

Topic 5: Inductors and RL Circuits

1. The circuits shown in Fig. 1 and 2 are considered to be under DC conditions

a) Find v_c , i_L , and the energy stored in the capacitor and inductor.

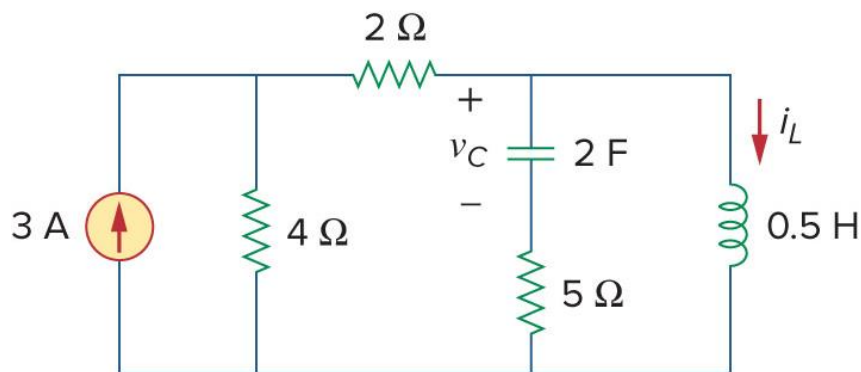


Fig. 1.

b) Find v_c , i_L , i , and the energy stored in the capacitor and inductor.

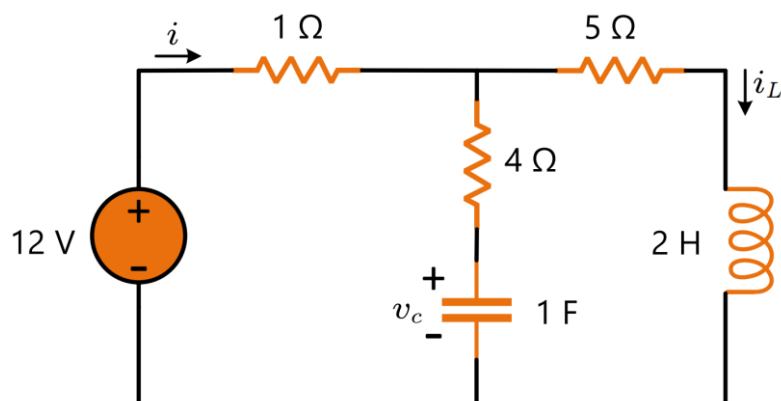


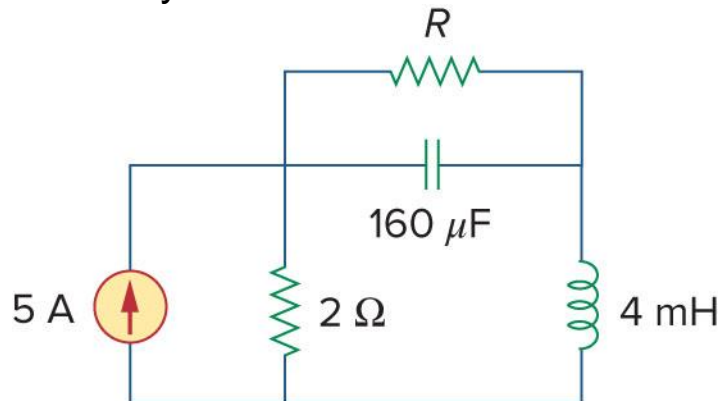
Fig. 2.

Answer:

a) $v_c = 0$ V, $i_L = 2$ A, $w_c = 0$ J, and $w_L = 1$ J

b) $v_c = 10$ V, $i_L = i = 2$ A, $w_c = 50$ J, and $w_L = 4$ J

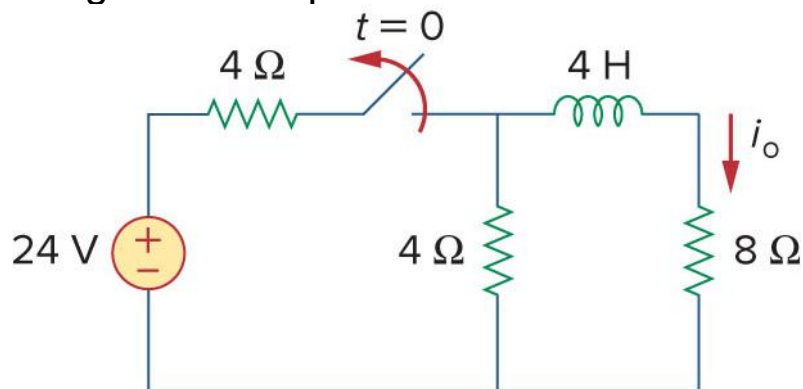
2. In the following circuit, Calculate the value of R that will make the energy stored in the capacitor the same as that stored in the inductor under steady-state conditions.



Answer: $R = 5\ \Omega$,

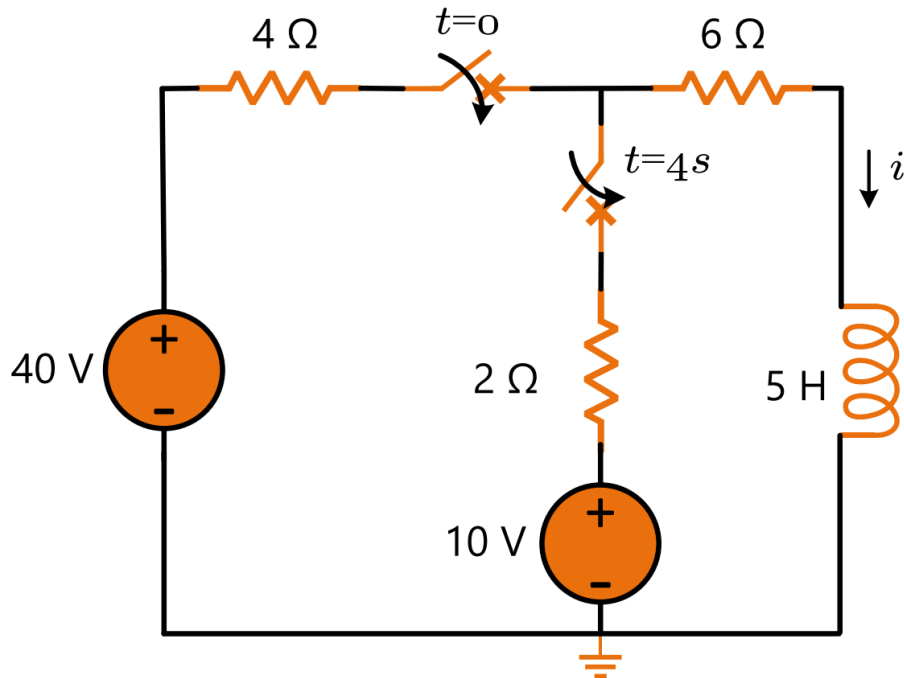
Hint: Find the capacitor and inductor energies in term of R .

3. The switch in the following circuit has been closed for a long time. At $t = 0$, the switch is opened. Calculate $i_o(t)$ for all time (i.e., for both $t < 0$ and $t > 0$), and sketch the current $i_o(t)$ as a function of time showing all critical points in the sketch.



Answer: $i_o(t) = \begin{cases} 1.2\ \text{A} & t \leq 0 \\ 1.2e^{-3t}\ \text{A} & t \geq 0 \end{cases}$

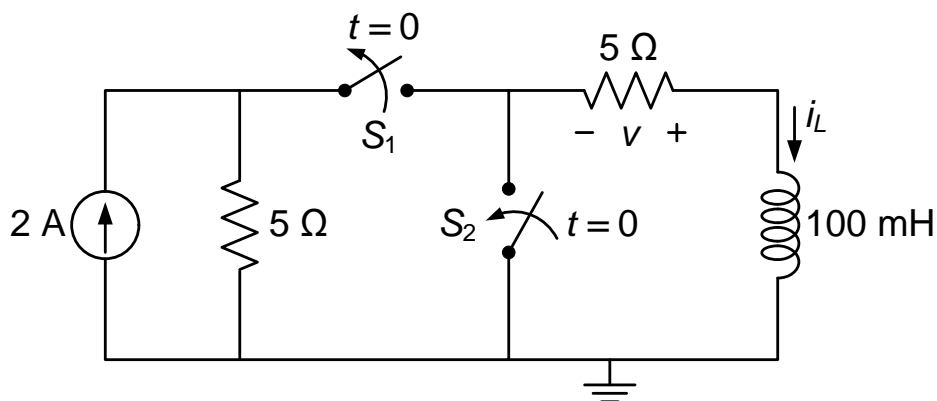
4. In the following circuit, at $t = 0$, switch 1 is closed (next to 4- Ω resistor), and switch 2 is closed 4 seconds later. Find $i(t)$ for all time (i.e., for both $t < 0$ and $t > 0$), and calculate $i(t)$ at $t = 2$ s and $t = 5$ s. Sketch $i(t)$ waveform showing all critical points in the sketch.



Answer:
$$i(t) = \begin{cases} 0 \text{ A}, & t \leq 0 \\ 4(1 - e^{-2t}) \text{ A}, & 0 \leq t \leq 4 \\ 2.727 + 1.273e^{-1.466(t-4)}, \text{ A} & t \geq 4 \end{cases}$$

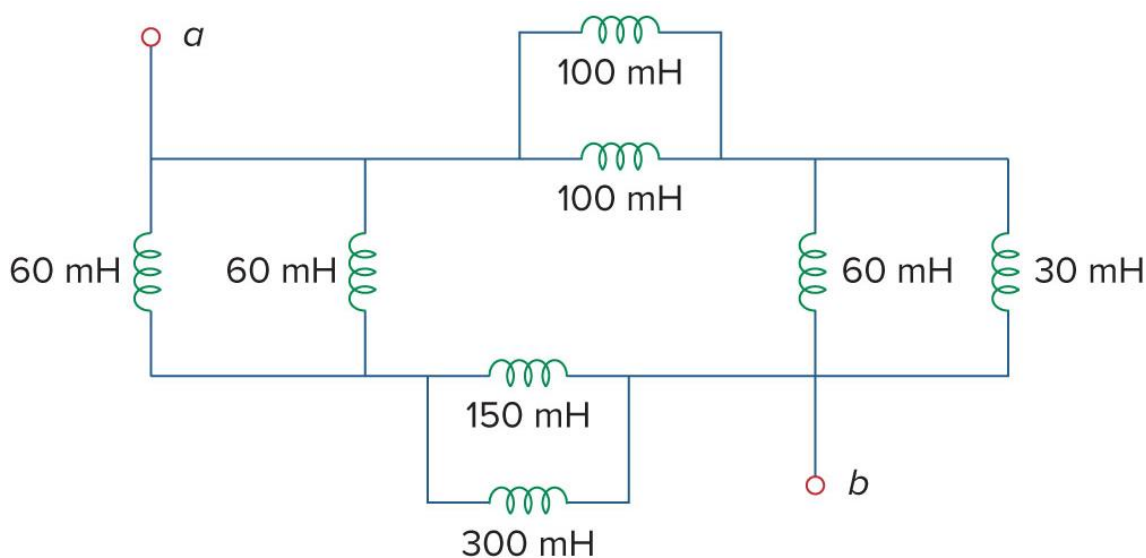
Hint: Use time shift property explained at the end of Topic 4.

5. **(Final Exam – S1, 2016)** Consider the circuit shown below, where switch S_1 has been closed for a long time and switch S_2 has been open for a long time. At $t = 0$, switch S_1 opens and switch S_2 closes. Derive an expression for the inductor current $i_L(t)$ and $v(t)$ for $t > 0$.



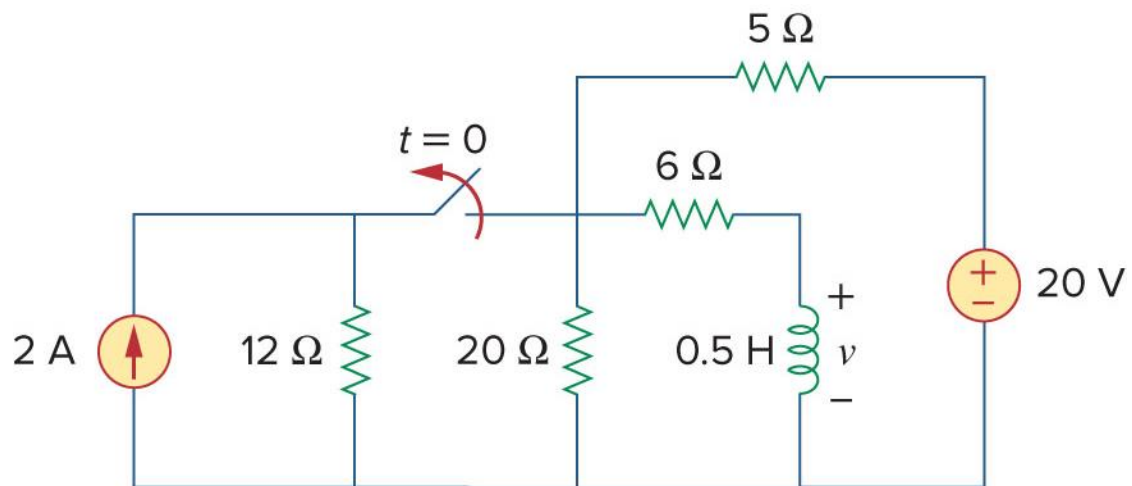
Answer: $i_L(t) = 1e^{-50t}u(t)$ A, $v(t) = -5e^{-50t}u(t)$ V

6. Find the equivalent inductance as seen from the terminals a - b in the circuit below.



Answer: $L_{eq} = 45.5$ mH

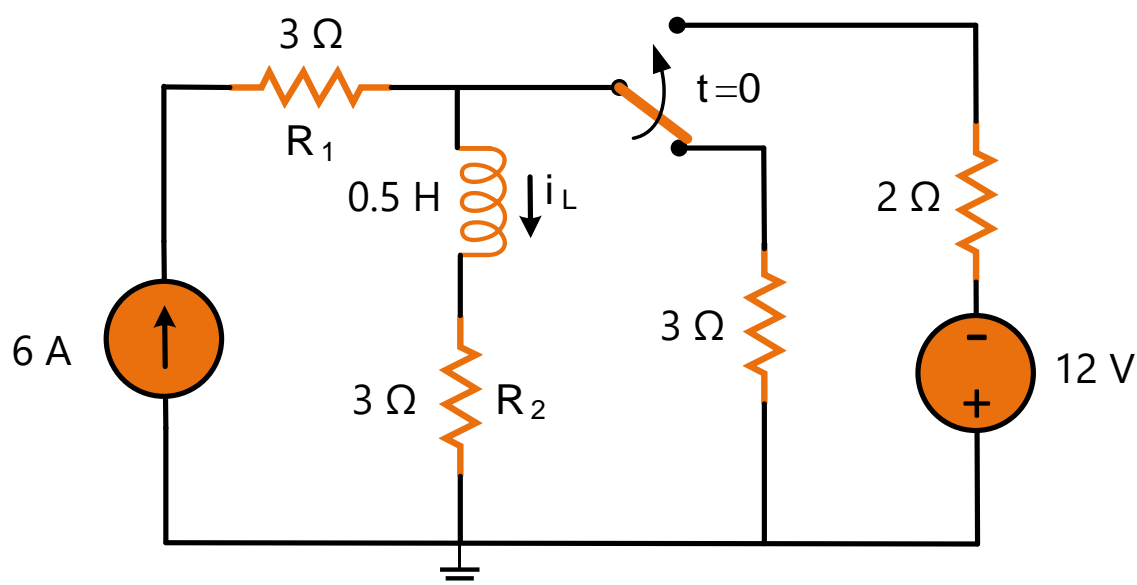
7. Find the voltage across inductor $v(t)$ for $t > 0$.



Answer: $v(t) = -4e^{-20t}u(t)$ V

8. (Final Exam – S1 2017) In the circuit below,

- Find the energy stored in the inductor under steady-state when the switch is in the open position (connected to $3\text{-}\Omega$ resistor).
- If the switch has been in the open position for a long time and closes at $t = 0$, derive an analytical expression for the current $i_L(t)$ through the inductor for $t > 0$.
- Plot the current through the inductor as a function of time.
- Derive an analytical expression for the voltages across resistors R_1 and R_2 (v_{R_1} and v_{R_2}) as a function of time for $t > 0$.



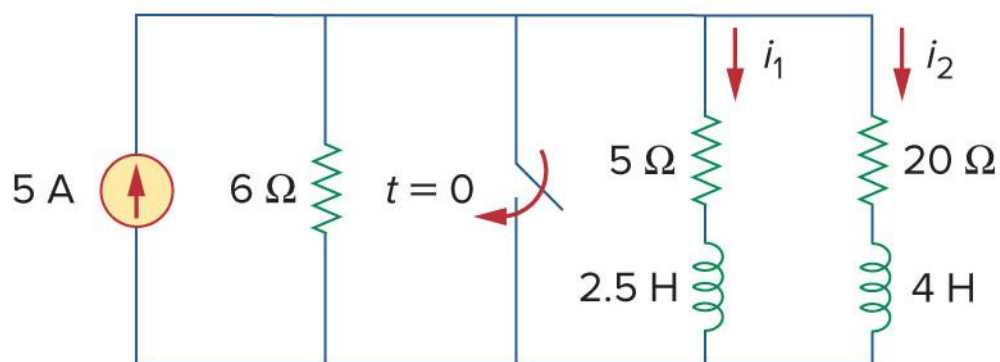
Answer:

a) $w_L(0) = 2.25 \text{ J}$

b) $i_L(t) = 3e^{-10t}u(t) \text{ A}$

c) $v_{R_1}(t) = 18 \text{ V}, v_{R_2}(t) = 9e^{-10t}u(t) \text{ V}$

9. Derive an expression for $i_1(t)$ and $i_2(t)$ for $t > 0$.



Answer: $i_1(t) = 2.4e^{-2t}u(t)$ A, $i_2(t) = 0.6e^{-5t}u(t)$ A