Student Name: ☞

Student ID: ☞

PSS Room/Demonstrator: ☞

School of Mechanical and Manufacturing Engineering

MMAN1300 – ENGINEERING MECHANICS 1

2018 S1 Block Test 4

Instructions:

- Time allowed: 45 minutes
- Total number of questions: 3
- Answer all the questions in the test
- Answer all questions in the spaces provided
- The 6 marks allocations shown are worth 6% of the course overall
- Candidates may bring drawing instruments, rulers and UNSW approved calculators to the test
- Print your name, student ID and all other requested details above
- Record your answers (with appropriate units) in the ***ANSWER BOXES*** provided

Notes:

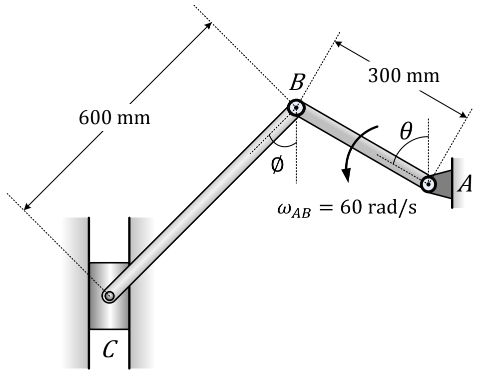
Your work must be complete, clear and logical

Do not skip steps, sign conventions, units and relevant diagrams and clearly state the final answers

No part of this paper is to be retained by candidates until handed back after marking

Question 1: (2 Marks)

Link *AB* is rotating with an angular velocity of $\omega_{AB} = 60\ \mathrm{rad/s}$. Determine the velocity of the slider block *C* and the angular velocity of link *BC* at the instant $\theta = 60°$ and $\emptyset = 45°$.



Solution:

Perform the relative velocity analysis for link AB:

$$v_B = v_A + v_{B/A}$$

Construct the velocity triangle for the following velocities (directions are essential for all three velocities):

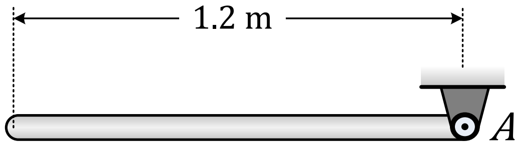
$$v_C = v_B + v_{C/B}$$

Obtain the velocity of the slider block C (v_C) *and the angular velocity of link BC* (ω_{BC}):

Answers:	$v_C =$	$\omega_{BC} =$

Question 2: (2 Marks)

The 5-kg slender bar is released from rest in the horizontal position shown. At the instant it is released, determine (a) the bar's counterclockwise angular acceleration, and (b) the horizontal and vertical components of the reaction at the pin *A*.



Solution:

Present your solution here (including the free-body diagram if needed):

If needed *use the following information:*

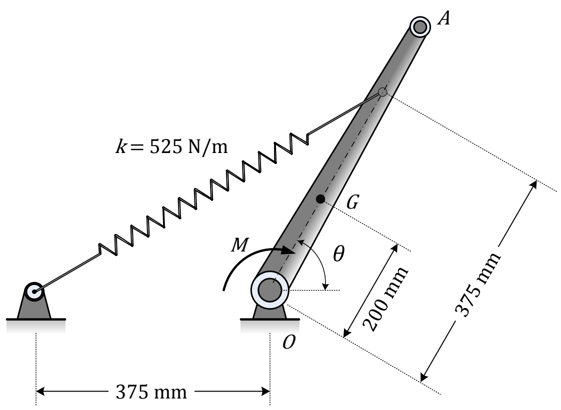
Normal component of acceleration = $r\omega^2$
Tangential component of acceleration = αr
Mass moment of inertia of a slender rod about its centre of mass = $ml^2/12$

Continue your solution to Question 2 here:

Answers:	A_x	$A_y =$	$\alpha =$

Question 3: (2 Marks)

The tapered 5.5 kg lever *OA* with mass moment of inertia of $0.344\ \text{kg.m}^2$ about *O*, is initially at rest in the vertical position ($\theta = 90°$), where the attached spring of stiffness $k = 525\ \text{N/m}$ is unstretched. A constant moment **M** is applied to the lever at *O* that will give the lever an angular velocity $\omega = 4\ \text{rad/s}$ as the lever reaches the horizontal position $\theta = 0$.



Solution:

(a) Calculate the change in elastic potential energy (ΔV_e), gravitational potential energy (ΔV_g) resulting from the lever moving from $\theta = 90°$ to $\theta = 0°$:

(b) Calculate the change in kinetic energy (ΔT) when the lever reaches $\theta = 0°$ and calculate the constant moment M required to achieve the final angular velocity of $\omega = 4$ rad/s:

Answers:	$\Delta V_e =$	$\Delta V_g =$	$\Delta T =$	$M =$

Equation Sheet

Linear motion

$$v = \frac{ds}{dt} \qquad a = \frac{dv}{dt} \qquad v\,dv = a\,ds$$

Constant linear acceleration equations $(t_o = 0)$

$$v = v_o + at \qquad v^2 = v_o^2 + 2a(s - s_o) \qquad s = s_o + v_o t + \frac{1}{2}at^2$$

Angular motion

$$\omega = \frac{d\theta}{dt} \qquad \alpha = \frac{d\omega}{dt} \qquad \omega\,d\omega = \alpha\,d\theta$$

Displacement, velocity and acceleration components

Rectangular coordinates

$$\mathbf{r} = x\mathbf{i} + y\mathbf{j} \qquad \mathbf{v} = \dot{x}\mathbf{i} + \dot{y}\mathbf{j} \qquad \mathbf{a} = \ddot{x}\mathbf{i} + \ddot{y}\mathbf{j}$$

Normal and tangential coordinates

$$\mathbf{v} = v\mathbf{e_t} \qquad \mathbf{a} = a_t\mathbf{e_t} + a_n\mathbf{e_n} \qquad v = \omega r \qquad a_t = \dot{v} = \alpha r \qquad a_n = \frac{v^2}{\rho} = \omega^2 r$$

Relative motion

$$\mathbf{r}_A = \mathbf{r}_B + \mathbf{r}_{A/B} \qquad \mathbf{v}_A = \mathbf{v}_B + \mathbf{v}_{A/B} \qquad \mathbf{a}_A = \mathbf{a}_B + \mathbf{a}_{A/B}$$

Equation of motion (Newton's 2nd law)

$$\sum \mathbf{F} = m\mathbf{a}$$

Work-Energy

$$W_{1-2} = \Delta T + \Delta V_g + \Delta V_e \qquad W_{1-2} = F\Delta s \text{ and/or } M\Delta\theta$$

$$\Delta T = \frac{1}{2}m\left(v_2^2 - v_1^2\right) \text{ and/or } \frac{1}{2}I\left(\omega_2^2 - \omega_1^2\right)$$

$$\Delta V_g = mg(h_2 - h_1)$$

$$\Delta V_e = \frac{1}{2}k\left(x_2^2 - x_1^2\right) \quad \text{for a linear spring}$$

For a rigid body in plane motion

$$\sum \mathbf{F} = m\mathbf{a} \qquad \sum M = I\alpha$$

Mass moment of inertia $\quad I = \int r^2 dm$

Centroid of a cross-section:

$$\bar{x} = \frac{\int x\,dA}{\int dA} = \frac{\sum_i x_i A_i}{\sum_i A_i}, \quad \bar{y} = \frac{\int y\,dA}{\int dA} = \frac{\sum_i y_i A_i}{\sum_i A_i}$$

DATA: Acceleration in free fall due to gravity g = 9.81 m/s^2

Quadratic formula:

For: $ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$