Median:1970
```

90

90

90

New York : 174

Tennessee: 92

GAME\_DATE

91

:1490

Atlanta

(Other)

:1970

:2002

3rd Qu.:1980

MATCHUP

Mean

Max.

## Mean

## Max.

##

##

##

:1.280e+08

:1.622e+09

3rd Qu.:2.180e+07

SEASON\_ID

Heat

Jazz

Kings

TEAM\_ABBREVIATION

(Other) :2015

```
##
    Min.
           :22018
                     LAL
                                92
                                         11/23/2018:
                                                       27
                                                            MEM @ UTA
                                                                            4
##
    1st Qu.:22018
                     MEM
                                92
                                         4/7/2019
                                                       27
                                                            UTA vs. MEM:
##
    Median :22018
                     ATL
                                91
                                         11/21/2018:
                                                       26
                                                            ATL @ CHI
                                                                             3
##
    Mean
            :22018
                     GSW
                                90
                                         4/5/2019 :
                                                       25
                                                            ATL @ IND
                                                                             3
    3rd Qu.:22018
##
                     MIA
                                90
                                         12/19/2018:
                                                       24
                                                            ATL vs. NYK:
                                                                             3
##
            :22018
                     SAC
                                         2/23/2019 :
                                                       24
                                                            BKN @ IND
                                                                             3
    Max.
                                90
##
                                                    :2407
                                                            (Other)
                     (Other):2015
                                         (Other)
                                                                         :2540
                                  PTS
                                                                     FGM
##
    WL
                   MIN
                                                   PTSAGN
##
         0
                     :197
                                     : 53.0
                                              Min.
                                                      : 53.0
                                                               Min.
                                                                       :17.00
     :
              Min.
                             Min.
    L:1286
              1st Qu.:239
                             1st Qu.:100.0
                                              1st Qu.:100.0
                                                                1st Qu.:37.00
##
##
    W:1274
             Median:240
                             Median :110.0
                                              Median :110.0
                                                                Median :40.00
                             Mean
                                              Mean
                                                               Mean
##
              Mean
                     :239
                                     :109.2
                                                      :109.1
                                                                       :40.36
              3rd Qu.:241
                             3rd Qu.:118.0
##
                                              3rd Qu.:118.0
                                                                3rd Qu.:44.00
                             Max.
              Max.
##
                     :341
                                    :168.0
                                              Max.
                                                      :168.0
                                                                Max.
                                                                       :61.00
##
                                              NA's
                                                      :88
         FGA
                           FG PCT
                                              FG3M
                                                                FG3A
##
           : 55.00
                                                : 2.00
##
    Min.
                      Min.
                              :0.2620
                                         Min.
                                                          Min.
                                                                  :13.00
##
    1st Qu.: 83.00
                      1st Qu.:0.4208
                                         1st Qu.: 9.00
                                                          1st Qu.:27.00
##
    Median: 88.00
                      Median :0.4580
                                         Median :11.00
                                                          Median :31.00
##
    Mean
           : 88.21
                      Mean
                              :0.4580
                                         Mean
                                                :11.16
                                                          Mean
                                                                  :31.75
    3rd Qu.: 93.00
##
                      3rd Qu.:0.4940
                                         3rd Qu.:13.00
                                                          3rd Qu.:36.00
    Max.
           :123.00
                                         Max.
##
                      Max.
                              :0.6490
                                                 :27.00
                                                          Max.
                                                                  :70.00
##
##
       FG3 PCT
                            FTM
                                             FTA
                                                             FT PCT
                                               : 4.00
##
    Min.
            :0.0800
                      Min.
                              : 2.00
                                        Min.
                                                         Min.
                                                                 :0.2630
    1st Qu.:0.2920
                      1st Qu.:13.00
                                        1st Qu.:18.00
                                                         1st Qu.:0.7000
##
##
    Median : 0.3480
                      Median :17.00
                                        Median :22.00
                                                         Median :0.7680
##
    Mean
            :0.3508
                      Mean
                              :17.32
                                        Mean
                                               :22.72
                                                         Mean
                                                                 :0.7631
##
    3rd Qu.:0.4060
                      3rd Qu.:21.00
                                        3rd Qu.:27.25
                                                         3rd Qu.:0.8330
##
    Max.
           :0.8420
                      Max.
                              :44.00
                                        Max.
                                               :54.00
                                                         Max.
                                                                 :1.0000
##
         OREB
                           DREB
##
                                           REB
                                                            AST
           : 1.00
                                                       Min.
                                                               : 7.00
                                     Min.
##
    Min.
                     Min.
                             :17.0
                                             :22.00
##
    1st Qu.: 8.00
                     1st Qu.:30.0
                                      1st Qu.:40.00
                                                       1st Qu.:20.00
    Median :10.00
                     Median:34.0
                                     Median :44.00
                                                       Median :24.00
##
    Mean
                             :34.4
##
           :10.34
                     Mean
                                     Mean
                                             :44.75
                                                       Mean
                                                              :24.03
##
    3rd Qu.:13.00
                     3rd Qu.:38.0
                                      3rd Qu.:49.00
                                                       3rd Qu.:28.00
##
    Max.
           :26.00
                     Max.
                             :55.0
                                      Max.
                                             :71.00
                                                       Max.
                                                               :42.00
##
         STL
                            BLK
                                              TOV
                                                                 PF
##
           : 0.000
                      Min.
##
    Min.
                              : 0.000
                                         Min.
                                                 : 3.00
                                                          Min.
                                                                  : 9.00
    1st Qu.: 6.000
                      1st Qu.: 3.000
##
                                         1st Qu.:11.00
                                                          1st Qu.:18.00
    Median : 7.000
                                         Median :13.00
##
                      Median : 5.000
                                                          Median :21.00
##
           : 7.694
                             : 4.974
                                                          Mean
    Mean
                      Mean
                                         Mean
                                                :13.61
                                                                  :20.85
##
    3rd Qu.:10.000
                      3rd Qu.: 6.000
                                         3rd Qu.:16.00
                                                          3rd Qu.:24.00
```

```
:20.000
                             :19.000
                                               :27.00
##
    Max.
                     {\tt Max.}
                                       {\tt Max.}
                                                        {\tt Max} .
                                                               :38.00
##
##
      PLUS_MINUS
                                    not.paired
                         home
           :-56.00000
                         :
                                        : 0.00
                              0
    1st Qu.: -9.00000
                                   1st Qu.:
##
                         A:1279
                                             0.00
                                  Median: 0.00
    Median : -1.00000
                         H:1281
##
    Mean
          : -0.04188
                                  Mean
                                         : 34.34
                                   3rd Qu.: 0.00
    3rd Qu.:
              9.00000
           : 56.00000
                                          :999.00
##
    Max.
                                  Max.
##
# We can list all the variable names
names (NBAR18)
    [1] "CITY"
                             "TEAM NAME"
                                                  "TEAM ID"
##
    [4] "GAME_ID"
                             "NICKNAME"
                                                  "STATE"
    [7] "YEAR_FOUNDED"
                             "SEASON_ID"
                                                   "TEAM_ABBREVIATION"
                             "MATCHUP"
                                                  "WL"
## [10] "GAME_DATE"
## [13] "MIN"
                             "PTS"
                                                  "PTSAGN"
## [16] "FGM"
                             "FGA"
                                                  "FG PCT"
## [19] "FG3M"
                             "FG3A"
                                                  "FG3 PCT"
## [22] "FTM"
                             "FTA"
                                                  "FT PCT"
## [25] "OREB"
                             "DREB"
                                                  "REB"
## [28] "AST"
                             "STL"
                                                  "BLK"
## [31] "TOV"
                             "PF"
                                                   "PLUS_MINUS"
## [34] "home"
                             "not.paired"
# Many datasets contain missing variables.
# Missing variables in a column will usually cause operations to fail.
# The command ".dropna()" will eliminate missing variables.
# Compare the counts of variables below after the na.omit() below to the counts in the
NBAR18 <- NBAR18 %>% na.omit()
NBAR18 %>% summary()
##
             CITY
                                       TEAM_NAME
                                                        TEAM_ID
##
    Atlanta
                   88
                        Atlanta Hawks
                                            :
                                               88
                                                            :1.611e+09
                                                    \mathtt{Min}.
                   88
                                               88
                                                     1st Qu.:1.611e+09
    Memphis
                        Memphis Grizzlies
                        Miami Heat
##
    Miami
                   88
                                               88
                                                    Median :1.611e+09
                   87
    Cleveland :
                        Cleveland Cavaliers:
                                               87
                                                    Mean
                                                            :1.611e+09
                   87
                        Los Angeles Lakers :
                                               87
    Los Angeles:
                                                    3rd Qu.:1.611e+09
##
                   87
                        Utah Jazz
    Utah
                                               87
                                                    Max.
                                                            :1.611e+09
```

88

NICKNAME

:1947

STATE

California: 257

YEAR FOUNDED

:1946

Min.

:1947

:2.180e+07

(Other)

Grizzlies:

##

##

##

(Other)

Min.

GAME ID

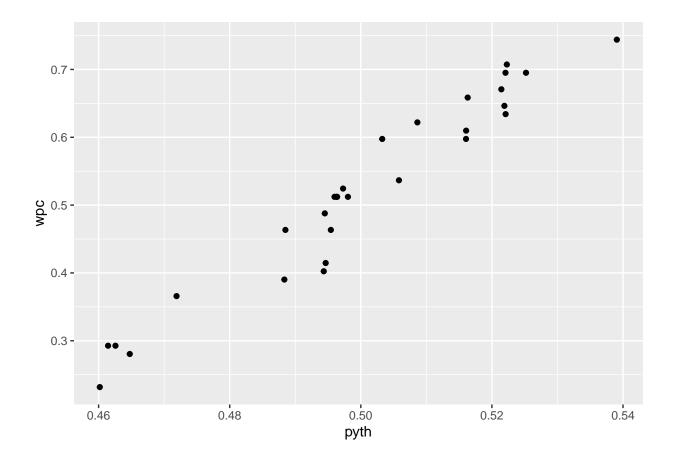
```
## 1st Qu.:2.180e+07
                                                   : 252
                                                           1st Qu.:1949
                        Hawks
                                :
                                    88
                                         Texas
                                                   : 173
## Median :2.180e+07
                                    88
                                                           Median:1970
                        Heat
                                         Florida
##
   Mean
           :1.281e+08
                        Cavaliers:
                                    87
                                         New York
                                                   : 170
                                                           Mean :1970
##
    3rd Qu.:2.180e+07
                        Jazz
                                    87
                                         Atlanta
                                                      88
                                                           3rd Qu.:1980
   Max. :1.622e+09
##
                        Lakers
                                 :
                                    87
                                         Tennessee :
                                                      88
                                                           Max.
                                                                  :2002
                                         (Other)
##
                        (Other) :1947
                                                   :1444
##
                    TEAM ABBREVIATION
      SEASON ID
                                           GAME DATE
                                                               MATCHUP
          :22018
                                      11/21/2018:
##
                    ATL
                           :
                              88
                                                   26
                                                        MEM @ UTA
   Min.
    1st Qu.:22018
                    MEM
                              88
                                      11/23/2018:
##
                           :
                                                   26
                                                        UTA vs. MEM:
                                                                       4
   Median :22018
                                                   26
##
                    MIA
                              88
                                      4/7/2019 :
                                                        ATL @ CHI
##
   Mean
          :22018
                    CLE
                              87
                                      12/19/2018:
                                                   24
                                                        ATL @ IND
                                                                       3
##
    3rd Qu.:22018
                    LAL
                              87
                                      2/23/2019 :
                                                   24
                                                        ATL vs. NYK:
##
   Max. :22018
                    UTA
                              87
                                      4/5/2019 :
                                                   24
                                                        BKN @ IND
                                                                       3
                           :
                                                        (Other)
##
                    (Other):1947
                                      (Other)
                                                :2322
                                                                   :2452
                                                 PTSAGN
##
   WL
                  MIN
                                  PTS
                                                                  FGM
    : 0
                                 : 53.0
                                                    : 53.0
##
            Min.
                    :197.0
                                             Min.
                                                                    :17.00
                             Min.
                                                             Min.
             1st Qu.:239.0
                             1st Qu.:100.0
                                             1st Qu.:100.0
##
   L:1236
                                                             1st Qu.:37.00
##
   W:1236
            Median :240.0
                             Median :110.0
                                             Median :110.0
                                                             Median :40.00
                    :238.9
##
             Mean
                             Mean
                                  :109.1
                                             Mean
                                                  :109.1
                                                             Mean
                                                                    :40.34
##
             3rd Qu.:241.0
                             3rd Qu.:118.0
                                             3rd Qu.:118.0
                                                             3rd Qu.:44.00
                             Max. :168.0
                    :341.0
                                             Max. :168.0
                                                             Max. :61.00
##
             Max.
##
        FGA
##
                         FG PCT
                                           FG3M
                                                           FG3A
##
   Min. : 55.00
                     Min.
                            :0.2620
                                      Min.
                                             : 2.00
                                                      Min.
                                                             :13.00
##
    1st Qu.: 83.00
                     1st Qu.:0.4208
                                      1st Qu.: 9.00
                                                      1st Qu.:27.00
##
   Median : 88.00
                     Median :0.4580
                                      Median :11.00
                                                      Median :31.50
##
   Mean
          : 88.14
                                      Mean
                                             :11.19
                                                      Mean
                                                             :31.83
                     Mean
                            :0.4581
##
    3rd Qu.: 93.00
                     3rd Qu.:0.4940
                                      3rd Qu.:14.00
                                                      3rd Qu.:36.00
##
   Max. :123.00
                     Max. :0.6490
                                      Max. :27.00
                                                      Max.
                                                             :70.00
##
##
      FG3 PCT
                          FTM
                                          FTA
                                                        FT PCT
                     Min. : 2.00
                                                    Min.
##
   Min.
           :0.0800
                                     Min. : 4.0
                                                           :0.2630
                     1st Qu.:13.00
                                     1st Qu.:18.0
##
    1st Qu.:0.2930
                                                    1st Qu.:0.7000
   Median : 0.3500
                     Median :17.00
                                     Median:22.0
                                                    Median :0.7670
##
   Mean
          :0.3511
                     Mean
                          :17.21
                                     Mean
                                            :22.6
                                                    Mean
                                                           :0.7626
    3rd Qu.:0.4070
                     3rd Qu.:21.00
                                     3rd Qu.:27.0
##
                                                    3rd Qu.:0.8330
##
   Max.
          :0.8420
                     Max. :44.00
                                     Max. :54.0
                                                    Max.
                                                           :1.0000
##
##
         OREB
                         DREB
                                         REB
                                                         AST
##
   Min.
          : 1.00
                    Min.
                           :17.00
                                    Min.
                                           :22.00
                                                    Min.
                                                           : 7.00
   1st Qu.: 8.00
##
                    1st Qu.:30.00
                                    1st Qu.:40.00
                                                    1st Qu.:20.00
                                    Median :44.00
##
                    Median :34.00
                                                    Median :24.00
   Median :10.00
##
   Mean
         :10.32
                    Mean :34.41
                                    Mean :44.73
                                                    Mean
                                                           :24.05
##
   3rd Qu.:13.00
                    3rd Qu.:38.00
                                    3rd Qu.:49.00
                                                    3rd Qu.:28.00
##
   Max. :26.00
                    Max. :55.00
                                    Max. :71.00
                                                    Max.
                                                           :42.00
```

```
##
##
        STL
                          BLK
                                           TOV
                                                            PF
##
   Min.
          : 0.000
                     Min. : 0.000
                                      Min.
                                             : 3.00
                                                      Min.
                                                            : 9.00
    1st Qu.: 6.000
                     1st Qu.: 3.000
                                      1st Qu.:11.00
                                                      1st Qu.:18.00
   Median : 7.000
                     Median : 5.000
                                      Median :13.00
                                                      Median :21.00
##
                          : 4.933
         : 7.675
##
   Mean
                     Mean
                                      Mean
                                            :13.64
                                                      Mean
                                                             :20.75
##
   3rd Qu.:10.000
                     3rd Qu.: 6.000
                                      3rd Qu.:16.00
                                                      3rd Qu.:23.00
          :20.000
                           :19.000
                                             :27.00
##
   Max.
                     Max.
                                      Max.
                                                      Max.
                                                             :37.00
##
##
      PLUS MINUS
                                   not.paired
                        home
##
   Min.
          :-56.00000
                        :
                                 Min.
                                        :0
    1st Qu.: -9.00000
                        A:1236
##
                                 1st Qu.:0
   Median: 0.00000
                                 Median:0
                        H:1236
##
         : -0.01909
                                        :0
   Mean
                                 Mean
   3rd Qu.: 9.00000
                                 3rd Qu.:0
## Max.
          : 56.00000
                                 Max.
                                        :0
##
# The game result is the column labeled 'WL'.
# We create a variable which has a value of '1' if the team won, and zero if it lost.
# This type of variable, where a condition (here winning) is
# either true (1) or not true (0) is called a "dummy variable".
# We will encounter them frequently.
NBAR18[,'result'] = ifelse(NBAR18$WL == 'W',1,0)
NBAR18 %>% summary()
##
             CITY
                                     TEAM NAME
                                                     TEAM ID
## Atlanta
                 88
                       Atlanta Hawks
                                             88
                                                         :1.611e+09
               :
                                          :
                                                  Min.
                                                  1st Qu.:1.611e+09
##
   Memphis
                  88
                       Memphis Grizzlies
                                             88
   Miami
                       Miami Heat
                                                  Median :1.611e+09
##
                  88
                                             88
                                                         :1.611e+09
## Cleveland :
                  87
                       Cleveland Cavaliers:
                                             87
                                                  Mean
   Los Angeles:
                       Los Angeles Lakers :
                                                  3rd Qu.:1.611e+09
                  87
                                             87
##
   Utah
                  87
                       Utah Jazz
                                                         :1.611e+09
                                             87
                                                  Max.
    (Other)
##
               :1947
                       (Other)
                                          :1947
##
       GAME ID
                             NICKNAME
                                                            YEAR FOUNDED
                                                STATE
   Min.
           :2.180e+07
                        Grizzlies:
                                    88
                                         California: 257
                                                           Min.
                                                                :1946
##
   1st Qu.:2.180e+07
                       Hawks
                                    88
                                         Texas
                                                   : 252
                                                           1st Qu.:1949
   Median :2.180e+07
                                                           Median:1970
##
                       Heat
                                         Florida
                                                   : 173
                                    88
##
   Mean
          :1.281e+08
                       Cavaliers:
                                    87
                                         New York : 170
                                                           Mean
                                                                :1970
##
    3rd Qu.:2.180e+07
                        Jazz
                                    87
                                         Atlanta
                                                      88
                                                           3rd Qu.:1980
          :1.622e+09
                        Lakers
                                                                  :2002
##
   Max.
                                 :
                                    87
                                         Tennessee: 88
                                                           Max.
##
                        (Other) :1947
                                         (Other)
                                                   :1444
##
      SEASON ID
                    TEAM ABBREVIATION
                                           GAME DATE
                                                               MATCHUP
           :22018
                    ATL
                                      11/21/2018: 26
##
   Min.
                        : 88
                                                        MEM @ UTA :
```

```
## 1st Qu.:22018
                            88
                                    11/23/2018: 26
                                                      UTA vs. MEM:
                   MEM
## Median :22018
                   MIA
                             88
                                    4/7/2019 :
                                                 26
                                                      ATL @ CHI
##
   Mean
          :22018
                   CLE
                             87
                                    12/19/2018:
                                                 24
                                                      ATL @ IND
                                                                    3
##
   3rd Qu.:22018
                   LAL
                             87
                                    2/23/2019 :
                                                 24
                                                      ATL vs. NYK:
          :22018
                                                      BKN @ IND
##
   Max.
                   UTA
                         :
                            87
                                    4/5/2019 : 24
                                                                    3
##
                   (Other):1947
                                     (Other)
                                                      (Other)
                                              :2322
                                                                 :2452
                 MIN
                                PTS
                                               PTSAGN
                                                               FGM
##
   WL
            Min.
                            Min. : 53.0
                                                  : 53.0
##
   : 0
                   :197.0
                                           Min.
                                                           Min.
                                                                 :17.00
   L:1236
            1st Qu.:239.0
                                          1st Qu.:100.0
##
                            1st Qu.:100.0
                                                          1st Qu.:37.00
##
   W:1236
            Median :240.0
                            Median :110.0
                                           Median :110.0
                                                          Median :40.00
##
            Mean
                   :238.9
                            Mean
                                  :109.1
                                           Mean :109.1
                                                          Mean
                                                                 :40.34
##
            3rd Qu.:241.0
                            3rd Qu.:118.0
                                           3rd Qu.:118.0
                                                           3rd Qu.:44.00
##
            Max.
                   :341.0
                            Max. :168.0
                                           Max.
                                                  :168.0
                                                          Max.
                                                                 :61.00
##
     FGA
                                         FG3M
                                                         FG3A
##
                      FG PCT
   Min. : 55.00
                    Min. :0.2620
                                    Min. : 2.00
##
                                                    Min.
                                                          :13.00
   1st Qu.: 83.00
                                    1st Qu.: 9.00
                                                    1st Qu.:27.00
##
                    1st Qu.:0.4208
##
  Median : 88.00
                    Median :0.4580
                                    Median :11.00
                                                    Median :31.50
##
   Mean
         : 88.14
                                                         :31.83
                    Mean :0.4581
                                    Mean :11.19
                                                    Mean
                                    3rd Qu.:14.00
##
   3rd Qu.: 93.00
                    3rd Qu.:0.4940
                                                    3rd Qu.:36.00
                    Max. :0.6490
                                    Max. :27.00
                                                    Max. :70.00
##
   Max. :123.00
##
##
                         FTM
                                        FTA
      FG3 PCT
                                                      FT PCT
                                                  Min. :0.2630
                    Min. : 2.00
##
   Min. :0.0800
                                   Min. : 4.0
##
   1st Qu.:0.2930
                    1st Qu.:13.00
                                    1st Qu.:18.0
                                                  1st Qu.:0.7000
##
   Median :0.3500
                    Median :17.00
                                   Median:22.0
                                                  Median :0.7670
##
   Mean
         :0.3511
                    Mean :17.21
                                   Mean :22.6
                                                  Mean :0.7626
##
   3rd Qu.:0.4070
                    3rd Qu.:21.00
                                   3rd Qu.:27.0
                                                  3rd Qu.:0.8330
   Max. :0.8420
                                   Max. :54.0
##
                    Max. :44.00
                                                  Max. :1.0000
##
##
      OREB
                        DREB
                                       REB
                                                       AST
   Min. : 1.00
                   Min.
                                                  Min. : 7.00
                         :17.00
                                  Min.
##
                                         :22.00
   1st Qu.: 8.00
                   1st Qu.:30.00
                                   1st Qu.:40.00
                                                  1st Qu.:20.00
##
                                  Median :44.00
   Median :10.00
                   Median :34.00
                                                  Median :24.00
##
   Mean
         :10.32
                   Mean :34.41
                                  Mean :44.73
                                                  Mean :24.05
                   3rd Qu.:38.00
                                                  3rd Qu.:28.00
   3rd Qu.:13.00
                                   3rd Qu.:49.00
##
##
   Max. :26.00
                   Max. :55.00
                                  Max.
                                         :71.00
                                                  Max. :42.00
##
                         BLK
                                         TOV
                                                          PF
##
        STL
##
   Min.
          : 0.000
                    Min. : 0.000
                                    Min. : 3.00
                                                    Min. : 9.00
##
   1st Qu.: 6.000
                    1st Qu.: 3.000
                                    1st Qu.:11.00
                                                    1st Qu.:18.00
##
   Median : 7.000
                    Median : 5.000
                                    Median :13.00
                                                    Median :21.00
##
   Mean
         : 7.675
                    Mean : 4.933
                                    Mean :13.64
                                                    Mean :20.75
##
   3rd Qu.:10.000
                    3rd Qu.: 6.000
                                    3rd Qu.:16.00
                                                    3rd Qu.:23.00
##
   Max. :20.000
                    Max. :19.000
                                    Max. :27.00
                                                    Max. :37.00
```

```
##
##
      PLUS MINUS
                        home
                                   not.paired
                                                   result
           :-56.00000
                        : 0
                                         :0
## Min.
                                 Min.
                                              Min.
                                                      :0.0
    1st Qu.: -9.00000
                        A:1236
                                 1st Qu.:0
                                               1st Qu.:0.0
## Median: 0.00000
                        H:1236
                                 Median :0
                                              Median:0.5
         : -0.01909
## Mean
                                 Mean
                                        : 0
                                              Mean
                                                     :0.5
##
    3rd Qu.: 9.00000
                                 3rd Qu.:0
                                              3rd Qu.:1.0
   Max. : 56.00000
                                                      :1.0
                                 Max.
                                         :0
                                              {\tt Max.}
##
# For the Pythagorean Expectation we need only the result, points scored (PTS) and poi
             <- NBAR18 %>% group_by(TEAM NAME)%>%
NBAteams18
            dplyr::summarise(result = sum(result),
                             PTS = sum(PTS),
                             PTSAGN = sum(PTSAGN)
                           )%>%
                           ungroup()
head (NBAteams18)
## # A tibble: 6 x 4
                                  PTS PTSAGN
##
     TEAM NAME
                         result
##
     <fct>
                          <dbl> <int>
                                       <int>
## 1 Atlanta Hawks
                             30 9742
                                       10306
## 2 Boston Celtics
                             53 9489
                                        9082
## 3 Brooklyn Nets
                             42 9375
                                        9443
## 4 Charlotte Hornets
                             42 9290
                                        9359
## 5 Chicago Bulls
                             24 8783
                                        9467
## 6 Cleveland Cavaliers
                             24 8976
                                        9697
tail(NBAteams18)
## # A tibble: 6 x 4
##
     TEAM_NAME
                            result
                                     PTS PTSAGN
     <fct>
                             <dbl> <int>
                                          <int>
## 1 Portland Trail Blazers
                                    9581
                                            9167
                                57
## 2 Sacramento Kings
                                42
                                    9445
                                            9521
## 3 San Antonio Spurs
                                49
                                    9366
                                           9305
## 4 Toronto Raptors
                                58
                                    9631
                                            9211
## 5 Utah Jazz
                                52
                                    9479
                                            9069
## 6 Washington Wizards
                                32
                                    9449
                                            9672
# So now we can create the value for win percentage for each team in the 82 game seaso
NBAteams18[,'wpc'] = NBAteams18[,'result']/82
NBAteams18[,'pyth'] = NBAteams18[,'PTS']**2/(NBAteams18[,'PTS']**2 + NBAteams18[,'PTSAGN
head (NBAteams18)
```

```
## # A tibble: 6 x 6
##
     TEAM NAME
                                  PTS PTSAGN
                        result
                                               wpc pyth
##
     <fct>
                          <dbl> <int>
                                       <int> <dbl> <dbl>
## 1 Atlanta Hawks
                             30 9742
                                       10306 0.366 0.472
## 2 Boston Celtics
                             53 9489
                                        9082 0.646 0.522
## 3 Brooklyn Nets
                             42 9375
                                        9443 0.512 0.496
## 4 Charlotte Hornets
                             42 9290
                                        9359 0.512 0.496
## 5 Chicago Bulls
                                 8783
                                        9467 0.293 0.463
                             24
## 6 Cleveland Cavaliers
                             24 8976
                                        9697 0.293 0.461
tail(NBAteams18)
## # A tibble: 6 x 6
##
     TEAM_NAME
                                     PTS PTSAGN
                            result
                                                  wpc pyth
##
     <fct>
                             <dbl> <int>
                                         <int> <dbl> <dbl>
## 1 Portland Trail Blazers
                                57
                                    9581
                                           9167 0.695 0.522
## 2 Sacramento Kings
                                42
                                    9445
                                           9521 0.512 0.496
## 3 San Antonio Spurs
                                           9305 0.598 0.503
                                49
                                    9366
## 4 Toronto Raptors
                                58
                                    9631
                                           9211 0.707 0.522
## 5 Utah Jazz
                                52
                                    9479
                                           9069 0.634 0.522
## 6 Washington Wizards
                                32
                                    9449
                                           9672 0.390 0.488
# We now plot the data. Our results look very similar to the MLB case.
ggplot(data = NBAteams18,aes(x = pyth,y = wpc )) + geom_point()
```



### Self test

run ggplot again, but this time write y= W instead of y= wpc. What do you find? Does it make a difference?

```
# Finally we generate a regression.
pyth_lm = lm(formula = 'wpc ~ pyth', data = NBAteams18)
pyth_lm %>% summary()
##
## Call:
## lm(formula = "wpc ~ pyth", data = NBAteams18)
##
## Residuals:
                  1Q
                       Median
                                     3Q
## -0.08010 -0.02624 0.01040 0.02256 0.05657
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.7572
                            0.1551
                                    -17.77
                                              <2e-16 ***
                 6.5536
                            0.3100
                                     21.14
## pyth
                                              <2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.03453 on 27 degrees of freedom
## Multiple R-squared: 0.943, Adjusted R-squared: 0.9409
## F-statistic: 447 on 1 and 27 DF, p-value: < 2.2e-16</pre>
```

#### Self test

Run the regression above but instead write 'wpc  $\sim$  result' instead of 'wpc  $\sim$  result' in the line starting pyth\_lm. What difference does this make?

## Conclusion

We have found that the Pythagorean model fits the NBA data in roughly same way as it fits the MLB data. Let's now look at fourth example: English Premier League soccer.