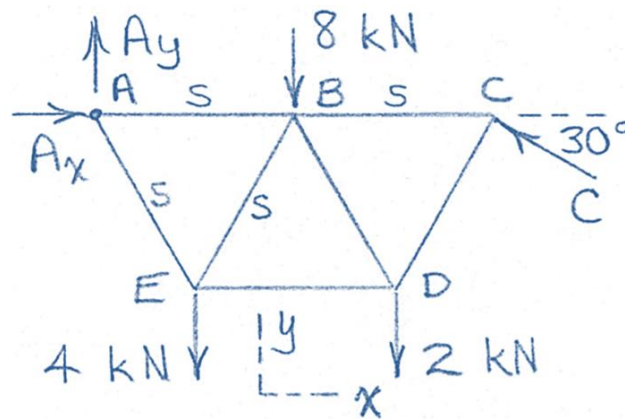
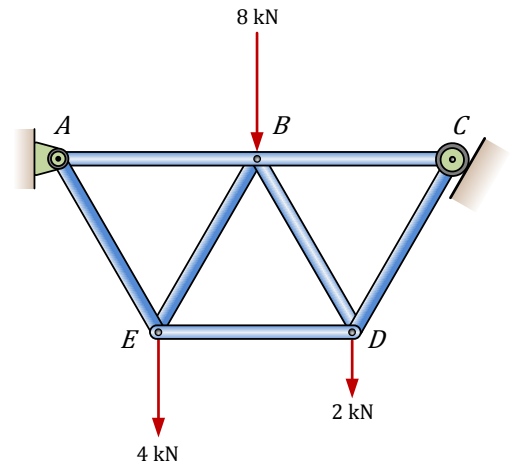


## Question 3.10.

Determine the magnitude and nature of forces in each member of the loaded truss. All triangles are equilateral.

### Solution



Consider the equilibrium of the whole truss

$$+\circlearrowleft \sum M_A = 0$$

$$-8s - 4\left(\frac{s}{2}\right) - 2\left(\frac{3s}{2}\right) + C \sin 30^\circ (2s) = 0$$

$$C = 13 \text{ kN}$$

$$+\rightarrow \sum F_x = 0$$

$$A_x - C \cos 30^\circ = 0$$

$$A_x - 13 \cos 30^\circ = 0$$

$$A_x = 13 \frac{\sqrt{2}}{2} = 11.26 \text{ kN}$$

$$+\uparrow \sum F_y = 0$$

$$C \sin 30^\circ - 4 - 2 - 8 + A_y = 0$$

$$A_y = 14 - 13 \sin 30^\circ = 7.5 \text{ kN}$$

### Joint A

$$+\uparrow \sum F_y = 0$$

$$7.5 - AE \sin 60^\circ = 0$$

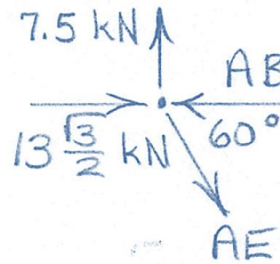
$$AE = 5\sqrt{3} = 8.66 \text{ kN (T)} \quad \text{(Answer)}$$

$$+\rightarrow \sum F_x = 0$$

$$11.26 - AB + AE \cos 60^\circ = 0$$

$$11.26 - AB + 8.66 \cos 60^\circ = 0$$

$$AB = 9\sqrt{3} = 15.59 \text{ kN (C)} \quad \text{(Answer)}$$



### Joint E

$$+\uparrow \sum F_y = 0$$

$$5\sqrt{3} \sin 60^\circ - BE \sin 60^\circ - 4 = 0$$

$$BE = 7\left(\frac{\sqrt{3}}{3}\right) = 4.04 \text{ kN (C)}$$

(Answer)

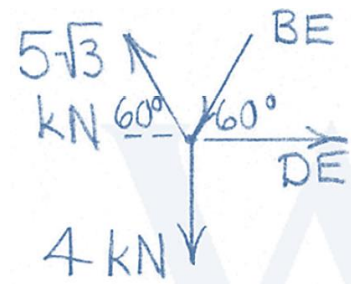
$$+\rightarrow \sum F_x = 0$$

$$DE - 5\sqrt{3} \cos 60^\circ - BE \cos 60^\circ = 0$$

$$DE - 5\sqrt{3} \cos 60^\circ - 7\left(\frac{\sqrt{3}}{3}\right) \cos 60^\circ = 0$$

$$DE = 11\left(\frac{\sqrt{3}}{3}\right) = 6.35 \text{ kN (T)}$$

(Answer)



### Joint D

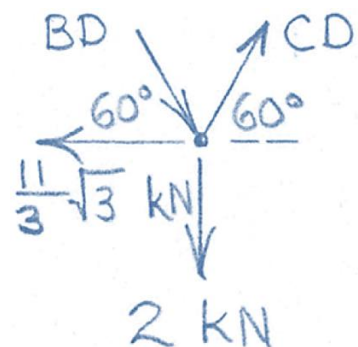
$$+\uparrow \sum F_y = 0$$

$$CD \sin 60^\circ - BD \sin 60^\circ - 2 = 0 \quad \text{----- (a)}$$

$$+\rightarrow \sum F_x = 0$$

$$CD \cos 60^\circ + BD \cos 60^\circ - 11\left(\frac{\sqrt{3}}{3}\right) = 0$$

----- (b)



Solving (a) and (b) simultaneously

$$CD = 13 \left( \frac{\sqrt{3}}{3} \right) = 7.505 \text{ kN (T)}$$

(Answer)

$$BD = 3\sqrt{3} = 5.196 \text{ kN (C)}$$

(Answer)

Joint C

$$+\rightarrow \sum F_x = 0$$

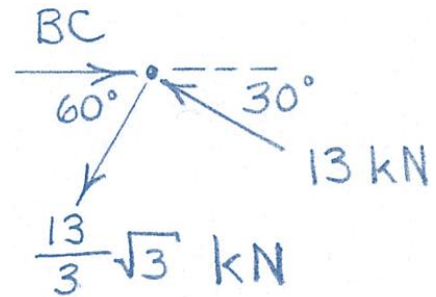
$$BC - 13 \cos 30^\circ - 13 \left( \frac{\sqrt{3}}{3} \right) \cos 60^\circ = 0$$

$$CD = 13 \left( \frac{\sqrt{3}}{3} \right) = 7.505 \text{ kN (T)}$$

(Answer)

$$BC = 26 \left( \frac{\sqrt{3}}{3} \right) = 15.01 \text{ kN (C)}$$

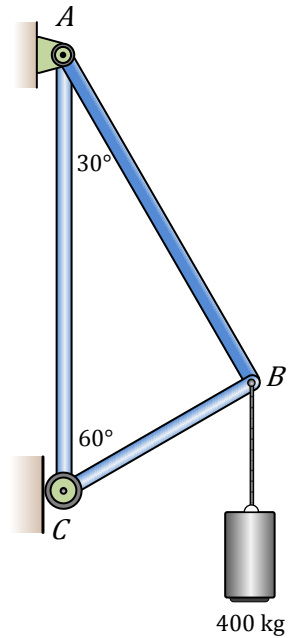
(Answer)



### Question 3.11.

Determine the magnitude and nature of forces in each member of the loaded truss.

#### Solution



#### Joint B

$$+\rightarrow \sum F_x = 0$$

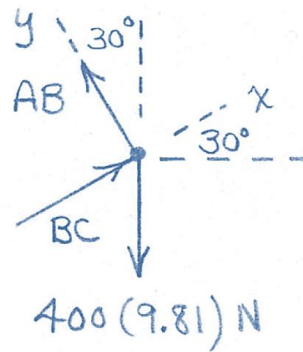
$$BC - 400(9.81) \cos 60^\circ = 0$$

$$BC = 1962 \text{ N (C)} \quad (\text{Answer})$$

$$+\uparrow \sum F_y = 0$$

$$AB - 400(9.81) \sin 60^\circ = 0$$

$$AB = 3400 \text{ N (T)} \quad (\text{Answer})$$

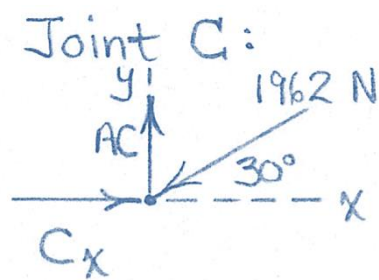


#### Joint C

$$+\uparrow \sum F_y = 0$$

$$AC - 1962 \sin 30^\circ = 0$$

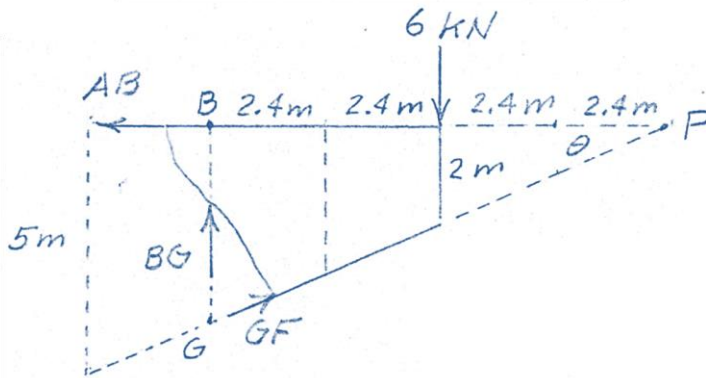
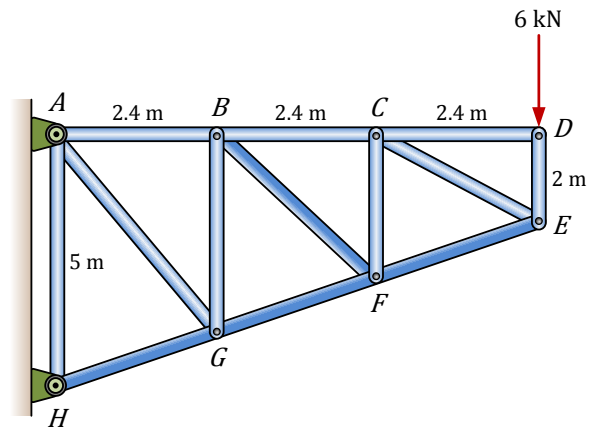
$$AC = 981 \text{ N (T)} \quad (\text{Answer})$$



### Question 3.12.

Determine the magnitude and nature of the forces in members  $AB$ ,  $BG$  and  $GF$ .

### Solution



$$\tan \theta = \frac{5}{12}$$

$$\cos \theta = \frac{12}{13}$$

$$+\circlearrowleft \sum M_D = 0$$

$$BG(8)(2.4) - 6(2)(2.4) = 0$$

$$BG = 3 \text{ kN (C)} \quad \text{(Answer)}$$

$$+\circlearrowleft \sum M_B = 0$$

$$GF \left( \frac{12}{13} \right) (4) - 6(2)(2.4) = 0$$

$$GF = 7.8 \text{ kN (C)} \quad \text{(Answer)}$$

$$+\circlearrowleft \sum M_G = 0$$

$$AB(4) - 6(2)(2.4) = 0$$

$$AB = 7.2 \text{ kN (T)} \quad \text{(Answer)}$$

### Question 3.13.

Determine the force in members  $EF$ ,  $CF$ , and  $BC$ , and state if the members are in tension or compression.

### Solution

*Support Reactions. Not required.*

*Method of Sections:  $F_{BC}$  and  $F_{EF}$  can be determined directly by writing the moment equations of equilibrium about points  $F$  and  $C$ , respectively, by referring to the FBD of the upper portion of the truss section through  $a-a$  shown below.*

$$+\circlearrowleft \sum M_F = 0$$

$$F_{BC}(1.5) - 4(2) = 0$$

$$F_{BC} = 5.33 \text{ kN (C)} \quad \text{(Answer)}$$

$$+\circlearrowleft \sum M_C = 0$$

$$F_{EF}(1.5) - 4(2) = 0$$

$$F_{EF} = 5.33 \text{ kN (T)} \quad \text{(Answer)}$$

*Also, write the force equation of equilibrium along the  $x$  axis,*

$$+\rightarrow \sum F_x = 0$$

$$4 - F_{CF} = 0$$

$$F_{CF} = 4 \text{ kN (T)} \quad \text{(Answer)}$$

