# Question 1 (Start a new page)

### Marks

a. Show that the exact value of  $\cos 15^{\circ}$  is  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$ 

2

b. For what values of  $x (x \neq 0)$  does the geometric series

4

- $1 + \frac{2x}{x+1} + \left(\frac{2x}{x+1}\right)^2 + \dots$  have a limiting sum?
- c. Use the table of standard integrals to find  $\int_0^4 \frac{1}{\sqrt{9 + x^2}} dx$
- 2
- d. Six men and five women are arranged at random in a row so that each woman is between two men.
- 4

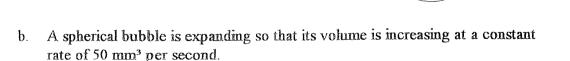
- i. How many such arrangements are possible?
- ii. What is the probability that two specified men, A and B, sit at the ends of the row?

### Question 2 (Start a new page)

(a) From a cliff 100 metres high, the straight line distance to the horizon is 36 kilometres.

100 m 4 36 km

Calculate the radius of the earth.



3

3

What is the rate of increase of its surface rea when the radius is 8 mm?

c. Show that 
$$tan^{-1}\left(\frac{1}{4}\right) + tan^{-1}\left(\frac{3}{5}\right) = \frac{\pi}{4}$$

2

d. In the expansion of  $(\sqrt[5]{x} + \sqrt[3]{x})^9$ , find the term(s) where the power of x is an integer.

4

## Question 3 (Start a new page)

Marks

a. i. Show that  $\frac{\sec^2 x}{\tan x} = \frac{1}{\sin x \cos x}$ 

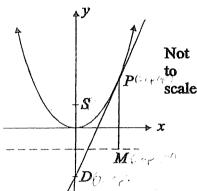
b.

4

- (ii) Use the substitution  $u = \tan x$  to show that  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{dx}{\sin x \cos x} = \log_e 3$
- The point P(2ap, ap<sup>2</sup>) lies on the parabola defined by  $x^2 = 4ay$ .

4

The line PM is drawn parallel to the axis of the parabola to meet the directrix in M. S is the focus of the parabola.



- i. State why SP is equal to PM.
- ii. The tangent at P meets the y-axis at D. Find the coordinates of D.
- (i)i. Show that SPMD is a rhombus.

4

c. Use the Principle of Mathematical Induction to prove that, for all positive integers, n,

$$\sum_{r=1}^{n} \frac{1}{(4r-3)(4r+1)} = \frac{n}{4n+1}$$

Question 4 (Start a new page)

a. The point C(-6, 1) divides the interval AB externally in the ration 3:1. If A by the Sinates (0, 4), find the coordinates of B

2

b. i. Express  $4\sin\theta - 3\cos\theta$  in the form  $A\sin(\theta - \alpha)$ , A > 0,  $0 < \alpha < 90^{\circ}$  4

3

ii. Find all solutions of  $4\sin\theta - 3\cos\theta = 1$  for  $0 \le \theta \le 360^{\circ}$ 

Ouestion 4 is continued on the next page.

### Question 4 (continued)

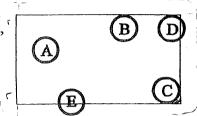
#### Marks

2



At the Easter Show, there is a new game in which a small hoop of radius 100 mm is to be thrown onto a rectangular table 3 metres by 2 metres. If the hoop lands so that no part of it extends past the edge of the table, a prize is won. If part of the hoop extends over the edge of the table, no prize is won. (In the diagram, hoops A, B and C would win prizes but hoops D and E would not)

Assuming that the hoop lands on the table, what is the probability of winning a prize with one throw?



- The quadratic equation  $x^2 + 6x + c = 0$  has two real roots. These roots have opposite signs and differ by 2n, where  $n \neq 0$ .
- 4

- i. Show that  $n^2 = 9 c$
- ii. Find the set of all possible values of n.

### Question 5 (Start a new page)

a. A factory machining car parts finds that 98% are machined correctly. From a sample of 40 car parts, calculate to 3 decimal places the probability that

4

- i. exactly 38 of the parts are correctly machined.
- ii less than three parts are incorrectly machined.
- b. i. Show that the equation  $\log_e x + x^2 4x = 0$  has a root between x = 3 and  $x = 4 + \infty$

4

- ii. Using x = 3.5 as a first approximation, find a better approximation using Newton's method once.
- c. i. Show that  $\cos 4x = 8(\cos^4 x \cos^2 x) + 1$

4

ii. Hence or otherwise solve  $\cos^2 x - \cos^4 x = \frac{1}{16}$ ,  $0 \le x \le \frac{\pi}{2}$ 

## Question 6 (Start a new page)

Marks

An F18 jet is climbing at a speed of 504 kilometres per hour at an angle of 30° to the horizontal. When the jet is 600 metres above the ocean, it drops a flare from a wing. The only force acting on the flare is gravity.

5

7

Take  $g = 10 \text{ ms}^{-2}$ .

- i. Find the time taken for the flare to hit the ocean.
- ii. Calculate the maximum height reached by the flare.
- iii. What is the horizontal distance travelled by the flare?

(b) The velocity,  $\nu$  ms<sup>-1</sup>, of a particle moving in Simple Harmonic Motion along the x-axis is given by the expression

$$v^2 = 28 + 24x - 4x^2$$

- i. Between what two points is the particle oscillating?
- ii. What is the amplitude of the motion?
- iii. Find the acceleration of the particle in terms of x.
- iv. Find the period of the oscillation.
- v. If the particle starts from the point furthest to the right, draw a graph of the displacement of the particle against time over two complete periods.

### Student Name / Number .....

### Question 7 (Start a new page)

Marks

a. The arc of the curve  $y = \frac{1}{2}(1 + \sin x)$  between  $x = -\frac{\pi}{2}$  and  $x = \frac{\pi}{2}$  is rotated about the x-axis.

4

Find the volume of the solid formed.



i. Use the substitution  $u = \cos x$  to evaluate  $\int_0^{\frac{\pi}{2}} \sin^5 x \, dx$ , leaving your answer as a fraction.

8

ii. Given  $y = \sin^{2n-1} x \cos x$ , where *n* is a positive integer, find an expression for  $\frac{dy}{dx}$  in terms of powers of  $\sin x$ 

iii. Hence show that  $\int_0^{\frac{\pi}{2}} \sin^{2n} x \, dx = \frac{2n-1}{2n} \int_0^{\frac{\pi}{2}} \sin^{2n-2} x \, dx$ , where n is a positive integer.

iv. Evaluate  $\int_0^{\frac{\pi}{2}} \sin^6 x \, dx$  in terms of  $\pi = \frac{1}{2} \int_0^{\frac{\pi}{2}} 1$ 

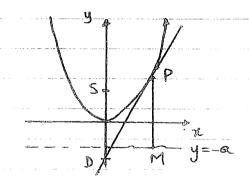
2000 NSW Independent Trial Exams : 3 UNIT SOLUTIONS, 2000 Mathematics 81.(a) COO (A-B) = COO A COO B + Sun A Sun B (c) / 1 on Cos (45-30) = cos 45 cos 30 + sn. 45 sm30  $=\frac{1}{\sqrt{2}}\left(\frac{\sqrt{3}}{3}+\frac{1}{2}\right)$ = [lu (x+ \( 9+x^{2} \) ] \\ \]  $\cos 15 = \sqrt{3} + 1$ = lu (4+ \( 9+42 \) - lu (0+ \( 9+ = lu 9 - lu 3 (b) |r| < |= lu 3  $\frac{1}{2x}$ (d) (i) 6p x 5p = 86400 either 2x < 1 (ii) Ignore the women: Critical pounts at x = - 1 and Number of permetations with A 2x = 1 at the ends is 2px 4p = 48  $2x = x + / \Rightarrow x = /$  x < -1 -1 < x < 1 x > 1. . P(A+B are at the ends) Test x=0: frue :- 1< x < 1 Dr 22 > -1 Critical por at x=-1 and 2x = /  $dR = -R - / \Rightarrow \mathcal{H} = -\frac{1}{3}$  R < -1  $\begin{cases} R > -\frac{1}{3} \\ \end{cases}$ Test x=0: free : x<-1 xx-1 dolution is:  $-\frac{1}{3} < x < 1$ ,  $x \neq 0$ 

These suggested answers/marking cohomogonic

P3((1) LHS = See 20 toux

$$T = \int_{\sqrt{3}}^{\sqrt{3}} du$$

3



(i) Parabola is locus of points equilistant from fows, S, and director, y=-a \_'.PS = FM

ii) Tangent at P: 
$$y = px - ap^2$$

$$At x = 0, \quad y = -ap^2$$

$$\therefore D(0, -ap^2)$$

(ii) 
$$a_{pm} = ap^2 - a = a(p^2 + 1)$$
  
 $a_{3p} = a - -ap^2 = a(1+p^2)$   
 $PM = PS = SD$  and  $SD//PM$ 

so SPMD is a rhombus

(c) 
$$S(n): \sum_{r=1}^{n} \frac{1}{(4r-3)(4r+1)} = n$$

$$S(1): LHS = \frac{1}{(4-3)(4+1)} = \frac{1}{5}$$

$$RHS = \frac{1}{4+1} = \frac{1}{5} = LHS$$

Assume n=k:

18 sume 
$$N = R$$
:  
Le  $S(k)$ :  $\sum_{i=1}^{k} \frac{1}{(4k-3)(4k+1)} = \frac{1}{4k}$ 

Prove n= K+1 1.2. S(k+1): \(\sum\_{r=1}^{k+1}\) \(\frac{1}{(4r-3)(4r+1)}\)

$$LHS = \frac{k}{4k+1} + \frac{1}{(4k+1)(4k+5)}$$

$$= k(4k+5) + 1$$

$$(4k+1)(4k+5)$$

$$= 4h^2 + 5k + 1$$

$$(4k + 1)(4k + 5)$$

$$= \frac{(4k+1)(k+1)}{(k+1)}$$

$$= \frac{k+1}{4k+5} = RHS$$

. If S(k) is stone, then S(k+ But 5(1) is true, so 5(2) is & whence S(3) is force and so for all positive integer va of n.

3 UNIT TRIAL SOLUTIONS

$$34.6)$$
  $H(0.4)$   $\times B(x_1, y_1)$   $\Rightarrow k:l = -3:1$ 

$$Z = \frac{kx_1 + lx}{k + l}, \Rightarrow -6 = \frac{-3x_1 + 1 \times 0}{l}$$

$$12 = -3x_2 \Rightarrow x_2 = 4$$

$$y = ky_1 + ly_1 \Rightarrow 1 = -3y_1 + 1 \times 4$$
  
 $k+l$   $-3+1$ 

$$-2 = -3y_2 + 4 = 3y_2 = 2$$

$$\Rightarrow \alpha = -n - 3$$
but  $\alpha \times (\alpha + 2n) = C$ 

$$(-n-3)x(-n-3+2n)=c$$

$$-R^{2}+9 = C$$
so  $R^{2}=9-C$ 

$$-1$$
.  $A\cos\alpha = 4$ 

where 
$$\alpha = +an^{-1}(3/4)$$

$$Sum (\theta - \alpha x) = K$$

$$-' \cdot \theta = 11^{\circ}32' + 36^{\circ}52' = 46^{\circ}24'$$

and 
$$\theta = 168°28' + 36°51' = 205°20'$$

Area where hoop does not protrude

5 (a) let p = probability of correctly

machined part = 0.98

g = prob. of sucorrectly machined

X = no. of correctly machined parts:

P(x=r) = "C, (0.98)" (0.02)40-r

(i)  $P(X=38) = {}^{4}C_{38} (0.98)^{38} (0.02)^{2}$ 

(a) P(X > 38) = P(X = 38) + P(X = 39) + P(X = 40)

= 0.1448 + "Gq (98) 39 .02+ Cro (98)

= 0.954

b) let f(x) = loge x + x2 - 4x

(i)  $f(3) = \ln 3 + 9 - 12 < 0$   $f(4) = \ln 4 + 16 - 16 > 0$ 

· root exists between x=3 x=4

(ii) f(x) = + + 2x -4

Then x, = x - lix + x2- 4x

15- lu3.5+3.5-4x3.5 12-+2x3.5-4

= 3.65/3

Better approximation is 2 = 3.65

(c)(1) Lon 4x = Cos 2x2x

= 2 cos 2 dx -/

= 2 Resize - 172-1

= 2 (4co 4x - 4co x+1)-1

= 8con 4 - 8con 7x + L - 1

Mr 4:= Proto 1 + 1

(ii)  $\cos^2 x - \cos^4 x = \frac{1}{16}$ 

Cos4x = 8. - 1 +1

3 UNIT TRIAL SOLUTIONS, 200

$$16.(a)$$
  $\ddot{x} = 0$   $\ddot{y} = -10$   
 $\dot{x} = V\cos\alpha$   $\dot{y} = -10t + V\sin\alpha$   
 $x = Vt\cos\alpha$ ;  $y = -5t^2 + Vt\sin\alpha + 600$ 

(iii) 
$$v^{2} = 28 + 24x - 4x^{2}$$
  
 $\frac{1}{2}v^{2} = 14 + 12x - 2x^{2}$   
 $\frac{d}{dx}(\frac{1}{2}v) = 12 - 4x$ 

Also 
$$504 \text{ km/hr} = 140 \text{ m/s}$$
  
 $\dot{x} = 70\sqrt{3}$   $\dot{y} = -10t + 70$   
 $x = 70\sqrt{3}$   $\dot{y} = -5t^2 + 70t + 600$ 

$$-1 a = 12 - 4x$$

(i) 
$$y=0 \Rightarrow -5t^2 + 70t + 600 = 0$$
  
 $-5(t^2 - 14t - 120) = 0$   
 $-5(t-20)(t+6) = 0$   
 $= )t = 20$  seconds

(w) 
$$a = -4(x-3)$$
  
=  $-2^{2}(x-3)$   
:  $n = 2$   
Period,  $T = 2x$ 

(ii) 
$$y=0 \Rightarrow -10t+70 =0$$
  
 $t=7$   
At t=7,  $y=-5\times7^2+70\times7+600$   
= 845 metres

iii) At t=20, x=70/3 x 20 = 2424.87 = 2.425 kilometres

1) (i) 
$$v^2 = 28 + 24x - 4x^2$$

1( $v = 0 \Rightarrow 28 + 24x - 4x^2 = 0$ 

1( $7 + 6x - x^2$ ) = 0

1( $x^2 - 6x - 7$ ) = 0

1( $x - 7(x + 1) = 0$ 

(ii) medpoint of motion to x=3 'Amplitude to 4m

SUNIT TRIAL SOLUTIONS

$$= \pi \left[ x - 2\cos x + \frac{1}{2} \left( x - \frac{1}{2} \sin 2x \right) \right]^{\frac{4}{2}}$$

$$= \overline{4} \left\{ \left( \frac{1}{2} - 0 + \frac{1}{2} \left( \frac{\pi}{2} - 0 \right) \right) \right\}$$

$$-\left\{-\frac{\pi}{2}-0+\frac{1}{2}\left(-\frac{\pi}{2}-0\right)\right\}\right]$$

$$= \frac{1}{4} \left( \frac{1}{2} + \frac{1}{4} + \frac{1}{2} + \frac{1}{4} \right)$$

$$= \frac{3\pi^2}{8}$$

(b)(1) 
$$u = \cos x$$
  $du = -s_{uv} x \cdot dx$   
of  $x = 0$ ,  $u = 1$ ;  $x = \overline{x}$ ,  $u = 0$ 

$$=\int_{1}^{0}\left(1-u^{2}\right)^{2}-olu$$

$$= \int_0^1 1 - \lambda u^2 + u^4 \cdot ohe$$

$$= \left[ Lu - 2u^3 + \frac{u}{5} \right]_0^1$$

$$= 1 - \frac{2}{3} + \frac{1}{5} = \frac{2}{5}$$

(ii) 
$$dy = (2n-1) \sin^{2n-2} x \cdot \cos x \cdot \cos x$$
  
 $dx + \sin^{2n-1} - \sin x$   
 $= (2n-1) \sin^{2n-2} x \cdot (1-\sin^{2} x) + \sin^{2n-2} x$   
 $= (2n-1) \sin^{2n-2} x - (2n-1) \sin^{2n} x - \sin^{2n} x$ 

$$= (2n-1)\sin^{2n-2}x - (2n-1)\sin^{2n}x - \sin^{2n}x$$

$$= (2n-1)\sin^{2n-2}x - 2n\sin^{2n}x$$

$$= \lim_{x \to \infty} \frac{2n-1}{x} \cos x + C$$

$$4 \int_{0}^{\frac{\pi}{2}} (2n-1) \sin^{2n-2} x - 2n \sin^{2n} x dx$$

$$= \left[ \operatorname{Am}^{2n-1} \times \operatorname{Cosx} \right]_{0}^{n/2} = 0$$

$$\int_{0}^{\pi/2} dn \sin^{2n}x \, dn = \int_{0}^{\pi/2} (2n-1) \sin^{2n}x \, dn = \int_{0}^{\pi$$

$$\int_0^{\pi} \sin^4 x \, dx = \frac{3}{4} \int_0^{\pi} \sin^4 x \, dx$$

$$\int_0^{\pi/2} dx = \frac{1}{2} \int_0^{\pi/2} dx = \frac{1}{2} \left[ x \right]$$

$$=\frac{5\Pi}{32}$$

3 UNIT TRIAL SOLUTION

$$1 - \frac{1}{4} \times \frac{3}{5}$$

$$\tan \theta = 1$$

$$\theta = \sqrt{4}$$

(d) 
$$(x^{\frac{1}{5}} + x^{\frac{1}{3}})^{9} = \sum_{r=0}^{9} {\binom{r}{r}} {\binom{x^{\frac{1}{5}}}{9}} {\binom{r}{r}} {\binom{x^{\frac{1}{5}}}{9}} {\binom{x^{\frac{1}{5}}}{7}} {\binom{x^{\frac{1}{5}}}{9}} {\binom{x^{\frac{1}{5}}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}}} {\binom{x^{\frac{1}5}}{7}} {\binom{x^{\frac{1}5}}{7}}}$$

$$=\sum_{r=0}^{9}\left(\chi^{\frac{21+2r}{15}}\right)$$

Integer powers occur whe

27-12r is an integer

This occurs when 
$$r = 9$$

$$\Rightarrow \frac{27 + 2x9}{15} = 3$$

The term is 
$${}^{9}C_{9} x^{3}$$

$$= x^{3}$$

= 8 Ter. 50 4 Ter

(b) dV = 50; r = 8

olv = 4 ar2, dr at at

 $V = \frac{4}{2} \times r^3$ 

and S = 4 Tr2

ds = 8xr. dr

12(a)

Now

 $BX.AX = Tx^{\perp}$ 

·/x (2r+·1)=362

2+1 = 362

 $r = \frac{1}{2} \left( \frac{36^2 - 1}{66} \right)$ 

~ 6480 km

= 6479-95 km

c) Let 
$$\theta = \tan^{-1}(\frac{1}{5}) + \tan^{-1}(\frac{3}{5})$$

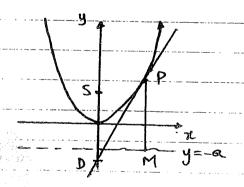
$$tan\theta = tan \left(tan^{-1}\left(\frac{1}{4}\right) + tan^{-1}\left(\frac{3}{5}\right)\right)$$

13e(1) LHS = see x

if 
$$u = \tan x$$
,  $du = \sec^2 x \, dx$   
if  $x = \frac{\pi}{3}$ ,  $u = \tan \frac{\pi}{3} = \sqrt{3}$ 

$$I = \int_{\sqrt{3}}^{5} du$$

$$= \int_{\sqrt{6}}^{1} u du$$



- (i) Parabola is locus of pourts equidistant from focus, S, and disectors, y=-a. PS = FM
- ii) Tangent at P:  $y = px ap^2$ At x = 0,  $y = -ap^2$   $D(0, -ap^2)$

ii) 
$$\alpha_{pm} = ap^2 - a = a(p^2 + 1)$$
  
 $\alpha_{sp} = a - -ap^2 = a(1+p^2)$   
 $pm = PS = SD$  and  $SD \parallel PM$ 

so SPMD is a rhombus,

(c) 
$$S(n): \sum_{r=1}^{n} \frac{1}{(4r-3)(4r+1)} = n$$

$$S(1): LHS = 1 = 1/5$$

Assume n = k: Le. S(k):  $\sum_{r=1}^{k} \frac{1}{(4k-3)(4k+1)} = k$ 

Prove 
$$n = k+1$$

1.2.  $S(k+1)$ :  $\sum_{r=1}^{k+1} \frac{1}{(4r-3)(4r+1)} = k+1$ 

$$LHS = k + 1$$

$$4k+1 \quad (4k+1)(4k+5)$$

$$= k(4k+5) + 1$$

$$(4k+1)(4k+5)$$

$$= 4h^2 + 5k + 1$$

$$= \frac{(4k+1)(4k+5)}{(4k+1)(k+1)}$$

$$= \frac{k+1}{4k+5} = RHS$$

i. If S(k) to stone, then S(k+1) to But S(1) to stone, so S(2) to stone whence S(3) to stone and so on for all positive integer values 898 of n

3 UNIT TRIAL SOLUTIONS,

34.6)  $H(0.4) \times B(x_2, y_1) + k:l = -3:1$   $\chi = k\chi_2 + l\chi_1 \Rightarrow -6 = -3\chi_2 + 1\times0$  $k+\ell$ 

 $12 = -3x_2 \Rightarrow x_2 = 4$   $y = ky_2 + ly_1 \Rightarrow 1 = -3y_2 + 1 \times 4$ k+l = -3+1

-2 = -3y2+4 =>y=2

-'. B(-4,2)

(d) Sem of roots 10-6

Product of roots to C

(i) Assume the roots are  $\alpha$ ,  $\alpha$ +

Then  $\alpha$ +  $\alpha$ +  $\alpha$ +  $\alpha$ +  $\alpha$ +  $\alpha$ +

But  $\alpha \times (\alpha + 2n) = C$ 

(-n-3)x(-n-3+2n)=c $-n^2+9=c$ 

so n2 = 9-c

(bxi) A sm (0-a)= Asmocoa - Acososma

-'. Acos & = 4 Asm & = 3

whence  $\alpha = + 4 \ln^{-1} \left( \frac{3}{4} \right) + A = 5$ 

1. 45m 0 - 3cos0 = 5 sm (0 - x)

where  $\alpha = +a_{-}^{-1}(3/4)$ 

(ii)  $55m(\theta-\alpha)=1$  $5m(\theta-\alpha)=1$ 

 $\theta - \propto = 11^{\circ}32', 168^{\circ}28'$ 

-'-0 = 11°32' + 36°52' = 48°24'

and  $\Theta = 168^{\circ}28' + 36^{\circ}51' = 205^{\circ}20'$ 

=) Landing area = 3000 x 2000

Area where hoop does not protrude

= 2800 x 1800

P(wm prize) = 2800 x 1800 3000 x 2000

= 0.84

(ii) Succe the roots are opposite in sign, the product must be nega

: c <0

but c= 9-n (above)

.: 9-n2<0 n2>9

- 77

\* n<-3, n>3

5. (a) Let p= probability of correctly (ii)  $\cos^2 x - \cos^4 x = \frac{1}{16}$ machined part = 0.98 ... Co, 4x = 8. -1 +1 9 = prob. of sucorrectly machined X = no. of correctly machined parts:  $P(X=r) = {}^{40}C_{1}(0.98)^{1}(0.02)^{40-r}$  $4x = \frac{\pi}{3}$   $4x = \frac{5\pi}{3}$ (i)  $P(X=38) = {}^{40}C_{38} (0.98)^{38} (0.02)^{2}$ (u) P(X > 38) = P(X = 38) + P(X = 39) + P(X = 40)  $= 0.1448 + {}^{4}G_{9}(98)^{39} \cdot 02 + {}^{40}G_{98}(98)$ = 0.954b) let f(x) = loge x + x - 4 x (i)  $f(3) = \ln 3 + 9 - 12 < 0$ f(4) = lu4 + 16-16 >0 - Poot exists between x=3, x=4 (i)  $f'(x) = \frac{1}{x} + 2x - 4$ Then x, = x - lux + x2 - 4x lu3.5 + 3.5 - 4x3.5 13.5 + 2x3.5 - 4 = 3.65/3 .. Better approximation. 5 x= 3.65 (c)(1) Con 4 x = Cos 2x2x = 2 cos 2x -/ = 2 Resize -17 -1 = 2 (4e0x 4 - 4cox x+1)-1

= 8 con 12 - 8 con 2 + L-1

= Nrm 41 - Contx 1 + 1

3 UNIT TRIAL SOLUTIONS, 200

$$\frac{16.(a)}{x} = 0$$

$$\ddot{y} = -10$$

(iii) 
$$v^{2} = 28 + 24x - 4x^{2}$$
  
 $\frac{1}{2}v^{2} = 14 + 12x - 2x^{2}$   
 $\frac{d}{dx}(\frac{1}{2}v^{2}) = 12 - 4x$ 

$$16.(a)$$
  $\ddot{x} = 0$   $\ddot{y} = -10$   
 $\dot{x} = V\cos\alpha$   $\dot{y} = -10t + V\sin\alpha$   
 $x = Vt\cos\alpha$ ;  $y = -5t^2 + Vt\sin\alpha + 600$ 

$$\frac{1}{2} a = 12 - 4x$$

Also 
$$504 \text{ km/hr} = 140 \text{ m/s}$$
  
 $\dot{x} = 70\sqrt{3}$   $\dot{y} = -10t + 70$   
 $x = 70\sqrt{3}$   $\dot{y} = -5t^2 + 70t + 600$ 

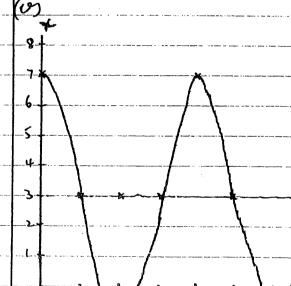
(w) 
$$a = -4(x-3)$$
  
=  $-2^{2}(x-3)$ 

(i) 
$$y=0 \Rightarrow -5t^2 + 70t + 600 = 0$$
  
 $-5(t^2 - 14t - 120) = 0$   
 $-5(t-20)(t+6) = 0$   
 $= )t = 20$  records

$$Pluod, T = 2\tau$$

$$= \tau Seconds$$

(ii) 
$$\dot{y} = 0 \Rightarrow -10t + 70 = 0$$
  
 $t = 7$   
At  $t = 7$ ,  $y = -5 \times 7^2 + 70 \times 7 + 600$   
 $= 845$  metres



iii) At 
$$t = 20$$
,  $\chi = 70\sqrt{3} \times 20$   
=  $2424.87$   
 $= 2.425$  kilometres

1) (i) 
$$v^{2} = 28 + 24 \times - 4 \times^{2}$$
  
 $4v = 0 \Rightarrow 28 + 24 \times - 4 \times^{2} = 0$   
 $4(7 + 6x - x^{2}) = 0$   
 $-4(x^{2} - 6x - 7) = 0$   
 $-4(x - 7)(x + 1) = 0$   
 $x = -1$  and  $x = 7$ 

Oscillates between x=-1, x=7

(i) mospout of motion is 
$$x = 3$$
.

- amplitude is  $4m$