

QUESTION 1 Use a SEPARATE writing sheet.

Marks

(a) Find the value of $\frac{\sqrt{12.35} - 8.66}{6.5}$ correct to two decimal places

2

(b) Solve the equation $\frac{x+6}{3} = \frac{4}{5}$

2

(c)

2

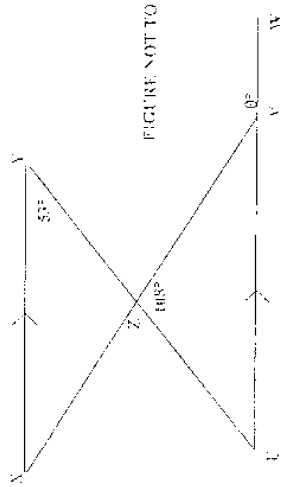


FIGURE NOT TO SCALE

The diagram shows XY parallel to VW, $\angle XVU = 53^\circ$, $\angle ZVW = 108^\circ$ and $\angle ZVW = 62^\circ$.

Find the value of θ . Give reasons.

(d) Find a primitive function for $x^2 - 4$.

2

(e) A function $g(x)$ is defined as

$$g(x) = \begin{cases} 2x-1 & \text{when } x < 2 \\ x^2 & \text{when } x \geq 2 \end{cases}$$

Evaluate $g(4) + g(2)$.

2

(f) Graph the solution of $2x - 3 \geq 2$ on the number line.

2

QUESTION 2

Use a SEPARATE writing sheet.

Marks

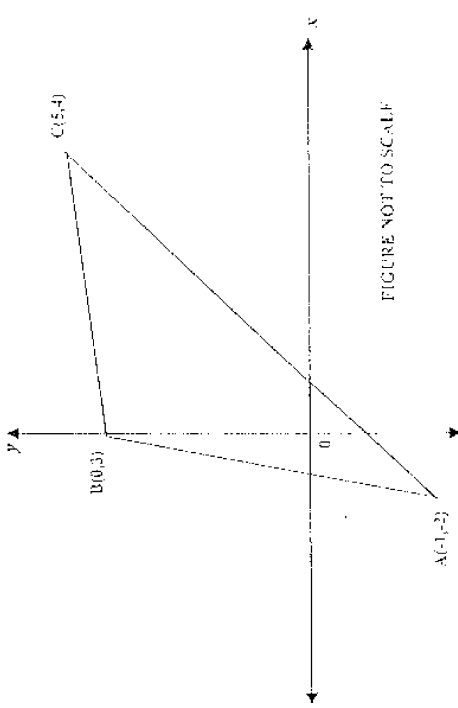


FIGURE NOT TO SCALE

The diagram shows $\triangle ABC$ with vertices $A(-1, -2)$, $B(0, 3)$ and $C(5, 4)$.

Copy the diagram onto your answer sheet.

(a) E is the midpoint of AC. Show that the coordinates of E are $(2, 1)$.

1

(b) Show that the gradient of AC is 1.

1

(c) A line L is drawn through B, perpendicular to AC. Show the equation of line L is $y = 3 - x$.

2

(d) Show that E lies on line L.

1

(e) On your diagram, draw line L and plot point E. Prove $\triangle BEC$ is congruent to $\triangle BEA$.

3

(f) AC is a diameter of a circle.

1

(i) Calculate the radius of the circle.

2

(ii) Hence find the equation of the circle.

2

QUESTION 4 Use a *SEPARATE* writing sheet. Marks

- (a) The third term and the tenth term of an arithmetic series are 7 and 42 respectively. Find the:
- (i) first term and the common difference.
 - (ii) sum of the first ten terms of the series.
- (b) A box contains five blue, three yellow and eight red beads. Two beads are selected at random from the box without replacement. Find the probability that:
- (i) both beads are blue.
 - (ii) at most one of the beads is blue.

QUESTION 3 Use a *SEPARATE* writing sheet. Marks

- (a) Differentiate the following expressions with respect to x :

(i) $(3x^2 - 2)^4$

(ii) $3x \cos 2x$

(iii) $\frac{e^{3x}}{x}$

- (b) Evaluate the following definite integrals:

(i) $\int_0^{\pi/2} \sin 3x \, dx$

(ii) $\int_2^3 e^{2x-1} \, dx$

(c) Find $\int \frac{x}{x^2 + 4} \, dx$

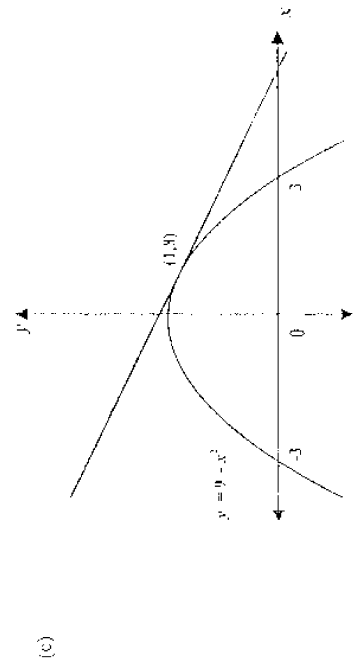


FIGURE NOT TO SCALE

The diagram shows the graph of the parabola $y = 9 - x^2$. A tangent is drawn to the parabola at the point (1, 8).

- (i) Show that the equation of the tangent at (1, 8) is $2x + y = 10$.
- (ii) Explain how you know the tangent crosses the x -axis at (5, 0).
- (iii) Calculate the area bounded by the parabola, the tangent and the x -axis.

QUESTION 5	Use a SEPARATE writing sheet	Marks
(a)	4	

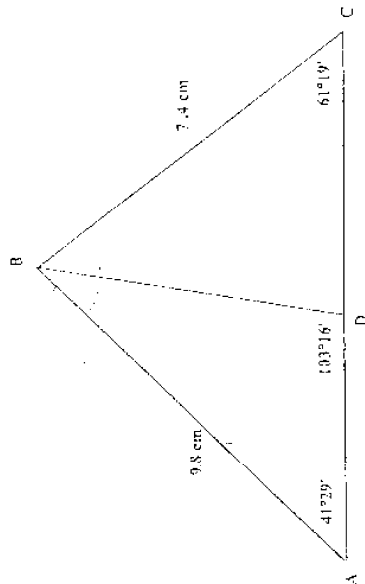


FIGURE NOT TO SCALE

In the diagram, $AB = 9.8$ cm, $BC = 7.4$ cm, $\angle BCD = 61^\circ 19'$, $\angle BDA = 103^\circ 16'$ and $\angle BAD = 41^\circ 29'$.

- Find the length of BD correct to the nearest mm.
- Calculate the area of $\triangle ABC$ correct to the nearest cm^2 .

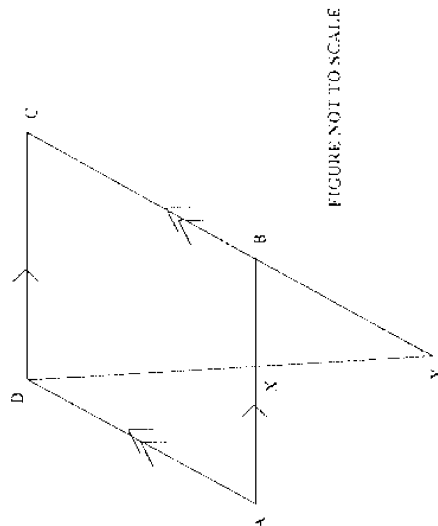
- Consider the curve $y = 4x^3 + 6x^2$.

- Find the coordinates of any turning points and determine their nature.
- Find the x coordinate of any points of inflexion.
- Sketch the curve for the domain $-2 \leq x \leq 1$.
- What is the maximum value of $4x^3 + 6x^2$ in the domain $-2 \leq x \leq 1$?

QUESTION 6	Use a SEPARATE writing sheet	Marks
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- Find all the values of x for which $\sin x = 2 \ln x$

-



In the diagram, $ABCD$ is a parallelogram. X is a point on AB . DX and CB are both produced to Y .

- Copy this diagram onto your answer sheet.
- Prove that $\triangle ADX$ is similar to $\triangle CYD$
- Hence find the length of XY given $AX = 8$ cm, $DC = 12$ cm and $DX = 10$ cm.

QUESTION 6

(Continued)

Marks

(c)

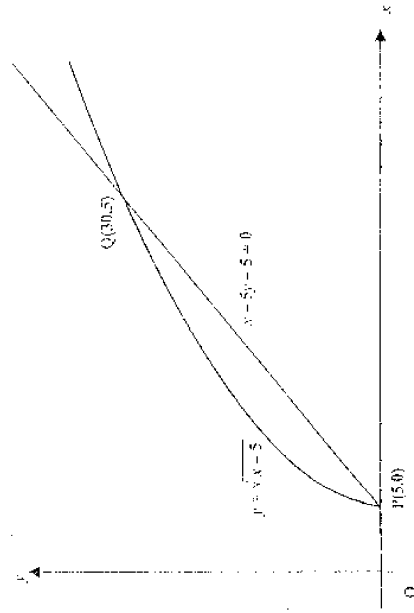


FIGURE NOT TO SCALE

The diagram shows the graphs of the curve $y = \sqrt{x-5}$ and the line $x - 5y - 5 = 0$. The curve and the line intersect at the points $P(5,0)$ and $Q(30,5)$. The region bounded by the curve and the line is shaded about the y-axis. Find the volume of the solid generated.

QUESTION 7

Use a SEPARATE writing sheet

Marks

5

(a) An experimental vaccine was injected into a cat. The amount, M millilitres, of vaccine present in the bloodstream of the cat, t hours later was given by $M = e^{2t} + 3$.

- How much vaccine was initially injected into the cat?
- At what rate was the amount of vaccine decreasing at the end of 3 hours?
- Show that there will always be more than 3 millilitres of vaccine present in the cat's bloodstream.
- Sketch the curve of $M = e^{2t} + 3$ to show how the amount of vaccine present in the cat's bloodstream changes over time.

7

(b) A particle moves in a straight line. At time t seconds, its displacement, x metres from a fixed point O on the line is given by

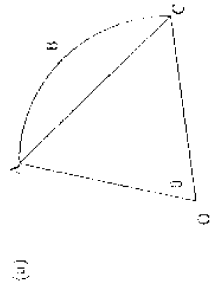
$$x = 1 - \cos \pi t$$

- What is the initial displacement of the particle?
- Sketch the graph of x as a function of t .
- Find an expression for the velocity of the particle at any time t .
- What is the velocity of the particle at time $t = \frac{1}{6}$?
- At what time does the particle first reach its maximum speed?

QUESTION 9 Use a SEPARATE writing sheet

Marks

4

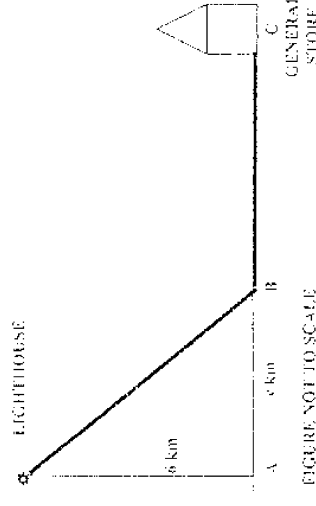


The diagram shows a sector OAC with area $90\pi \text{ cm}^2$ and $OA = 15 \text{ cm}$

- (i) Find the size of θ in radians.
 (ii) Find the perimeter of the segment ABC. Give your answer correct to the nearest cm.

FIGURE NOT TO SCALE

(b)



The water's edge is a straight line ABC which runs East-West. A lighthouse is 6 km due north of A, 10 km due east of A is the general store. To get to the general store as quickly as possible, the lighthouse keeper rows to a point B, x km from A, and then jogs to the general store. The lighthouse keeper's rowing speed is 6 km/h and his jogging speed is 10 km/h.

- (i) Show that it takes the lighthouse keeper $\frac{\sqrt{25+x^2}}{6}$ hours to row from the lighthouse to B.

- (ii) Show that the total time taken for the lighthouse keeper to reach the general store is given by:

$$T = \frac{\sqrt{25+x^2}}{6} + \frac{10-x}{10} \text{ hours}$$

- (iii) Hence show that when $x = 4.5$ km, the time it takes for the lighthouse keeper to row to the lighthouse to the general store is a minimum.

- (iv) Hence find the earliest time it takes the lighthouse keeper to go to the general store from the lighthouse. Give your answer correct to the nearest minute.

QUESTION 8 Use a SEPARATE writing sheet

Marks

6

- (a) When Jack left school, he borrowed \$15 000 to buy his first car. The interest rate on the loan was 18% p.a. and Jack planned to pay back the loan in 60 equal monthly instalments of \$M.

- (i) Show that immediately after making his first monthly instalment, Jack owed

$$S[15\,000 \times (1.015 - M)]$$

- (ii) Show that immediately after making his third monthly instalment, Jack owed

$$S[15\,000 \times 1.015^3 - M(1 + 1.015 + 1.015^2)]$$

- (iii) Calculate the value of M.

- (b) The table shows the values of a function $f(x)$ for five x values.

x	0	2	4	6	8
$f(x)$	0.9	1.4	1.8	2.1	1.7

- Approximate the value of $\int_0^8 f(x) dx$ using the five function values and Simpson's rule.

- (i) On the same number plane, sketch the curves $y = \sin x$ and $y = \tan \frac{x}{2}$ in the domain $0 \leq x \leq 2\pi$

- (ii) Hence find the number of real solutions to the equation $\sin x = \tan \frac{x}{2}$ for $0 \leq x \leq 2\pi$.

QUESTION 10

Use a *SEPARATE* writing sheet

Marks

(a)

7

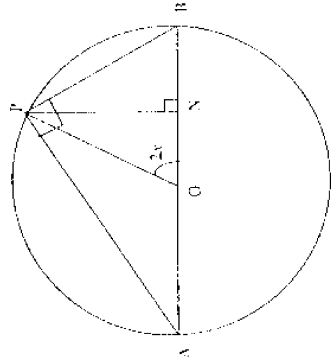


FIGURE NOT TO SCALE

The diagram shows a circle with centre O and diameter AB . P is a point on the circumference of the circle. PN is drawn perpendicular to AB and AP is perpendicular to PB . Let $\angle POB = 2x$.

- (i) Explain why $\triangle APO$ is isosceles.
- (ii) Explain why $\angle OAP = \angle OPA = x$.
- (iii) Show that $\sin 2x = \frac{2PN}{AB}$.
- (iv) Use $\triangle APN$ and $\triangle PAB$ to show that $2 \sin x \cos x = \sin 2x$.

- (b) Kellie and Lachlan play a game where they each take turns at throwing two ordinary dice. The winner is the first person to throw a double. Kellie throws first.

5

- (i) Show that the probability that Lachlan wins the game on his first throw is $\frac{5}{36}$.
- (ii) Show that the probability Lachlan wins the game on his first or second throw is given by $\frac{5}{36} + \frac{5}{64}$.
- (iii) Calculate the probability that Lachlan wins the game.