

MMAN2300

Engineering Mechanics 2

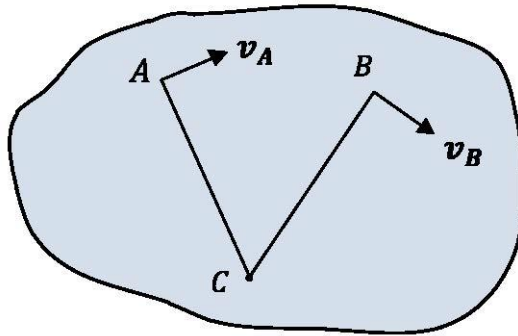
Part A: Week 3

Method of instant centres

(Chapter 5/5 Meriam & Kraige,
Chapter 4 Waldron & Kinzel)

1. Instantaneous centres of zero velocity

At every instant during the motion of a rigid body in a plane there exists a point that is instantaneously at rest. This point is called the instantaneous centre of zero velocity.



The body rotates about C instantaneously.

Note:

- (1) The location of an instantaneous centre can be determined by the directions of two velocities.
- (2) Point C may lie on or off the body and C may not be fixed.
- (3) At the instant shown, $v_C = 0$ m/s. Point C is called the instantaneous centre of zero velocity.

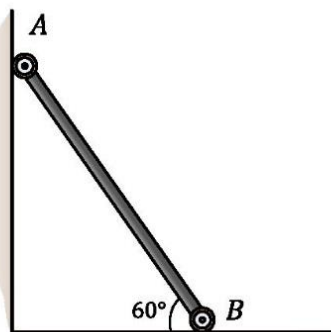
Applications of the instantaneous centre of zero velocity:

- To determine the linear velocity of any points in the body;
- To determine the direction of the instant velocity of any points in the body.

Example 1

Given: $AB = 4$ m and $v_A = 2$ m/s \downarrow

Find v_B and ω_{AB} . Use the method of instantaneous centre of zero velocity.



2. Instant Centres

Definition: Given two bodies 2 & 3 moving with planar motion relative to each other in a reference frame R , there is, in general, one and only one location in the plane motion where the coincident points at a given instant have the same velocity with respect to the reference R . One coincident point is in body 2 and the other in body 3. This location is called the instant centre of velocity for bodies 2 & 3, and is represented by 23 or 32.

$$\mathbf{v}_{23(2)} = \mathbf{v}_{23(3)}$$

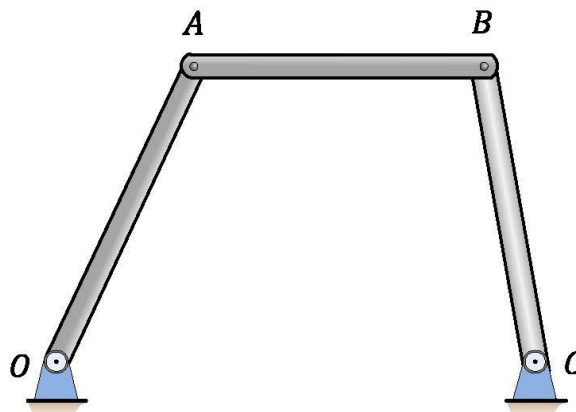
i.e., At any instant we can find a common point to two bodies which has the same instantaneous velocity in each body.

$$\mathbf{v}_{23(2)} = \omega_2(\overline{12 - 23})$$

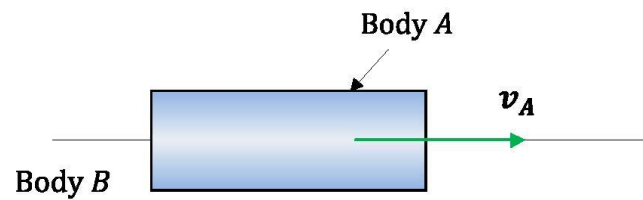
$$\mathbf{v}_{23(3)} = \omega_3(\overline{13 - 23})$$

$$\Rightarrow \omega_2(\overline{12 - 23}) = \omega_3(\overline{13 - 23})$$

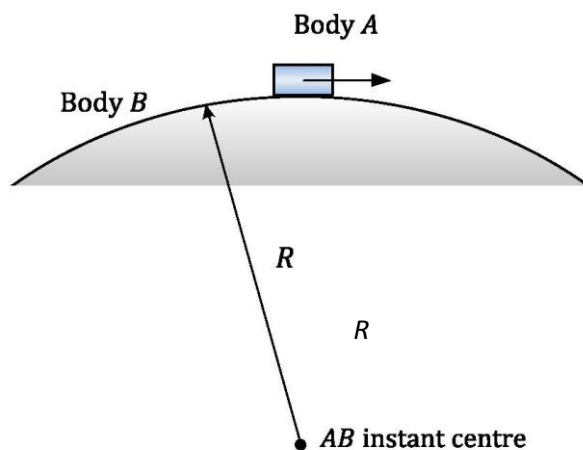
Example 2: Locate instant centres (common points)



- Location of an instant centre can tend toward infinity



- An instant centre needs not be physically located on each link. It may be located on an imaginary extension to a link
- An instant centre can also be considered as a point about which one body rotates relative to another body at a given instant



Body A is a block moving on a circular arc on body B.

The centre of the arc (AB) is the instant centre of both bodies.

3. Three Centre Theorem (Kennedy's Theorem)

Kennedy's Theorem consists of two major components:

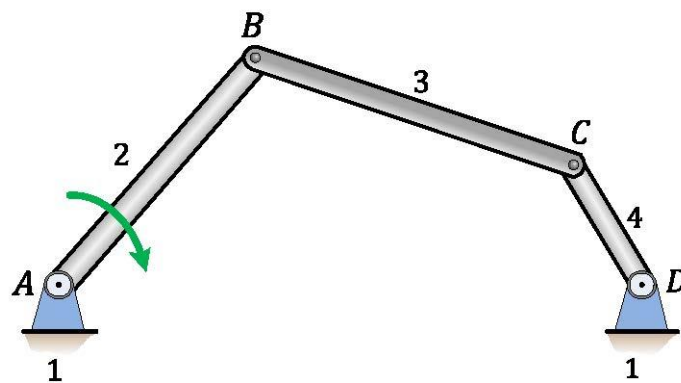
(a) If there are n bodies and we take them two at a time, the total number of instant centres are:

$$N_{Ic} = \frac{n(n-1)}{2}$$

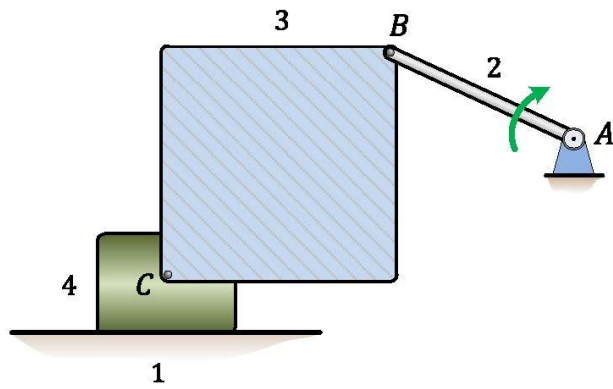
(b) Three Centre Theorem: The 3 instant centres for 3 independent bodies in plane motion will lie on a straight line.

Example 3: Locate all instant centres for the following mechanisms

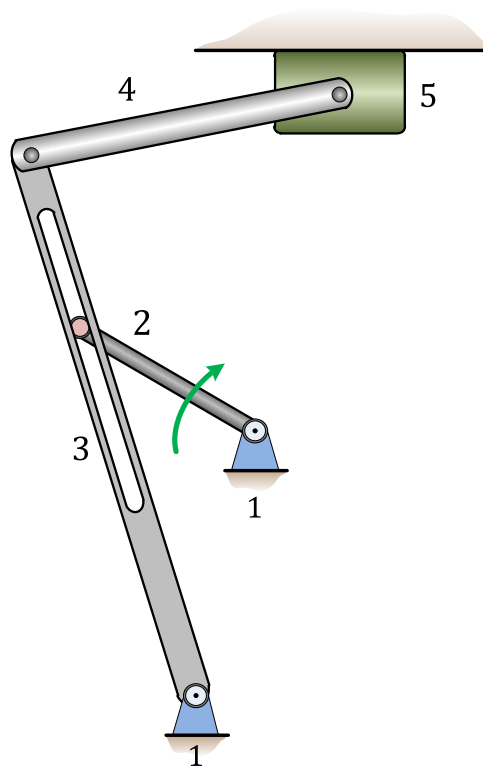
(a)



(b)



(c)



Example 4

At the instant shown, bar AB has a clockwise angular velocity of $\omega = 4 \text{ rad/s}$. Using the method of instant centres, calculate:

- (a) the velocity of point C ,
- (b) the angular velocities of links BC and CD .

