MTRN4110 Robot Design Week 2 – Localisation I

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Today's agenda

Introduction to Localisation

Map Representation

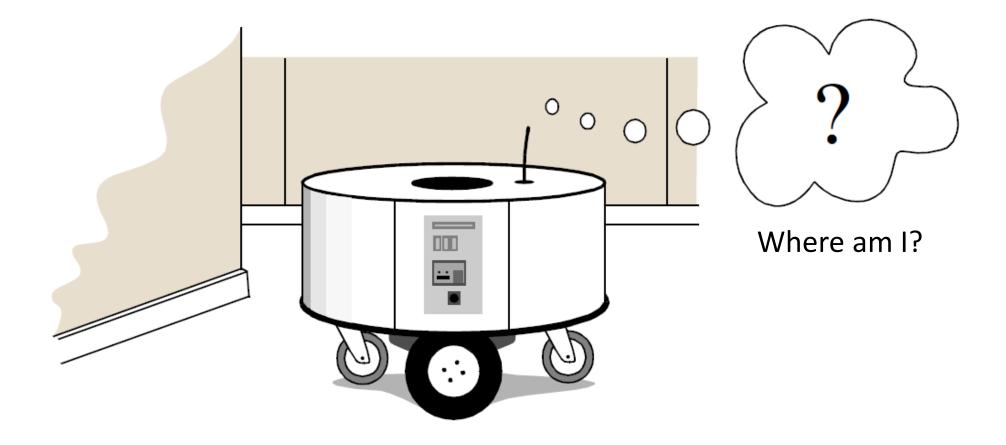
Localisation Methods



Introduction to Localisation

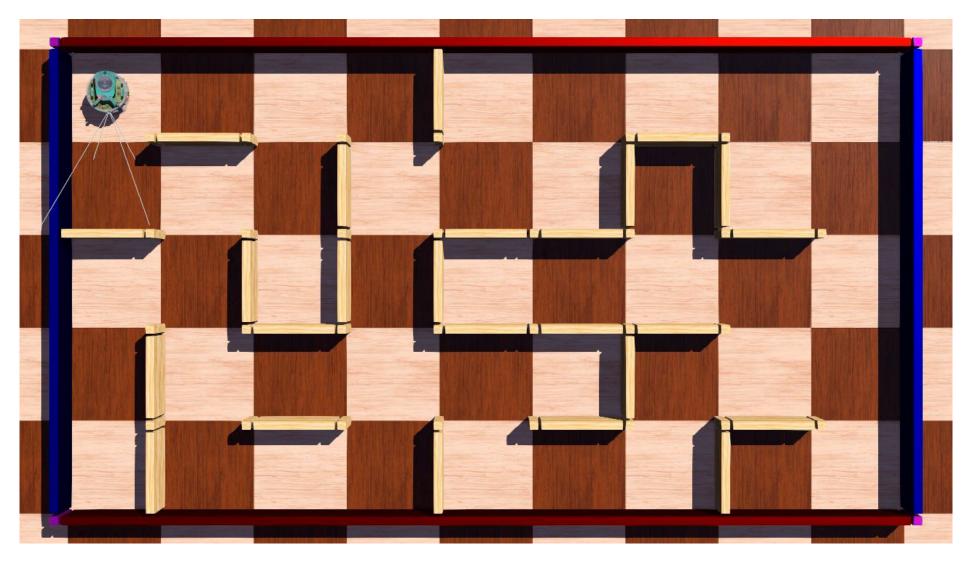
Localisation

• The process that the robot determines its position in the environment



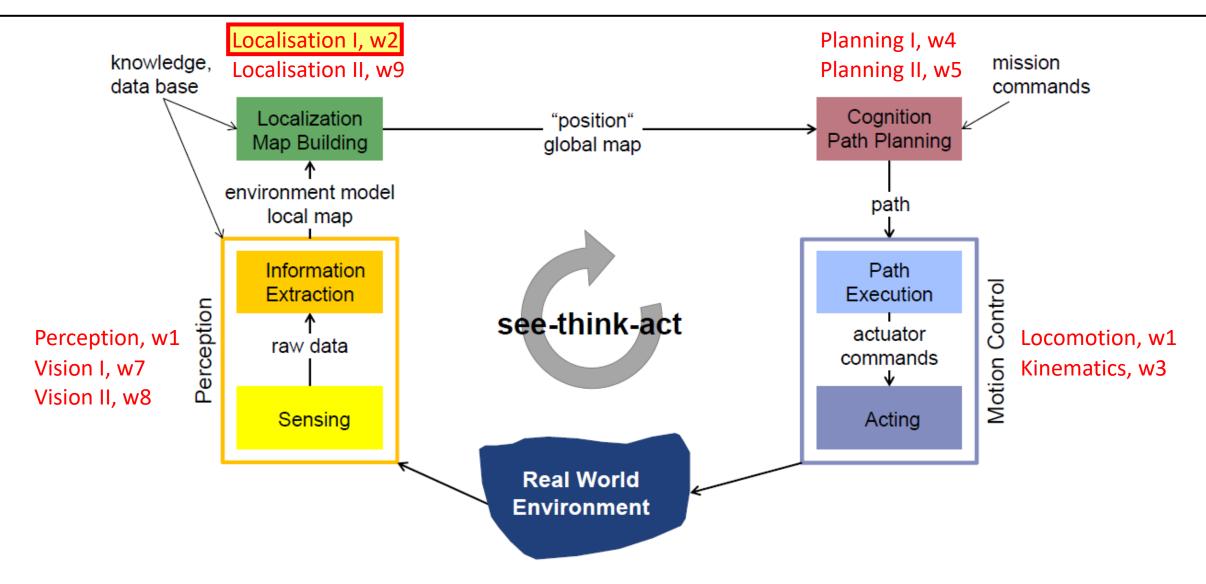


Localisation in the maze-solving task



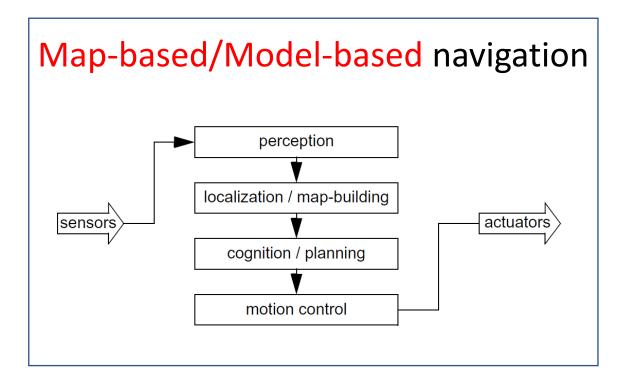


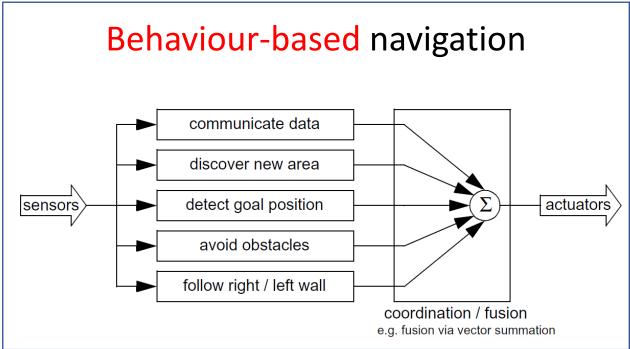
The See-Think-Act cycle





To localise or not to localise







- -"Hi, I'm going to attend Leo's lecture, do you know how to get to the theatre?"
- -"Sure, you are now at the centre of Quadrangle Lawn, you just need to go south for 50 meters and then go west for 40 meters. You'll be able to find the Webster Theatres. The lecture is on the second floor."
- -"Hi, the lecture is really boring. I'm gonna take a tram to join my friend's party at the CBD, do you know where the nearest station is?"
- -"Easy, you just need to get out of the door and step down the stairs to the ground floor. Walk around the Robert Webster Building clockwise until you reach the University Mall Road, then follow it in the downward direction for about 5min until you cross the Anzac Parade. You should then be able to see the station on your right-hand side. But seriously, why taking a tram when a bus is much faster???



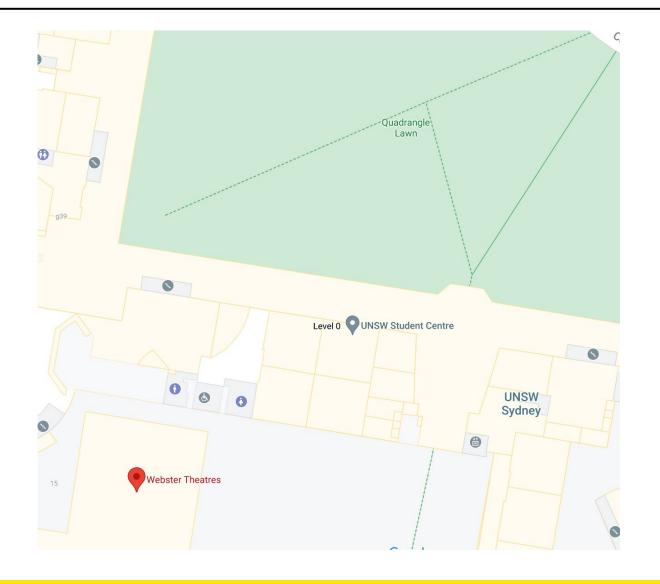


Which of the shown methods is behaviour-based navigation?

(i) Start presenting to display the poll results on this slide.

Which of the following is behaviour-based navigation?

- -"Hi, I'm going to attend Leo's lecture, do you know how to get to the theatre?"
- -"Sure, you are now at the centre of Quadrangle Lawn, you just need to go south for 50 meters and then go west for 40 meters. You'll be able to find the Webster Theatres. The lecture is on the second floor."





Which of the following is behaviour-based navigation?



-"Hi, the lecture is really boring. I'm gonna take a tram to join my friend's party at the CBD, do you know where the nearest station is?"

-"Easy, you just need to get out of the door and step down the stairs to the ground floor. Walk around the Robert Webster Building clockwise until you reach the University Mall Road, then follow it in the downward direction for about 5min until you cross the Anzac Parade. You should then be able to see the station on your right-hand side. But seriously, why taking a tram when a bus is much faster???

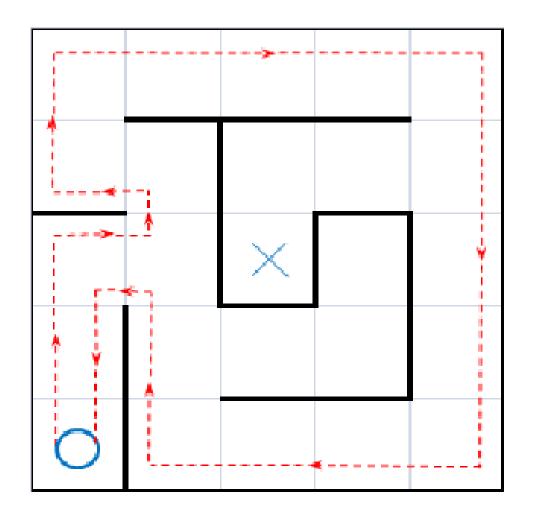


Behaviour based approach - Right (or Left) Wall Follower



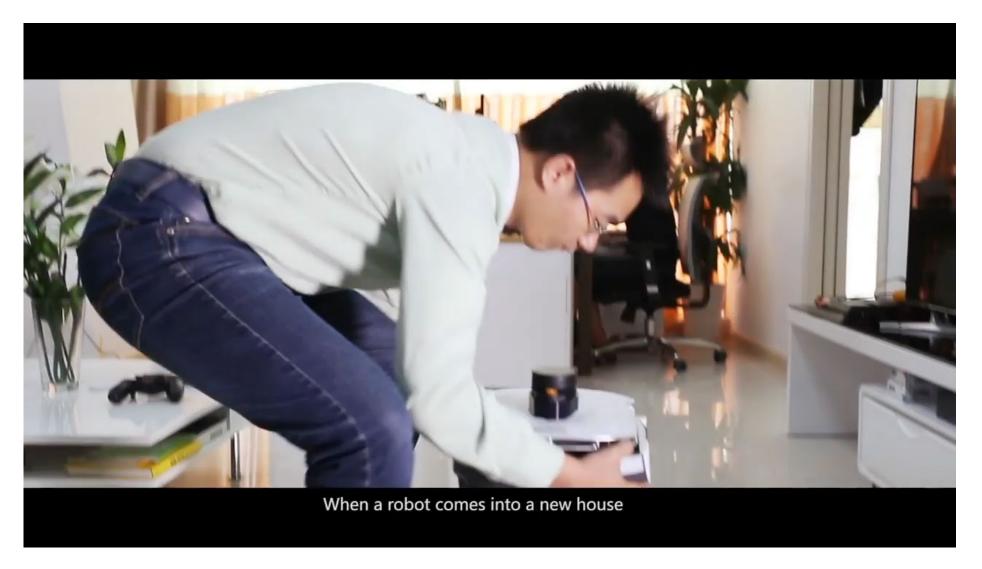


What about this one?





Map based navigation





Behavior based approach vs. Map based approach

Behavior based approach

- Pros
 - Avoids inaccuracy of mapping
 - Easy to implement (if works)
- Cons
 - Does not directly scale to other environments or to larger environments
 - Must be carefully designed to produce the desired behaviour
 - May have multiple active behaviours at any one time

Map based approach

- Pros
 - Position available to human operators
 - The map, if created by the robot, can be used by humans as well
 - Ability to scale changing maps
- Cons
 - More up-front development effort
 - May go diverging even if the raw sensor values are transiently incorrect



Map Representation

Map representation

Continuous line-based

- Cell decomposition
 - Exact cell decomposition
 - Fixed cell decomposition
 - Adaptive cell decomposition

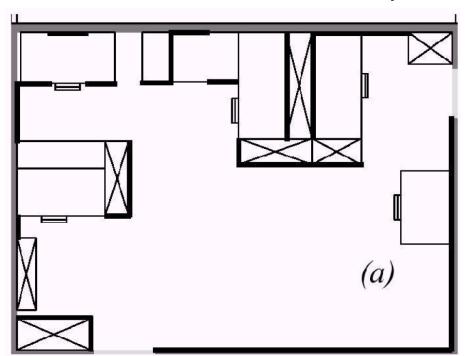
Topological map

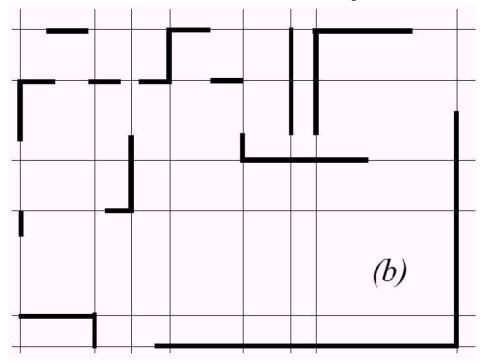




Map representation – Continuous line-based

- Representation with set of finite or infinite lines
- Closed-World Assumption Only need to store the information of the lines
 - CWA: What is not currently known to be true, is false.
 - OWA: What is not currently known to be true, can be either true or false.







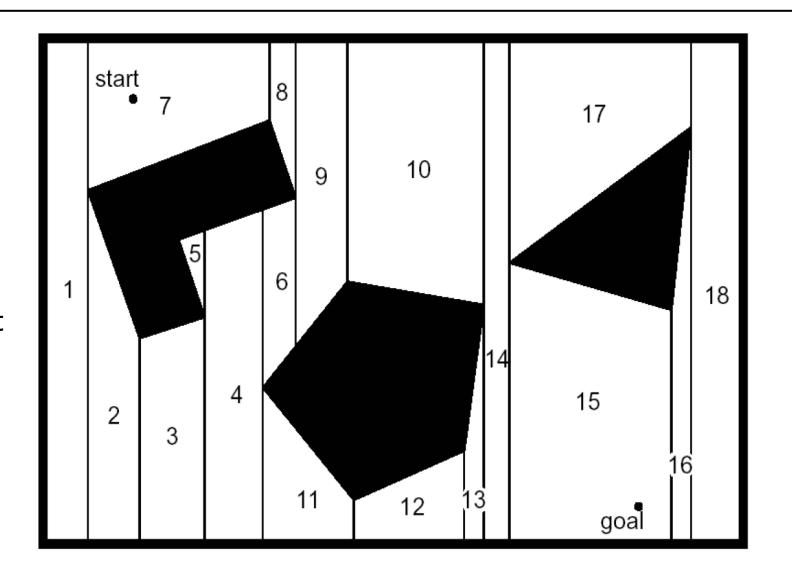
Map representation – Exact cell decomposition (Polygon)

• Pros:

• Can be extremely compact

• Cons:

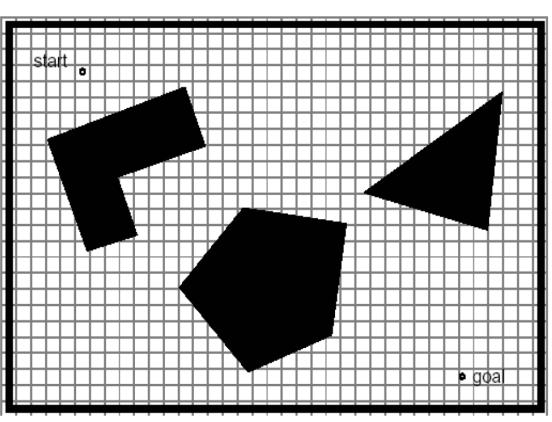
• The information of the obstacles and free space may be expensive to collect



Map representation – Fixed cell decomposition (Occupancy grid)

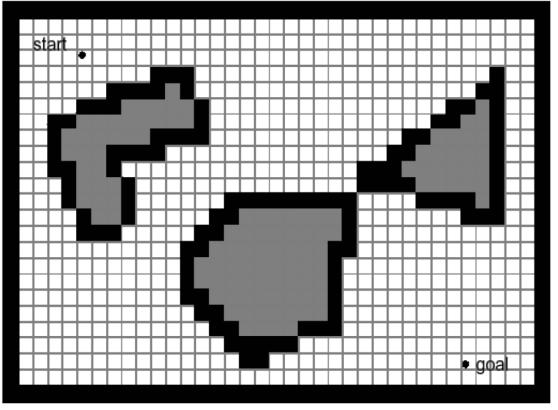
• Pros:

 Easy to implement for robots with range-based sensors



• Cons:

- Narrow passages may disappear
- Huge memory may be needed



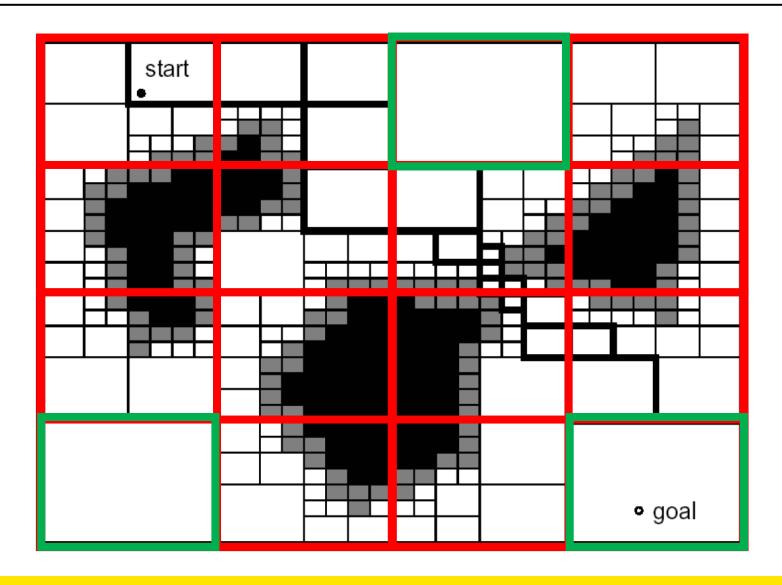


Map representation – Adaptive cell decomposition

Resolution = 1/4

Resolution = 1/16

Resolution = Predefined





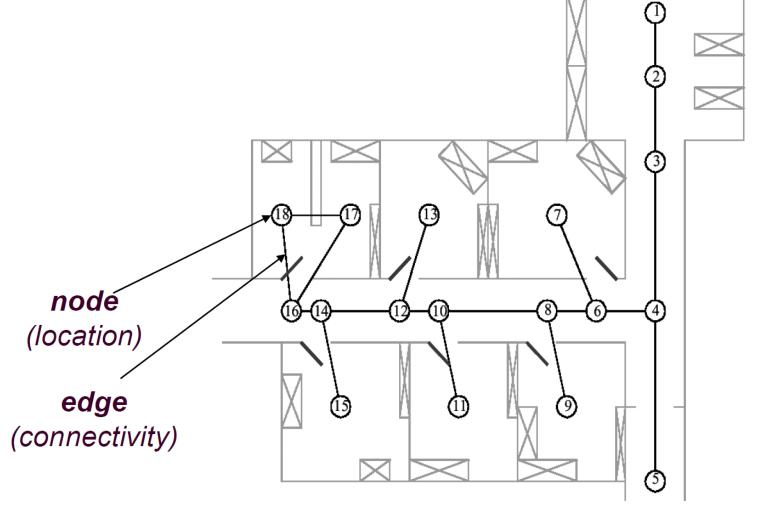
Map representation – Topological representation

 Represents environment with nodes and edges

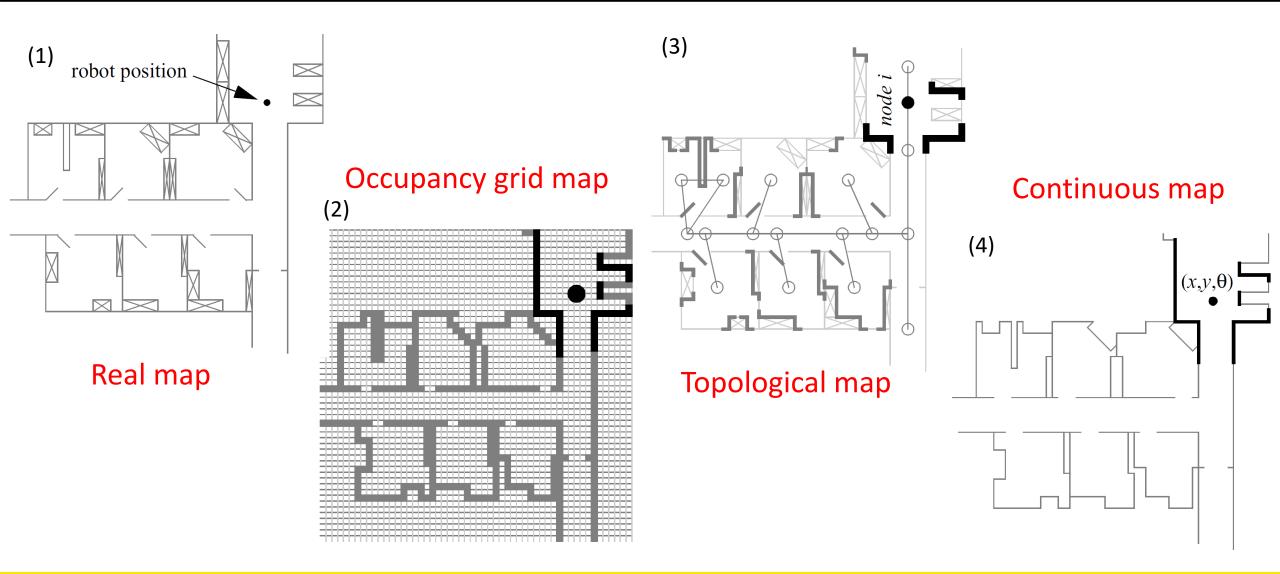
Lacks scale and distances

 Maintains topological relationships (connectivity)

Adapts to geometric change











Which map do you think is best suited to represent the maze?

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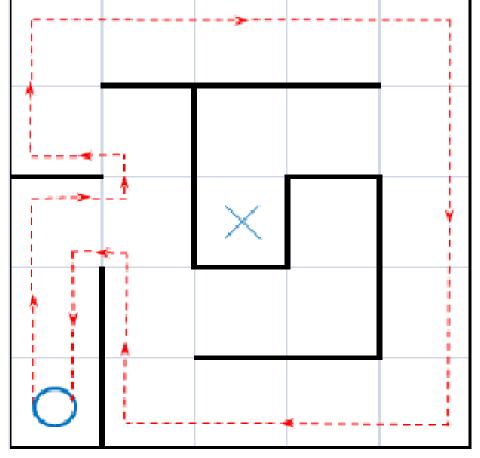
An example map for the maze

$$HorizontalWall = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix}_{6\times5}$$

$$VerticalWall = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 \end{bmatrix}_{5\times6}$$

$$CellValue = \begin{bmatrix} 8 & 7 & 6 & 5 & 4 \\ 9 & 10 & 1 & 2 & 3 \\ 12 & 11 & 0 & 13 & 4 \\ 13 & 10 & 11 & 12 & 5 \\ 14 & 9 & 8 & 7 & 6 \end{bmatrix}_{5\times5}$$

RobotPos = (4,0) (assuming the top-left cell is (0,0))





Localisation Methods

Two types of localisation

Global localisation

- The robot is not told its initial position
- Its position must be estimated from scratch

Position tracking

- A robot knows its initial position
- It just needs to estimate the displacement relative to the initial position



Four localisation methods

Localisation based on landmarks/artificial markers/external sensors

Dead reckoning/Odometry

- Map based localisation without external sensors/artificial landmarks, just use robot onboard sensors
 - Probabilistic map based localisation

Simultaneous Localisation and Mapping (SLAM)



Four localisation methods

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Simultaneous localisation and Mapping (SLAM)



Artificial-marker based localisation



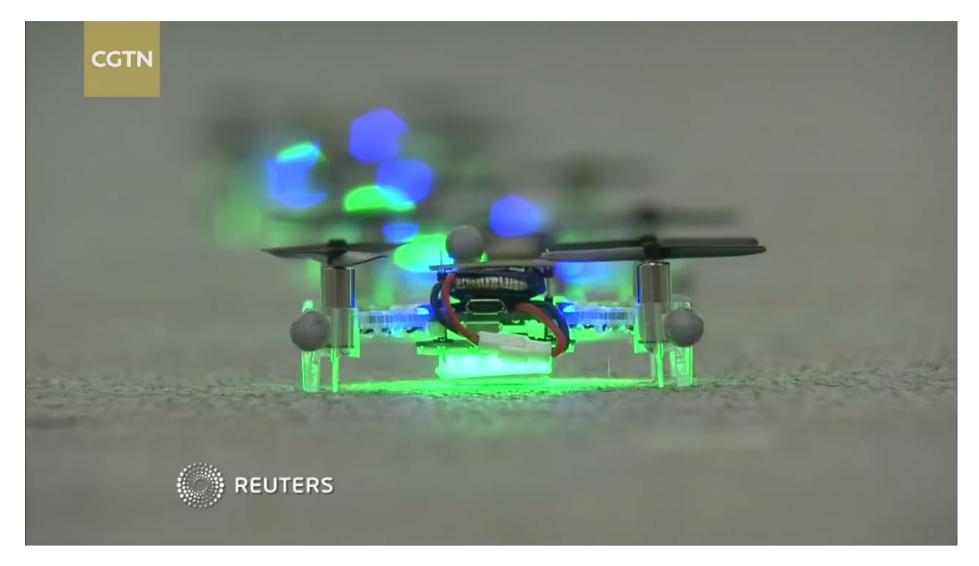


Landmark based localisation



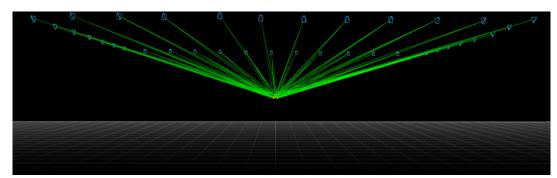


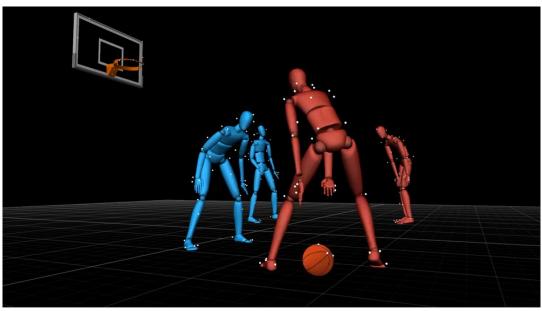
Motion-capture-system based localisation

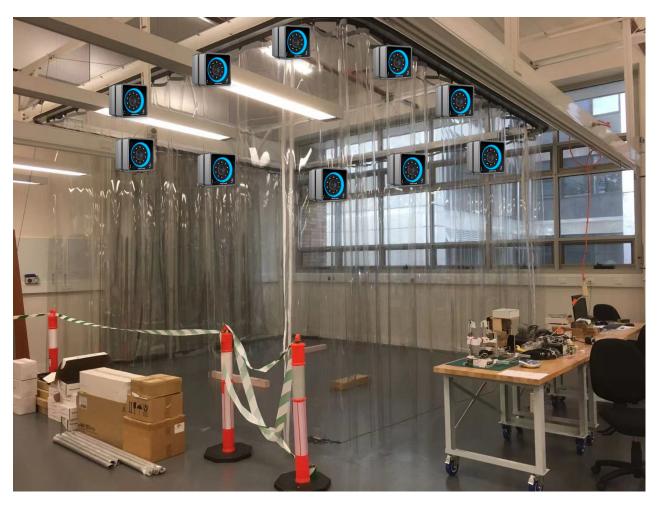




Motion-capture-system at Mechatronics Research Lab, MME, UNSW









Four localisation methods

- Localisation based on landmarks/artificial markers/external sensors
 - Capable of global localisation
 - Needs modification or detailed information of the environment

Dead reckoning/Odometry

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Simultaneous localisation and Mapping (SLAM)



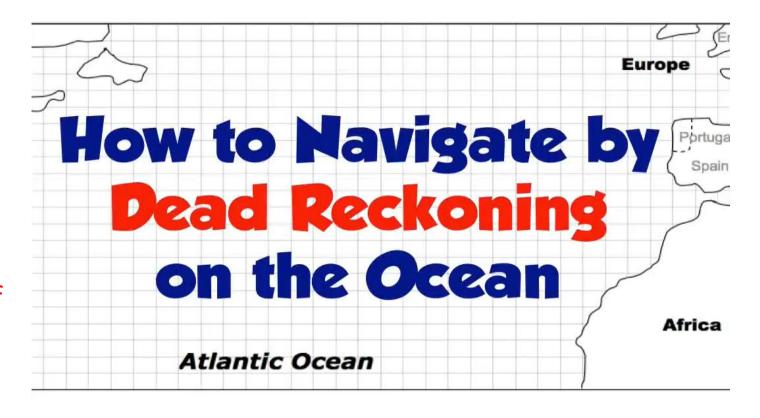
Dead reckoning/Odometry

Dead reckoning (Deduced reckoning)

 A simple mathematical procedure for determining the present location of a vessel by advancing some previous position through known course and velocity information over a given length of time.

Odometry

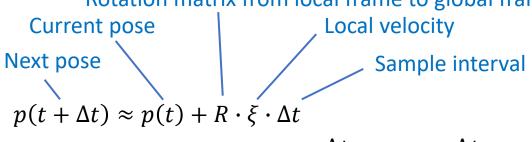
 Dead reckoning by using only wheel encoders, sometimes interchangeable with Dead reckoning



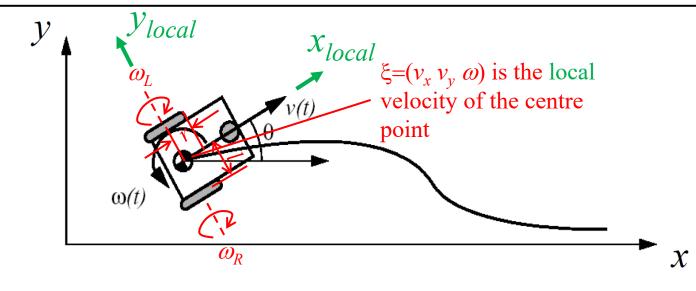


Dead reckoning – Differential-drive

Rotation matrix from local frame to global frame



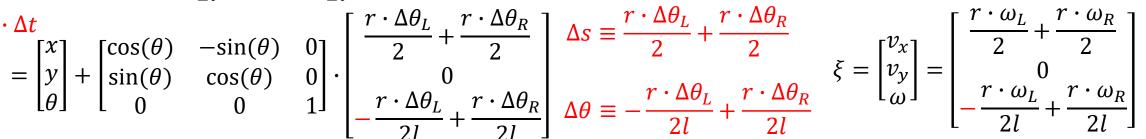
$$= \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} + R \cdot \begin{bmatrix} \frac{r \cdot \omega_L \cdot \Delta t}{2} + \frac{r \cdot \omega_R \cdot \Delta t}{2} \\ 0 \\ -\frac{r \cdot \omega_L \cdot \Delta t}{2l} + \frac{r \cdot \omega_R \cdot \Delta t}{2l} \end{bmatrix}$$



$$\Delta\theta_{R} = \omega_{R} \cdot \Delta t$$

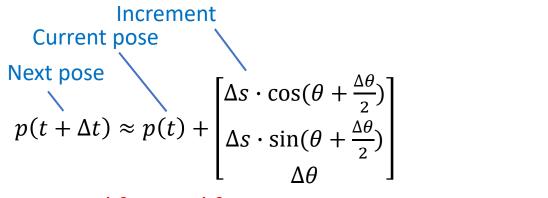
$$= \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} + \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} \frac{r \cdot \Delta\theta_{L}}{2} + \frac{r \cdot \Delta\theta_{R}}{2} \\ 0 \\ -\frac{r \cdot \Delta\theta_{L}}{2l} + \frac{r \cdot \Delta\theta_{R}}{2l} \end{bmatrix}$$

$$= \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} + \begin{bmatrix} \Delta s \cdot \cos(\theta) \\ \Delta s \cdot \sin(\theta) \\ \Delta \theta \end{bmatrix} \approx \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} + \begin{bmatrix} \Delta s \cdot \cos(\theta + \frac{\Delta \theta}{2}) \\ \Delta s \cdot \sin(\theta + \frac{\Delta \theta}{2}) \\ \Delta \theta \end{bmatrix}$$





Dead reckoning – Differential-drive

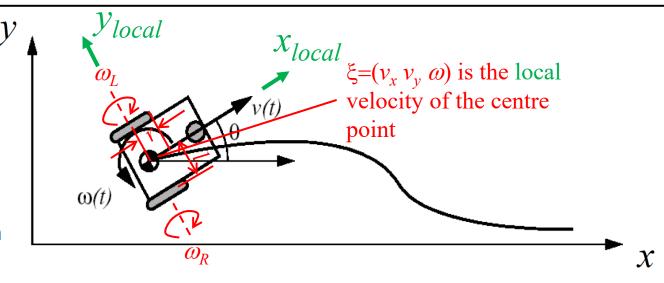


$$\Delta s \equiv \frac{r \cdot \Delta \theta_L}{2} + \frac{r \cdot \Delta \theta_R}{2} \quad --- \quad \text{Incremental linear motion}$$

$$\Delta\theta \equiv -\frac{r \cdot \Delta\theta_L}{2I} + \frac{r \cdot \Delta\theta_R}{2I}$$
 Incremental rotation

$$\Delta \theta_L = \omega_L \cdot \Delta t$$
 — Incremental rotation of left wheel

$$\Delta \theta_R = \omega_R \cdot \Delta t$$
 — Incremental rotation of right wheel

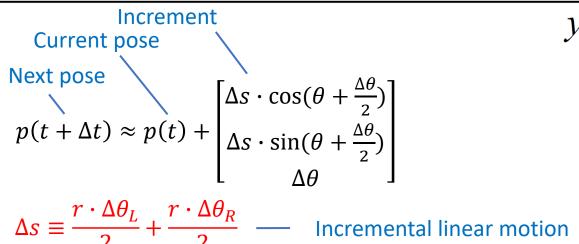


Case 1: $\Delta \theta_L = \Delta \theta_R$ - Pure linear motion

Case 2: $\Delta \theta_I = -\Delta \theta_R$ - Pure rotation



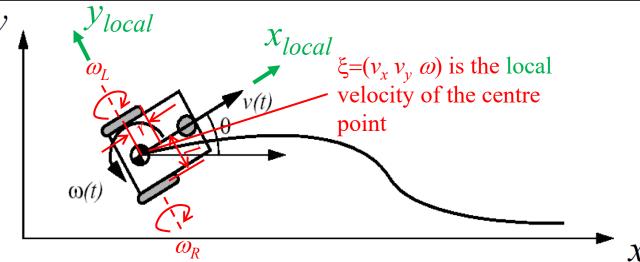
Dead reckoning - Differential-drive: Example



$$\Delta\theta \equiv -\frac{r \cdot \Delta\theta_L}{2l} + \frac{r \cdot \Delta\theta_R}{2l}$$
 Incremental rotation

$$\Delta \theta_L = \omega_L \cdot \Delta t$$
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 — Incremental rotation of right wheel



Q: Suppose a differential-drive robot is running at a constant speed. The wheels have diameter 40mm and spaced at 100mm. The encoders of two wheels are read twice. The differences from the first to the second reading are 30deg and 60deg for the left and right wheels, respectively. Assume at the first reading, the robot's pos is (0mm, 0mm, 0deg). What is the robot's pose at the second reading? ($\pi = 3.14$)



Dead reckoning – Differential-drive: Example

Increment
Current pose
Next pose
$$p(t + \Delta t) \approx p(t) + \begin{bmatrix} \Delta s \cdot \cos(\theta + \frac{\Delta \theta}{2}) \\ \Delta s \cdot \sin(\theta + \frac{\Delta \theta}{2}) \\ \Delta \theta \end{bmatrix}$$

$$\Delta s \equiv \frac{r \cdot \Delta \theta_L}{2} + \frac{r \cdot \Delta \theta_R}{2}$$

$$\Delta\theta \equiv -\frac{r \cdot \Delta\theta_L}{2l} + \frac{r \cdot \Delta\theta_R}{2l}$$

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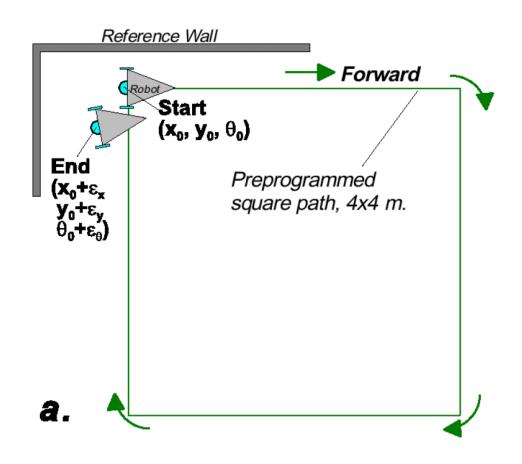
Homework:

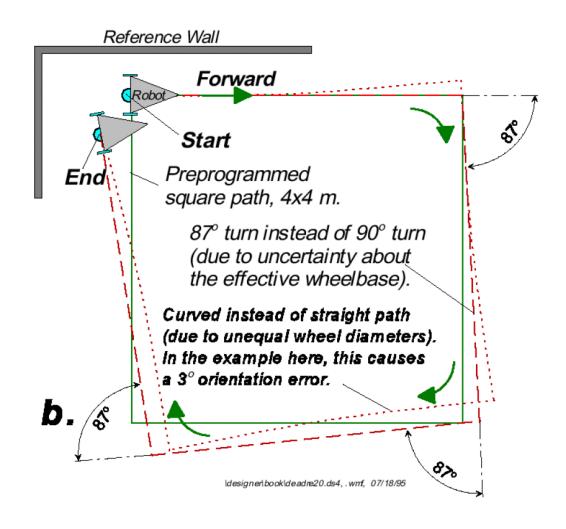
Solve this problem and write a program in MATLAB (or any other language) for the calculation.

Hints: The solution is: (15.7mm, 0.83mm, 0.105rad).



Dead reckoning – Square path experiment







Dead reckoning – Error sources

Deterministic (Systematic)

 Can be reduced/eliminated by proper calibration of the system

- Examples
 - Misalignment of the wheels
 - Unequal wheel diameter

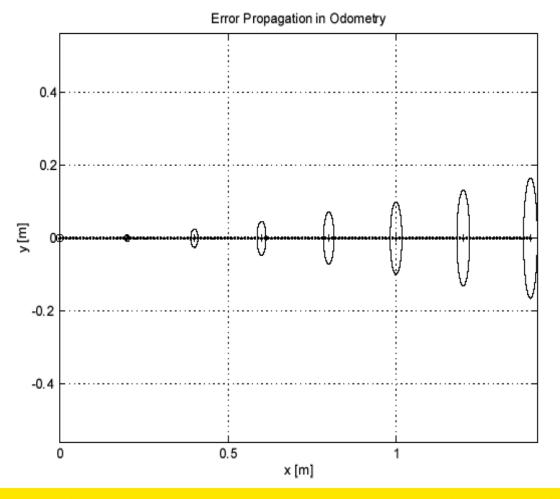
Non-Deterministic (Non-Systematic)

- Are random errors, have to be described by error models, and will always lead to uncertain position estimate
- Examples
 - Variation in the contact point of the wheel
 - Unequal floor contact (slippage, non-planar, etc.)



Dead reckoning – Growth of pose uncertainty for straight line movement

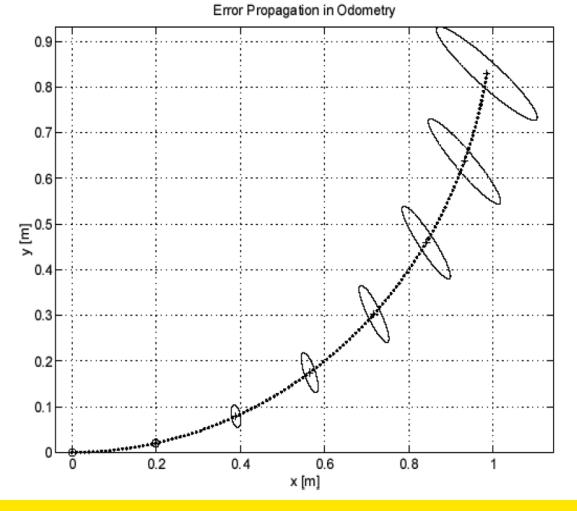
Errors perpendicular to the direction of movement are growing much faster!





Dead reckoning – Growth of pose uncertainty for a circular movement

• Errors ellipse does NOT remain perpendicular to the direction of movement





Calibration of the robot parameters

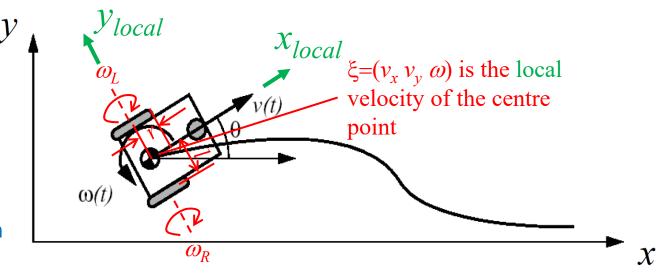
Increment
Current pose
Next pose
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$$\Delta s \equiv \frac{r \cdot \Delta \theta_L}{2} + \frac{r \cdot \Delta \theta_R}{2} \quad --- \quad \text{Incremental linear motion}$$

$$\Delta\theta \equiv -\frac{r \cdot \Delta\theta_L}{2l} + \frac{r \cdot \Delta\theta_R}{2l}$$
 Incremental rotation

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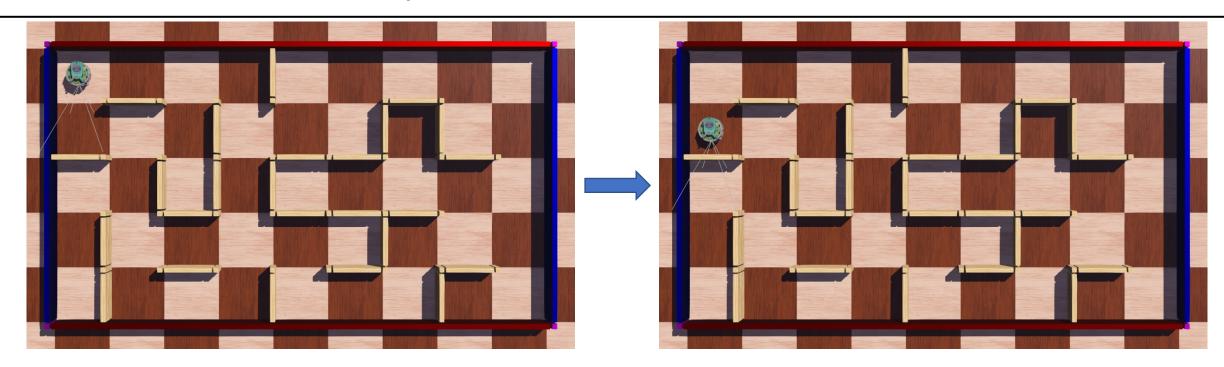


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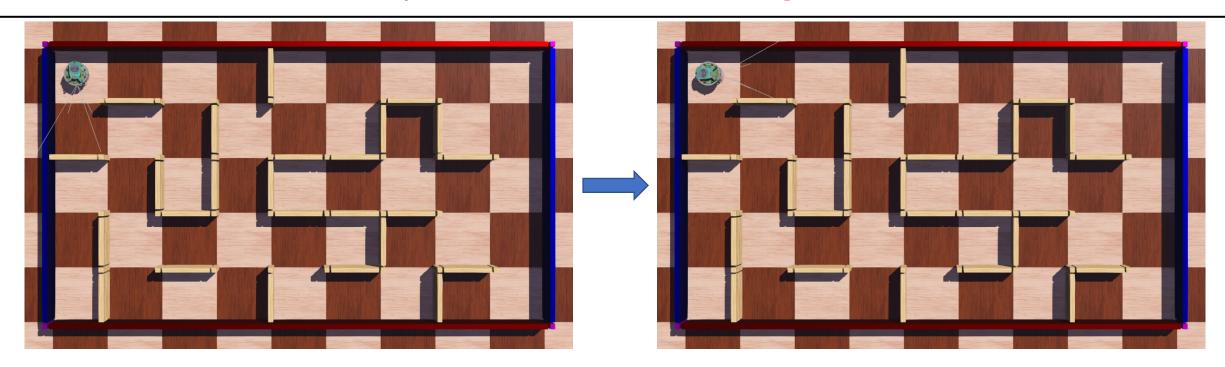
Calibration of the robot parameters – Wheel radius



- 1. Make $\Delta \theta_L = \Delta \theta_R = \emptyset$: pure translation
- 2. Tune this value Ø, i.e., the rotation angles of both motors until the robot moves to the centre of next cell
- 3. Calculate r from $\Delta s \equiv \frac{r \cdot \Delta \theta_L}{2} + \frac{r \cdot \Delta \theta_R}{2}$
- Note 1 It may make the calibration more accurate by moving the robot for a longer distance, e.g., 10 cells (you can put the robot outside the maze to avoid wall collision)
- Note 2 The recommended corrections to the parameters were obtained from this calibration process; you can also calibrate the robot to get your own corrections if interested



Calibration of the robot parameters – Axle length



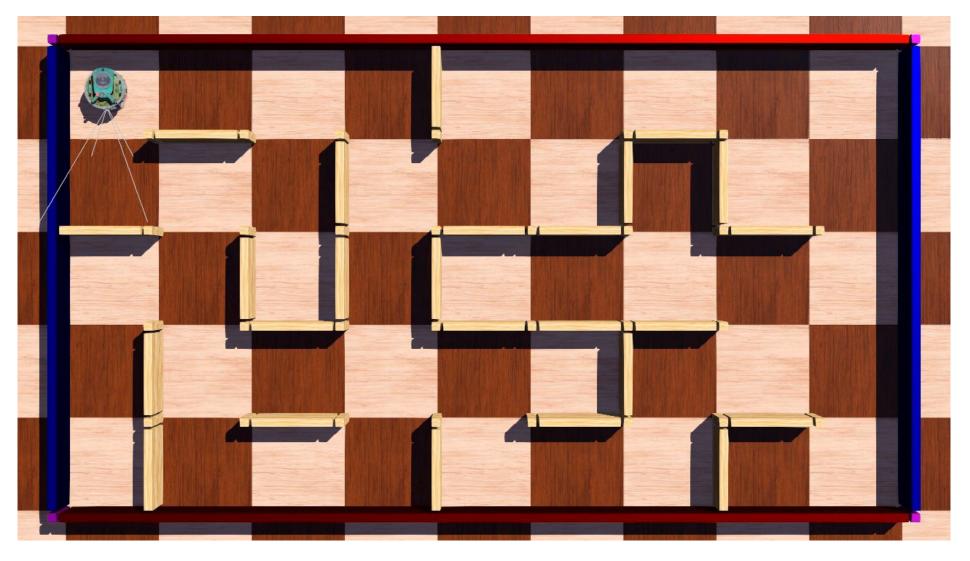
- 1. Make $\Delta \theta_L = -\Delta \theta_R = \emptyset$: pure rotation
- 2. Tune this value Ø, i.e., the rotation angles of both motors until the robot rotates to a certain angle, e.g., 360deg
- 3. Calculate l from $\Delta \theta \equiv -\frac{r \cdot \Delta \theta_L}{2l} + \frac{r \cdot \Delta \theta_R}{2l}$ and the calibrated r
- Note 1 It may make the calibration more accurate by rotating the robot more turns, e.g., 10 turns
- Note 2 The recommended corrections to the parameters are obtained from this calibration process; you can also calibrate the robot to get your own corrections if interested



Four localisation methods

- Localisation based on landmarks/artificial markers/external sensors
 - Capable for global localisation
 - Needs modification or detailed information of the environment
- Dead reckoning/Odometry
 - Only suitable for position tracking
 - Subject to deterministic and non-deterministic errors
 - Error may accumulate over time
 - Heading sensors (e.g. gyroscope) may help reduce the accumulated errors
 - $\Delta\theta$ measured by heading sensors instead of estimated by odometry
- Map based localisation without external sensors/artificial landmarks, just use robot onboard sensors
 - Probabilistic map based localisation
- Simultaneous localisation and Mapping (SLAM)







slido

What methods/sensors can be used for localisation in the course project?

(i) Start presenting to display the poll results on this slide.

What we have learnt today

- Behaviour-based navigation vs. Map-based navigation
- Five different map representations

- Two different localisation methods
 - Global localisation
 - Dead reckoning/Odometry
- Error sources and calibration for dead reckoning



Next week: Kinematics

