

Q. 18 is 3 Unit Trial

$$(1) \frac{2.35 - 8.66}{6.5} = 0.2955289$$

$$= 0.30 \text{ (2 dec pt)}$$

$$(2) \frac{2.46}{5} = \frac{4x}{5}$$

$$2.46 - 4x = 0$$

$$5x - 2.46 = 0$$

$$\frac{2.46 - 5x}{5} = 0$$

$$2.46 - 5x = 0$$

$$(3) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$5x = 2.46 \Rightarrow x = 0.492$$

$$(4) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(5) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(6) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(7) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(8) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(9) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(10) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(11) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

$$(12) \frac{2.46 - 5x}{5} = 0 \Rightarrow 2.46 - 5x = 0$$

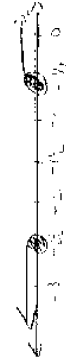
$$(1) 2x + 3 \geq 0$$

$$-2 \geq -3 \geq 2$$

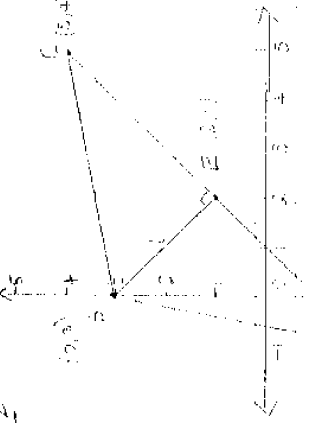
$$-5 \geq 2x \geq 5$$

$$-\frac{5}{2} \geq x \geq \frac{5}{2}$$

$$-2.5 \leq x \leq 2.5$$



Q. 2



$$(1) E = \left(\frac{-1+5}{2}, \frac{-2+4}{2} \right)$$

$$= (2, 1)$$

$$(2) \text{m of AC} = \frac{4-2}{3-0} = \frac{2}{3}$$

$$= \frac{2}{3}$$

$$= \frac{2}{3}$$

$$= \frac{2}{3}$$

$$(1) \text{m of AC} = \frac{4-2}{3-0} = \frac{2}{3}$$

$$\text{Thus m of L} = -\frac{3}{2}$$

$$\text{Equation of L}$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = -\frac{3}{2}(x - 0)$$

$$y - 2 = -\frac{3}{2}x$$

$$y = -\frac{3}{2}x + 2$$

$$(2) E = (2, 1) \text{ If E lies}$$

$$\text{of L then E satisfies the}$$

$$\text{eqn}$$

$$\text{Subst E (2, 1) into } y = -\frac{3}{2}x + 2$$

$$1 = -\frac{3}{2}(2) + 2$$

$$-1 = -3 + 2$$

$$-1 = -1$$

$$\text{True, Thus E lies on L}$$

$$(3) \text{On diagram}$$

$$\text{Since } \triangle BEC \cong \triangle BEA$$

$$\text{BE is common}$$

$$\angle BEC = \angle BEA = 90^\circ$$

$$\text{AE} = \text{EC} \text{ (E is mid pt)}$$

$$\text{Thus } \triangle BEC \cong \triangle BEA \text{ (SAS)}$$

$$(4) \text{m of AC} = \frac{4-2}{3-0} = \frac{2}{3}$$

$$= \frac{2}{3}$$

$$= \frac{2}{3}$$

$$= \frac{2}{3}$$

$$= \frac{2}{3}$$

$$= \frac{2}{3}$$

$$(1) (x-2)^2 + (y-1)^2 = 7^2$$

$$\text{where } (h, k) \text{ is the centre}$$

$$\text{and } r = \text{radius}$$

$$h = 2$$

$$k = 1$$

$$r = 7$$

$$(x-2)^2 + (y-1)^2 = 49$$

Q. 3

$$(1) (1) y = (3x^2 + 5)^3$$

$$\frac{dy}{dx} = 3(3x^2 + 5)^2 \cdot 6x$$

$$= 18x(3x^2 + 5)^2$$

$$= 18x(3x^2 + 5)^2$$

$$(2) y = 3x \cos 2x$$

$$\frac{dy}{dx} = 3x \cdot -\sin 2x \cdot 2 +$$

$$3 \cos 2x \cdot 1$$

$$= -6x \sin 2x + 3 \cos 2x$$

$$= 3 \cos 2x - 6x \sin 2x$$

$$(3) y = \frac{e^{3x}}{x}$$

$$\frac{dy}{dx} = \frac{3e^{3x} \cdot x - e^{3x} \cdot 1}{x^2}$$

$$= \frac{3xe^{3x} - e^{3x}}{x^2}$$

$$= \frac{e^{3x}(3x - 1)}{x^2}$$

$$= \frac{e^{3x}(3x - 1)}{x^2}$$

$$= \frac{e^{3x}(3x - 1)}{x^2}$$

$$= \frac{e^{3x}(3x - 1)}{x^2}$$

(10) (i) $\int_0^{\pi} \sin 3x \, dx$

$= \left[-\frac{1}{3} \cos 3x \right]_0^{\pi}$

$= \left(-\frac{1}{3} \cos 3\left(\frac{\pi}{4}\right) \right) - \left(-\frac{1}{3} \cos 3(0) \right)$

$= \left(-\frac{1}{3} \cos \frac{3\pi}{4} \right) - \left(-\frac{1}{3} \right)$

$= \frac{1}{3\sqrt{2}} - \frac{1}{3}$

$= \frac{1 + \sqrt{2} - 1}{6}$

$= \frac{1 + \sqrt{2} - 1}{6}$

$= \frac{1 + \sqrt{2}}{6} = \frac{1}{3} \left(\frac{1 + \sqrt{2}}{2} \right)$

(ii) $\int_0^3 e^{2x+3} \, dx$

$= \left[\frac{e^{2x+3}}{2} \right]_0^3$

$= \frac{e^{2(3)+3}}{2} - \frac{e^{2(0)+3}}{2}$

$= \frac{e^9}{2} - \frac{e^3}{2} = \frac{1}{2} (e^9 - e^3)$

(i) $\int \frac{dx}{x^2+1}$

$= \tan^{-1} x + C$

Sol 4

(a) $u_3 = 7$
 $u_{10} = 42$

(i) $u_3 = a + 2d = 7$ — (1)
 $u_{10} = a + 9d = 42$ — (2)

(2) - (1)

$7d = 35$
 $d = 5$

Subst $d = 5$ into (1)

$a + 2(5) = 7$

$a + 10 = 7$

$a = -3$

Thus first term is -3 +
difference is 5

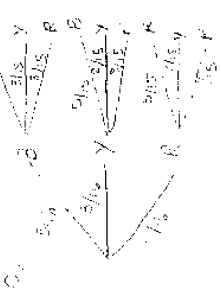
(ii) $S_n = \frac{n}{2} (a + l)$

$210 = \frac{10}{2} (-3 + 42)$

$= 5 (39)$

$= 195$

$\frac{10}{2} \times \frac{39}{2}$



$\therefore P(BB) = \frac{1}{5} \times \frac{1}{5} = \frac{1}{25}$

$P(\text{at most } 1B) = 1 - P(BB)$

$= 1 - \frac{1}{25}$

$= \frac{24}{25}$

(c) $y = 9 - x^2$
 $\frac{dy}{dx} = -2x$

(i) when $x = 0$
 $m = -2(0)$
 $= 0$

$y - y_1 = m(x - x_1)$
 $y - 9 = -2(x - 0)$
 $y - 9 = -2x$
 $2x + y = 9$

(ii) Subst $(5, 0)$ into (i)

$2(5) + 0 = 9$

$10 = 9$

$10 \neq 9$

True. Tangent

Passes through $(5, 0)$

OR

tangent crosses the x

axis at $y = 0$

$2x - 0 = 9$

$2x = 9$

$x = \frac{9}{2}$

the pt is $(\frac{9}{2}, 0)$

(iii) Required A = A of A - A of cur

$= \left(\frac{1}{2} \times 4 \times 8 \right) - \int_0^2 9 - x^2 \, dx$

$= 16 - \left[9x - \frac{x^3}{3} \right]_0^2$

$= 16 - \left[(9(2) - \frac{2^3}{3}) - (9(0) - \frac{0^3}{3}) \right]$

$= 16 - 9\frac{2}{3}$

$= 6\frac{2}{3} \text{ units}^2$

Sol 5

(a) (i) $\frac{ED}{\sin 41.29^\circ} = \frac{9.2}{\sin 58.71^\circ}$

$ED = \frac{9.2 \sin 41.29^\circ}{\sin 58.71^\circ}$

$\approx 6.7 \text{ cm}$

(ii) $\angle ABC = 180^\circ - (41.29^\circ + 58.71^\circ)$

$= 77.2^\circ$

A of A = $\frac{1}{2} \times 9.2 \times 7.4 \times \sin 77.2^\circ$

$= 35.3589 \approx 35.4 \text{ cm}^2$

$\approx 35 \text{ cm}^2$

(b) $y = 4x^3 + 6x^2$

(i) $\frac{dy}{dx} = 12x^2 + 12x$

$\frac{d^2y}{dx^2} = 24x + 12$

$\frac{d^3y}{dx^3} = 24$

$\frac{d^4y}{dx^4} = 0$

start pts occur when $\frac{dy}{dx} = 0$

$$2x' + 12x = 0$$

$$2x(x+1) = 0$$

$$2x=0 \text{ or } x+1=0$$

$$x=0, \quad x=-1$$

when $x=0$

$$y = 4(0)^2 + 6(0)^2 = 0$$

when $x=-1$

$$y = 4(-1)^2 + 6(-1)^2 = -4 + 6 = 2$$

The co-ordinates of start pts are $(0,0)$ & $(-1,2)$

Value of start: $\frac{dy}{dx} = 0$

$$\frac{dy}{dx} = 24(6) + 12 = 150 > 0 \quad \therefore \text{min}$$

when $x=-1$

$$\frac{dy}{dx} = 24(-1) + 12 = -12 < 0 \quad \therefore \text{max}$$

So $(0,0)$ is a min. pt
 & $(-1,2)$ is a max. pt

(ii) 2% of inferior when $\frac{d^2y}{dx^2} = 0$

$$24x + 12 = 0$$

$$12(2x+1) = 0$$

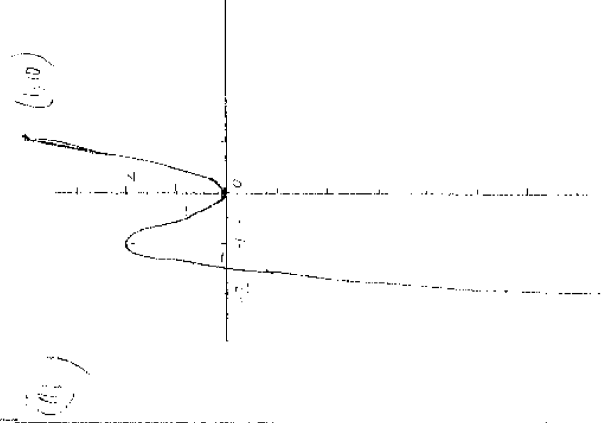
$$2x+1=0$$

$$2x = -1$$

$$x = -1/2$$

x	$\frac{dy}{dx}$	$\frac{d^2y}{dx^2}$
-1	-12	0
-1/2	0	12

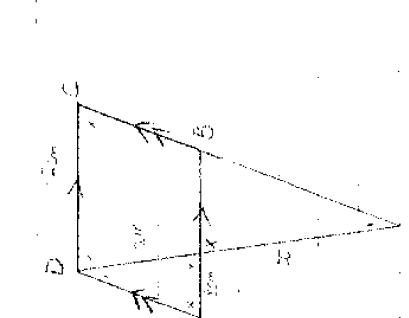
Concavity changes at the pt of inflection. Got the pt. where $x = -1/2$



(iii) The max value of $4x^3 + 6x^2$ in the domain $[-2, 2]$ is 10

Ques

(a) $\ln x = 2 \ln x$
 $x = x^2$
 $x^2 - x = 0$
 $x(x-1) = 0$
 $x = 0, 1$
 $x \neq 0$ thus $x = 1$ only



(ii) $\angle BDC = \angle DBC$ (alt. angles)
 $\angle DAC = \angle DCB$ (opp equal sides)
 Thus $\triangle DAC \cong \triangle DBC$ (3rd angle)
 So $\triangle DAC \cong \triangle DBC$ (equal sides)

$$\frac{1}{2} \times \frac{10}{10+1}$$

$$8(10+1) = 120$$

$$80+8x = 120$$

$$8x = 40$$

$$x = 5$$

(c) $\pi \int_0^5 (5y+5)^2 dy$

$$= \pi \int_0^5 (25y^2 + 50y + 25) dy$$

$$= \pi \left[\frac{25y^3}{3} + \frac{50y^2}{2} + 25y \right]_0^5$$

$$= \pi \left[\frac{25(5)^3}{3} + \frac{50(5)^2}{2} + 25(5) \right]$$

$$= \pi (625 + 625 + 625) = 1875\pi$$

Volume required is 1875π end

Q7

(i) $M = 2^{-2t} + 3$
 Initially $t=0$
 $M = 2^{-2(0)} + 3 = 1 + 3 = 4$

(ii) $\frac{dM}{dt} = -2e^{-2t}$
 $= -2e^{-2(0)} = -2$
 $\frac{dM}{dt} = -2$

(1) Length of Arc ABC = $\frac{1}{2} \times 4\pi \times \frac{15}{180}$

= $15 \times \frac{4\pi}{180}$

= 12π

Length AC = $15^2 + 15^2 = 150 \times \frac{4\pi}{180}$

= 38.53169549

Thus total perimeter is $12\pi + 38.5 = 66.23$

(2) (i) $S = \frac{D}{T}$

$6 = \frac{\sqrt{64x^2}}{T}$

$T = \frac{\sqrt{64x^2}}{6}$

(ii) SC = $10 - x$
 carrying speed from base to 10 km

$\frac{D}{T} = \frac{D}{T}$

$10 = \frac{10-x}{T}$

$T = \frac{10-x}{10}$

Thus total time taken for length house to travel here is $\frac{\sqrt{64x^2}}{6} + \frac{10-x}{10}$

(1) $T = \frac{\sqrt{36+x^2} + 10-x}{6}$

$T = \frac{(36+x^2)^{1/2} + 10-x}{6}$

$\frac{dT}{dx} = \frac{1}{2} \times \frac{1}{\sqrt{36+x^2}} - \frac{1}{10}$

= $\frac{x}{6\sqrt{36+x^2}} - \frac{1}{10}$

= $\frac{x}{6\sqrt{36+x^2}} - \frac{1}{10}$

minimum occurs when $\frac{dT}{dx} = 0$

$\frac{x}{6\sqrt{36+x^2}} - \frac{1}{10} = 0$

$\frac{x}{6\sqrt{36+x^2}} = \frac{1}{10}$

$\frac{x}{6\sqrt{36+x^2}} = \frac{1}{10}$

$10x = 6\sqrt{36+x^2}$

$100x^2 = 36(36+x^2)$

$100x^2 = 36^2 + 36x^2$

$100x^2 - 36x^2 = 36^2$

$\frac{64x^2}{64} = \frac{36^2}{64}$

$x = \frac{\sqrt{36^2}}{\sqrt{64}}$

= $\frac{36}{8}$

= 4.5

(11) quickest time when

$T = \frac{\sqrt{36+x^2} + 10-x}{6}$

when $x = 4.5$

$T = \frac{\sqrt{36+(4.5)^2} + 10-4.5}{6}$

= $\frac{\sqrt{36+20.25} + 5.5}{6}$

= $\frac{15.6 + 5.5}{6}$

= $\frac{21.1}{6}$

= 3.5166

= $1 \text{ hr } 48 \text{ mins}$

= $1 \text{ hr } 48 \text{ mins}$

Sum (11) 10 = 10 (equal roads)

Then $\angle FPO = 100 \text{ degrees}$

$\angle OAP = \angle OPA \text{ equal}$

From ΔOAP $\angle OAP = 20^\circ$

From $\Delta OAP - \angle OPA = 20^\circ$

(11) $5 = 22 = \frac{516}{1000}$

$\frac{516}{1000} = \frac{13}{25}$

$\frac{13}{25} = \frac{13}{25}$

$\frac{13}{25} = \frac{13}{25}$

$\frac{13}{25} = \frac{13}{25}$

$\frac{13}{25} = \frac{13}{25}$

(12) ΔPAB , $\sin x = \frac{PB}{AB}$

$\cos x = \frac{AP}{AB}$

$\sin x = \frac{PB}{AB}$

$\cos x = \frac{AP}{AB}$

$\sin x = \frac{PB}{AB}$

$\cos x = \frac{AP}{AB}$

$\sin x = \frac{PB}{AB}$

$\cos x = \frac{AP}{AB}$

$\sin x = \frac{PB}{AB}$

$\cos x = \frac{AP}{AB}$

(13)

$\frac{4}{5} \text{ km}$

$\frac{4}{5} \text{ km}$

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$\frac{4}{5} \text{ km}$

$\frac{4}{5} \text{ km}$

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$\frac{4}{5} \text{ km}$

$\frac{4}{5} \text{ km}$

$\frac{4}{5} \text{ km}$

$$= \frac{5}{36} + \left[\frac{5}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6} \right]$$

$$= \frac{5}{36} + \frac{5^3}{6^4}$$

$$(11) \quad P(LW) = P(X=1) \times P(Y=1) \text{ or } P(X=1) \times P(Y=2) \\ P(X=1) \times P(Y=1) \text{ or } P(X=1) \times P(Y=2) \\ P\left(\frac{1}{6}\right) \times P\left(\frac{1}{6}\right) \times P\left(\frac{1}{6}\right) \times$$

$$= \left(\frac{5}{6} \times \frac{1}{6}\right) + \left(\frac{5}{6} \times \frac{5}{6} \times \frac{1}{6}\right) + \left(\frac{5}{6} \times \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6}\right)$$

$$= \left(\frac{5}{6} \times \frac{1}{6}\right) + \left(\frac{5^2}{6^2} \times \frac{1}{6}\right) + \left(\frac{5^3}{6^3} \times \frac{1}{6}\right)$$

$$S_{\infty} = \frac{a}{1-r} \quad a = \frac{5}{6} \times \frac{1}{6}$$

$$= \frac{5}{6} \times \frac{1}{6} \quad r = \frac{5}{6}$$

$$= \frac{\frac{5}{6} \times \frac{1}{6}}{1 - \frac{5}{6}}$$

$$= \frac{5}{36} + \frac{1}{36}$$

$$= \frac{5}{36} + \frac{1}{36}$$