

# Higher-order Functions

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## ❖ Higher-order Functions

Recall the quicksort library function

```
void qsort(void *base, size_t nelems, size_t width,  
           int (*compare)(const void *, const void *));
```

Sorts an array of items of any type (hence **(void \*)**)

- **base** is the address of the first element
- **nelems** is the number of elements in the array
- **width** is the size (in bytes) of each element
- **compare** is a function to compare two items
  - parameters are *pointers to items* to be compared
  - **compare(a, b)** returns -ve if  $a < b$ , +ve if  $a > b$ , 0 if equal

Example call: **qsort(myArray, 10, sizeof(char \*), strcmp)**

## ❖ ... Higher-order Functions

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**qsort()** is an example of a **higher-order** function

- a function that has parameters which are also functions

**Functional programming languages** support higher-order functions

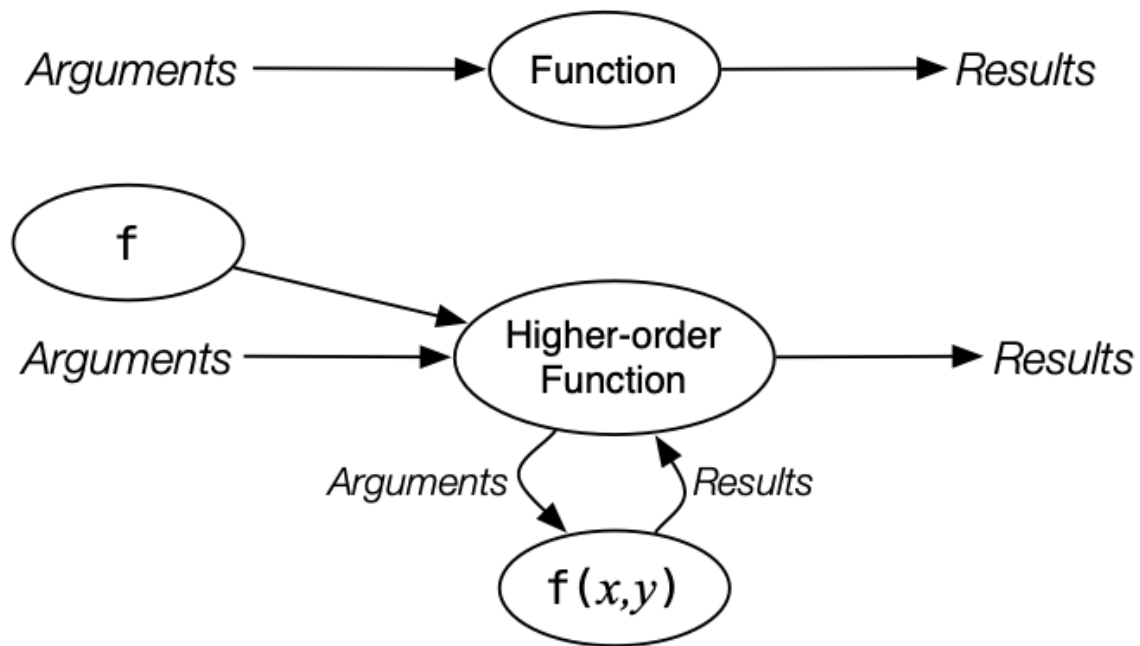
- intrinsic to the language (functions are first-class citizens)
- used extensively to express algorithms concisely
- e.g. Haskell, Curry, Miranda, Lisp, Scheme, ML, Ruby, even Javascript

A useful place to explore higher-order functions: (recursive) functions on lists

Note that recursive functions are not necessarily higher-order, but they can be

## ❖ ... Higher-order Functions

Regular functions vs Higher-order functions (in C)



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## ❖ Pointers to Functions

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C is definitely not a functional language

- but somewhat supports higher-order functions via **function pointers**

Consider `int (*compare)(const void *, const void *)`

- **compare** is a pointer to a function
- that takes two **(void \*)** pointers
- and returns an **int** result

The **const** declaration doesn't change the meaning

- but signals that the function should treat the arguments as read-only

## ❖ ... Pointers to Functions

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How to get a value which is a function pointer ...

- write just the function name e.g. **qsort**, **strcmp**
- write the function name preceded by **&**, e.g. **&qsort**

Writing a function name followed by a parenthesis '('

- is a *call* to the named function
- passing the supplied values as parameters

Example: **strcmp("abc", "def")**,  
**fgets(buf, 10, stdin)**, ...

- ... and pretty much every other function you've called in C

## ❖ ... Pointers to Functions

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Function pointers ...

- are references to memory address of a function
- are pointer values and can be assigned/passed

Example of use:

```
//define a function pointer variable "fp"
int (*fp)(List);
// assign a value to this variable
fp = &length;
// apply the function being pointed to
n = (*fp)(L);    // same as n = length(L)
```

## ❖ Recursive functions on Lists

For this discussion, we define **List** as:

```
// a list node contains an integer value
typedef struct _node {
    int val;
    struct _node *next;
} Node;
// a List is a pointer to its first Node
typedef Node *List;
// we also uses Sedgewick's definition
typedef Node *Link;
```

The difference between **List** and **Link**

- type-wise they are identical
- **List** used for pointer to first node in a list
- **Link** used for pointer to some node in a list



## ❖ ... Recursive functions on Lists

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The following functions help with list manipulation:

```
// returns a new empty List
List new();
// checks whether L is empty
bool empty(List L);
// returns first element in L
int head(List L);
// returns all but first element in L
List tail(List L);
// returns new list with x as head and L as tail
List insert(int x, List L);
// returns new list with x as last element
List append(List L, int x);
// returns new list which is concatenation of lists L1 and L2
List concat(List L1, List L2);
```

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## ❖ Folding Lists

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Example: determining the length of a list

```
// empty list has length 0
// a non-empty list has at least one element
// plus as many as are in the rest of the list

int length(List L)
{
    if (empty(L))
        return 0; // base case
    else
        return 1 + length(tail(L));
}
```

Exercise: write an iterative version using the empty/head/tail operations

## ❖ ... Folding Lists

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Example: sum of values in a list

```
// empty list has sum 0
// a non-empty list has at least one element
// plus the sum of the rest of the list

int sum(List L)
{
    if (empty(L))
        return 0; // base case
    else
        return head(L) + sum(tail(L));
}
```

Note similar structure to **length()**

## ❖ ... Folding Lists

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**sum()** and **length()** are examples of ...

- a common pattern of computation
- that reduces a list to a single value

This is commonly called **fold()** and defined as

```
int fold(List L, int (*f)(int x, int y), int id)
```

- **L** is the list to be reduced
- **f** is a function that takes two **ints** and returns an **int**
- **id** is the identity for the **f** function

## ❖ ... Folding Lists

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The **sum** function could be defined using **fold**

```
int add(int x, int y) { return x+y; }  
int sum(List L) { return fold(L, add, 0); }
```

We could define **product** using the same approach

```
int mult(int x, int y) { return x*y; }  
int product(List L) { return fold(L, mult, 1); }
```

## ❖ ... Folding Lists

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The **fold** function is defined as

```
// compute f(L1, f(L2, f(L3, ... f(Ln,id))))  
  
int fold(List L, int (*f)(int x, int y), int id)  
{  
    if (empty(L))  
        return id;  
    else  
        return f( head(L), fold(tail(L),f,id) );  
}
```

Example: **fold([1,2,3],add,0)** computes  
**add(1,add(2,add(3,0)))**

## ❖ Mapping a List

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Example: print items in a list (one per line)

```
// print first item, on a line by itself  
// then print the rest of the items
```

```
void putList(List L) {  
    if (!empty(L)) {  
        showItem(head(L));  
        putList(tail(L));  
    }  
}
```

## ❖ ... Mapping a List

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Example: doubling each item in a list

```
// apply a function to each item in a list

void doubleUp(List L)
{
    if (!empty(L)) {
        head(L) = 2 * head(L);
        doubleUp(tail(L));
    }
}
```

Notes:

- **#define head(L) L->val**
- modifies each **Node** in the list



## ❖ ... Mapping a List

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**printList()** and **doubleUp()** are examples of ...

- a common pattern of computation
- that applies a function to each node in a list
- one difference: only **doubleUp** changes the node

This is commonly called **map()** and defined as

```
void map(List L, void (*f)(Link x));
```

- **L** is the list to be mapped
- **f** is a function that operates on a node

## ❖ ... Mapping a List

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Defining **doubleUp** using **map**

```
void timesTwo(Link n) { n->val = n->val * 2; }  
void doubleUp(List L) { map(L, timesTwo); }
```

Defining **printList** using **map**

```
void showItem(Link n) { printf("%d\n",n->val); }  
void printList(List L) { map(L, showItem); }
```

## ❖ ... Mapping a List

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The **map** function could be defined as

```
void map(List L, void (*f)(Link x))
{
    if (!empty(L)) {
        f(L);
        map(tail(L), f);
    }
}
```

## ❖ ... Mapping a List

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A variation on **map** returns a new list

```
List mapp(List L, int (*f)(int x))
{
    if (empty(L))
        return new();
    else
        return insert( f(head(L)), mapp(tail(L),f) );
}
```

Reminder:

**insert(int x, List L)** puts a new node containing **x** at the front of the list

## ❖ Example: list of fibs

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If we had the following two functions:

```
// returns a list [1,2,3,...,n]
List seq(int n) { ... }
// returns n'th fibonacci number
int fibonacci(int n) { ... }
```

Then we could build a list of the first n Fibonacci numbers as

```
List firstNfib(int n) { return map(seq(n), fibonacci); }
```

## ❖ Example: length of a List

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A function that computes the length of a list by

- replacing each value in the list by 1
- summing the elements of the new list

```
int one(int x) { return 1; }  
int add(int x, int y) { return x+y; }  
  
int length(List L)  
    { return fold(mapp(L,one), add, 0); }
```

Produced: 7 Aug 2020