

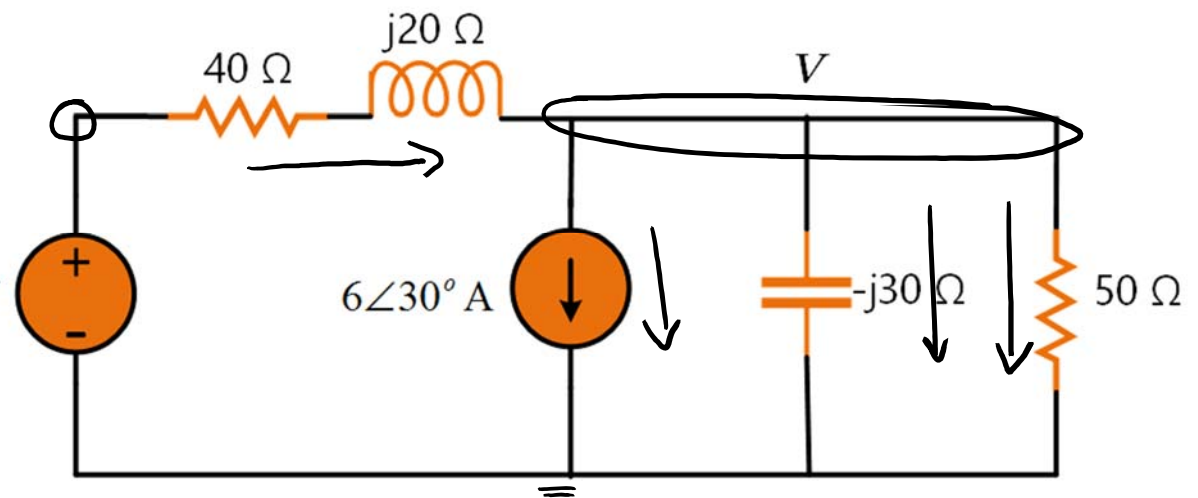
KCL at node:

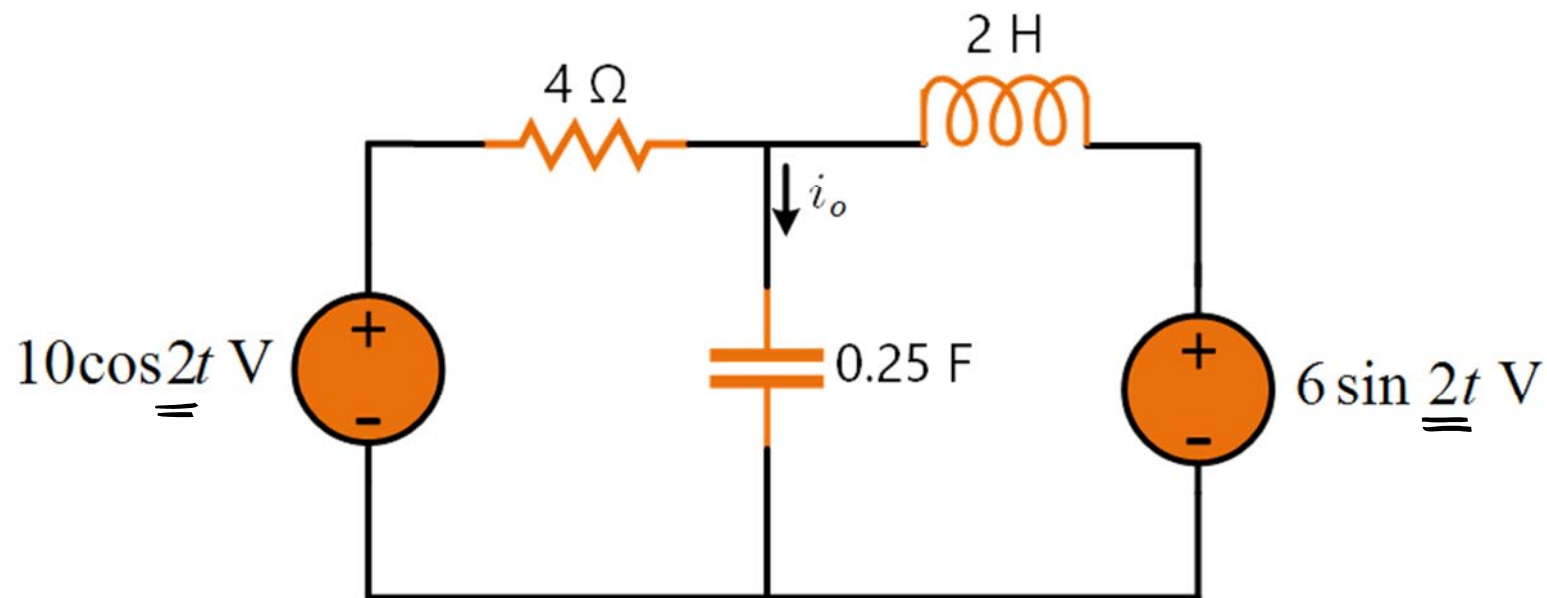
$$\frac{120 \angle -15^\circ - V}{40 + j20} = 6 \angle 30^\circ + \frac{V}{-j30} + \frac{V}{50}$$

$$\Rightarrow \frac{120 \angle -15^\circ}{40 + j20} - 6 \angle 30^\circ = V \left[\frac{1}{50} + \frac{1}{-j30} + \frac{1}{40 + j20} \right]$$

$$\Rightarrow -3.1885 - j4.7805 = (0.04 + j0.0233)V$$

$$\Rightarrow V = \frac{-3.1885 - j4.7805}{0.04 + j0.0233} = \underline{\underline{124.08 \angle -154^\circ \text{ V}}}$$





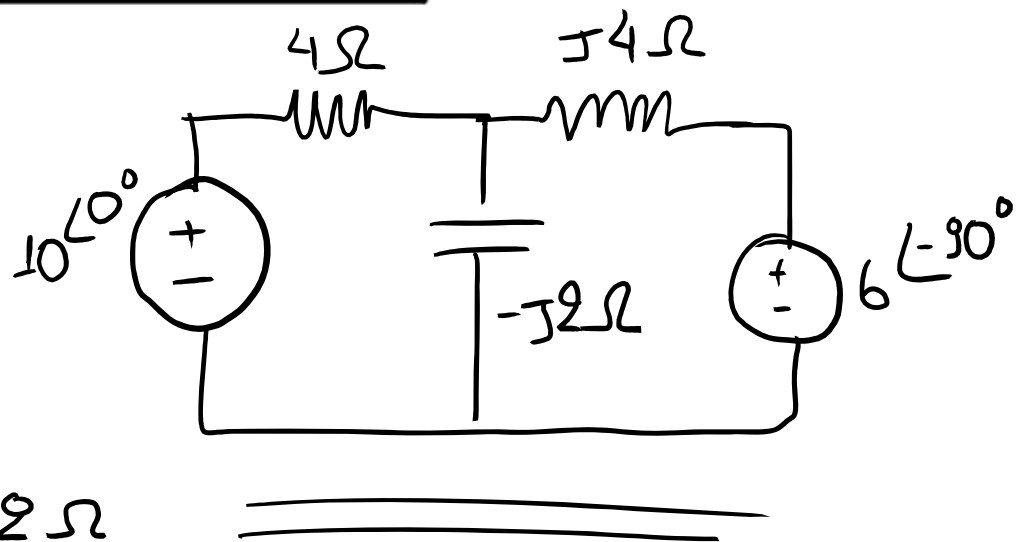
$$\omega = 2 \text{ rad/sec}$$

$$10 \cos 2t \rightarrow 10 \angle 0^\circ \text{ V}$$

$$6 \sin 2t = 6 \angle -90^\circ \text{ V}$$

$$2 \text{ H} \rightarrow j\omega L = j4 \Omega$$

$$0.25 \text{ F} \rightarrow \frac{1}{j\omega C} = \frac{1}{j2 \cdot 0.25} = -j2 \Omega$$



Mesh Analysis:

$$\text{Mesh 1: } -10 + 4I_1 + (-j2)(I_1 - I_2) = 0$$

$$\Rightarrow (4 - j2)I_1 + j2I_2 = 10 \quad (1)$$

$$\text{Mesh 2: } (-j2)(I_1 - I_2) + j4I_2 + (-j6) = 0$$

$$\Rightarrow j2I_1 + j2I_2 = j6 \quad (2)$$

Solve the system of equations: \rightarrow Substitution or Cramer's Rule

$$\begin{bmatrix} 4-j2 & j2 \\ j2 & j2 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 10 \\ 6 \end{bmatrix}$$

$$\Delta = 2(1-j)$$

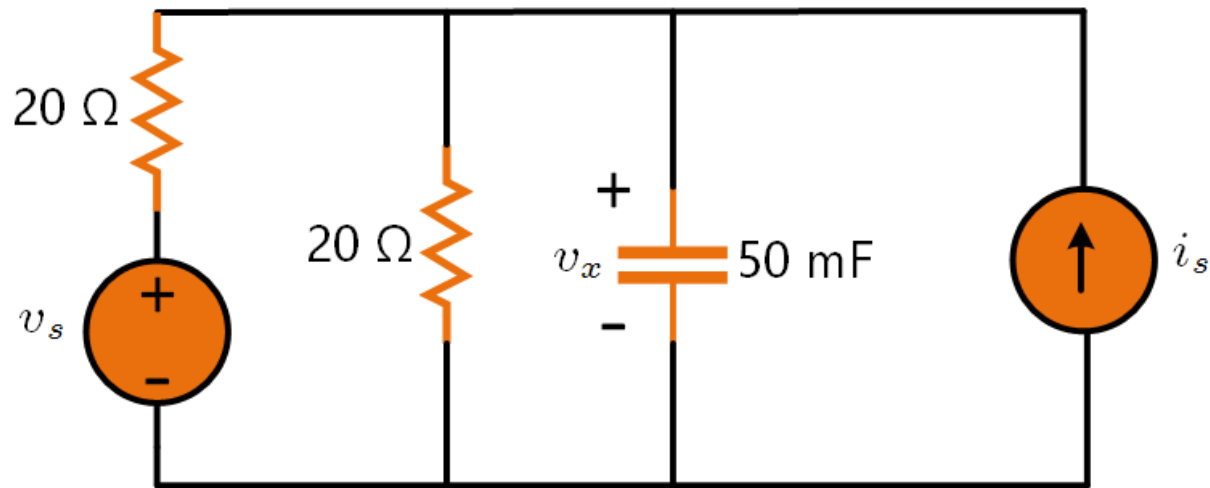
$$\Delta_1 = 5-j3$$

$$\Delta_2 = 1-j3$$

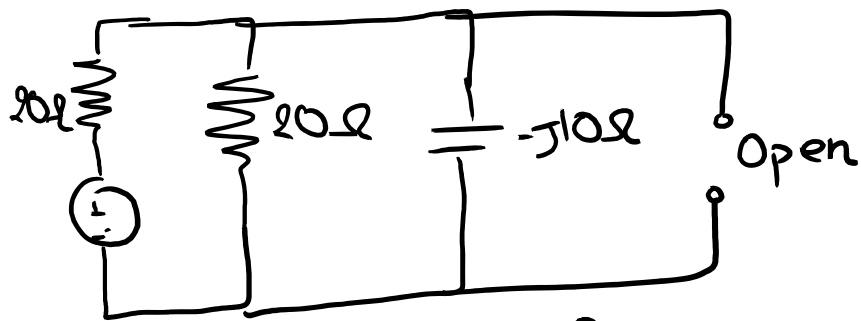
$$I_0 = I_1 - I_2 = \frac{\Delta_1}{\Delta} - \frac{\Delta_2}{\Delta} = \frac{\Delta_1 - \Delta_2}{\Delta}$$

$$= \frac{4}{2(1-j)} = 1+j = 1.41 \angle 45^\circ$$

$$i_0(t) = 1.41 \cos(2t + 45^\circ) \text{ A}$$

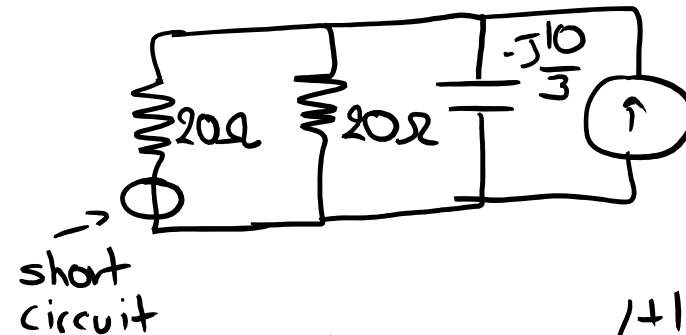


Only v_s $\omega = 2 \text{ rad/s}$
 $C \rightarrow \frac{1}{j\omega C} = -j10 \Omega$



$V_s \rightarrow 50 \angle 0^\circ$
 for $\sin 2\omega t$

Only i_s $\omega = 6 \text{ rad/sec}$
 $C \rightarrow \frac{1}{j\omega C} = -\frac{j10}{3} \Omega$



$i_s \Rightarrow 12 \angle +10^\circ \text{ A}$
 for $\cos 6\omega t$

Nodal analysis:

$$\frac{V_1 - 50}{20} + \frac{V_1}{20} + \frac{V_1}{(-j10)} = 0$$

$$\Rightarrow [0.1 + j0.1] V_1 = 2.5$$

$$\Rightarrow V_1 = \frac{2.5}{0.1 + j0.1}$$

$$\Rightarrow V_1 = 17.67 \angle -45^\circ \text{ V}$$

$$v_1(t) = 17.67 \sin(2t - 45^\circ) \text{ V}$$

Nodal Analysis:

$$\frac{V_2}{20} + \frac{V_2}{20} + \frac{V_2}{(-j\frac{10}{3})} = 12 \angle 10^\circ$$

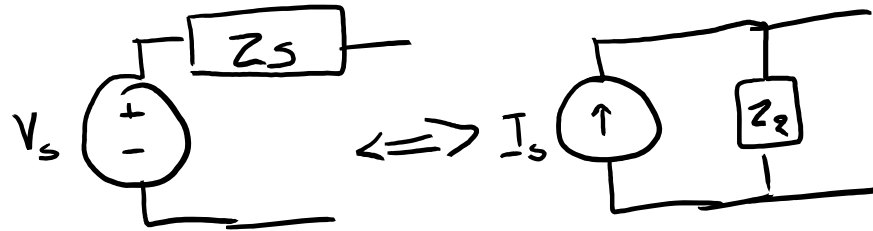
$$\Rightarrow (0.1 + j0.3) V_2 = 12 \angle 10^\circ$$

$$\Rightarrow V_2 = \frac{12 \angle 10^\circ}{0.316 \angle 71.57^\circ}$$

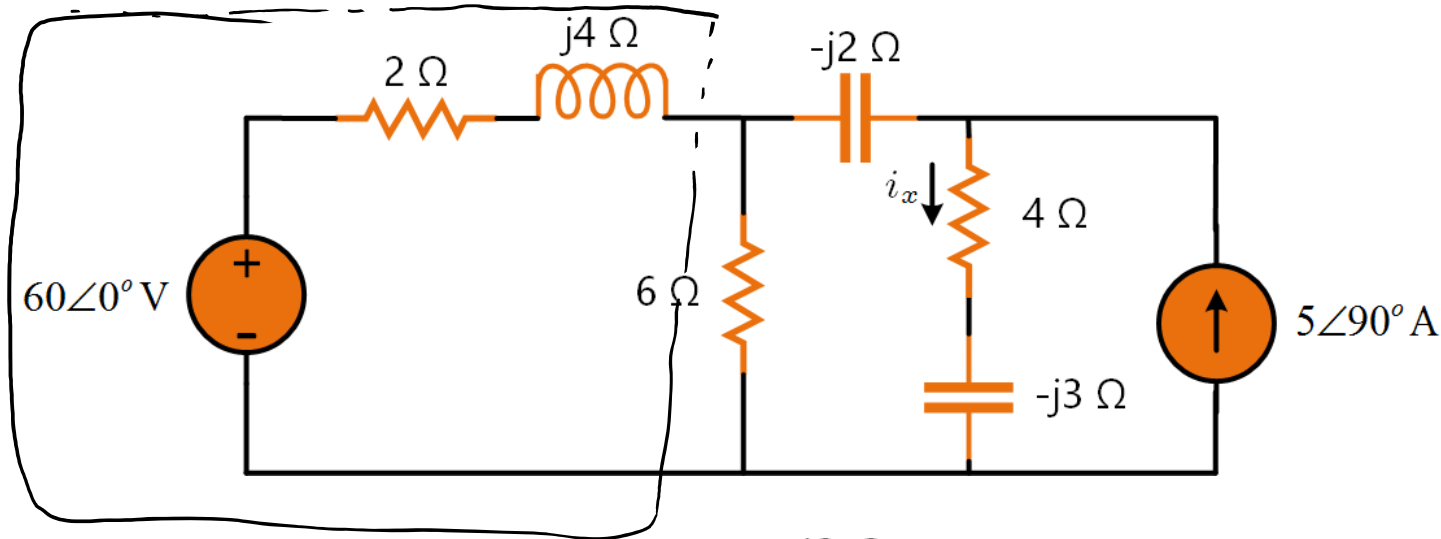
$$\Rightarrow V_2 = 37.95 \angle -61.57^\circ \text{ V}$$

$$v_2(t) = 37.95 \cos(6t -$$

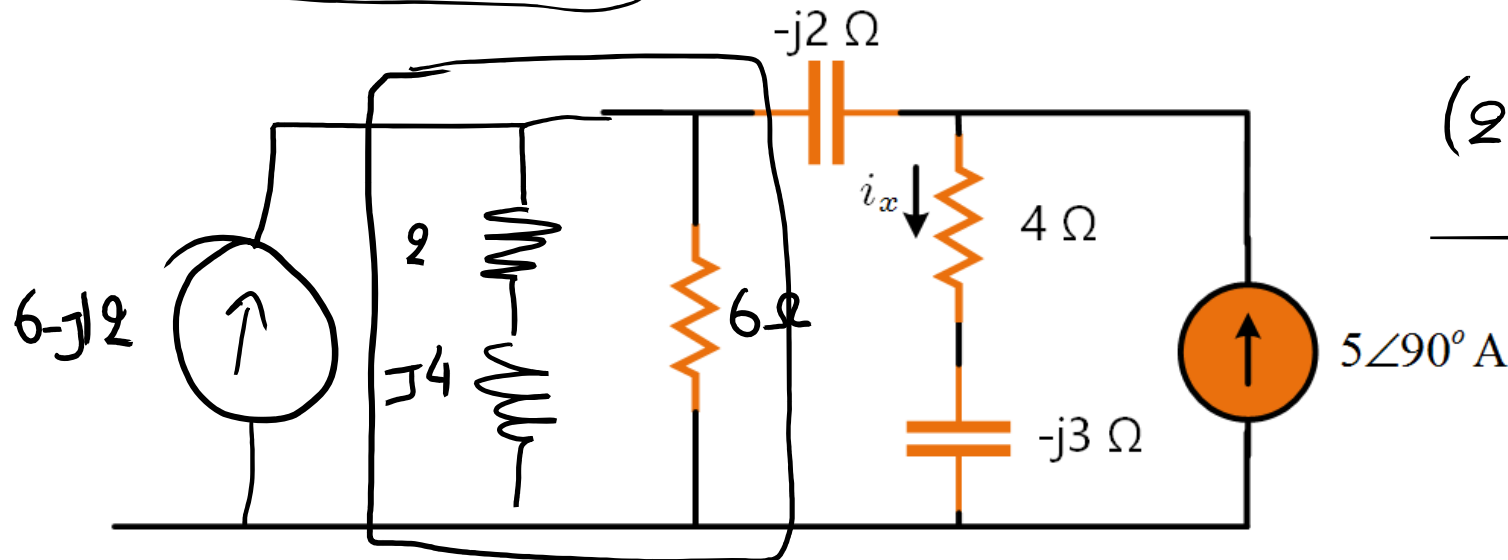
Source Transformation



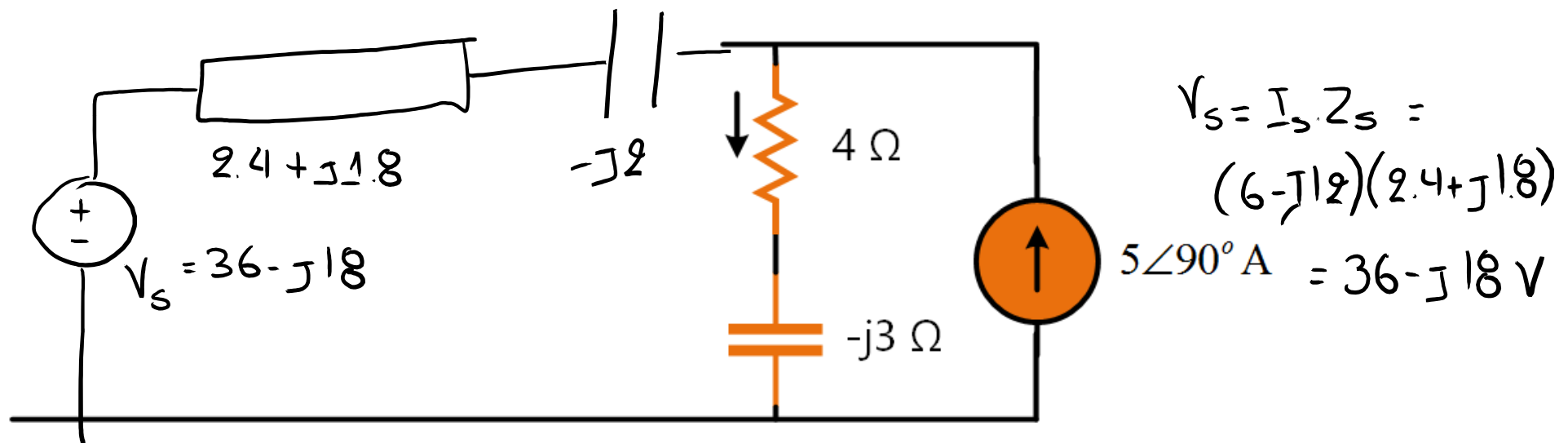
$$I_s = \frac{V_s}{Z_s}$$



$$I_s = \frac{60\angle 0^\circ}{2 + j4} = 6 - j12 \text{ A}$$

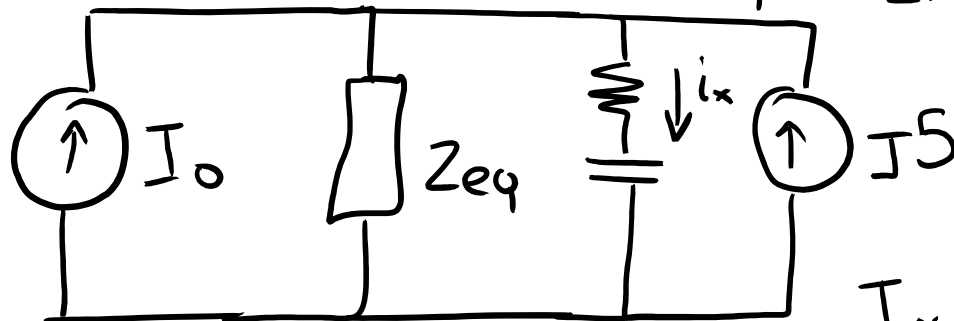


$$\frac{(2 + j4) \parallel 6}{8 + j4} = \frac{6(2 + j4)}{8 + j4} = 2.4 + j1.8\ \Omega$$



$$Z_{eq} = 2.4 + j1.8 - j2 = 2.4 - j0.2 \Omega$$

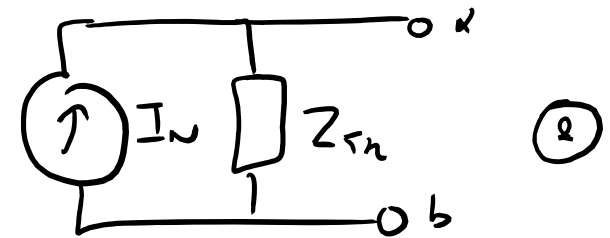
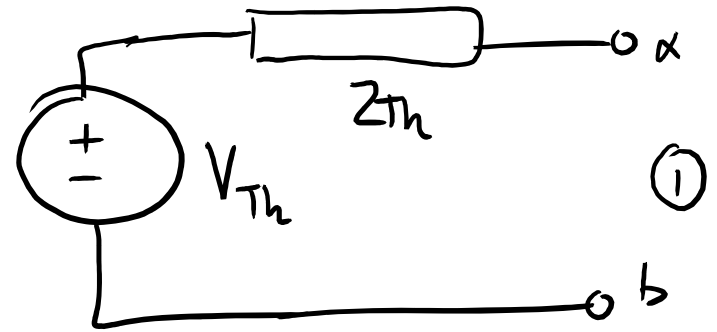
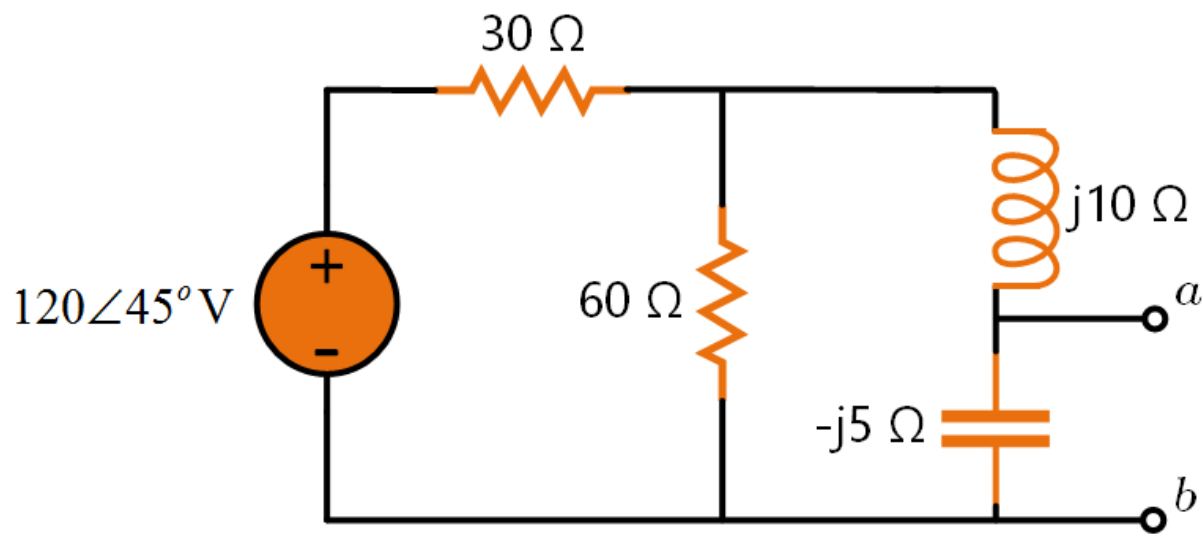
$$I_o = \frac{V_s}{Z_{eq}} = \frac{36 - j18}{2.4 - j0.2} = 15.517 - j6.207$$



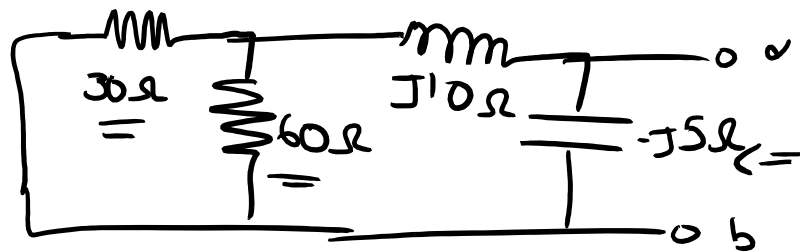
To find I_x :
current division

$$I_x = \frac{Z_{eq}}{Z_{eq} + (4 - j3)} (I_o + j5) =$$

$$= \frac{2.4 - j0.2}{6.4 - j3.2} (15.517 - j1.207) = 5 + j1.5625 = 5.238 \angle 17.35^\circ \text{ A}$$



1) Z_{Th} → short circuit voltage source

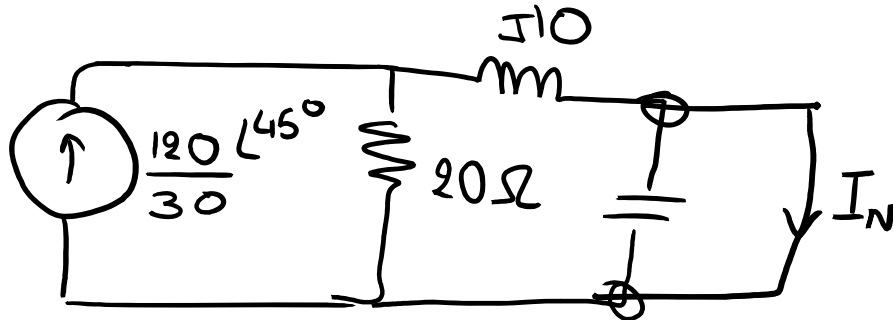


$$Z_{Th} = (-j5) \parallel (j10 + 20)$$

$$= \frac{(-j5)(20 + j10)}{20 + j5}$$

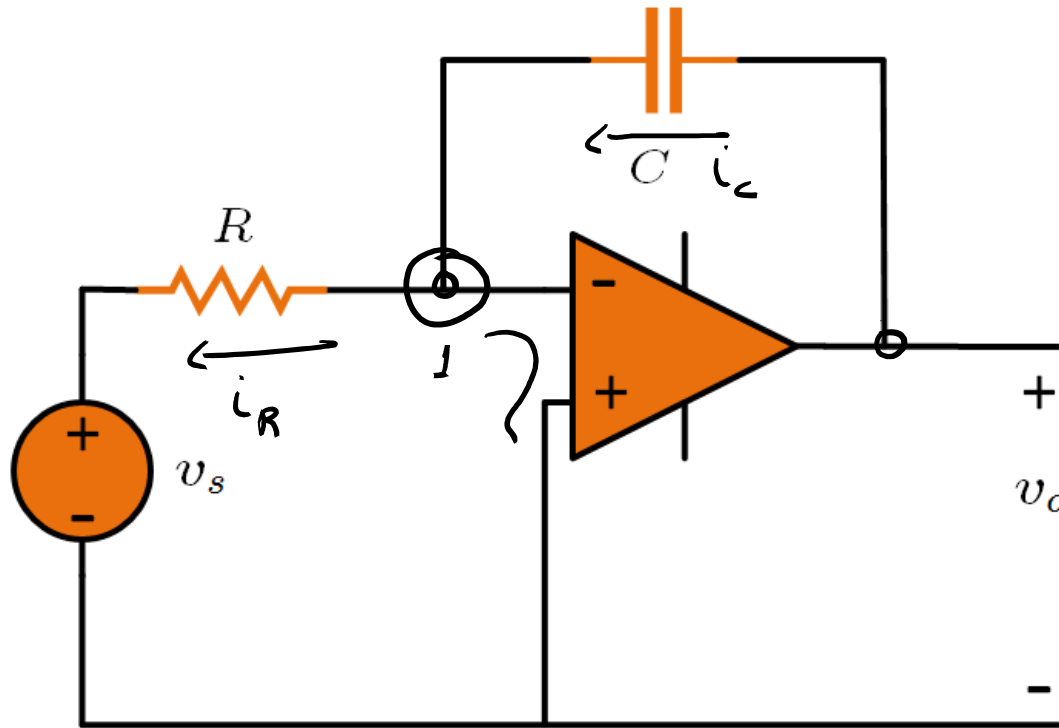
$$= 5.423 \angle -77.47^\circ \Omega$$

2) V_{Th} and I_N Source transformation



$$I_N = \frac{20}{20 + j10} 4 \angle 45^\circ = 3.578 \angle 18.43^\circ \text{ A}$$

$$V_{Th} = Z_{Th} \cdot I_N = 19.4 \angle -59^\circ \text{ V}$$



Find $\frac{V_o}{V_s}$

i) When in time domain:

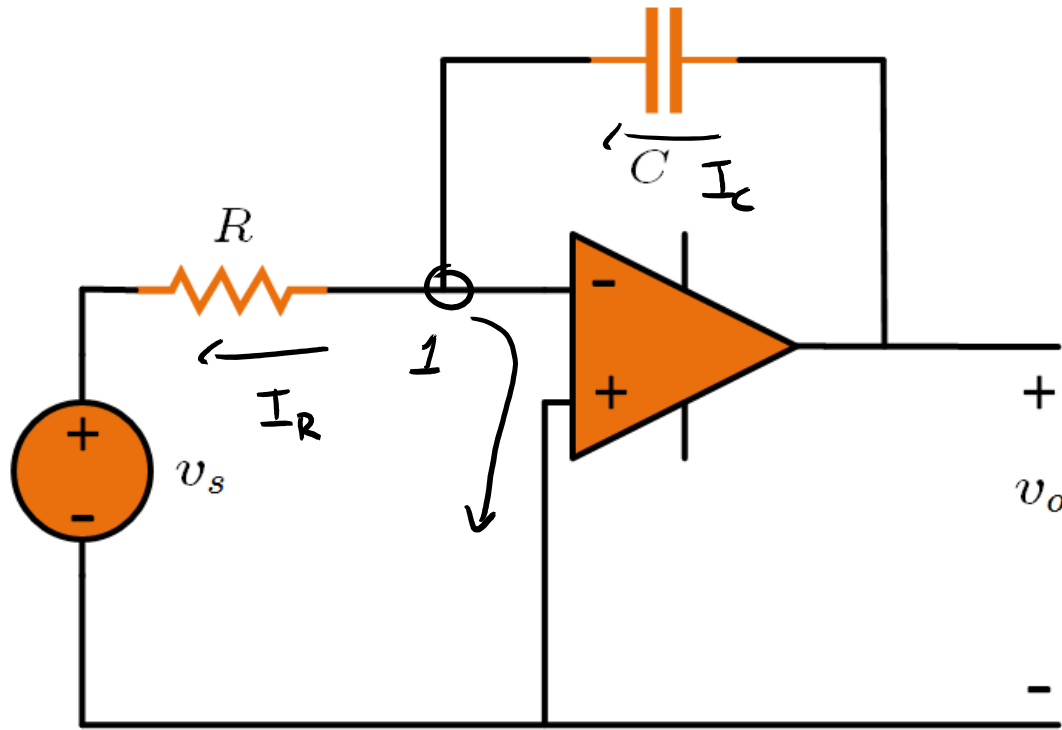
KCL at node 1

$$i_C = i_R \Rightarrow$$

$$C \frac{d(V_o - 0)}{dt} = \frac{0 - V_s}{R}$$

$$\Rightarrow \frac{dV_o}{dt} = -\frac{V_s}{RC} dt \Rightarrow V_o(t) = -\frac{1}{R \cdot C} \int_0^t V_s(t) dt + V_c[0]$$

general integrator transfer function



In frequency domain

$$C \rightarrow \frac{1}{j\omega C}$$

$$I_C = I_R \Rightarrow$$

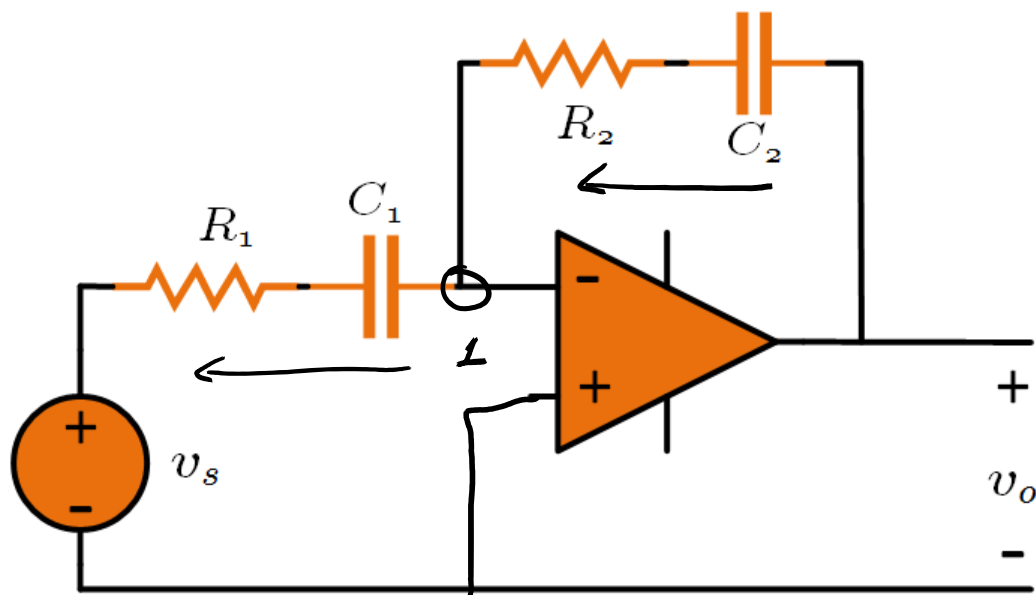
$$\frac{V_o}{Z_C} = \frac{0 - V_s}{R} \Rightarrow$$

$$\Rightarrow \frac{V_o}{\frac{1}{j\omega C}} = -\frac{V_s}{R}$$

$$\Rightarrow V_o(j\omega C) = -\frac{V_s}{R} \Rightarrow V_o = -\frac{V_s}{j\omega R C}$$

$$\text{and } \frac{V_o}{V_s} = -\frac{1}{j\omega R C} = \frac{j}{\omega R C}$$

Remember $j = 1 \angle 90^\circ$
phase shift of phasor



KCL at node 1:

$$Z_1 = R_1 + \frac{1}{j\omega C_1}$$

$$Z_2 = R_2 + \frac{1}{j\omega C_2}$$

$$\begin{aligned} \frac{V_o}{Z_2} &= \frac{0 - V_s}{Z_1} \Rightarrow \frac{V_o}{V_s} = -\frac{Z_2}{Z_1} = -\frac{R_2 + \frac{1}{j\omega C_2}}{R_1 + \frac{1}{j\omega C_1}} \\ &= -\frac{\frac{j\omega R_2 C_2 + 1}{j\omega C_2}}{\frac{j\omega R_1 C_1 + 1}{j\omega C_1}} = -\frac{j\omega C_1}{j\omega C_2} \cdot \frac{j\omega C_2 R_2 + 1}{j\omega C_1 R_1 + 1} \end{aligned}$$

at $\omega = 0$

$$\frac{V_o}{V_s} = -\frac{C_1}{C_2}$$

at $\omega = \infty$

$$\frac{V_o}{V_s} = -\frac{R_2}{R_1}$$