Recursion

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#### Recursion

Recursion is a powerful problem-solving strategy

- employing a variant of divide-and-conquer
- leading to simple, elegant solutions

It is related to induction in mathematics, which has

- a base case (a problem instance where the solution is trivial)
- an inductive step (build solution from a simpler version of the problem)

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### **❖** Example #1: factorial

A simple example: computing factorial (n!)

- base case:  $\mathbf{n}$  is  $1 \Rightarrow \mathbf{n}$ ! is 1
- for larger values:
  - I can't solve the whole problem directly
  - o but I do know the value of **n**
  - I could compute (n-1)! (easier than n!?)
- multiply **n** by (**n**-1)!, giving **n**!

E.g.

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### ❖ ... Example #1: factorial

Expressing this as a C function:

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# **❖** Example #2: Summing values in a list

Another simple example: summing integer values in a list

- base case: empty list ⇒ sum is zero
- for larger lists:
  - I can't solve the whole problem directly
  - but I do know the first value in the list
  - sum the rest of the list (smaller than whole list, easier?)
- add first value to sum-of-rest, giving sum of whole

E.g.

```
sum [1,2,3] = 1 + sum [2,3]
= 1 + (2 + sum [3])
= 1 + (2 + (3 + sum []))
= 1 + (2 + (3 + 0)) = 6
```

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## ❖ ... Example #2: Summing values in a list

Expressing previous method as an (abstract) function

```
int sum(List L) {
   if (empty(L))
     return 0;
   else {
     int first, sumRest;
     first = head(L);
     sumRest = sum(tail(L));
     return first + sumRest;
   }
}
```

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### ❖ ... Example #2: Summing values in a list

And then expressing using typical list data structure:

```
struct Node { int val; struct Node *next; };
int sum(struct Node *L) {
   if (L == NULL)
      return 0;
   else {
      int first, sumRest;
      first = L->val;
      sumRest = sum(L->next);
      return first + sumRest;
}
or
int sum(struct Node *L) {
   if (L == NULL)
      return 0;
   else
      return L->val + sum(L->next);
}
```

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#### How it works

Recursion is a function calling itself

Won't the system get confused?

No, because each call to the function is a separate instance

- each function call creates a new mini-environment
- this holds all of the data needed by the function

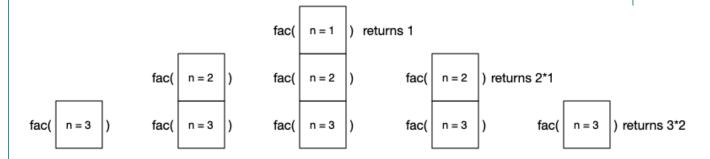
The "mini-environments" are called stack frames

- they are created as part of the function call
- they are removed when the function **return**s

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### ... How it works

#### How the memory state changes during execution



State of stack during recursive evaluation of fac(3)

fac(3) calls fac(2) calls fac(1) returns 1 returns 2\*1 returns 3\*2 returns 6

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## Using Recursion

While it is useful to know how it works ...

Sometimes it is confusing to think about stacks, etc.

When designing (or reading) recursive functions

- return to recursion basics
- identify the base case
- see how the problem can be reduced
- see how results can be built from base + recursive case

COMP2521 has many examples of recursively-defined algorithms

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### Postscript

Generally, recursive solutions are efficient (except stack space)

Sometimes, they can be very inefficient, e.g.

```
// returns n'th fibonacci number
int fibonacci(int n) {
   if (n == 1)
      return 1;
   else if (n == 2)
      return 1;
   else
      return fibonacci(n-1) + fibonacci(n-2);
}
```

Trace the recursive calls for **fibonacci(5)** to see the problem

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