

1) Identify all nodes

2) From the independent sources:

$$V_1 = V_2 + 60 \text{ or } V_2 = V_1 - 60$$

$$V_1 = V_0 + 120 \text{ or } V_0 = V_1 - 120$$

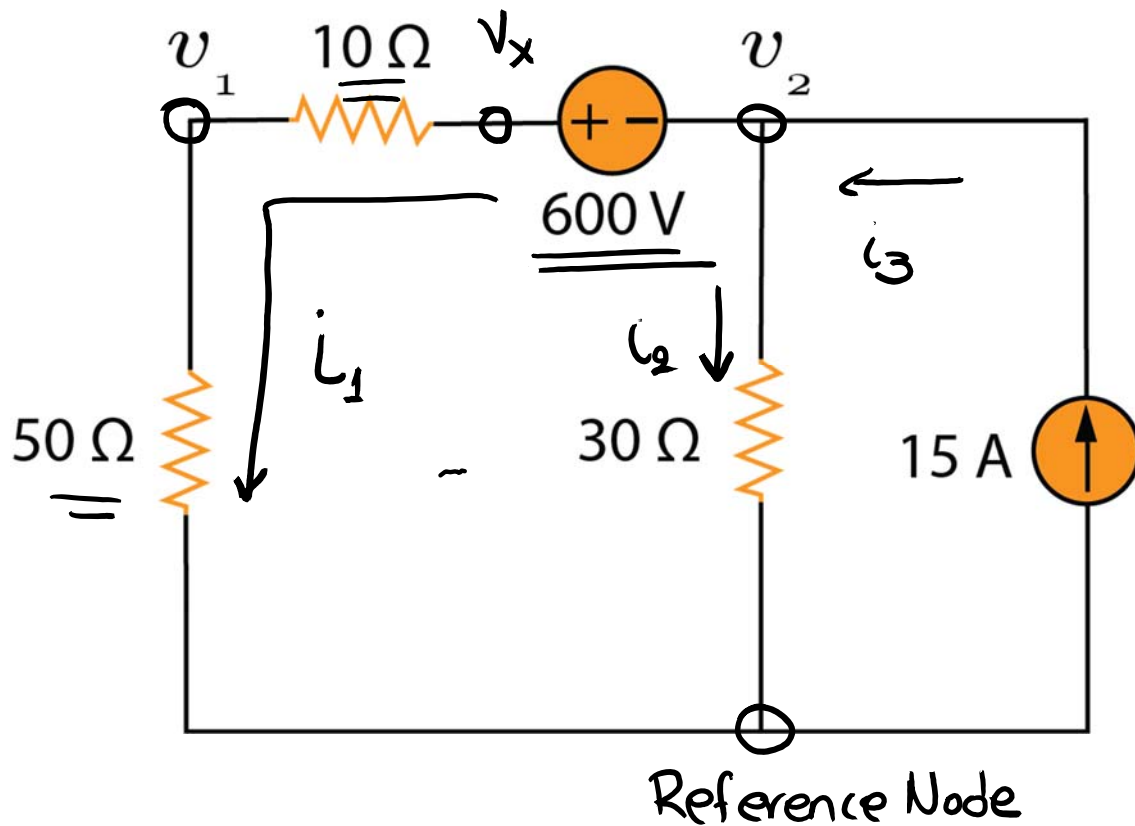
3) Define currents so KCL at node 1:  $i_1 + i_2 + i_3 = 0$

Because of series elements:  $i_1 = \frac{V_2}{30k}$        $i_3 = \frac{V_0}{120k}$

$$\text{KCL: } \frac{V_2}{30k} + \frac{V_1}{120k} + \frac{V_0}{120k} = 0 \Rightarrow \frac{V_1 - 60}{30k} + \frac{V_1}{120k} + \frac{V_1 - 120}{120k} = 0$$

$$\Rightarrow 6V_1 = 360 \Rightarrow V_1 = 60V$$

$$V_0 = V_1 - 120 = 60 - 120 = \underline{\underline{-60V}}$$



1) From series connection

$$\frac{v_1}{50} = \frac{v_x}{60}$$

2) At node x:

$$v_x = v_2 + 600$$

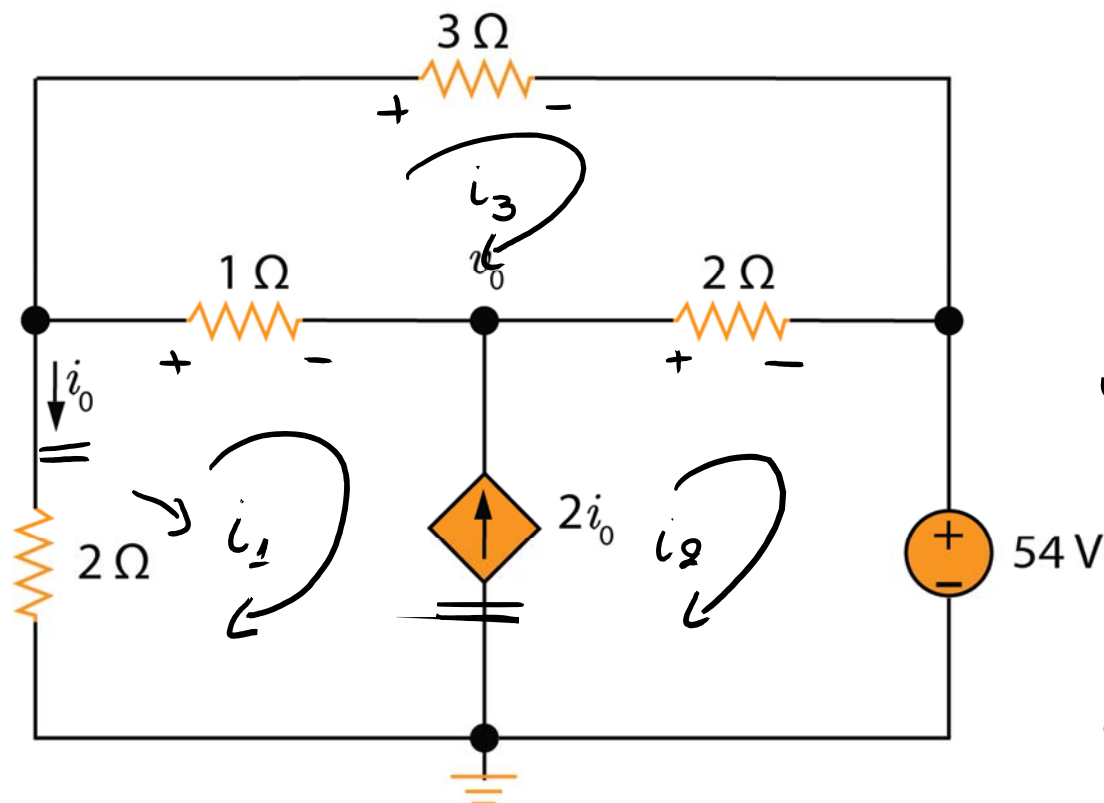
3) Nodal analysis at node 2

$$i_1 + i_2 = i_3$$

$$\Rightarrow \frac{v_x}{60} + \frac{v_2}{30} = 15 \Rightarrow$$

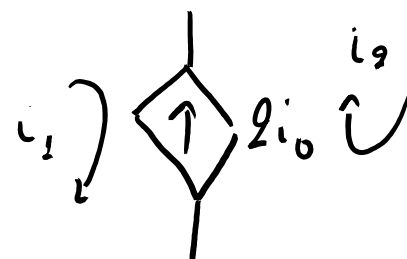
$$\Rightarrow \frac{v_2 + 600}{60} + \frac{v_2}{30} = 15 \Rightarrow 3v_2 + 600 = 900 \Rightarrow \underline{v_2 = 100V}$$

$$\frac{v_1}{50} = \frac{v_2 + 600}{60} \Rightarrow \underline{v_1} = \frac{50}{60} (100 + 600) = 583.3V$$



i) Current source between two meshes:

Supermesh:

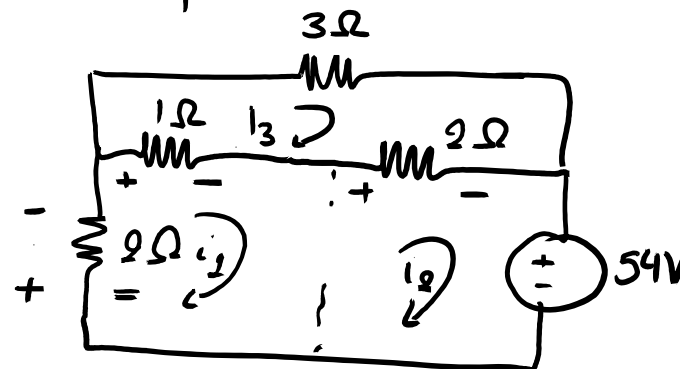


$$i_1 - i_2 = -2i_0$$

or

$$i_2 - i_1 = 2i_0 \quad (1)$$

Supermesh:



$$\begin{aligned} \text{Mesh 3: } 3i_3 - 2(i_2 - i_3) - 1(i_1 - i_3) &= 0 \\ \Rightarrow 6i_3 - 2i_2 - i_1 &= 0 \quad (3) \end{aligned}$$

$$\text{Finally } i_0 = -i_1$$

$$\begin{aligned} (1) \rightarrow i_2 - i_1 &= 2i_0 = -2i_1 \\ \Rightarrow i_2 &= -i_1 \quad (4) \end{aligned}$$

$$\begin{aligned} 2i_1 + 1(i_1 - i_3) + 2(i_2 - i_3) + 54 &= 0 \\ \Rightarrow 3i_1 + 2i_2 - 3i_3 &= -54 \quad (2) \end{aligned}$$

$$\left. \begin{aligned} i_2 &= -i_1 \\ 3i_1 + 2i_2 - 3i_3 &= -54 \\ -i_1 - 2i_2 + 6i_3 &= 0 \end{aligned} \right\} \Rightarrow \text{Solving this system:}$$

$$i_1 = -36 \text{ A}$$

$$i_2 = 36 \text{ A}$$

$$i_3 = 6 \text{ A}$$

$$V_o = 54 + 2 \cdot (i_2 - i_3) = 54 + 2 \cdot (36 - 6) = 54 + 60 = 114 \text{ V}$$

also

$$V_o = -2i_1 - 1(i_1 - i_3) = -2(-36) - 1(-36 - 6) = 72 + 42 = 114 \text{ V}$$