**Text Compression** 

- Text Compression
- Huffman Code
- Decompression
- Analysis of Huffman Encoding

COMP2521 20T2 ♦ Text Compression [0/10]

>>

>>

## Text Compression

Problem: Efficiently encode a given string  ${\cal T}$  by a smaller string  ${\cal E}$ 

### Applications:

• Save memory and/or bandwidth

#### Huffman's algorithm

- computes frequency *f(c)* for each character *c*
- encodes high-frequency characters with short code word
- no code word is a prefix of another code word (e.g. can't have 00 + 001)
- uses encoding tree to determine the code words
- many encodings are possible; aims to find optimal encoding

COMP2521 20T2 ♦ Text Compression [1/10]

>>



## ... Text Compression

#### Code...

• mapping of each character to a binary code word (e.g. ascii)

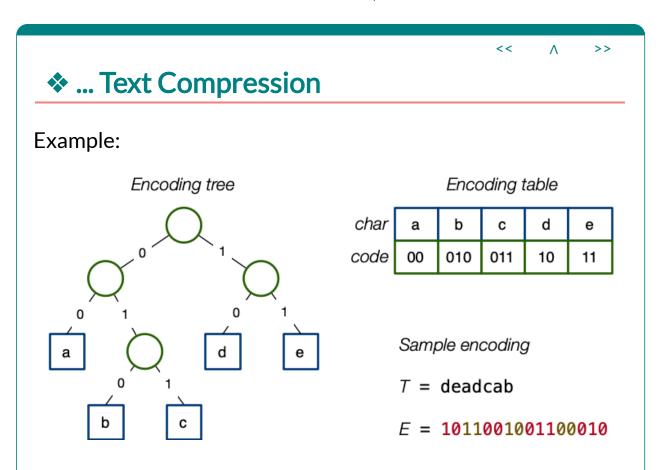
#### Prefix code ...

• binary code such that no code word is prefix of another code word

#### Encoding tree ...

- represents a prefix code
- each leaf stores a character
- code given by the path from the root to the leaf (0 for left, 1 for right)

COMP2521 20T2 \$\times Text Compression [2/10]



T as ascii chars would require 56 bits; E needs only 16 bits

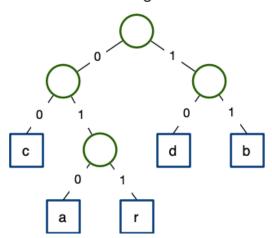
COMP2521 20T2 ♦ Text Compression [3/10]

> << >>

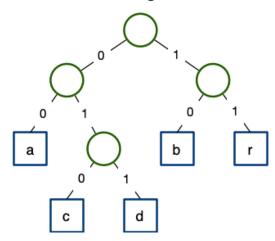
## ... Text Compression

#### Example: T = abracadabra

Encoding tree T1



Encoding tree T2



Encoding with  $T_1$  is **010.11.011.010.00.010.10.010.11.011.010** i.e. 29 bits

Encoding with  $T_2$  is **00.10.11.00.010.00.011.00.10.11.00** i.e. 24 bits

The dots are there only to distinguish characters; they are not part of the encoding.

COMP2521 20T2 ♦ Text Compression [4/10]

>>



## ... Text Compression

#### Text compression problem

Given a text T...

• find a *prefix code* that yields the *shortest encoding* of *T* 

Some obvious strategies ...

- shorter codewords for frequent characters
- longer code words for rare characters

But how to ensure optimal encoding?

COMP2521 20T2 \$\times Text Compression [5/10]

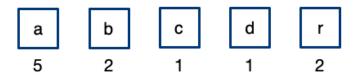
# ... Text Compression

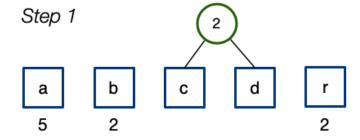
## Huffman's algorithm

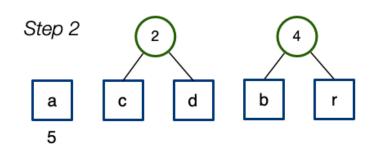
- computes frequency *f(c)* for each character
- successively combines pairs of lowest-frequency characters
- builds encoding tree "bottom-up"

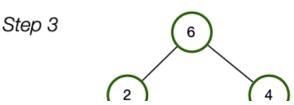
Example: T = abracadabra

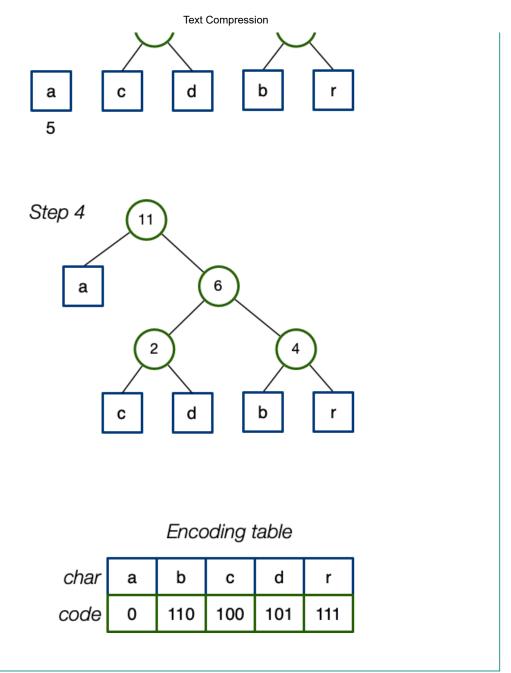
Initially











COMP2521 20T2 ♦ Text Compression [6/10]

## Huffman Code

Huffman's algorithm using a priority queue:

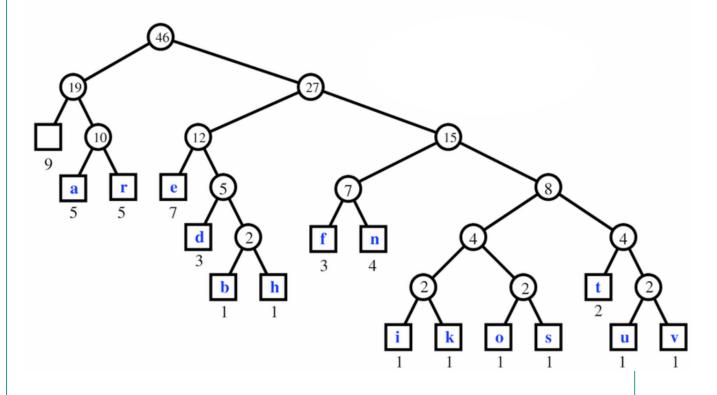
```
HuffmanCode(T):
Input string T of size n
Output optimal encoding tree for T
compute frequency array
Q = new priority queue (ordered low key to high key)
for all characters c do
   T = new single-node tree storing c
   join(Q,T) with frequency(c) as key
end for
while |Q|≥2 do
   f_1 = Q.minKey(), T_1 = leave(Q)
   f_2 = Q.minKey(), T_2 = leave(Q)
   T = new tree node with subtrees T_1 and T_2
   join(Q,T) with f_1+f_2 as key
end while
return leave(Q)
```

COMP2521 20T2 ♦ Text Compression [7/10]

# ... Huffman Code

Larger example: T = a fast runner need never be afraid of the dark

Character		a	b	d	e	f	h	i	k	n	0	r	s	t	u	v
Frequency	9	5	1	3	7	3	1	1	1	4	1	5	1	2	1	1



COMP2521 20T2 \$ Text Compression [8/10]

## Decompression

Decompression involves repeated traversal of paths in tree ...

```
decompress(B, T):
 Input bit-string B, encoding tree T
 Output original string
 start from root of Tree
 for each b in Bits do
     if b = 1 then
         go right in Tree
     else
         go left in Tree
     end if
     if reached leaf then
         print char in leaf
         return to root of Tree
 end if
 end for
```

COMP2521 20T2 ♦ Text Compression [9/10]

<<

Λ

## Analysis of Huffman Encoding

Analysis of Huffman's algorithm:

- assume length(T) = m, vocab(T) = v
- build frequency table: scan entire input (m)
- build the tree: use frequency table (v) via priority queue (log<sub>2</sub>v)

Gives complexity:  $O(m + v \log v)$  time

Many variations exist to improve compression (e.g. gzip, bzip2, xz)

COMP2521 20T2 ♦ Text Compression [10/10]

Produced: 9 Aug 2020