

Midterm Solutions

Wednesday, 26 April 2017 07:56

Question 1: $R_{eq} = 10\Omega$

• $8\Omega \rightarrow$ short circuited

$$4 \parallel 4 = 2\Omega$$

$$4 + 4 = 8\Omega$$

$$24 \parallel 8 = 6\Omega$$

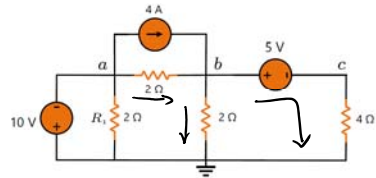
$$10 + 6 + 4 = 20\Omega$$

$$20 \parallel 5 = 4\Omega$$

$$2 + 4 + 4 = 10\Omega$$

$$R_{eq} = (4 \parallel 4) + 4 + (5 \parallel [10 + (8 \parallel 24) + 4])$$

Question 2:



i)

$$V_a = -10V \quad V_b = V_c + 5$$

KCL at supernode:

$$\frac{-10 - V_b}{2} + 4 = \frac{V_b}{2} + \frac{V_c}{4} \Rightarrow$$

$$\frac{-10 - V_c - 5}{2} + 4 = \frac{V_c + 5}{2} + \frac{V_c}{4} \Rightarrow$$

$$-20 - 2V_c - 10 + 16 = 2V_c + 10 + V_c \Rightarrow$$

$$\Rightarrow 5V_c = 40 - 16 \Rightarrow 5V_c = 24 \Rightarrow V_c = -4.8V$$

$$V_b = 0.2V$$

ii)

Current source

$$V = 10.2V$$

$$I = 4 \quad p = V \cdot i \text{ or } p = -V \cdot i$$

$$p = -10.2 \times 4 = -40.8W$$

$$\text{or } 40.8W \text{ generates}$$

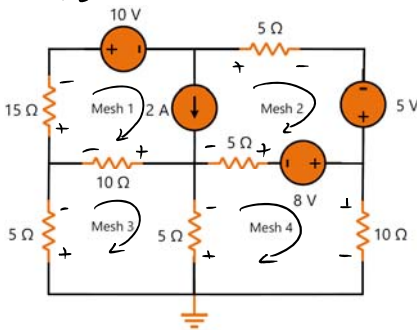
iii)

Resistor

$$p = \frac{V^2}{R} \text{ or } i^2 R \text{ or } V \cdot i$$

$$p = 50W \text{ or absorbs } 50W$$

Question 3:



Mesher 1 and 2

$$i_1 - i_2 = 2 \quad (1)$$

$$+25i_1 + 10i_2 - 10i_3 - 5i_4 = -13 \quad (2)$$

Mesh 3:

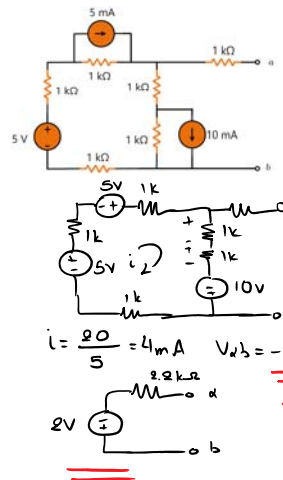
$$-10i_1 + 20i_3 - 5i_4 = 0 \quad (3)$$

Mesh 4:

$$-5i_2 - 5i_3 + 20i_4 = 8 \quad (4)$$

Question 4:

$$R_{Th} = 1 + 2 \parallel 3 = 2.2k\Omega$$



i) V_{oc} : Different methods
most probable: source transf.

ii) Mesh analysis
↳ 3 equations

iii) Superposition
↳ many calculations

iv) V_{oc} and I_{sc}

$$i = \frac{20}{5} = 4mA$$

$$V_{ab} = -2V$$

Question 5 i)

$$W_{L1} = \frac{1}{2} L i^2 = 16J$$

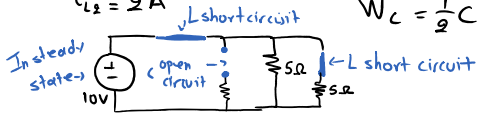
$$i_{L1} = 4A$$

$$W_{L2} = \frac{1}{2} L i^2 = 4J$$

$$i_{L2} = 2A$$

$$V_C = 10V$$

$$W_C = \frac{1}{2} C V^2 = 50J$$



Question 5 ii)

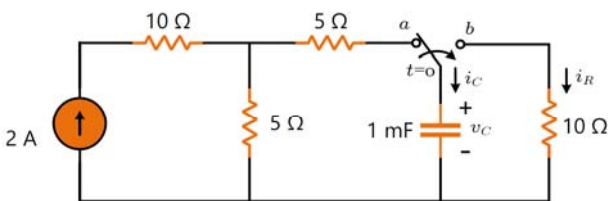


Figure 6.

$$V_C(0^-) = V_C(0^+) = 10V$$

$$V_C(\infty) = 0V$$

$$\tau = 1mF \cdot 10\Omega = 10 \cdot 10^{-3} \text{ sec}$$

$$\text{or } 10ms$$

$$V_C(t) = 10 e^{-t/10^{-2}} V, t \rightarrow \text{sec}$$

$$\text{or } 10 e^{-100t} V, t \rightarrow \text{sec}$$

$$\text{or } 10 e^{-t/10} V, t \rightarrow \text{msec}$$

$$i_R = -i_C$$

$$i_C = C \cdot \frac{dV}{dt} \text{ or } \frac{V_C(t)}{R}$$

$$i_R = e^{-100t} A, t \rightarrow \text{sec}$$

etc...

UNITS IN ALL ANSWERS?