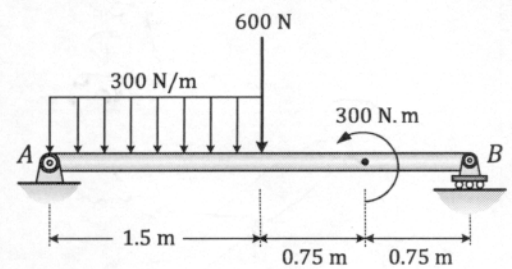


Question 2:

(2 Marks)

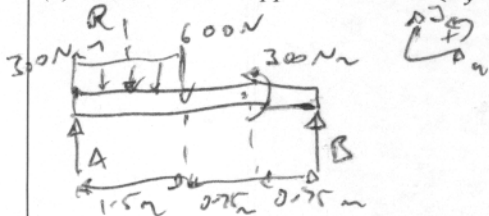
A simply supported beam AB is subjected to the loads and moment as shown. Determine the following:

(Proceed according to the steps provided in solution boxes)



Solution:

(a) Determine the support reactions (A_y and B_y)



$$R = 300 \times 1.5 = 450 \text{ N}$$

$$\sum M_A = 0$$

$$-450\left(\frac{1.5}{2}\right) - 600(1.5) + 300 + B(3) = 0$$

$$\therefore B = 312.5 \text{ N} \uparrow$$

$$\sum F_y = 0$$

$$A - R - 600 + B = 0$$

$$A = 450 + 600 - 312.5 = 737.5 \text{ N} \uparrow$$

(b) Draw the free body diagram, shear force diagram and bending moment diagram, on the axis provided.
(Use this space for relevant working **if needed** else you are free to draw the SFD and BMD by inspection)

$$0 < x < 1.5$$

$$\sum F_y = 0$$

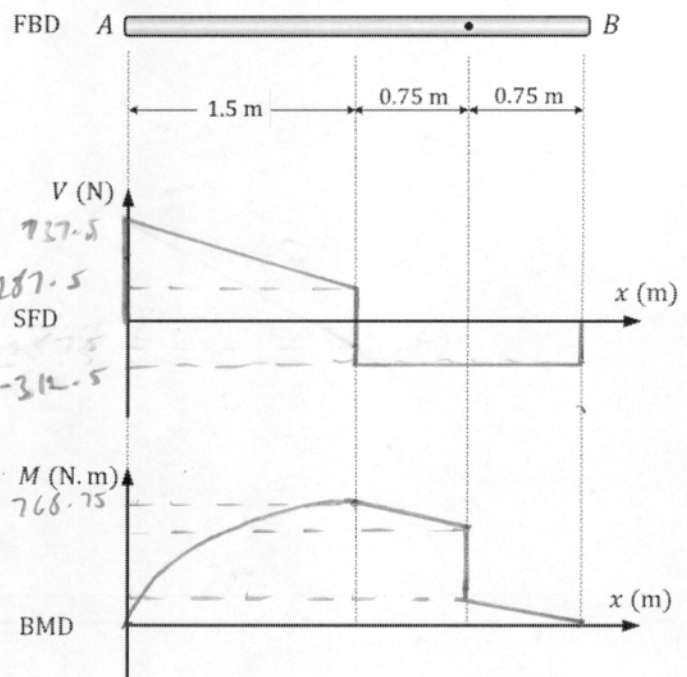
$$A - R + V = 0$$

$$V = 737.5 - 450 = 287.5 \text{ N} \uparrow$$

$$\sum M = 0$$

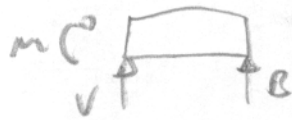
$$-A(1.5) + R\left(\frac{1.5}{2}\right) + M = 0$$

$$M = 768.75 \text{ N.m} \curvearrowright$$



Continue your working for part (b) here:

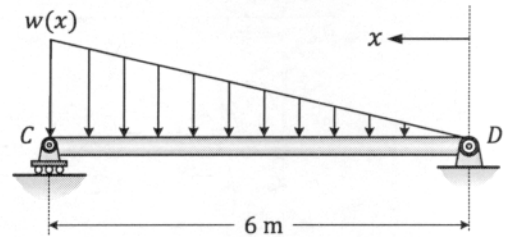
$$2.25 < x < 3$$



The bending moment function for the loaded beam shown is given as:

$$M(x) = 6x - \frac{x^3}{6} \quad (\text{kN.m})$$

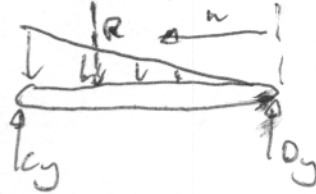
Knowing that $\frac{d^2 M(x)}{dx^2} = -w(x)$, determine the loading function $w(x)$ and then calculate the support reactions C_y and D_y at C and D respectively.



$$\frac{dM(x)}{dx} = 6 - \frac{x^2}{2}$$

$$\frac{d^2 M(x)}{dx^2} = -x$$

$$\therefore w(x) = x$$



$$R = w(6) = 6 \text{ kN} \downarrow$$

$$\sum M_D = 0$$

$$-C_y(6) + R\left(\frac{2}{3} \times 6\right) = 0$$

$$\therefore C_y = 4 \text{ kN} \uparrow$$

$$\sum F_y = 0$$

$$C_y + D_y - R = 0$$

$$\therefore D_y = 2 \text{ kN} \uparrow$$

2.1

Using the bending moment function given above, determine the location x_{\max} and the magnitude M_{\max} of the maximum bending moment.

$$\text{For } M_{\max}: \frac{dM(x)}{dx} = 0$$

$$\therefore 6 - \frac{x^2}{2} = 0$$

$$\therefore x = 2\sqrt{3} \text{ m}$$

$$\therefore M_{\max} = 6 \times (2\sqrt{3}) - \frac{(2\sqrt{3})^3}{6}$$

$$= 13.9 \text{ kNm}$$

Answers:

$$C_y = 4 \text{ kN} \uparrow$$

$$D_y = 2 \text{ kN} \uparrow$$

$$x_{\max} = 2\sqrt{3} \text{ m}$$

$$M_{\max} = 13.9 \text{ kNm}$$



Index of comments

2.1 not correct