# Hand-in Problems Week 4 – Frames, Machines, Friction and Springs (complete by W5)

# Question 4.7.

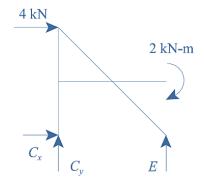
Determine the horizontal and vertical components of forces at pins B and C.

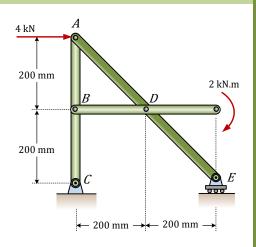
#### Solution

Draw the FBD of the entire structure

$$+ \rightarrow \sum F_x = 0$$
 $C_x + 4 = 0$ 
 $C_x = -4 \text{ kN } (\rightarrow)$  (Answer)

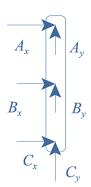
$$+\circlearrowleft \sum M_E = 0$$
  
 $-2 - C_y(0.4) - 4(0.4) = 0$   
 $C_y = -9 \text{ kN ($\uparrow$)}$  (Answer)





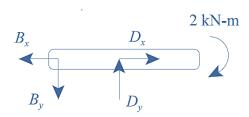
Draw the FBD of body ABC

$$+\circlearrowleft \sum M_A = 0$$
 
$$B_x(0.2) + C_x(0.4) = 0$$
 
$$B_x(0.2) + (-4)(0.4) = 0$$
 
$$B_x = 8 \text{ kN } (\to)$$
 (Answer)



Draw the FBD of body BD

$$+\circlearrowleft \sum M_D = 0$$
  
 $B_y(0.2) - 2 = 0$   
 $B_y = 10 \text{ kN } (\downarrow)$  (Answer)



# Question 4.8.

Determine the reactions at member ABCD at joints A, C and D.

#### Solution

#### Solution

Draw the FBD of the entire structure

$$+ \circlearrowleft \sum M_A = 0$$

$$D_{y}(0.6) - 600(1) = 0$$

$$D_y = 1000 \text{ N} (\uparrow)$$

(Answer)

$$+ \rightarrow \sum F_{x} = 0$$

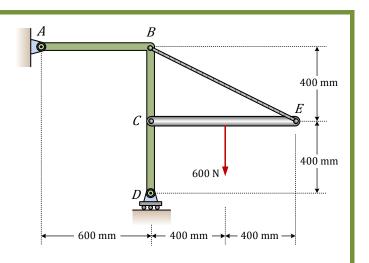
$$A_x = 0$$

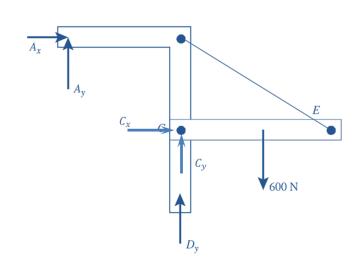
(Answer)

$$+\uparrow \Sigma F_y = 0$$

$$D_y + A_y - 600 = 0$$

$$A_y = -400 \text{ N} (\uparrow)$$
 (Answer)





Now examine bar CE. Note that the reactions on ABD are opposite to those on CE

$$+ \circlearrowleft \sum M_E = 0$$

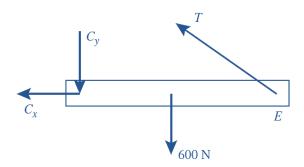
$$600(0.4) + C_y(0.8) = 0$$

$$C_y = -300 \text{ N } (\downarrow)$$
 (Answer)

$$+ \circlearrowleft \sum M_B = 0$$

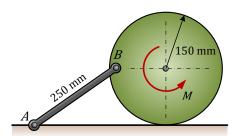
$$-C_x(0.4) - 600(0.4) = 0$$

$$C_x = -600 \text{ N } (\leftarrow)$$
 (Answer)



# Question 4.9.

The strut AB of negligible mass is hinged to the horizontal surface at A and to the uniform 25 kg wheel at B. Determine the minimum couple M applied to the wheel which will cause it to slip if the coefficient of static friction between the wheel and the surface is 0.40.



## Solution

$$\sin \theta = \frac{150}{250} = 0.6$$

$$\cos \theta = 0.8$$

$$\overline{AC} = \overline{AB}\cos\theta + 0.15$$

$$\overline{AC}$$
 = (0.25)0.8 + 0.15 = 0.35 m

$$+ \rightarrow \sum F_x = 0$$

$$P\cos\theta - 0.4 = 0$$

$$P(0.8) - 0.4N = 0$$
 ---- (a)

$$+\uparrow \Sigma F_y = 0$$

$$N + P(0.6) - 25(9.81) = 0$$
 ----- (b)

$$+ \circlearrowleft \sum M_A = 0$$

$$M - 25(9.81)(0.35) + N(0.35) = 0$$
 ----- (c)



$$N = 188.7 \text{ N}$$

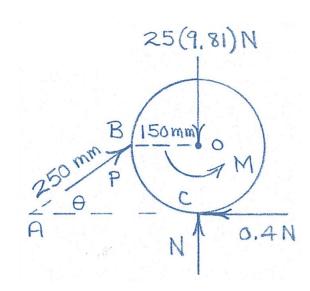
(Answer)

$$M = 19.81 \text{ N. m}$$

(Answer)

$$P = 94.3 \text{ N}$$

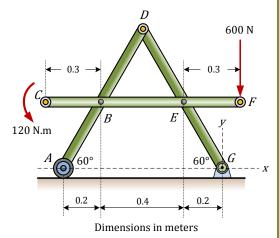
(Answer)



# Question 4.10.

Calculate the x - and y - components of all forces acting on each member of the loaded frame.

## Solution



As a whole

$$+ \circlearrowleft \sum M_G = 0$$

$$120 - A_{y}(0.8) - 600(0.1) = 0$$

$$A_{\nu} = 75 \text{ N}$$

(Answer)

$$+\uparrow \sum F_{\nu} = 0$$

$$G_y + A_y - 600 = 0$$

$$G_y + 75 - 600 = 0$$

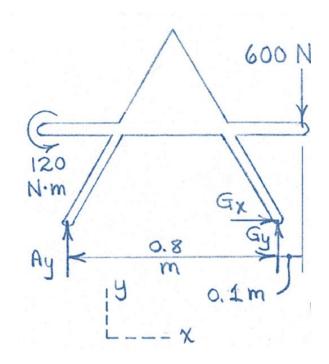
$$G_y = 525 \text{ N}$$

(Answer)

$$+ \rightarrow \sum F_x = 0$$

$$G_x=0$$

(Answer)



Member CF

$$+\circlearrowleft \sum M_B = 0$$

$$120 + E_{\nu}(0.4) - 600(0.7) = 0$$

$$E_{\nu} = 750 \text{ N}$$

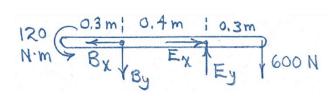
(Answer)

$$+\uparrow \Sigma F_y = 0$$

$$750 - 600 - B_y = 0$$

$$B_y = 150 \text{ N}$$

(Answer)



Member AD

$$+\uparrow \Sigma F_y = 0$$

$$75 - 150 - D_y = 0$$

$$D_y = 225 \text{ N}$$
 (Answer)

$$+ \circlearrowleft \sum M_B = 0$$

$$0.346D_x + 0.2(225) - 0.2(75) = 0$$

$$D_x = 173.2 \text{ N}$$
 (Answer)

$$+ \rightarrow \sum F_x = 0$$

$$B_x - 173.2 = 0$$

$$B_x = 173.2 \text{ N}$$
 (Answer)

Member DG

$$+ \rightarrow \sum F_{x} = 0$$

$$173.2 - E_x = 0$$

$$E_x = 173.2 \text{ N}$$
 (Answer)

