Study Problems Week 4 – Frames, Machines, Friction and Springs

Question 4.11.

Determine the components of all forces acting on each member of the loaded frame.

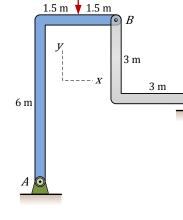
Solution

BC is a two force member

$$+$$
 $\leq M_A = 0$

$$-5(1.5) + B\cos 45^{\circ}(6) + B\sin 45^{\circ}(3) = 0$$

$$B = 1.179 \text{ kN}$$



Resolving into components

$$B_x = -B\cos 45^\circ$$

$$B_x = -0.833 \text{ kN}$$

(Answer)

$$B_{\rm v} = B \sin 45^{\circ}$$

$$B_{\rm v} = 0.833 \, {\rm kN}$$

(Answer)

$$+\uparrow \sum F_{\nu} = 0$$

$$A_{\nu} + B \sin 45^{\circ} - 5 = 0$$

$$A_{\nu} + (1.179) \sin 45^{\circ} - 5 = 0$$

$$A_y = 4.166 \text{ kN}$$

(Answer)

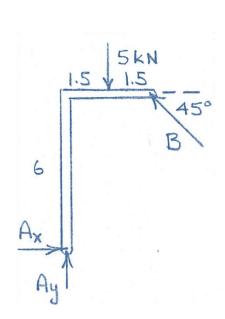
$$+ \rightarrow \sum F_x = 0$$

$$A_x - B\cos 45^\circ = 0$$

$$A_x - B\cos 45^\circ = 0$$

$$A_x = 0.833 \text{ kN}$$

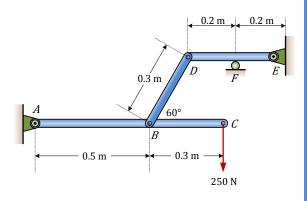




Question 4.12.

Determine the reaction at the roller F for the frame loaded as shown.

Solution

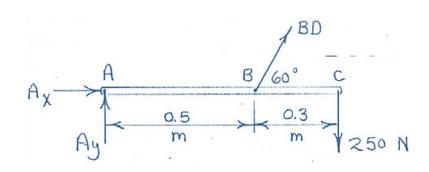


Consider member ABC

$$+ \circlearrowleft \sum M_A = 0$$

$$-250(0.8) + BD \sin 60^{\circ}(0.5) = 0$$

$$BD = 462 \text{ N}$$

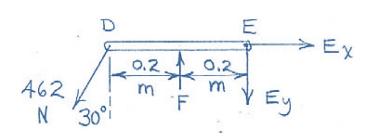


Consider member DE

$$+\circlearrowleft \sum M_E = 0$$

$$462\cos 30^{\circ}(0.4) - F(0.2) = 0$$

$$F = 800.2 \text{ N} \qquad \text{(Answer)}$$



Question 4.13.

The cable makes 20° angle with the horizontal and the beam CD is horizontal, when the crank AB is vertical. Calculate the moment M required for the frame to be in equilibrium.

Solution

0.65 m 0.5 m 0.2 m 0.2 m 0.2 m

FBD of the pulley

$$+ \rightarrow \sum F_{x} = 0$$

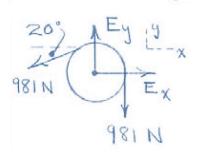
$$E_x - 981\cos 20^\circ = 0$$

$$E_x = 922 \text{ N}$$

$$+\uparrow \Sigma F_y = 0$$

$$E_y - 981\sin 20^\circ - 981 = 0$$

$$E_y = 1317 \text{ N}$$



FBD of member CDE

$$\theta = \tan^{-1}\left(\frac{1.15}{1}\right) = 48.99^{\circ}$$

$$+ \circlearrowleft \sum M_C = 0$$

$$-1317(3) - 922(0.6) + BD \sin 48.99^{\circ} = 0$$

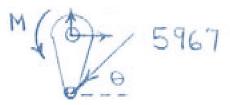
$$BD = 5967 \text{ N}$$

FBD of crank AB

$$+ \circlearrowleft \sum M_A = 0$$

$$M - 5967 \cos 48.99^{\circ} (0.5) = 0$$

$$M = 1958 \text{ N. m}$$
 (Answer)

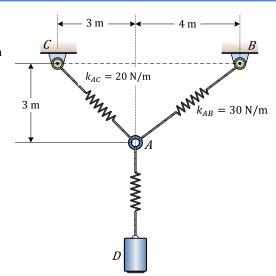


Question 4.14.

Determine the mass of the block at D, if the block is held in the equilibrium position shown. The spring AB is 3 m long when unstretched.

Solution

$$F = kx = 30(5 - 3) = 60 \text{ N}$$



$$+ \rightarrow \sum F_x = 0$$

$$T\cos 45^\circ - 60\left(\frac{4}{5}\right) = 0$$

$$T = 67.88 \text{ N}$$

$$+\uparrow \Sigma F_y = 0$$

$$67.88\sin 45^{\circ} - W + 60\left(\frac{3}{5}\right) = 0$$

$$W = 84 \text{ N}$$

$$m = \frac{W}{g}$$

$$m = \frac{84}{9.81} = 8.56 \text{ kg}$$

(Answer)