SOLUTIONS: EXTENSION | TRIAL EXAM 2002

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b) 
$$\int e^{-2x} dx = \left[ -\frac{1}{2} e^{-2x} + C \right]$$

a i) \( \frac{\chi}{4+\chi^2} d\alpha = \frac{1}{2} \frac{2\chi}{4+\chi^2} d\alpha = \frac{1}{2} \left| \frac{2\chi}{4+\chi^2} d\alpha = \frac{1}{2} \left| \frac{1}{6+\chi^2} d\alpha = \frac{1}{2} \left| \frac{1}{6+\chi^2}

ii) \( \frac{1}{8} \tam^2 2\times d\( \text{n} = \int\_{\frac{1}{8}}^{\frac{1}{8}} \left( \sec^2 2\times - 1) d\( \text{n} \)

= [2 tam 2x - x] =

c) 
$$\int_{0}^{4} \frac{dx}{\sqrt{x^{2}+4}} dx = \left[\log_{c}(x+\sqrt{x^{2}+4})\right]_{0}^{4}$$
  
=  $\log_{c}(4+\sqrt{20}) - \log_{c}(0+a)$   
=  $\log_{c}(4+2\sqrt{6}) - \log_{c}2$   
=  $\log_{c}(3+\sqrt{6})$ 

= 25-2-11

= | 24 (1253 - 12 - 17)

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= 12 tan = - = - 2 tan = -

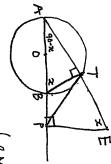
$$\begin{array}{c}
\uparrow f(x) \\
\downarrow 2\pi \\
3
\end{array}$$

E . W.S = 7

dom: - 1 = 2 - 1

 $f(x) = 4 \sin^{-1} \frac{x}{3}$   $f(x) = 4 \sin^{-1} \frac{x}{3}$ 

$$\frac{6}{10} = \frac{1}{1-r} \left( r + r^2 + r^3 + \dots + \right) - \frac{1}{1-r} \left( r + r^2 + r^3 + \dots + r^3 + \dots + \right) - \frac{1}{1-r} \left( r + r^2 + r^3 + \dots + r^$$



## (i) LATB=90 (Linsem

let P(n) = 6"-1

- LEPB : TOPE is cyclic QED

(ext L = int opp L of gread).

(11) let LE=x

...LTRB = 90 - x (L'S OF DEPA)

...LETP = 90 - x (L in alt Seq.)

...LETP = x (L'S on Str Line)

...LETP = x (L'S on Str Line)

...LETP = X (Sides OPP = L'S)

 $\frac{7x}{5-x} = \frac{7}{7}$   $\frac{7x}{5-x} = \frac{7}{7}$   $\frac{7x}{5-x} = \frac{7}{7}$   $\frac{7x}{5-x} = \frac{7}{7}$   $\frac{7x}{7} = \frac{7}{7}$ 

8/n: 5-2-5

36) when n=1 6<sup>n</sup>-1=6-1 now 6 \*+1 = 6 = 6 - 1 we want to show that P(K+1) is divis so by the process of mathematical induction, the statement P(n) is true for all  $n \in \mathbb{Z}^+$ let we assume I k such that 1.e 6 k+1 -1 is divisible by 5. which is divisible by 5. 6x-1 = 5m for some m = 2 which is divisible by 5 = 6.5m + 6 6 x = 5m+1 (5m+1)6 -

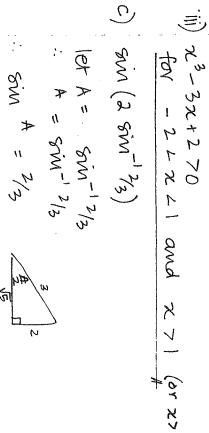
 $dm = 3x^{2} dx$   $\therefore x^{2} dx = 5 dx$   $when x = 1 \ y = a$   $x = -1 \ y = 0$ 

 $\frac{6t}{1+t^{2}} + \frac{4(1-t^{2})}{1-t^{2}} = 5$   $6t + 4 + 4t^{2} = 5 + 5t^{2}$   $6t + 4 + 4t^{2} = 5 + 5t^{2}$   $4t^{2} - 6t + 1 = 0$  (3t - 1)(3t - 1) = 0  $5x + 180^{2}x = \frac{1}{3}$   $7x = 180^{2}x = \frac{1}{3}$   $7x = 180^{2}x = \frac{1}{3}$   $10x + 10x + 10x = \frac{1}{3}$   $10x + 10x + 10x = \frac{1}{3}$   $10x + 10x + 10x = \frac{1}{3}$   $10x + 10x = \frac{1}$   $10x + 10x = \frac{1}{3}$   $10x + 10x = \frac{1}{3}$   $10x + 10x = \frac{1}$ 

4 b) i)  $f(x) = x^3 - 3x + 2$  f(1) = 1 - 3 + 2 = 050 (x - 1) is a factor  $\frac{x^2 + x - 2}{x^3 - x^2}$   $\frac{x^2 - 3x}{x^2 - 3x} + 2$  - 2x + 2 - 2x + 2 50 f(x) = (x - 1)(x + 2)(x - 1)

 $3 \sin x + 4 \cos x = 5$ let  $t = \tan 2x$ 

 $||| \psi - || \psi = || \psi - || \psi -$ 



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(i) 
$$f(x) = x^3 - 8x + 8$$
  
 $f(-4) = (-3)^3 - 8(-3) + 8$   
 $f(-4) = (-4)^3 - 8(-4) + 8$   
 $f(-4) = -24$   
 $f'(x)$   
 $f'(x) = 3x^2 - 8$   
 $f'(x) = 3x^2 - 8$ 

=-3.26 is an approx for f(x)=0.

1) i) 
$$x = a \cos(2t + \beta)$$
  
 $x = -2a \sin(2t + \beta)$   
 $x = -4a \cos(2t + \beta)$   
 $x = -4x \text{ and satisfies eq}^n$ 

iii) when t=0,  $\chi=5$  when t=0, V=0,  $\chi=5$  a cos  $\beta-\square$   $| :: \lambda=-20, \chi=0$  squaing and adding: -1=0; sin  $\beta$   $| :: \lambda=-20, \chi=0$   $| :: \lambda=-20, \chi=0$  | ::

at x=0, t=0  $0=1+c_2$   $c_1=-1$   $e^{x/2}=t+1$  |oq(t+1)=x  $|\sqrt{x}=2|oqc(t+1)|$ 8) act  $-\infty$ ,  $x\to\infty$  | so but diphacement

 $\frac{1}{12} \sqrt{2} = 3e^{-x} + \frac{1}{2}c,$   $\frac{1}{12} \sqrt{2} = 4e^{-x} + c,$   $\frac{1}{12} \sqrt{2} = 4e^{-x$ 

β) 1e-x >0 for all x

so v² does not change sign

since v=2 at x=0, it

remans positive.

 $\frac{dt}{dx} = \frac{e^{x_{12}}}{2}$   $\frac{dt}{dx} = \frac{e^{x_{12}}}{2}$   $\frac{dt}{dx} = \frac{e^{x_{12}}}{2}$ 

6 a) dut = -3 m/s
we want dix when x=2

also, when x = 2, y=16-4

Sw  $\frac{dx}{dt} = \frac{dx}{dy} \times \frac{dy}{dt}$   $= \frac{716-y^2}{716-12} \times -3$   $= 3\sqrt{3}$   $= 3\sqrt{3}$ 

of 3/3 m/s #

Grad of tang = p(x-2ax)

). Grad of tang = p  $y - ap^{2} = p(x - 2ap)$   $y - ap^{2} = px - 2ap^{2}$   $y - ap^{2} = px - 2ap^{2}$ When x = 0,  $y = -ap^{2}$   $y = (0, -ap^{2})^{2}$ dist  $y = (0, -ap^{2})^{2}$   $y = (0, -ap^{2})^{2}$  $y = (0, -ap^{2})^{2}$ 

)  $dist^{2}Sp = (a + ap^{2})^{2}$   $dist^{2}Sp = (2ap)^{2} + (ap^{2} - a)^{2}$   $= 24a^{2}p^{2} + a^{2}p^{2} + a^{2}p^{2} + a^{2}p^{2} + a^{2}p^{2}$   $= a^{2} + 2a^{2}p^{2} + a^{2}p^{2}$  $= (a + ap^{2})^{2}$ 

SP = SQ QED.

: LPSQ + 2 LSQD = 180° (7 sum of ΔPSQ)

(6 c)i) sub  $A = A_0 e^{kt}$  into de = kAUts =  $de (A_0 e^{kt})$ =  $A_0 \cdot ke^{kt}$ 

ii) when t = 3,  $A = 2A_0$   $2A_0 = A_0 e^{3k}$   $e^{3k} = 2$  $k = \pm \log e^2$ 

ii)  $A = A_0 e^{kt}$  where  $k = \frac{1}{5} \ln 2$ when  $A_0 = 3$ , A = 70,000  $\therefore 20,000 = 3 e^{kt}$  20000  $t = \frac{1}{5} \log_2 \frac{20000}{3}$ 

= 38, 108249... weeks t = 39 it will take 39 complete weeks in  $\triangle \varphi \circ C$   $q \circ C = r^{2} + 4r^{2} - 2r \cdot 2r \cdot \omega \circ \theta$   $4x^{2} = 5r^{2} + 4r^{2} \cdot \omega \circ \theta$   $x^{2} = 5r^{2} + 4r^{2} \cdot \omega \circ \theta$   $x^{2} = 5r^{2} + r^{2} + r^{2} \cdot \omega \circ \theta$   $2 - 7 \cdot \omega \circ \theta = \frac{5}{4} + \iota \omega \circ \theta$   $3 \cdot \iota \omega \circ \theta = \frac{5}{4} + \iota \omega \circ \theta$   $4 \cdot \iota \omega \circ \theta = \frac{7}{4}$   $4 \cdot \iota \omega$ 

wax occurs when dx =0

10250-15x<sup>2</sup>

15x²=20250 x²= 1350 x= 15√6

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= 15x2 + 20150 - 30x2

 $(\chi^2 + 1350)^2 + (15\chi)^2$ 

 $tam(\theta + \phi) = \frac{70}{12}$   $tam(\theta + \phi) = \frac{15}{2}$   $tam(\theta + \phi) = \frac{1}{2}$   $(x^2 + 1350) tam(\theta + \phi) = \frac{1}{2}$   $tam(\theta + \phi) = \frac{1}{2}$   $(x^2 + 1350) tam(\theta + \phi) = \frac{1}{2}$   $tam(\theta + \phi) = \frac{1}{2}$   $tam(\theta + \phi) = \frac{1}{2}$   $(x^2 + 1350) = \frac{1}{2}$   $tam(\theta + \phi) = \frac{1}{2}$   $tam(\theta + \phi$ 

1) in \( \Delta \text{ Apo} \)
\( \chi^2 = 2r^2 - 2r^2 \text{ WS & \quad \text{ II}} \)

let AQ=x