

STANDARD INTEGRALS

$\int x^n dx$	$= \frac{1}{n+1} x^{n+1}, n \neq -1; x \neq 0, \text{ if } n < 0$
$\int \frac{1}{x} dx$	$= \ln x, x > 0$
$\int e^{ax} dx$	$= \frac{1}{a} e^{ax}, a \neq 0$
$\int \sin ax dx$	$= -\frac{1}{a} \cos ax, a \neq 0$
$\int \cos ax dx$	$= \frac{1}{a} \sin ax, a \neq 0$
$\int \sec^2 ax dx$	$= \frac{1}{a} \tan ax, a \neq 0$
$\int \sec ax \tan ax dx$	$= \frac{1}{a} \sec ax, a \neq 0$
$\int \frac{1}{a^2 + x^2} dx$	$= \frac{1}{a} \tan^{-1} \frac{x}{a}, a \neq 0$
$\int \frac{1}{\sqrt{a^2 - x^2}} dx$	$= \sin^{-1} \frac{x}{a}, a > 0, a < x < a$
$\int \frac{1}{\sqrt{x^2 - a^2}} dx$	$= \ln \left(x + \sqrt{x^2 - a^2} \right), x > a > 0$
$\int \frac{1}{\sqrt{x^2 + a^2}} dx$	$= \ln \left(x + \sqrt{x^2 + a^2} \right)$

NOTE: $\ln x = \log_e x, x > 0$

HSC TRIAL EXAMINATION PAPER 2001 SOLUTIONS + MAPPING GRID MATHEMATICS - EXTENSION I

QUESTION 1

(a) $\lim_{x \rightarrow 0} \frac{\sin 3x}{x} = \lim_{x \rightarrow 0} \frac{3 \sin 3x}{3x} = 3$

(1 mark)

(b) Since $x-2$ is a factor $\therefore P(2)=0$

$\therefore P(2)=8p+20-3p=0 \therefore p=-4$
(2 marks)

(c) $y = x \tan^{-1} x$

Using product rule:

Let $u = x \quad v = \tan^{-1} x$

$\therefore u' = 1 \quad v' = \frac{1}{1+x^2}$

$\therefore \frac{dy}{dx} = \tan^{-1} x + \frac{x}{1+x^2}$ (2 marks)

(d) $y = \ln(2x+1) \therefore \frac{dy}{dx} = \frac{2}{2x+1}$

At $x=0, \frac{dy}{dx} = 2$

At $x = \frac{1}{2}, \frac{dy}{dx} = 1$

$\therefore \tan \alpha = \left| \frac{2-1}{1+2 \times 1} \right| = \frac{1}{3}$

$\therefore \alpha = 18^\circ 26'$ (to nearest minute).
(2 marks)

(e) $\int_0^{\frac{1}{6}} \frac{9 dx}{\sqrt{1-9x^2}} = \frac{1}{3} \int_0^{\frac{1}{6}} \frac{9 dx}{\sqrt{1-x^2}}$

$= \int_0^{\frac{1}{6}} \frac{3 dx}{\sqrt{1-x^2}} = 3 [\sin^{-1} x]_0^{\frac{1}{6}}$

$= 3 \left[\frac{\pi}{6} - 0 \right] = \frac{\pi}{2}$
(3 marks)

(f) $\frac{1}{x} > \frac{1}{x+2}$

$\therefore \frac{1}{x} - \frac{1}{x+2} > 0 \therefore \frac{2}{x(x+2)} > 0$

$\frac{x}{x(x+2)}$	+	-	+
$\frac{-2}{x(x+2)}$	+	-	+

\therefore Solution is $x < -2$ or $x > 0$.

QUESTION 2

(a) Arrangements = $\frac{8!}{2!} = 280$

(we divide by $2!$, $2!$ & $4!$)

because the red, blue & green are

identical.

(2 marks)

(b) $\sin 2\theta = 2 \cos^2 \theta, 0 \leq \theta \leq 2\pi$

$2 \sin \theta \cos \theta = 2 \cos^2 \theta$

$\cos \theta (\sin \theta - \cos \theta) = 0$

$\therefore \cos \theta = 0, \sin \theta = \cos \theta$

$\therefore \cos \theta = \cos \frac{\pi}{2}$

$\therefore \theta = \frac{\pi}{2} + 2k\pi \text{ or } \theta = -\frac{\pi}{2} + 2k\pi$
for $k=0, \theta = \frac{\pi}{2}$ for $k=1, \theta = \frac{3\pi}{2}$

$\sin \theta = \cos \theta$

$\therefore \tan \theta = \tan \frac{\pi}{4}$

$\therefore \theta = \frac{\pi}{4} + k\pi$

for $k=0, \theta = \frac{\pi}{4}$

for $k=1, \theta = 5\frac{\pi}{4}$

\therefore Solutions are $\theta = \frac{\pi}{4}, \frac{\pi}{2}, 5\frac{\pi}{4}, \frac{3\pi}{2}$
in the domain $0 \leq \theta \leq 2\pi$ (3 marks)

(c) $\int_0^{\frac{\pi}{2}} \frac{\cos x dx}{\sqrt{1+3 \sin x}}$ Let $u = 3 \sin x$
 $\therefore \cos x dx = \frac{du}{3}$
for $x=0, u=0$
for $x=\frac{\pi}{2}, u=3$

$= \frac{1}{3} \int_0^3 \frac{du}{\sqrt{1+u}}$

$= \frac{1}{3} \int_0^3 (1+u)^{-\frac{1}{2}} du = \frac{1}{3} [2\sqrt{1+u}]_0^3$
 $= \frac{2}{3} [2-1] = \frac{2}{3}$
(3 marks)

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(d)(i) $\frac{dy}{dx} = 2(x-1)$ (gradient function)

at $x=t+1$, $m_{\tan} = 2t$

Using gradient point formula

$y - t^2 = 2t(x - t - 1)$

$\therefore y - t^2 = 2tx - 2t^2 - 2t$

$\therefore y = 2tx - t^2 - 2t$ (2 marks)

(ii) Let $x=1$ in (i) to find C

$y = 2t - t^2 - 2t = -t^2 \therefore C(1, -t^2)$

Let $y=0$ in (i) to find B

$2tx = t^2 + 2t \therefore x = \frac{t+2}{2}$

$\therefore B$ is $(\frac{t+2}{2}, 0)$

$\therefore M_{AC} = (\frac{t+1}{2}, -\frac{t^2+t^2}{2})$

$= (\frac{t+2}{2}, 0)$

$\therefore B$ is mid-point of AC (2 marks)

Question 3

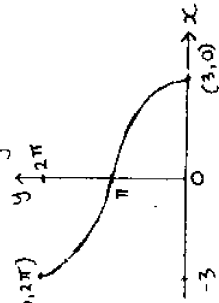
(a)(i) $y = 2 \cos^{-1} \frac{x}{3}$

Domain: $-1 \leq \frac{x}{3} \leq 1 \therefore -3 \leq x \leq 3$

(1 mark)

(ii) Range: $0 \leq \cos^{-1} \frac{x}{3} \leq \pi$

$\therefore 0 \leq y \leq 2\pi$



(2 marks)

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(iii) $y = 2 \cos^{-1} \frac{x}{3}$

$\therefore \frac{dy}{dx} = \frac{2/3}{\sqrt{1 - \frac{x^2}{9}}}$

At $x=0$, $m_{\tan} = 2/3$ (1 mark)

(b)(i) $v^2 = -7 + 8x - x^2$

$\therefore \frac{1}{2} v^2 = -\frac{7}{2} + 4x - \frac{x^2}{2}$

$\therefore \frac{d(\frac{1}{2} v^2)}{dx} = 4 - x$

\therefore Acceleration: $a = 4 - x$ (2 marks)

(ii) $a = -(x - 4)$

\therefore Acceleration is proportional to

displacement but negative (i.e.

directed towards the centre)

\therefore Motion is simple harmonic,

centred at $x=4$.

To find amplitude, let $v=0$.

$\therefore x^2 - 8x + 7 = 0 \therefore x=7$ or $x=1$

\therefore Particle is oscillating between

$x=1$ & $x=7$.

\therefore Amplitude = 3 (2 marks)

(iii) Maximum speed occurs when

$a=0$ (i.e. when $x=4$)

$\therefore v^2 = -7 + 32 - 16 = 9 \therefore v=3 \text{ m/s}$ (1 mark)

(c) Considering term T_{n+1}

$\therefore T_{n+1} = 8 C_r \left(\frac{x}{2}\right)^{8-r} \left(\frac{2}{x^2}\right)^r$

$= 8 C_r \cdot \frac{x^{32-4r}}{2^{8-r}} \cdot \frac{2^r}{x^{2r}}$

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$= 8 C_r \cdot 2^{2r-8} \cdot x^{32-6r}$

To get coefficient of x^2 we let

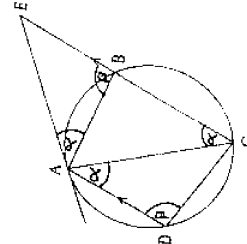
$32 - 6r = 2 \therefore r = 5$

\therefore Coefficient of $x^2 = 8 C_5 \cdot 2^2 = 224$

(3 marks)

Question 4

(a)



Data: ABCD is a cyclic quadrilateral

AD || BC

Aim: Prove that: (i) $\triangle ABE \sim \triangle ADC$

(ii) $AE \times DC = AC \times BE$

Construction: Figure

Proof: (i) Let $\angle EAB = \alpha$

$\therefore \angle ACB = \alpha$ (angle in alternate segment)

$\therefore \angle DAC = \alpha$ (alternate angles, AD || BC)

Let $\angle ABE = \beta$

$\therefore \angle CDA = \beta$ (exterior angle of cyclic

quadrilateral equals opposite interior

angle)

$\angle ACD = \angle AEB$ (remaining angles)

$\therefore \triangle ACD \sim \triangle AEB$ (equiangular).

(3 marks)

(ii) Since $\triangle ADC \sim \triangle ABE$ are

similar, their corresponding sides

are in the same ratio.

Ratio of sides: $\frac{AE}{AC} = \frac{BE}{DC}$

$\therefore AE \times DC = BE \times AC$ (1 mark)

(b)(i) Product of roots: $\sqrt{p} \times \frac{1}{\sqrt{p}} \times \alpha = -\frac{c}{A}$

$\therefore \alpha = -\frac{c}{A}$ (1 mark)

(ii) Sum of roots: $\frac{1}{\sqrt{p}} + \sqrt{p} + \alpha = -\frac{B}{A}$

$\therefore \sqrt{p} + \frac{1}{\sqrt{p}} = \frac{c-B}{A}$ (2)

Sum of roots 2 at a time:

$(\sqrt{p} \times \frac{1}{\sqrt{p}}) + \alpha \sqrt{p} + \frac{\alpha}{\sqrt{p}} = 2$

$\therefore 1 + \alpha(\sqrt{p} + \frac{1}{\sqrt{p}}) = 2$

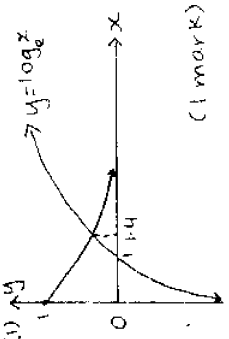
$\therefore \alpha(\sqrt{p} + \frac{1}{\sqrt{p}}) = 1$ (3)

Sub (2) & (1) in (3)

$\therefore -\frac{c}{A} \cdot \frac{c-B}{A} = 1$

$\therefore -c^2 + BC = A^2 \therefore A^2 + C^2 = BC$ (2 marks)

(c)(i) $y = \log_e x$



(1 mark)

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(ii) From the graph, we can see that

the curves $y = e^x$ & $y = \log_e x$

intersect near $x = 1.4$.

The equation $e^x = \log_e x$ C.i.e.

$e^x - \log_e x = 0$ has a root close to

$x = 1.4$. (1 mark)

(iii) Let $h(x) = e^x - \log_e x$

$\therefore h'(x) = e^x - \frac{1}{x}$

$\therefore h(1.4) = e^{1.4} - \log_e 1.4 = 0.08975272$

$\therefore h'(1.4) = e^{1.4} - \frac{1}{1.4} = 0.960882678$

$\therefore x_2 = 1.4 - \frac{h(1.4)}{h'(1.4)} = 1.306465925$

$\therefore h(1.306465925) = 3.4495834 \times 10^{-3}$

$\therefore x = 1.306465925$ is a better

approximation of the root. (2 marks)

Question 5

(a) (i) All real numbers except $x = 0$

(1 mark)

(ii) $f'(x) = \frac{e^x(e^x - 1) - e^{2x}}{(e^x - 1)^2}$

$= \frac{-e^x}{(e^x - 1)^2}$ (gradient function).

Since $e^x > 0$ for all x & denominator

is a perfect square greater than 0

$\therefore f'(x) < 0$ for all x (2 marks)

(iii) When $x \rightarrow +\infty$, $y = \frac{e^x}{e^x} \rightarrow 1$

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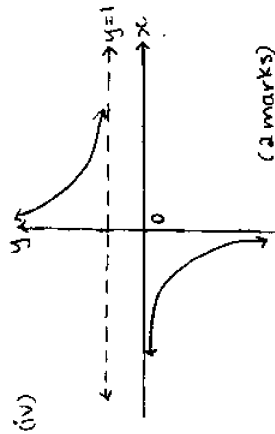
$\therefore y = 1$ is a horizontal asymptote

When $x \rightarrow -\infty$, $y = \frac{0}{1} \rightarrow 0$ (i.e. $e^{-\infty} = 0$)

$\therefore y = 0$ is a horizontal asymptote

When $x \rightarrow 0$, $y = \frac{1}{0} \rightarrow \pm \infty$

$\therefore x = 0$ is a vertical asymptote (2 marks)



(2 marks)

(v) Since $f(x)$ is a one-one function

(i.e. for every x , there is only one

y -value & vice versa).

\therefore It has an inverse function (1 mark)

(vi) By interchanging x & y :

$$x = \frac{e^y}{e^y - 1} \rightarrow \therefore e^y - x = e^y$$

$$\therefore e^y = \frac{x}{x-1}$$

$$\therefore \log_e e^y = \log_e \frac{x}{x-1}$$

$$\therefore y = \log_e \frac{x}{x-1} \quad (1 \text{ mark})$$

$$(b) (i) P(\text{ace}) = \frac{3}{10} \quad P(\text{no ace}) = \frac{7}{10}$$

$$\therefore P(\text{one ace}) = {}^6C_1 \left(\frac{3}{10}\right) \left(\frac{7}{10}\right)^5$$

$$= 0.302526 \quad (1 \text{ mark})$$

$$(ii) P(\text{at least 2 aces}) = 1 - P(\text{no ace}) - P(\text{ace})$$

$$= 1 - {}^6C_0 \left(\frac{3}{10}\right)^0 \left(\frac{7}{10}\right)^6 - {}^6C_1 \left(\frac{3}{10}\right) \left(\frac{7}{10}\right)^5$$

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$$= 1 - 0.117649 - 0.302526$$

$$= 0.579825 \quad (1 \text{ mark})$$

(iii) He has to serve ace, no ace, no ace,

no ace, no ace, ace in this order.

$$P = \left(\frac{3}{10}\right)^2 \left(\frac{7}{10}\right)^4 = 0.021609 \quad (1 \text{ mark})$$

Question 6

(a) Step 1: For $n = 1$, $3.2! = 1(1+2)!$

$\therefore 6 = 6$ Hence statement is true

for $n = 1$.

Step 2: Assume that the statement

is true for $n = k$

$$3.2! + 7.3! + \dots + (k^2 + k + 1)(k+1)!$$

$$= k(k+2)! \quad \text{①}$$

Our aim is to prove it true for $n = k+1$

$$\text{i.e. } 3.2! + 7.3! + \dots + [(k+1)^2 + k + 2](k+2)!$$

$$= (k+1)(k+3)!$$

Starting from ① and adding

$$[(k+1)^2 + k + 2](k+2)! \text{ to both sides:}$$

$$3.2! + 7.3! + \dots + [(k+1)^2 + k + 2](k+2)!$$

$$= k(k+2)! + [(k+1)^2 + k + 2](k+2)!$$

$$\therefore \text{LHS} = [k^2 + 4k + 3](k+2)! \quad (\text{factorizing})$$

$$= (k+1)(k+3)(k+2)!$$

$$= (k+1)(k+3)! \quad (\text{Since } (k+2)! =$$

$$(k+2)! \times (k+3).$$

Hence if the statement is true for

$n = k$, it is also true for $n = k+1$.

Step 3: If the statement is true

for $n = 1$ & so it is true for $n = 2$

& so on. Hence it is true for all

$n \geq 1$. (3 marks)

$$(b) (i) \frac{d(\frac{1}{2}v^2)}{dx} = -e^{-x} - e^{-2x}$$

$$\therefore \frac{1}{2}v^2 = \int (-e^{-x} - e^{-2x}) dx$$

$$\therefore \frac{1}{2}v^2 = e^{-x} + \frac{1}{2}e^{-2x} + c$$

When $x = 0$, $v = 2$

$$\therefore 2 = 1 + \frac{1}{2} + c \quad \therefore c = \frac{1}{2}$$

$$\therefore \frac{1}{2}v^2 = \frac{1}{2}e^{-2x} + e^{-x} + \frac{1}{2}$$

$$\therefore v^2 = e^{-2x} + 2e^{-x} + 1$$

$$\therefore v = (e^{-x} + 1)^2 \quad \therefore v = \pm (e^{-x} + 1)$$

Since when $x = 0$, $v = 2$ (positive)

\therefore Positive solution only is accepted.

$$\therefore v = e^{-x} + 1 \quad (3 \text{ marks})$$

$$(ii) \frac{dx}{dt} = e^{-x} + 1 \Rightarrow \frac{1 + e^x}{e^x}$$

$$\therefore \int dt = \int \frac{e^x dx}{1 + e^x} \quad \therefore t = \ln(e^x + 1) + d$$

When $t = 0$, $x = 0$

$$\therefore 0 = \ln 2 + d \quad \therefore d = -\ln 2$$

$$\therefore t = \ln(e^x + 1) - \ln 2 = \ln\left(\frac{e^x + 1}{2}\right) \quad \text{①}$$

$$v = \frac{1}{2}, \quad e^{-x} + 1 = \frac{1}{2} \quad \therefore \frac{1}{e^x} = \frac{1}{2}$$

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$$\therefore x^2 = 2 \quad \text{Sub in (i)}$$

$$\therefore t = \ln \frac{3}{2} \text{ seconds}$$

\therefore It will take the particle $\ln \frac{3}{2}$

seconds to drop its velocity to

1.5 m/s. (2 marks)

$$(c)(i) V = \pi \int x^2 dy \quad y = \sin^{-1} x$$

$$\therefore \sin y = x \quad \therefore x^2 = \sin^2 y$$

$$\text{as } \cos 2y = 1 - 2\sin^2 y \quad \therefore \sin^2 y = \frac{1}{2}(1 - \cos 2y)$$

$$\therefore x^2 = \frac{1}{2}(1 - \cos 2y)$$

$$\therefore V = \frac{\pi}{2} \int_0^h (1 - \cos 2y) dy$$

$$= \frac{\pi}{2} \left[y - \frac{1}{2} \sin 2y \right]_0^h$$

$$= \frac{\pi}{2} \left[(h - \frac{1}{2} \sin 2h) - 0 \right]$$

$$= \frac{\pi}{4} (2h - \sin 2h) \quad (2 \text{ marks})$$

$$(ii) \frac{dV}{dt} = \frac{dV}{dh} \cdot \frac{dh}{dt}$$

$$V = \frac{\pi}{4} (2h - \sin 2h) \quad \therefore \frac{dV}{dh} = \frac{\pi}{4} (2 - 2\cos 2h)$$

$$= \frac{\pi}{2} (1 - \cos 2h)$$

$$\therefore 2 = \frac{\pi}{2} (1 - \cos 2h) \cdot \frac{dh}{dt}$$

$$\therefore \frac{dh}{dt} = \frac{4}{\pi(1 - \cos 2h)} \quad (\text{rate at any depth})$$

$$\text{when } h = \frac{\pi}{4}, \frac{dh}{dt} = \frac{4}{\pi(1 - 0)} = \frac{4}{\pi} \text{ cm/s}$$

$$(2 \text{ marks})$$

QUESTION 7

$$(a)(i) y = -gt + v \sin \alpha$$

At maximum height, $y = 0$ (vertical

component) $\therefore 0 = v \sin \alpha \quad \therefore t = \frac{v \sin \alpha}{g}$

Substitute in y , we get:

$$\therefore y_{\max} = -\frac{1}{2}g \times \left(\frac{v \sin \alpha}{g}\right)^2 + v \sin \alpha \times \frac{v \sin \alpha}{g}$$

$$\therefore 8h = -\frac{v^2 \sin^2 \alpha}{2g} + \frac{v^2 \sin^2 \alpha}{g}$$

$$\therefore 8h = \frac{v^2 \sin^2 \alpha}{2g} \quad \therefore v^2 \sin^2 \alpha = 6gh$$

$\therefore v \sin \alpha = \sqrt{6gh}$ (since initial vertical

component is positive). (2 marks)

$$(ii) \text{ Let } y = 0 \quad \therefore -\frac{1}{2}gt^2 + v \sin \alpha t = 0$$

$$\therefore t(-\frac{gt}{2} + v \sin \alpha) = 0 \quad \therefore t = 0 \text{ (initial$$

time) or $t = \frac{2v \sin \alpha}{g}$ (time to return to

x -axis if it didn't strike plane at Q).

$$\therefore d = v \cos \alpha \times \frac{2v \sin \alpha}{g} = \frac{2v^2 \sin \alpha \cos \alpha}{g}$$

$$\therefore v \cos \alpha = \frac{gd}{2\sqrt{6gh}} \quad (2 \text{ marks})$$

$$(iii) x = v \cos \alpha t \quad \therefore t = \frac{x}{v \cos \alpha} = \frac{2x\sqrt{6gh}}{gd}$$

$$\therefore y = -\frac{1}{2}g \times \left(\frac{2x\sqrt{6gh}}{gd}\right)^2 + \sqrt{6gh} \times \frac{2x\sqrt{6gh}}{gd}$$

$$\therefore y = -\frac{1}{2}g \times \frac{4x^2 \times 6gh}{g^2 d^2} + \frac{12x\sqrt{6gh}}{gd}$$

$$\therefore y = -\frac{12x^2 h}{d^2} + \frac{12x\sqrt{6gh}}{d} = \frac{12xh}{d} \left(1 - \frac{x}{d}\right)$$

(2 marks)

(iv) The rocket will strike the plane at

Q when $y = h$.

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$$\therefore h = \frac{12xh}{d} \left(1 - \frac{x}{d}\right)$$

$$\therefore 1 = \frac{12x}{d} \left(1 - \frac{x}{d}\right)$$

$$\therefore d = 12x - \frac{12x^2}{d}$$

$$\therefore d^2 - 12xd + 12x^2 = 0$$

$$\therefore 12x^2 - 12dx + d^2 = 0$$

$$\therefore x = \frac{12d \pm \sqrt{144d^2 - 48d^2}}{24}$$

$$\therefore x = \frac{3d \pm d\sqrt{6}}{6} \quad \therefore x_Q = \frac{3d + d\sqrt{6}}{6}$$

Time taken by rocket to reach Q (s):

$$x = v \cos \alpha t$$

$$\therefore \frac{3d + d\sqrt{6}}{6} = 100(3 + \sqrt{6})t$$

$$\therefore t = \frac{d}{600} \quad (2 \text{ marks})$$

(v) The distance travelled by the plane

from P to Q is:

$$\frac{3d + d\sqrt{6}}{6} - \frac{3d - d\sqrt{6}}{6} = \frac{d\sqrt{6}}{3}$$

Time taken for plane to travel from P

to Q is the same time taken by rocket

to reach Q . $\therefore t = d/600$

$$\therefore u = \frac{d\sqrt{6}}{3} \times \frac{600}{d} = 200\sqrt{6} \text{ m/s}$$

(1 mark)

$$(b)(i) (1+x)^{2n+1} = {}^{2n+1}C_0 + {}^{2n+1}C_1 x^1 + \dots$$

$$+ {}^{2n+1}C_n x^n + {}^{2n+1}C_{n+1} x^{n+1} + \dots + {}^{2n+1}C_{2n} x^{2n}$$

$$+ {}^{2n+1}C_{2n+1} x^{2n+1}$$

For $x=1$:

$$2^{2n+1} = {}^{2n+1}C_0 + {}^{2n+1}C_1 + \dots + {}^{2n+1}C_n + {}^{2n+1}C_{n+1} + \dots + {}^{2n+1}C_{2n} + {}^{2n+1}C_{2n+1}$$

Using ${}^nC_r = {}^nC_{n-r}$

$$\therefore {}^{2n+1}C_n = {}^{2n+1}C_{2n+1-n}$$

$$\text{Also, } {}^{2n+1}C_0 = {}^{2n+1}C_{2n+1}$$

$$\therefore {}^{2n+1}C_1 = {}^{2n+1}C_{2n}$$

$$\therefore 2^{2n+1} = 2({}^{2n+1}C_0 + {}^{2n+1}C_1 + \dots + {}^{2n+1}C_n)$$

$$\therefore 2^{2n} - 1 = {}^{2n+1}C_1 + {}^{2n+1}C_2 + \dots + {}^{2n+1}C_n$$

$$\therefore (n-2)!(2^{2n}-1) = (n-2)!({}^{2n+1}C_1 + \dots + (n-2)!({}^{2n+1}C_n)$$

$$(ii) (n-2)!({}^{2n+1}C_1 + \dots + (n-2)!({}^{2n+1}C_n) > 1000000$$

$$\therefore (n-2)!(2^{2n}-1) > 1000000$$

By calculator, for $n=6$: 98280

for $n=7$: 1965960

$\therefore n=7$ is the smallest positive integer.

(1 mark)