$$O + O$$

$$= e^{2x} (2xix + uxx)$$

c)
$$\frac{dy}{dx} = \frac{1}{\sqrt{4-x^2}}$$

d)
$$(x-3)(x+2)>0$$

from the graph

$$\odot$$

0

x < -2 or x >3

e) Let & be the argle

$$+ \sum_{j=1}^{n} \phi_j = \left| \frac{1 - (-2)}{1 + 1 \times -2} \right|$$

 \odot

= 3

0

f) (i) $\int \frac{1+e^{x}}{e^{x}} dx = \int e^{x} + 1 dx$

①

(ii)
$$\int \frac{e^x}{1+e^x} dx = \log(1+e^x) + C.$$

 \odot

|<u>|</u>

d) (i) Expand RHI or
$$(\alpha + \beta)^{3} = \alpha^{3} + 3\alpha^{2}\beta + 3\alpha\beta^{2} + \beta^{3}$$

$$= \alpha^{3} + \beta^{3} + 3\alpha\beta(\alpha + \beta)$$
to $\alpha^{3} + \beta^{3} = (\alpha + \beta)[(\alpha + \beta)^{2} - 3\alpha\beta]$
or
$$= \alpha^{3} + \beta^{3} = (\alpha + \beta)[(\alpha + \beta)^{2} - 3\alpha\beta]$$

(ii) here
$$\alpha + \beta = -3$$
 and $\alpha \beta = -2$
so $\alpha^3 + \beta^3 = -3 \left[(-3)^2 - 3x - 2 \right]$ 0
= -45 0

3. a) (i)
$$kts = \frac{1}{2}(1-40128)$$

$$= \frac{1}{2}(1-40128+4428)$$

$$= \frac{1}{2}\cdot 2 + 428$$

$$= 443 \#$$

(ii)
$$\int_{0}^{\pi} \sin^{2}\theta d\theta = \int_{0}^{\pi} \frac{1}{2} (1 - \cos 2\theta) d\theta$$

= $\frac{1}{2} \left[\theta - \frac{1}{2} \sin 2\theta \right]_{0}^{\pi}$

b)
$$u = 1-x$$

at $x=0$ $u=1$ and at $x=1$ $u=0$
 $x=1-u$
 $dx=-du$

$$\int_{0}^{1} (1+3x) (1-x)^{7} dx = \int_{0}^{1} (4-3u) u^{7} \cdot (-du)$$

$$= \int_{0}^{1} 4u^{7} - 3u^{8} du$$

$$= \left[\frac{u^{8}}{2} - \frac{u^{9}}{3} \right]_{0}^{1}$$

$$= \frac{1}{2}$$

(ii) LHS =
$$\frac{1}{1+\sin\theta} \cdot \frac{1-\sin\theta}{1-\sin\theta}$$

$$= \frac{1-\sin\theta}{\cos^2\theta}$$

$$= \sec^2\theta - \sec\theta + \tan\theta$$

$$= RHS \#$$

(iii)
$$\int \frac{1}{1+\sin\theta} d\theta = \int cec^2\theta - sec\theta \tan\theta d\theta$$
$$= \tan\theta - sec\theta + C \qquad (iv)$$

c) (i)
$$A_0 = P$$

 $A_1 = P(1+R) - M$
 $A_2 = P(1+R)^2 - M(1+R) - M$
 \vdots
 $A_n = P(1+R)^2 - M[1+R)^{n-1} + \dots + (1+R) + 1$

$$= \rho (HR)^{2} - \frac{m[(HR)^{2} - 1]}{R}$$
(ii) Here $A_{n} = 0$ so $\rho = \frac{m[(HR)^{2} - 1]}{R(HR)}$

5 a) (i) x = -3 in 3t + 6 cm 3t x = - 9 con 3t - 18 sin 3t $= -3^{1}(\cos 3t + 2\sin 3t)$ (1) (ii) (= 1 + 2 = 5 so in == 15 and us == == **(** lun 1= JF , x = m'(1/3) **(** (=0.46 rads) (iii) r in pt +a) = 2 0 的 3七= 流(法)- 流(法) ヒ= う[い(た)-い(は)] 0 ± 0.2 to 1 dec. M. **b**) 0 exterior angle of again quadrilateral. (i) LOAR = LUDR (angle is altorate segrent) ① (ii) here QA 11 PS (works, pording angles equal) **(**) LPAS = LTPS (augle in the segment) (iii) = LORA (exterior angle of cyclic quadrilateral) (1) here in DORA and DPAS LOAR = LESA LPAS = LARA pover (i) eles DQRAIII DPAS (AA) ന C) (i) 4a (ii) is de right hand graph, the found high is ⚾ larger but the laters rectum is showler.

6 a) (i) 2 w g/min

(iii)

(ii) <u>a</u> g/L

1000 8/2 000 g/min

(i)

(iv) $\frac{dQ}{dt} = \text{iffor } - \text{outflows}$

 $= 2\omega - \frac{Q\omega}{1000} = -\frac{\omega}{1000} (Q - 2000)$

(v) LH1 = $-\frac{\omega}{1000} \cdot Ae^{-\omega t/1000}$ RH1 = $-\frac{\omega}{1000} \left(\frac{2000 + Ae^{-\omega t/1000}}{-2000} - \frac{2000}{1000} \right)$ = $-\frac{\omega}{1000} Ae^{-\omega t/1000}$

= LHI. #

(vi) at t=0 Q=0 so A = -2000and $Q = 2000 (1 - e^{-\omega t/0000})$

(Vii) at +00, e -10t/1000 →0 hua Q → 2000

(Viii) $1000 = 2000 (1 - e^{-1345/000})$ $e^{345/1800} = 2$

 $\omega = \frac{1000}{345} \log 2$ (= 2 L/min.)

b) (i)

(odle graphs)

(are possible)

(ii) for x < a for is weare down

for x > a for is weare up

herce for changes concernity and there is an infusion point.

More precisely, for the curve to rise from to 12 return to the x-axis it must be concave to the x-axis it must be concave.

Also for must

(ii)

(ii) along each tooth of radius
$$r$$
 the art travels $r(x+sinx)$ each successive tooth has radius corn times the previous $y = (x+sinx) + corn (x+sinx) + corn (x+sinx) + ...$

$$= \frac{x + y + x}{1 - w + x}$$

(iii)
$$y' = \frac{(-\omega x)(1+\omega x) - (x+\omega x)(\omega x)}{(1-\omega x)^{2}}$$

$$= \frac{\sin^{2}x - x \omega x - \omega^{2}x}{(1-\omega x)^{2}}$$

$$= \frac{-x \omega x}{(1-\omega x)^{2}} < 0 \text{ for } 0 < x \leq \frac{\pi}{2}$$
(1)

$$y(\tilde{z}) = \frac{\tilde{z}+1}{1-0} = \tilde{z}+1$$

$$o=A, A_0$$

(1)

(1)

(B)
$$a^2 + 2ar - t^2 = 0$$

$$a^2 + 2ar + r^2 = t^2 + r^2$$

$$(a+r)^2 = t^2 + r^2$$

$$a+r = \sqrt{t^2 + r^2}$$

