Western Region

2009

TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

Mathematics

Solutions

	Solutions	Marks/Comments
Question 1		
(a)Let $x = 0.53131$.	or $3 \cdot 5 \dot{3} \dot{1} = 5 + \frac{5}{10} + \frac{31}{1000} + \frac{31}{100000} \dots$	2 marks – 1 for correct method 1 correct answer
$10x = 5 \cdot 3131$	Limiting Sum $\frac{31}{1000} + \frac{31}{100000} + \frac{31}{10000000} \dots$	
$100x = 53 \cdot 1313$	$a = \frac{31}{1000} \qquad S_{\infty} = \frac{a}{1 - r}$	
1000x = 531.3131	31	
990 x = 526	$r = \frac{1}{100} = \frac{\frac{31}{1000}}{1 - \frac{1}{100}}$	
$x = \frac{526}{990} = \frac{263}{495}$	$=\frac{31}{1000} \div \frac{99}{100}$	
$\therefore \ 3 \cdot 531 = \ 3 \frac{263}{495}$	$=\frac{31}{990}$	
	$\therefore 3 \cdot 531 = 3 + \frac{5}{10} + \frac{31}{990} = 3\frac{263}{495}$	
(b)	$x^{2} = 7^{2} + 8^{2}$ $= 49 + 64$ $= 113$ Since $\tan \theta = \frac{7}{8} \text{ and } \cos \theta < 0$ $3^{\text{rd}} \text{ Quadrant } \therefore \csc \theta < 0$	
7 x	$x = \sqrt{113}$	1 Mark – Correct Answer
	$\therefore cosec \ \theta = -\frac{\sqrt{113}}{7}$	
8		
(c) $\frac{3 \cdot 24^2 - 2 \cdot 1^2}{\sqrt{36 + 2 \cdot 1}} = 0.9$	86242288	1 Mark – Correct rounded
= 0.9	286	answer
(d) $ 15 - 4x \le 3$ $15 - 4x \le 3$ or 1	5 An > 2	
· · · · · · · · · · · · · · · · · · ·	$3 - 4x \ge -3$ $-4x \ge -18$	
$x \ge 3$ or	$x \le 4\frac{1}{2}$	2 Marks – 1 for each solution
(e) $k = \frac{1}{3}m(v^2 -$	u^2)	2 Marks – 1 for substitution
$724 = \frac{1}{3}m(14\cdot 2)$	$^{2}-7.4^{2}$)	- 1 for answer

$$2172 = m(146.88)$$

$$m = \frac{2172}{146.88} = 14.7875817$$

$$= 14.8 \quad (3sf)$$

(f)
$$3y = \sin\left(2x - \frac{\pi}{4}\right)$$

 $y = \frac{1}{3}\sin\left(2x - \frac{\pi}{4}\right)$

2 marks - 1 for period 1 for amplitude

$$\therefore \text{ amplitude } = \frac{1}{3} \qquad \text{ period } = \frac{2\pi}{2} = \pi$$

(g)
$$130\% = \$67.50$$

 $1\% = \frac{67.50}{130} = 0.51923.....$

2 Marks - 1 for 1% 1 for Cost price

Cost Price =
$$\frac{67.50}{130} \times 100 = $51.92$$

Solutions	Marks/Comments
Question 2	
(a) $x - 2y + 9 = 0$ (1)	
4x - y - 20 = 0(2)	
From (2)	2 marks – 1 for method
y = 4x - 20(3)	1 for correct answer
Sub (3) into (1) B is the point (7, 8)	
x - 2(4x - 20) + 9 = 0	
$ \begin{array}{r} x - 8x + 40 + 9 = 0 \\ -7x = -49 \end{array} $	
-7x = -49 $x = 7$	
Hence $y = 8$	
Thence $y = \delta$	
(b) $m(AC) = \frac{4\frac{1}{2} - 0}{0 - 5}$ = $-\frac{9}{10}$	
(0) $m(AC) = 0.5$	
$=-\frac{7}{10}$	2 marks – 1 for gradient
$y - y_1 = m (x - x_1)$	1 for equation
$y-0=-\frac{9}{10}(x-5)$	1 for equation
10y = -9x + 45	
9x + 10y - 45 = 0	
(c) $AC = \sqrt{(0-5)^2 + (4\frac{1}{2} - 0)^2}$ = $\sqrt{(-5)^2 + (4\frac{1}{2})^2}$	
$(c) = \sqrt{(c-b) + (r_2 - b)}$	2 marks – 1 for substitution
$= \left (-5)^2 + \left(4^{\frac{1}{2}} \right)^2 \right $	1 for answer
-	
$=\sqrt{25+\frac{81}{4}}$	
<u>'</u>	
$=\frac{\sqrt{181}}{2}$	
(1) (2) 8-0 8 (1) 1	
(d) $m(BC) = \frac{8-0}{7-5} = \frac{8}{2} = 4$ $\therefore m(line) = -\frac{1}{4}$	
$y - y_1 = m (x - x_1)$	2 marks – 1 for gradient of line
$y-4\frac{1}{2}=-\frac{1}{4}(x-0)$	1 for equation
4y - 18 = -x	Tor equation
x + 4y - 18 = 0	
10(7) (40(0)) 451	
(e) $d = \frac{ 9(7) + 10(8) - 45 }{\sqrt{9^2 + 10^2}} = \frac{ 63 + 80 - 45 }{\sqrt{81 + 100}} = \frac{98}{\sqrt{181}}$	
17 10 VOITION VIOI	2 marks – 1 for substitution
Area = $\frac{1}{2}$ bh = $\frac{1}{2} \times \frac{\sqrt{181}}{2} \times \frac{98}{\sqrt{181}} = 24\frac{1}{2}$ square units.	1 for answer
$\frac{7}{180} = \frac{7}{2011} = \frac{7}{2} \qquad \frac{7}{181} = \frac{27}{2} $ square units.	
$(f) x - 2y + 9 \ge 0$	
(f) $x - 2y + 9 \ge 0$ $4x - y - 20 \le 0$	2 marks - lose 1 mark for each
$9x + 10y - 45 \ge 0$	incorrect
22 1 20y 10 <u>2</u> 0	
	1

Solutions	Marks/Comments
Question 3 (a) i. $\frac{d}{dx} \left[3x \sqrt[3]{x} \right] = vu' + uv'$ $= 3 \times x^{\frac{1}{8}} + 3x \times \frac{1}{3}x^{-\frac{2}{8}}$ $= 4x^{\frac{1}{8}}$ $= 4\sqrt[8]{x}$ Derivative = $4\sqrt[8]{x}$	2 marks – 1 for method 1 for answer
ii. $\frac{d}{dx} \left[\frac{\sin 2x}{e^{2x}} \right] = \frac{(e^{2x})(2\cos 2x) - (\sin 2x)(2e^{2x})}{(e^{2x})^2}$ $= \frac{2e^{2x} \left[\cos 2x - \sin 2x \right]}{(e^{2x})^2}$ $= \frac{2 \left[\cos 2x - \sin 2x \right]}{e^{2x}}$	2 marks – 1 for method 1 for answer
(b) i. $\int \frac{dx}{e^{3x}} = \int e^{-3x} dx = -\frac{1}{3}e^{-3x} + C$	2 marks – 1 for method 1 for answer
ii. $\int_0^{\pi} \sec^2 \frac{x}{4} dx = 4 \left[\tan \frac{x}{4} \right]_0^{\pi}$ $= 4 \left[\tan \frac{\pi}{4} - \tan 0 \right] = 4$	2 marks – 1 for integral 1 for answer
(c) i. $\alpha + \beta = -\frac{b}{a} = -\frac{-4}{3} = \frac{4}{3}$ $2\alpha^2 + 2\beta^2 = 2(\alpha^2 + \beta^2)$ $= 2\left[(\alpha + \beta)^2 - 2\alpha\beta\right]$ ii. $= 2\left[\left(\frac{4}{3}\right)^2 - 2\left(\frac{-7}{3}\right)\right]$ $= 2\left[\left(\frac{16}{9}\right) + \left(\frac{14}{3}\right)\right]$ 116	1 mark
$=\frac{116}{9}$	1 mark
iii. Equation with roots $2\alpha^2$ and $2\beta^2$ has equation $x^2 - (2\alpha^2 + 2\beta^2)x + (2\alpha^2 \times 2\beta^2) = 0$ i.e. $x^2 - 2[(\alpha + \beta)^2 - 2\alpha\beta]x + 4(\alpha\beta)^2 = 0$	2 marks – 1 for method 1 for answer

$x^{2} - 2\left[\left(\frac{4}{3}\right)^{2} - 2\left(\frac{-7}{3}\right)\right]x + 4\left(\frac{-7}{3}\right)^{2} = 0$ $x^{2} - 2\left[\frac{16}{9} + \frac{14}{3}\right]x + \frac{196}{9} = 0$	
$x^{2} - 2\left[\frac{58}{9}\right]x + \frac{196}{9} = 0$ $x^{2} - \frac{116}{9}x + \frac{196}{9} = 0$	
$9x^2 - 116x + 196 = 0$	

Solutions Marks/Comments		
Question 4		
(a) i. $\angle FBD = \theta$ (Given) $\angle DBC = 90^{\circ} - \theta$ $\angle BCD = 180^{\circ} - 90^{\circ} - (90 - \theta)$ (angle sum of $\triangle BCD$) $= \theta$ $\therefore \angle FEA = \theta$ (Corresponding angles to $\angle BCD$, FE BC)	2 marks – 1 for proof 1 for reasons	
ii. $\angle AFE = 90^{\circ}$ (Corresponding angles FE BC) $\tan \theta = \frac{AF}{y}$ $\therefore AF = y \tan \theta$	1 mark	
iii. In $\triangle ABD$, $\cos \theta = \frac{z}{AF + FB}$ $z = (AF + FB) \cos \theta$ $= (x + y \tan \theta) \cos \theta$	1 mark	
iv. $z = (x + y \tan \theta) \cos \theta$ $= x \cos \theta + y \tan \theta \cos \theta$ $= x \cos \theta + y \frac{\sin \theta}{\cos \theta} \cos \theta$ $= x \cos \theta + y \sin \theta$	1 mark	
(b) $a = 500\ 000000 \times 0.8$ $S_{\infty} = \frac{a}{1-r}$ $= \frac{500\ 000\ 000 \times 0.8}{1-\frac{4}{5}}$ $= \frac{400\ 000\ 000}{\frac{1}{5}}$ \$2 000 000 000	2 marks – 1 for substation into formula - 1 for answer	
(c) i. B 60nm A 120° θ	1 for correct diagram	
ii. $AC^2 = 50^2 + 60^2 - 2 \times 50 \times 60 \cos 120^\circ$ AC = 95.3939 = 95 nm	2 marks – 1 for substitution - 1 for answer	
$\frac{\sin \theta}{50} = \frac{\sin 120}{95.3939}$ $\sin \theta = \frac{50 \sin 120}{95.3939}$ $\theta = 27^{\circ} \text{(nearest degree)}$	2 marks – 1 for 27° - 1 for bearing	
Bearing = $270 - 27$ = 243°		

Question 5

(a) i. α . P(Wins first Prize) = $\frac{1}{1000}$

β. P(At least \$500) = $\frac{2}{1000}$ or 0.002

 γ . P(no prizes) = $1 - \frac{3}{1000} = \frac{997}{1000}$ or 0.997

ii. P(At least \$500) = $1 - (\frac{998}{1000} \times \frac{997}{999})$ = 0.003997997

(b) ABCD is a parallelogram and BP = DQ

Then

$$AP = AB - PB$$
$$= DC - DQ$$
$$= QC$$

In $\Delta \square$ s APD, BCQ

AP = QC (proven above)

AD = BC (opposite sides of parallelogram)

 $\angle PAD = \angle QCB$ (opposites angles of a parallelogram)

 $\Delta APD \equiv \Delta BCQ \text{ (SAS)}$

 \therefore DP = BQ (corresponding side in congruent triangles)

(c) i. $\log 3 + \log 9 + \log 27 + \dots$ $\log 3 + \log 3^2 + \log 3^3 + \dots$ $\log 3 + 2\log 3 + 3\log 3 + \dots$

Series is Arithmetic with a common difference of log 3

- ii. $S_n = \frac{n}{2} [2a + (n-1)d]$ $S_{10} = \frac{10}{2} [2(\log_a 3) + (10-1)\log_a 3]$ $= 5[2\log_a 3 + 9\log_a 3]$ $= 5[11\log_a 3]$ $= 55\log_a 3$ $= \log_a 3^{55}$
- (d) $4x^2 4x + 4y^2 + 24y + 21 = 0$ $x^2 - x + y^2 + 6y = -\frac{21}{4}$ $\left(x^2 - x + \frac{1}{4}\right) + \left(y^2 + 6y + 9\right) = -\frac{21}{4} + \frac{1}{4} + 9$ $\left(x - \frac{1}{2}\right)^2 + \left(y + 3\right)^2 = 4$ Centre $\left(\frac{1}{2}, -3\right)$, Radius = 2

1 mark

1 mark

1 mark

1 mark

3 marks – 1 for showing AP = QC1 for proving
triangles congruent

1 for DP = BQ

2 marks – 1 for type of series 1 for reason i.e the value of d

1 for S_{10} in either form

2 marks – 1 for centre 1 for radius

Question 6

(a) i.
$$\frac{dy}{dx} = 6(x-1)(x-2)$$
$$= 6(x^2 - 3x + 2)$$
$$= 6x^2 - 18x + 12$$
$$y = \int (6x^2 - 18x + 12) dx$$
$$= 2x^3 - 9x^2 + 12x + C$$

$$= 2x^{3} - 9x^{2} + 12x + C$$
When $x = 1$, $y = 2$

$$2 = 2(1)^{3} - 9(1)^{2} + 12(1) + C$$

$$2 = 2 - 9 + 12 + C$$

$$0 = 3 + C$$

$$C = -3$$

Equation of curve is $y = 2x^3 - 9x^2 + 12x - 3$

ii.
$$\frac{dy}{dx} = 6(x-1)(x-2)$$
 but $\frac{dy}{dx} = 0$ for Stationary Points i.e. $6(x-1)(x-2) = 0$

 $\frac{d^2y}{dx^2} = 12x - 18$

$$x = 1$$
 or $x = 2$
i.e. $(1, 2)$, $(2,1)$

At (1, 2),
$$\frac{d^2y}{dx^2} < 0$$
 Maximum at (1, 2)
At (2, 1), $\frac{d^2y}{dx^2} > 0$ Mimimum at (2,1)

iii.
$$\frac{d^2y}{dx^2} = 12x - 18 = 0$$
 for inflexion point $12x = 18$ $x = 1\frac{1}{2}$ i.e. $(1\frac{1}{2}, 1\frac{1}{2})$

At
$$(1\frac{1}{2}, 1\frac{1}{2})$$
 $\frac{x}{d^2y} - 0 + \text{Concavity changes at } x = 1\frac{1}{2}$

Point of inflexion at $(1\frac{1}{2}, 1\frac{1}{2})$

At
$$x = -1$$
, $y = 2(-1)^3 - 9(-1)^2 + 12(-1) - 3$
= -26

At
$$x = 3$$
, $y = 2(3)^3 - 9(3)^2 + 12(3) - 3$
= 6

At
$$x = 0$$
, $y = -3$

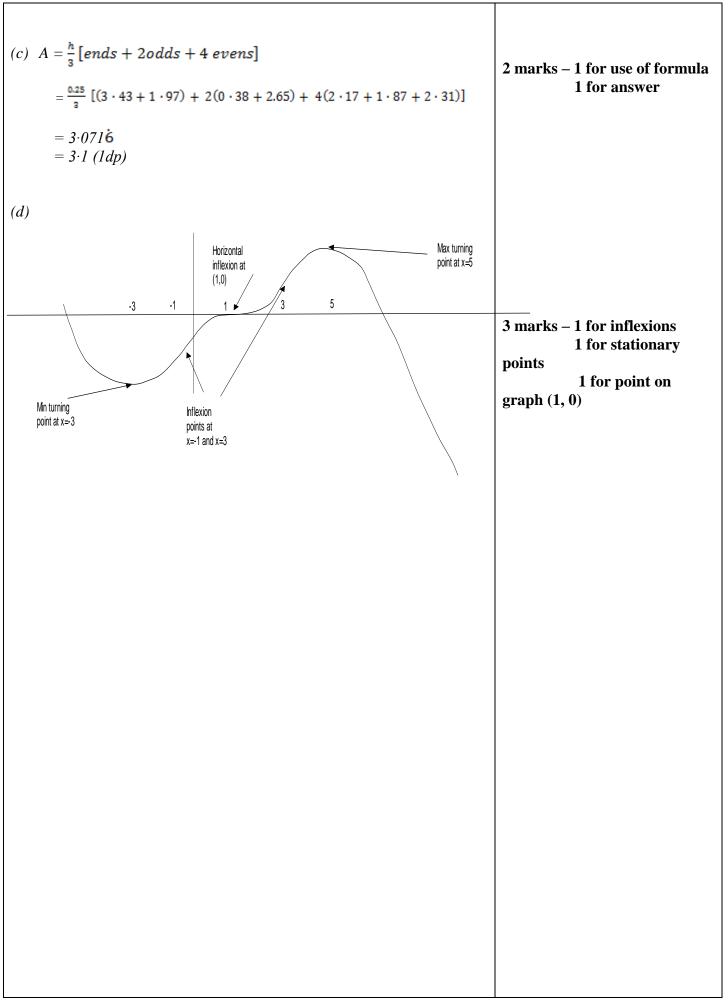
2 marks – 1 for integration 1 for equation with correct value of "c"

2 marks – 1 for points 1 for testing points

2 marks – 1 for inflexion point 1 for testing

Marks/Comments Solutions 2 marks - 1 for graph 1 for labels (b) $\frac{\left(1+tan^2\;\theta\right)\cot\theta}{cosec^2\;\theta} = \tan\theta$ $LHS = \frac{\left(1+tan^2\;\theta\right)\cot\theta}{cosec^2\;\theta} = \frac{sec^2\;\theta\;.\cot\theta}{cosec^2\;\theta}$ (3 marks) 1 mark $= \frac{1}{\cos^2\theta} \cdot \frac{\cos\theta}{\sin\theta} \, \div \, \frac{1}{\sin^2\theta}$ 1 mark 1 mark $= tan \theta = RHS$ (c) $\lim_{\theta \to 0} \frac{\sin 2\theta}{3\theta} = \frac{2}{3} \lim_{\theta \to 0} \frac{\sin 2\theta}{2\theta}$ 1 mark

Solutions Marks/Comments Question 7 (a) $y = x^2 - - - (1)$ y = x + 2 - - - (2)(1) In (2) 4 marks – 1 for each point (2) $x^2 = x + 2$ $x^2 - x - 2 = 0$ 1 for integration 1 for answer (x+1)(x-2)=0x = -1 or x = 2i.e. A (-1, 1) B (2, 4) $A = \left| \int_a^b (f(x) - g(x)) \ dx \right|$ $= \left| \int_{-1}^{2} (x + 2 - x^2) \, dx \right|$ $= \left[\frac{x^2}{2} + 2x - \frac{x^3}{3}\right]_{-1}^2$ $= \left(\frac{4}{2} + 4 - \frac{8}{3}\right) - \left(\frac{1}{2} - 2 + \frac{1}{3}\right)$ $= 3\frac{1}{3} - 1\frac{1}{6}$ $= 4\frac{1}{2} \quad sq \ units$ (b) i. Angle = $\frac{40}{60} \times 360$ = $240 \times \frac{\pi}{180}$ 1 mark $ii. l = r\theta$ $=12\left(\frac{4\pi}{3}\right)$ 1 mark $=16\pi$ cm. iii. $A = \frac{1}{2}r^2\theta$ $=\frac{1}{2}(12)^2\left(\frac{4\pi}{3}\right)$ 1 mark $=96\pi$ cm.



Solutions	Marks/Comments
Question 8	
(a) i. B, C, D	1 mark
ii. From A to C and then from C to E	1 mark
iii.	
A C E X	1 mark
(b) i. Let \$P\$ be the amount repaid each month $$A_n$ - Amount owing after n repayments A_1 = 15\ 000 \times 1.005 - P A_2 = A_1 \times 1.005 - P = (15\ 000 \times 1.005 - P) \times 1.005 - P = 15\ 000 \times 1.005^2 - P(1 + 1.005)$	2 marks - 1 for working 1 for proof
$A_3 = A_2 \times 1 \cdot 005 - P$ = $[15\ 000 \times 1 \cdot 005^2 - P(1 + 1 \cdot 005)] \times 1.005 - P$ = $[15\ 000 \times 1 \cdot 005^3 - P(1 \cdot 005 + 1 \cdot 005^2) - P$ = $15\ 000 \times 1 \cdot 005^3 - P(1 + 1 \cdot 005 + 1 \cdot 005^2)$ = $15\ 226 \cdot 13 - P(3 \cdot 015025)$	
ii. $A_{24} = 15\ 000 \times 1.005^{24} - P(1 + 1.005 + \dots + 1.005^{23})$ but $A_{24} = 10\ 000$	3 marks - 1 for working - 1 for sum of GS - 1 for answer

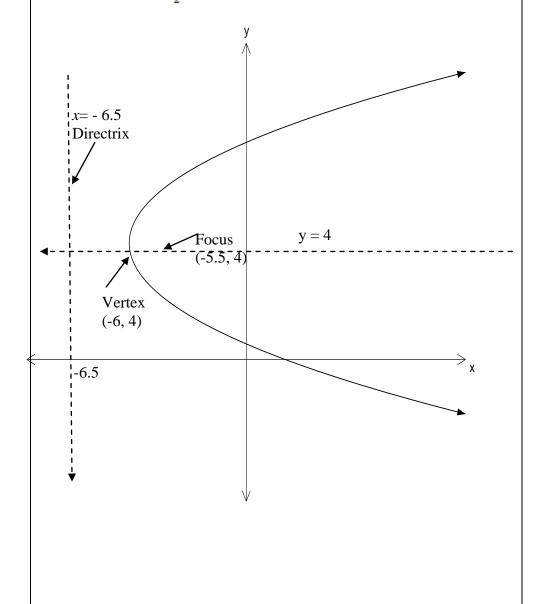
= \$271.60

(c) $2x = y^2 - 8y + 4$ $y^2 - 8y = 2x - 4$ $y^2 - 8y + 16 = 2x - 4 + 16$ $(y - 4)^2 = 2x + 12$ $(y - 4)^2 = 2(x + 6)$

Vertex = (-6, 4)4a = 2 $a=\frac{1}{2}$

Focus = $\left(-5\frac{1}{2}, 4\right)$

Directrix: $x = -6\frac{1}{2}$



4 marks - 1 for sketch1 for vertex

1 for focus

1 for directrix

Solutions	Marks/Comments
Question 9	Tracks/Commonts
(a) $x = 2 \sin 2t$ $\dot{x} = 4 \cos 2t$ $\ddot{x} = -8 \sin 2t$	
i. $t = 0$ $\dot{x} = 4\cos 2(0)$ = 4×1 = 4 m/s	1 mark
ii. $t = \frac{\pi}{12} \ddot{x} = -8 \sin 2 \left(\frac{\pi}{12}\right)$ $= -8 \sin \left(\frac{\pi}{6}\right)$ $= -8 \times \frac{1}{2}$ $= -4 \text{ m/s}^2$	1 mark
iii. $\dot{x} = 0$ then $4\cos 2t = 0$ i.e. $\cos 2t = 0$ $2t = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}, \dots$	2 marks – 1 for working 1 for answer
$t = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}, \dots$ $iv. x = 2\sin 2t$ $= 2\sin 2\left(\frac{\pi}{4}\right)$ $= 2$	2 marks - 1 for working 1 for answer
$\therefore x = \pm 2 \text{ m}$ (b) $V = \int_a^b [f(x)]^2 dx$ $= \int_1^3 \left(\sqrt{\frac{2x}{3x^2 - 1}}\right)^2 dx$	3 marks – 1 use of formula 1 for Integral 1 for answer
$= \int_{1}^{3} \frac{2x dx}{3x^{2} - 1}$ $= \frac{1}{3} [\ln(3x^{2} - 1)]_{1}^{3}$ $= \frac{1}{3} [\ln(3 \times 3^{2} - 1) - \ln(3 \times 1^{2} - 1)]$ $= \frac{1}{3} (\ln 26 - \ln 2)$ $= \frac{1}{3} (\ln \frac{26}{2})$ $= \frac{1}{3} (\ln 13)$	

(c) i.
$$\frac{dV}{dt} = \frac{1}{100} (30t - t^2)$$

when $t = 15$

$$\frac{dV}{dt} = \frac{1}{100} [30(15) - (15)^2]$$

$$= \frac{225}{100}$$

$$= 2\frac{1}{4} \text{ cm}^3 / \text{min}$$

ii.
$$V = \int_0^{15} \frac{1}{100} (30t - t^2)$$

$$= \frac{1}{100} \left[15t^2 - \frac{t^3}{3} \right]_0^{15}$$

$$= \frac{1}{100} \left\{ \left[15(15)^2 - \frac{15^3}{3} \right] - [0] \right\}$$

$$= \frac{1}{100} \left[3375 - 1125 \right]$$

$$= \frac{1}{100} (2250)$$

$$= 22.5 \text{ cm}^3$$

1 mark

2 marks – 1 for integral 1 for answer

Solutions	Marks/Comments
Question 10	
(a) i. $SA = \pi r^2 + 2\pi r h = 300$ $2\pi r h = 300 - \pi r^2$ $h = \frac{300 - \pi r^2}{2\pi r}$	2 marks – 1 for "h" 1 for "V"
$V = \pi r^{2} h$ $= \sqrt{r} r^{2} \left(\frac{300 - \pi r^{2}}{2 \sqrt{r}} \right)$ $= 150r - \frac{\pi r^{3}}{2}$ ii. $V = 150r - \frac{1}{2}\pi r^{3}$	
$\dot{V} = 150 - \frac{3}{2} \pi r^2$ $\ddot{V} = -3\pi r \qquad \text{which is less than 0 for positive } r$	4 marks – 1 for differentials 1 for value of 'r' 1 for test 1 for max volume
Stat Pts when $\dot{V} = 0$ i.e. $150 - \frac{3}{2} \pi r^2 = 0$	
$150 = \frac{3}{2} \pi r^2$ $100 = \pi r^2$ $r^2 = \frac{100}{\pi}$ $r^2 = \pm \sqrt{\frac{100}{\pi}}$	
$r^2 = \pm \sqrt{\frac{350}{\pi}}$ Now max Volume when $r > 0$ i.e. $r = \sqrt{\frac{100}{\pi}} = 5.641895835$	
$V = 150 \sqrt{\frac{100}{\pi}} - \frac{\pi}{2} \left(\sqrt{\frac{100}{\pi}} \right)^3 = 564 \cdot 1895835$ $= 564 \text{ m}^3 \text{ (nearest m}^3\text{)}$	
(b) i. $\frac{dP}{dt} = kP$: $P = P_0 e^{kt}$	
When $t = 0$, $P = 20\ 000$, $\therefore P_0 = 20\ 000$ So $P = 20\ 000\ e^{kt}$	3 marks – 1 for value of 'k'
When $t = 2$, $P = 25\ 000$ $25\ 000 = 20\ 000e^{2k}$	1 for equation 1 population
$\frac{5}{4} = e^{2k}$	
$ \ln\left(\frac{5}{4}\right) = 2k $	
$k = \ln\left(\frac{5}{4}\right) \div 2$	
$k = 0 \cdot 111571775$	
$\therefore P = 20\ 000 e^{0.111571775t}$	

When
$$t = 10$$
 $P = 20\ 000 e^{0.111571775(10)}$
= 61 000 people (nearest 100)

ii.
$$\frac{dp}{dt} = 61\ 000 \times 0 \cdot 111571775$$

= 6806 people / year

(c)
$$\log_a 2 + 2\log_a x - \log_a 6 = \log_a 3$$

 $\log_a 2 + \log_a x^2 - \log_3 6 = \log_a 3$
 $\log_a \frac{2x^2}{6} = \log_a 3$
 $\therefore \frac{2x^2}{6} = 3$
 $2x^2 = 18$
 $x^2 = 9$
 $x = \pm 3$

going back to original equation, cannot have log (-3) so

$$x = 3$$

1 for rate of change

 $\begin{array}{l} 2\;marks-1\;manipulation\;of\\ logs \end{array}$

1 for answer