

GOSFORD HIGH SCHOOL

2010

L HIGHER SCHOOL CERTIFICA

MATHEMATICS

Time Allowed - 3 hours

(plus 5 minutes reading time)

All necessary working should be shown.

Students must begin each new question on a new page. Full marks may not be awarded for unnecessarily untidy work or work that is poorly organized.

Questions will be collected separately at the conclusion of the assessment task.

All questions are to be attempted.

(12 marks) QUESTION 1 Use shading to represent the region satisfying $x + 2y \le 6$ (a)

Solve $x^2 - 3x - 10 = 0$ **(**P) Given x = 3 is a root of the quadratic equation $kx^2 - 20x + 2(k - 14) = 0$ <u>၁</u>

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Find the value of k. \odot

Find the other root. Ξ ਉ

If $\cos\alpha=0.64$ and $0\le\alpha\le 2\pi$, find all possible values of α (give answers correct to 3 significant figures)

 $\frac{5}{\sqrt{5}}$ and $\sin \theta < 0$ find the exact value of $\sec \theta$ Given that $\tan \theta =$ **e**

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(12 marks) QUESTION 2

Find $\int \frac{dx}{x^2}$ (a)

Evaluate $\int_{-1}^{1} e^{2x+2} dx$

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 $\frac{1}{x+1}$ at the point x=Find the gradient of the tangent to the curve y = 1

Find the equation of the parabola with focus (6,-2) and directrix the line x=-4

State the period and amplitude of the curve $y = 3\sin(2\theta)$

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For a particular series the sum to *n* terms S_n is given by $S_n = 2^{n+1}$ (£)

Show that $T_n = 2^n$

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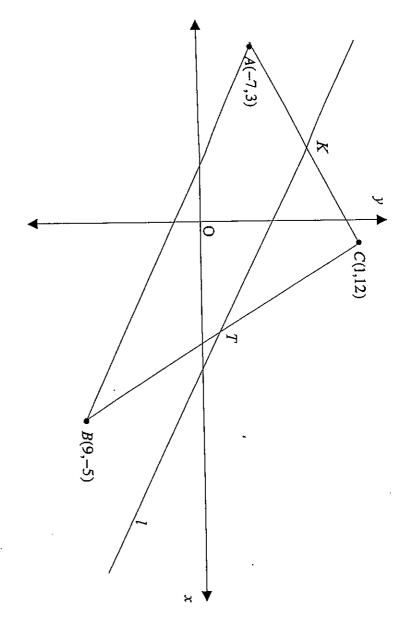
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In the diagram A, B, and C represent the points (-7,3), (9,-5) and (1,12). The line l passes through the midpoint K of AC and is parallel to AB. The line l meets BC at T

(iv)	iii)	(ii)	(i)
Find the equation of BC , writing your answer in general form	Find the gradient of BC	Find the coordinates of T	Find the midpoint of AC
(2)	Ξ	Ξ	Ξ

(vi)	3
) Find the perpendicular distance from A to BC	Find the length of BC
(2)	Ξ

(vi)

(2)	State the area of triangle KTC	(ix)	(iii)
	Find the area of triangle ABC	(viii) I	(vii)

(12 marks)

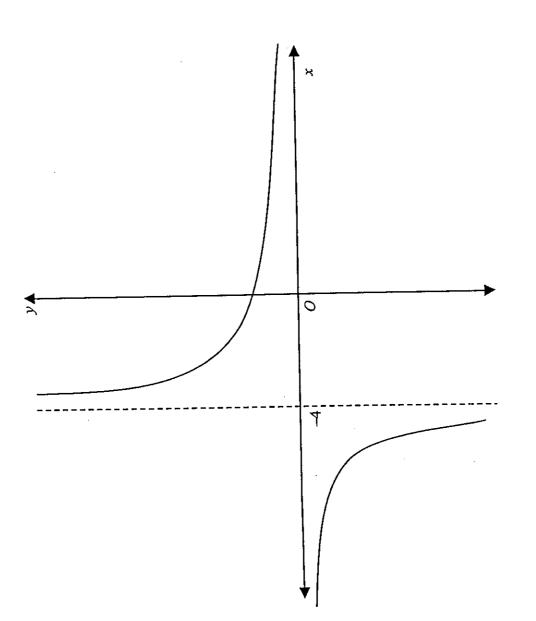
Use Simpson's rule with five function values to calculate $\int_0^4 2^x dx$ (a)

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- The curve $y = \frac{1}{x+4}$ has been drawn on the number plane below. **(**P)
- Show that the line x + 4y = 0 is a tangent to $y = \frac{1}{x+4}$ \odot

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 \mathfrak{S} Calculate the exact area of the region enclosed by the curve, the x axis and the ordinates at x = -2 and x = 4. (Ξ)



(c) Solve |12 - x| = 3x

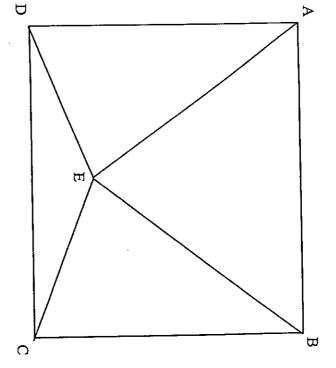
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- (12 marks)
- (a) In the diagram below ABCD is a square and triangle ABE is equilateral.
- (i) Prove $\triangle ADE = \triangle BCE$.
- (ii) Hence, or otherwise, state why $\angle AED = \angle BEC$.
- (iii) Find the size of $\angle DEC$ giving reasons

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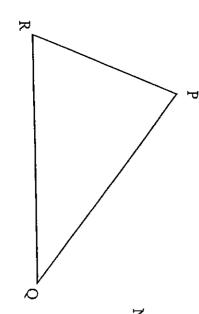
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NOT DRAWN TO SCALE

9 Use the Cosine Rule to show, without use of your calculator, that $\angle PQR = 30^{\circ}$ In the $\triangle PQR$, $PR = \sqrt{6}$, $PQ = 2\sqrt{3}$ and $RQ = 3 + \sqrt{3}$

(3)



NOT DRAWN TO SCALE

<u>©</u> Find the equation of the normal to the curve $y = \tan\left(\frac{x}{2}\right)$ at the point on the curve

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where
$$x = \frac{\pi}{2}$$

QUESTION 6 (1)

(a) Find
$$f'(e)$$
 if $f(x) = \sqrt{3 + \ln x}$

(b) Evaluate
$$\sum_{n=1}^{\infty} \frac{3}{2^n}$$

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(c) Find the values of m for which the quadratic equation
$$x^2 + (m-2)x + 4 = 0$$
 has no real roots. (3)

A particle moves along the x axis with acceleration at time t given by 9

$$\frac{d^2x}{dt^2} = 12\cos(2t)$$

Find x in terms of t given that when
$$t = 0$$
, $x = 0$ and $\frac{dx}{dt} = 0$

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QUESTION 7 (1

7 (12 marks)

The area of a sector AOB of a circle centre O and radius length 6cm is $27 \, cm^2$ (<u>a</u> \Im

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- 4 Find the first term and the common difference of the sequence.
- In 1810 Lily, an early settler of Gosford, left a will in which she established a fund of \$500 for its future citizens to spend on such things as schools, hospitals etc. Her instructions were that this money was to be invested at 6% p.a. compounded yearly.
- If Lily's instructions were followed, how much would have been in the fund 100 years after it was established? $\dot{\odot}$

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Suppose that at the beginning of each subsequent year after the establishment, a further \$500 had been added to the fund and had also earned 6% interest, compounded annually. Ξ

3 Express the amount of money (\$M) in the fund after 100 years as a Geometric series and hence derive the value of M correct to the nearest dollar.

(12 marks)

- (a) after t minutes is R litres/minute where $R = -(t-6)^2$ A tank is emptied by a tap from which the water flows so that, until the flow ceases, the rate of flow
- (i) What is the initial rate of flow?

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- (ii) How long does it take to empty the tank?
- (iii) How long will it take (to the nearest second) for the flow to drop to 20 litres/minute
- (iv) How much water was in the tank initially?
- After its engine is cut, a biplane travels in a straight line with negative acceleration proportional to its

velocity (V) i.e.
$$\frac{dV}{dt} = -kV$$

The plane is travelling at 400m/s when the engine is cut and 10 seconds later the velocity is 250m/s.

 \odot Show that this equation is satisfied by the equation $V = V_0 e^{-kt}$

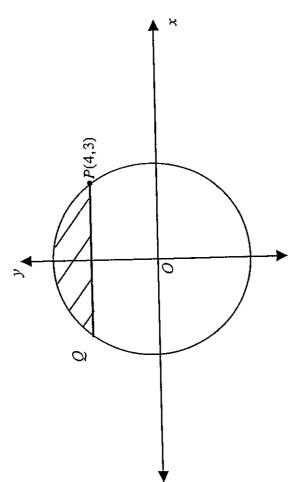
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- Ξ Find the value of V_0 and k (to 3 decimal places)
- (iii)Find how long it takes for the velocity to fall to 100m/s (answer to 1 decimal place)

- (12 marks)
- (a) P and Q lie on the circle with centre the origin O.



The shaded area, bounded by the circle and the line PQ, is rotated about the y axis

to form a spherical cap. Find the volume of the cap.

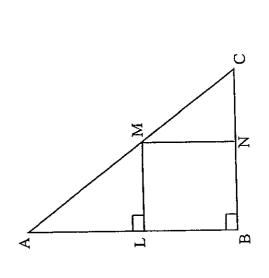
- (b) In the diagram below AB = 25 m and BC = 20 m.
- Prove that ΔABC is similar to ΔALM.

(5)

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- If LB = x m show that the area of the rectangle LBNM is $\frac{4x}{5}(25-x)$ square metres (ij)
 - Hence find the maximum possible area of the rectangle LBNM (iii)



(c) If $e^{4x} = 4$ show that $x = \frac{1}{2} \ln 2$

(2)

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QUESTION 10

(12 marks)

Consider the curve $y = \sin x(1 + \cos x)$ for $0 \le x \le 2\pi$

(i) Show that
$$\frac{dy}{dx} = 2\cos^2 x + \cos x - 1$$

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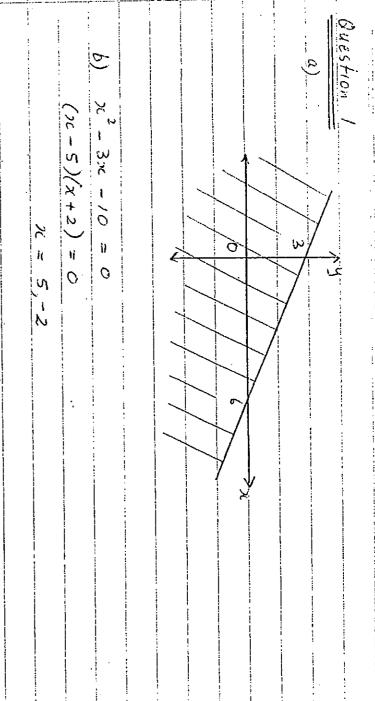
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(ii) Show that
$$\frac{d^2y}{dx^2} = -\sin x (4\cos x + 1)$$

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(3)

(2)



c) (i)
$$k(9) - 20(3) + 2(k - 14) = 0$$

 $9k - 60 + 2k - 28 = 0$
 $1/k = 88$

Expression

becomes

 $\overset{\varkappa}{\otimes}$

20x

0

(ii) Let
$$\alpha$$
 be the other root
$$\alpha + 3 = 20 \quad \text{Using } \alpha + 3 = -t$$

$$\alpha = -\frac{t}{3}$$

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$6) \qquad 2x+2 \qquad 2 \qquad 2x+3 \qquad 6 \qquad 3-1$
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$\frac{1}{z} \frac{d}{dx} = \frac{1}{x} + \frac{1}{x} = \frac{1}{x}$
rivalent of langear is 9
d) Amplitude = 3 , Period = 17
e) 2a=10 -> a=5.
$(x \cdot (y+2)^2 = 20(x-1)$
P) Tn = Sn = fn-1. Tn = Sn - Sn-1
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$$\frac{\text{Qiles From 3}}{\text{(i)}} \times (-3,7\frac{1}{2})$$

(ii)
$$T(5,3\frac{1}{2})$$

(11) Equation of BC is
$$y + 5 = \frac{17}{8}(x-9)$$

$$\frac{17y + 8y - 1/3 = 0}{8y - 40 = 1/3 = 0}$$

$$viii)$$
 Area = $\frac{1}{2} \times \sqrt{353} \times \sqrt{353}$.

 $viii)$ Area = $\frac{1}{2} \times \sqrt{3} \times \sqrt{3} \times \sqrt{3} \times \sqrt{2} \times \sqrt{3} \times \sqrt{2} \times \sqrt{3} \times \sqrt{3} \times \sqrt{2} \times \sqrt{3} \times$

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	= 3 x 65
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	b)(i) solving = +y and y = 1++
	<u> </u>
	J -4y+4
	1 = ht + zht -
	44-1+0
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	: Only one of intersection : 12+44=0 is a tangent
	(ii) Area = 1 1/4 dx.
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	- In (x+4)
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	- In 8 - In 2
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7. Water flowing out at 361

(11) whin RIO (6-6) 6 seconds

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 $V = -(\xi - \xi)^3 + C$

V=0 6 0

COKEN

= 72 lites

9	
	$ \frac{d}{dt} = V_0 e^{-kt} $
	1 1
	=-kV as required.
	(ii) 400 = 1/2 e" -> 1/2 = 400.
	1, 250 = 400 e -10k when t=10
	3
	p = In 0.625" = 0.047 (+63d.p)
	(iii) 100 = 400 e-kt
	0.25 = e-kt
	- kt = In 0.25
	t = In 6.25.
	= 29.5 seconds

LBNM

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(15-11) is a quadratic expression
\$
Maximum value occurs at 4.0.5.
ie when K = 12.5
"Max, tha = 4x 12:5 (25-12.5)
= 125 Sq units
c) e + + 4
1x = ln h
1
x = \$ ln4.
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(ii)
$$\frac{d^2y}{dx^2} = A\cos\chi \left(\frac{1}{2}\sin\chi\right) - \sin\chi$$
.

$$= -\sin x \left(4\cos x + 1 \right)$$

$$(2\cos^2x + \cos x - 1) = 0$$

 $(2\cos x - 1)(\cos x + 1) = 0$

$$\therefore \cos x = \frac{1}{2} \cdot \text{ond} - 1.$$

X500

$$(1, k = \frac{\pi}{3}, \frac{5\pi}{3}, \pi)$$

and
$$y = \frac{313}{4}, -\frac{313}{4}, 0$$

(iv) when
$$x = \frac{\pi}{3}$$
, $\frac{\partial^2 y}{\partial x^2} < 0$

in them
$$u = \frac{5\pi}{3}$$
 ($\frac{d^2y}{dx^2} > 0$

