MTRN4110 Robot Design Week 9 – Localisation II

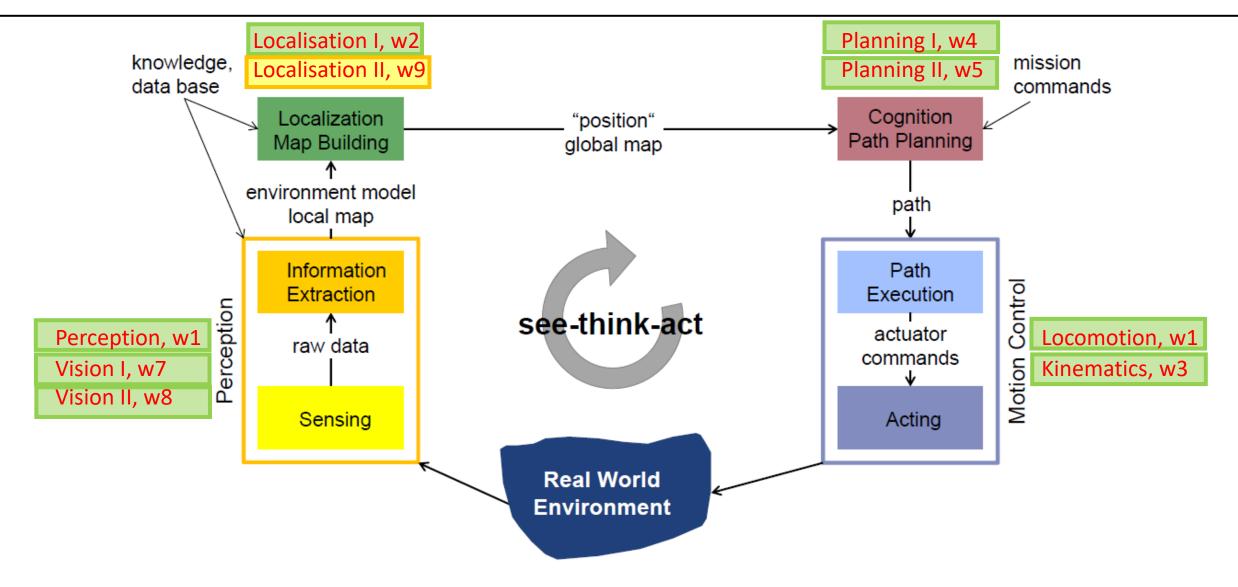
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https://sites.google.com/site/wuliaothu/



The See-Think-Act cycle





What we have learnt in Localisation I

- Introduction to localisation
 - Map-based approach vs Behaviour-based approach
- Map representations
 - Continuous line-based
 - Cell decomposition
 - Exact cell decomposition
 - Fixed cell decomposition
 - Adaptive cell decomposition
 - Topological map
- Localisation methods
 - Localisation based on landmarks/artificial markers/external sensors
 - Dead reckoning/odometry
 - Probabilistic map based localisation
 - Simultaneous Localisation and Mapping (SLAM)



Today's agenda

- Probabilistic map-based localisation
 - Markov localisation
 - Particle Filter localisation
 - Kalman Filter localisation

- Simultaneous Localisation and Mapping (SLAM)
 - Extended Kalman Filter SLAM
 - Graph-based SLAM
 - Particle Filter SLAM



Probabilistic Map-Based Localisation

Probabilistic map-based localisation

Localisation:

The process that the robot determines its position in the environment.

Map-Based:

Assuming a map of the environment is known.

Probabilistic:

 The data coming from the robot sensors are affected by measurement errors, and therefore we can only compute the probability of the location of the robot in a given configuration.



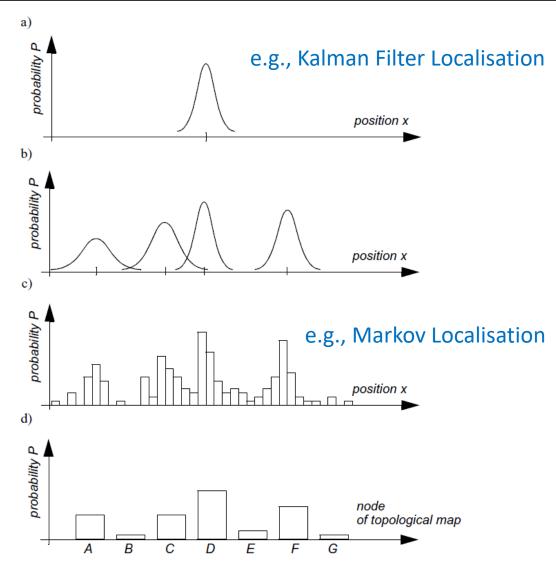
Probabilistic map-based localisation – Four ingredients

- 1. Belief representation
 - A representation of the robot's belief regarding its position on the map
- 2. Probability theory
 - Theorem of total probability
 - Bayes rule
- 3. Motion model
 - Odometry model
- 4. Sensing model
 - Measurement model



1. Belief representation

- a) Continuous map with singlehypothesis belief
- b) Continuous map with multiplehypothesis belief
- c) Discretised grid map with probability values for all possible robot positions
- d) Discretised topological map with probability values for all possible nodes



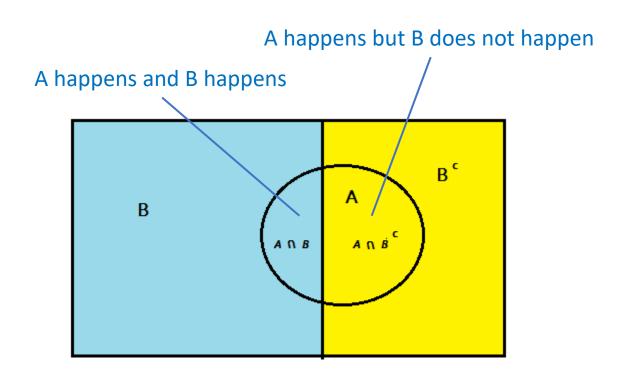


• 2.1 Theorem of total probability

- For discrete probabilities
 - $p(x) = \sum_{y} p(x|y)p(y)$
- For continuous probabilities

•
$$p(x) = \int_{y} p(x|y)p(y)dy$$

• Here $p(x|y) = \frac{p(x,y)}{p(y)}$ is called conditional probability









Thomas Bayes (1701 - 1761)

- Case study (data made up)
 - Given the following statistics, what is the probability that a person had infected COVID-19 if the person had a dry cough symptom?
 - 1. 0.2% of people worldwide could infect COVID-19.
 - 2. If a person had infected COVID-19, the possibility that the person had a dry cough symptom is 80%.
 - 3. If a person had not infected COVID-19, the possibility that the person had a dry cough symptom is 8.3%.

$$p(x) = 0.2\%$$

$$p(y|x) = 80\%$$

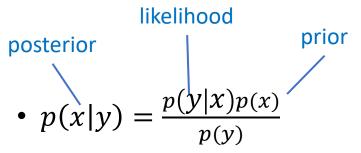
$$p(y) = p(y|x)p(x) + p(y|\sim x)p(\sim x)$$

= 80% × 0.2% + 8.3% × 99.8%
= 8.4434%

$$p(x|y) = \frac{p(y|x)p(x)}{p(y)} = \frac{80\% \times 0.2\%}{8.4434\%} = 1.89\%$$



• 2.2 Bayes rule posterior



What if we know that the person has had close contact with a confirmed infection case?

- Case study (data made up)
 - Given the following statistics, what is the probability that a person had infected COVID-19 if the person had a dry cough symptom?
 - 1. 0.2 50% of people worldwide (with close contact of confirmed infection cases) could infect COVID-19.
 - 2. If a person had infected COVID-19, the possibility that the person had a dry cough symptom is 80%.
 - 3. If a person had not infected COVID-19, the possibility that the person had a dry cough symptom is 8.3%.

$$p(x) = 0.250\%$$

$$p(y|x) = 80\%$$

$$p(y) = p(y|x)p(x) + p(y|\sim x)p(\sim x)$$

$$= 80\% \times 0.250\% + 8.3\% \times 99.850\%$$

$$= 8.443444.15\%$$

h
$$p(x|y) = \frac{p(y|x)p(x)}{p(y)} = \frac{80\% \times 0.250\%}{8.443444.15\%} = \frac{1.8990.6\%}{1.8990.6\%}$$

The Bayesian Brain
Predictive Processing

• 2.2 Bayes rule posterior | likelihood | prior | $p(x|y) = \frac{p(y|x)p(x)}{p(y)} = \frac{\eta p(y|x)p(x)}{\eta p(y)}$



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- Case study (data made up)
 - Given the following statistics, what is the probability that a person had infected COVID-19 if the person had a dry cough symptom?
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$$p(x) = 0.2\%$$

$$p(y|x) = 80\%$$

$$p(y) = p(y|x)p(x) + p(y|\sim x)p(\sim x)$$

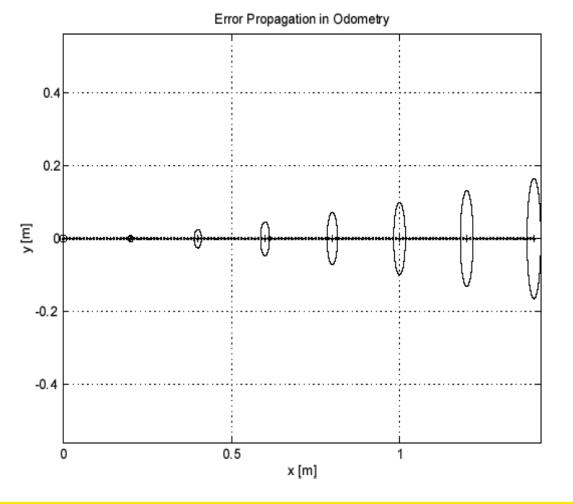
= 80% × 0.2% + 8.3% × 99.8%
= 8.4434%

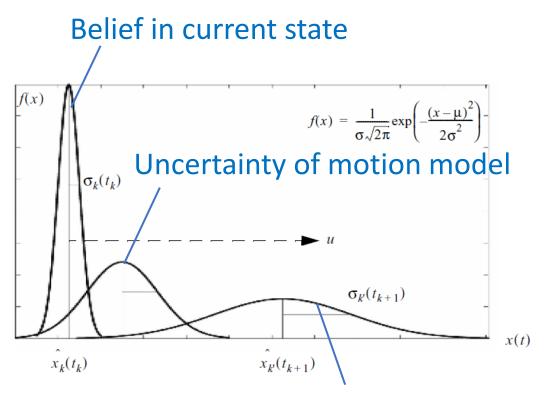
$$p(x|y) = \frac{p(y|x)p(x)}{p(y)} = \frac{80\% \times 0.2\%}{8.4434\%} = 1.89\%$$



3. Prediction (action) update

Applying the theorem of total probability and using the motion model



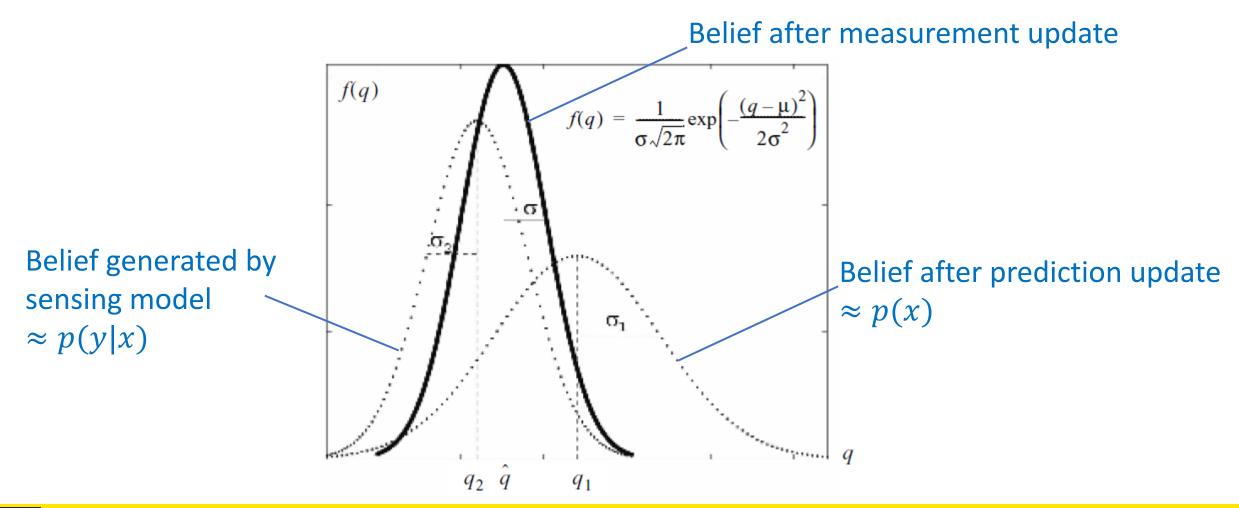


Belief after prediction update $\approx p(x)$



4. Measurement (perception) update

Applying the Bayes rule and using the sensing model





Markov Localisation

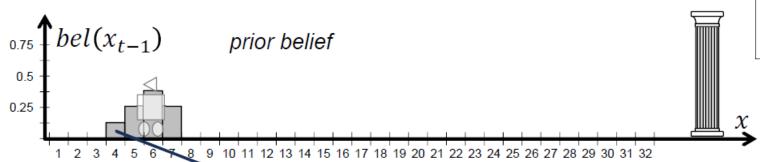
Markov localisation

- Markov assumption
 - The output x_t is a function ONLY of the previous state x_{t-1} and its most recent actions (odometry) u_t and perception z_t
- A general algorithm
 - bel() is belief after prediction update (Theorem of total probability)
 - bel() is belief after measurement update (Bayes' rule)
 - m is the information of the map

```
1: Algorithm Markov_localization(bel(x_{t-1}), u_t, z_t, m):
2: for all x_t do
3: \overline{bel}(x_t) = \int p(x_t \mid u_t, x_{t-1}, m) \ bel(x_{t-1}) \ dx (prediction update)
4: bel(x_t) = \eta \ p(z_t \mid x_t, m) \ \overline{bel}(x_t) (measurement update)
5: endfor
6: return bel(x_t)
```



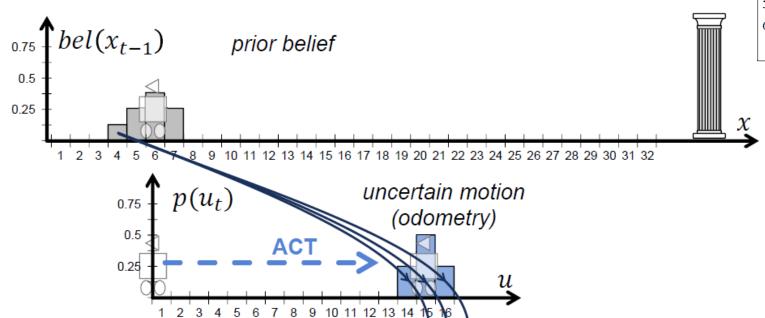
Andrey Markov (1856 - 1922)



```
1: Algorithm Markov_localization(bel(x_{t-1}), u_t, z_t, m):
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```

This is the belief of the position of the robot in state t-1.



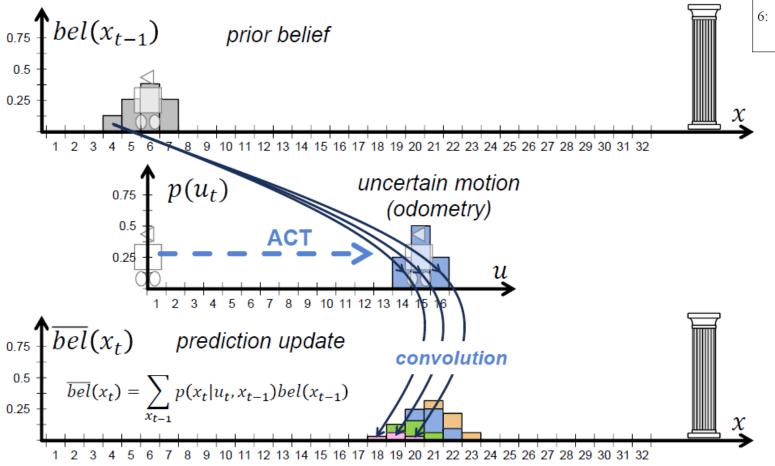


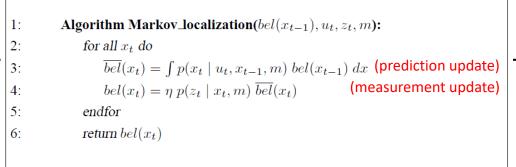
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5: endfor
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This is the belief of the position of the robot in state t-1.

The robot moves forward for 15 steps but there is uncertainty associated with the motion.





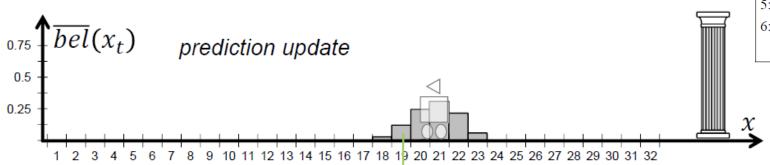


This is the belief of the position of the robot in state t-1.

The robot moves forward for 15 steps but there is uncertainty associated with the motion.

This is the belief after the prediction update (line 3 of the algorithm).

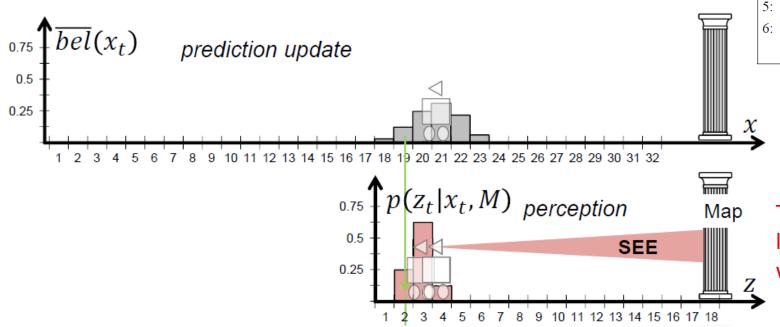




```
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4: bel(x_t) = \eta \ p(z_t \mid x_t, m) \ \overline{bel}(x_t) (measurement update)
5: endfor
6: return bel(x_t)
```

This is the belief after the prediction update (line 3 of the algorithm).



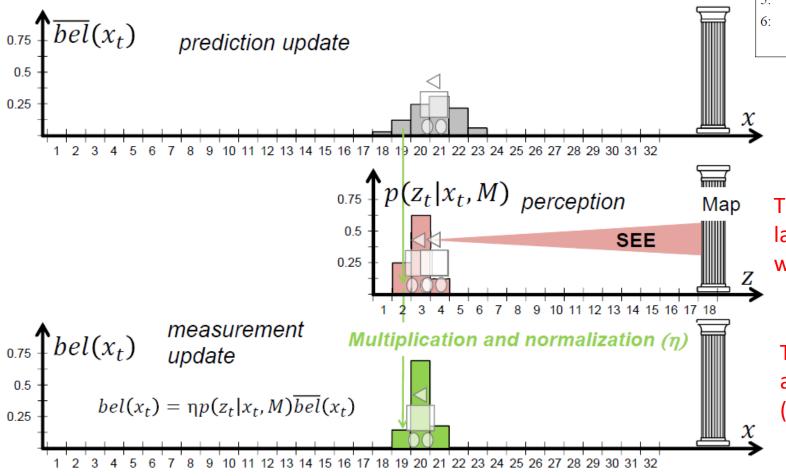


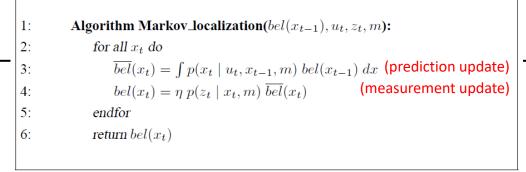
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4: bel(x_t) = \eta \ p(z_t \mid x_t, m) \ \overline{bel}(x_t) (measurement update)
5: endfor
6: return bel(x_t)
```

This is the belief after the prediction update (line 3 of the algorithm).

The robot detects the distance from the landmark but there is uncertainty associated with the measurement. Note – the map is known.







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The robot detects the distance from the landmark but there is uncertainty associated with the measurement. Note – the map is known.

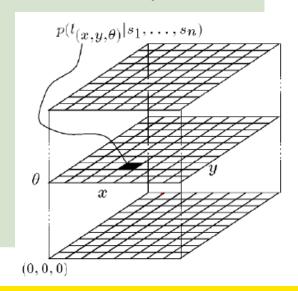
This is the belief of the position of the robot after the measurement update (line 4 of the algorithm).



Markov localisation - Summary

Advantages

- Localisation starting from any unknown position (global localisation)
- Recovers from ambiguous situation
- Can represent any arbitrary probability density function over the robot position

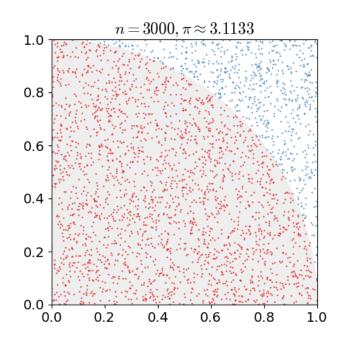


Disadvantages

- To update the probability of all positions within the whole state space at any time requires a discrete representation of the space (grid).
- The required memory and calculation power can thus become expensive if a fine grid is used.
- Example
 - 30m x 30m environment
 - Cell size of 0.1m x 0.1m x 1 deg
 - 300 x 300 x 360 = 32.4 million cells!



Particle Filter Localisation



- Monte Carlo (MC) methods are a subset of computational algorithms that use the process of repeated random sampling to make numerical estimations of unknown parameters.
- There are a broad spectrum of Monte Carlo methods, but they all share the commonality that they rely on random number generation to solve deterministic problems.





Monte Carlo Casino, Monaco

"Being secret, the work of John von Neumann and Stanislaw Ulam required a code name. A
colleague of von Neumann and Ulam, Nicholas Metropolis, suggested using the
name Monte Carlo, which refers to the Monte Carlo Casino in Monaco where Ulam's uncle
would borrow money from relatives to gamble."



An extension of Markov localisation with Monte Carlo sampling.

```
Algorithm MCL(\mathcal{X}_{t-1}, u_t, z_t, m):
                    \bar{\mathcal{X}}_t = \mathcal{X}_t = \emptyset
                   for m = 1 to M do
                          x_t^{[m]} = sample_motion_model(u_t, x_{t-1}^{[m]})
                          w_t^{[m]} = \mathbf{measurement\_model}(z_t, x_t^{[m]}, m)
5:
                          \bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle
6:
                    endfor
                    \overline{\text{for }}m=1 \text{ to } M \text{ do }
                          draw i with probability \propto w_t^{[i]}
9:
                          add x_t^{[i]} to \mathcal{X}_t
10:
11:
                    endfor
                    return \mathcal{X}_t
```

```
1: Algorithm Markov_localization(bel(x_{t-1}), u_t, z_t, m):
2: for all x_t do
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4: bel(x_t) = \eta \ p(z_t \mid x_t, m) \ \overline{bel}(x_t) (measurement update)
5: endfor
6: return bel(x_t)
```

Instead of calculating all the possible states, just sample a subset.

And an additional process: resampling.



Initialisation - Randomly and uniformly sampled particles.
No motion at the beginning.

```
bel(x)
```

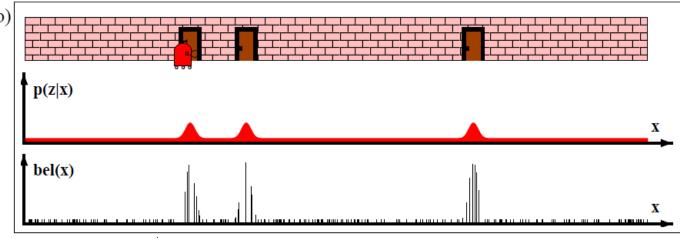
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5: w_t^{[m]} = \text{measurement\_model}(z_t, x_t^{[m]}, m)
6: \bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle
7: endfor
8: for m = 1 to M do
9: draw i with probability \propto w_t^{[i]}
10: add x_t^{[i]} to \mathcal{X}_t
11: endfor
12: return \mathcal{X}_t
```



Measurement update - Assign weights to the particles based on the measurement model.

```
bel(x)
```

```
1: Algorithm MCL(\mathcal{X}_{t-1}, u_t, z_t, m):
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```

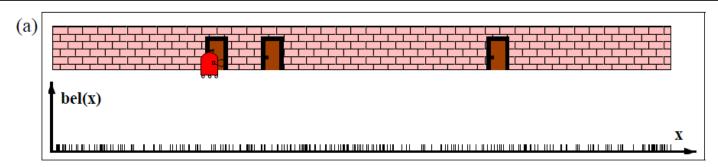


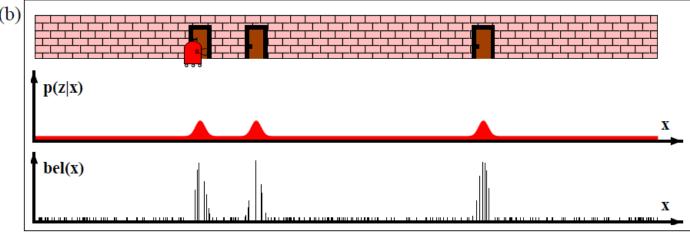


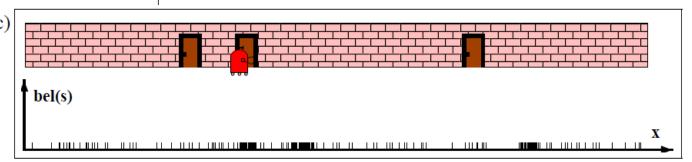
Resample – more density around the particles with higher weights.

Prediction update – applying motion model to the particles.

```
Algorithm MCL(\mathcal{X}_{t-1}, u_t, z_t, m):
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                        \bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle
                   endfor
                   for m = 1 to M do
                                                                                                    (c)
                        draw i with probability \propto w_t^{[i]}
                        add x_t^{[i]} to \mathcal{X}_t
10:
                   endfor
                   return \mathcal{X}_t
```





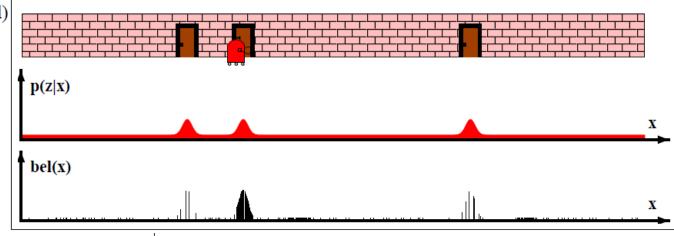




Measurement update - Assign weights to the particles based on the measurement model.

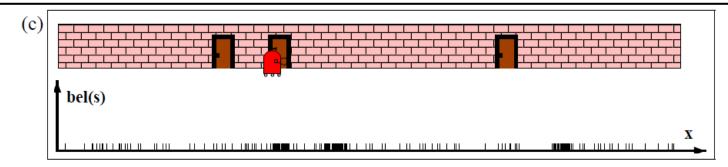
```
bel(s)
```

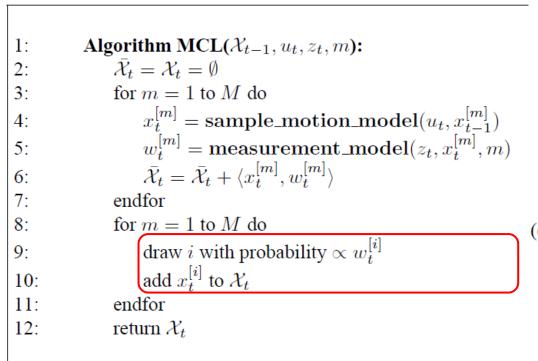
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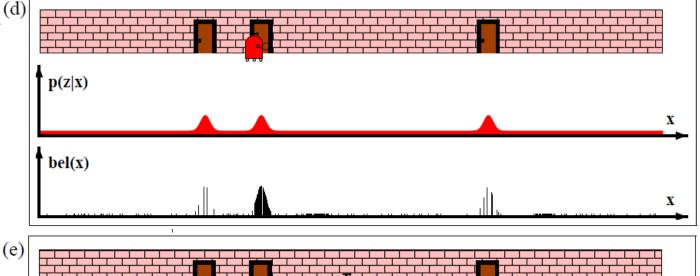


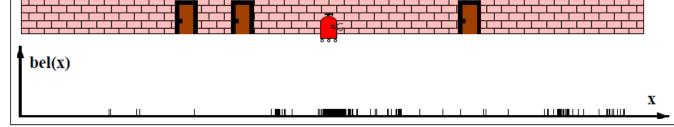


Resample – More density around the particles with higher weights.



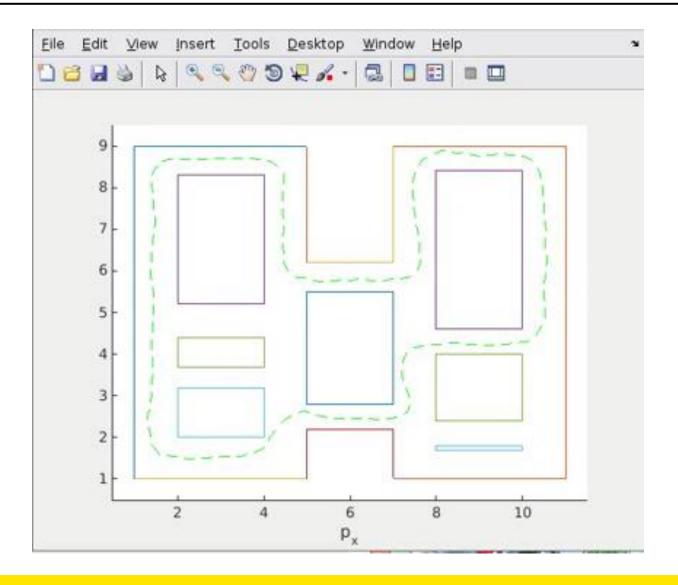






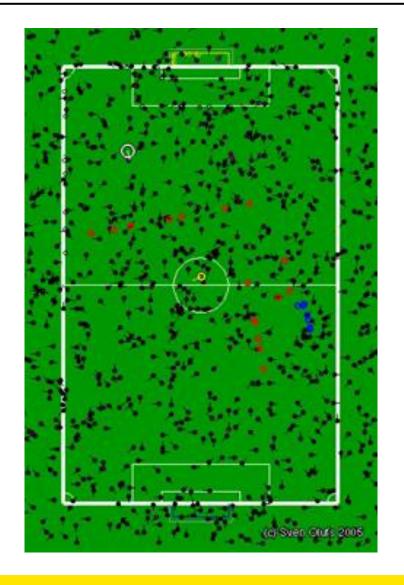


Particle filter localisation – Example I: Tracking





Particle filter localisation – Example II: Soccer robot





Particle filter localisation – Summary

Advantages

- Localisation starting from any unknown position (global localisation)
- Recovers from ambiguous situation
- Can represent any arbitrary probability density function over the robot position
- Less computational burden compared to Markov Localisation

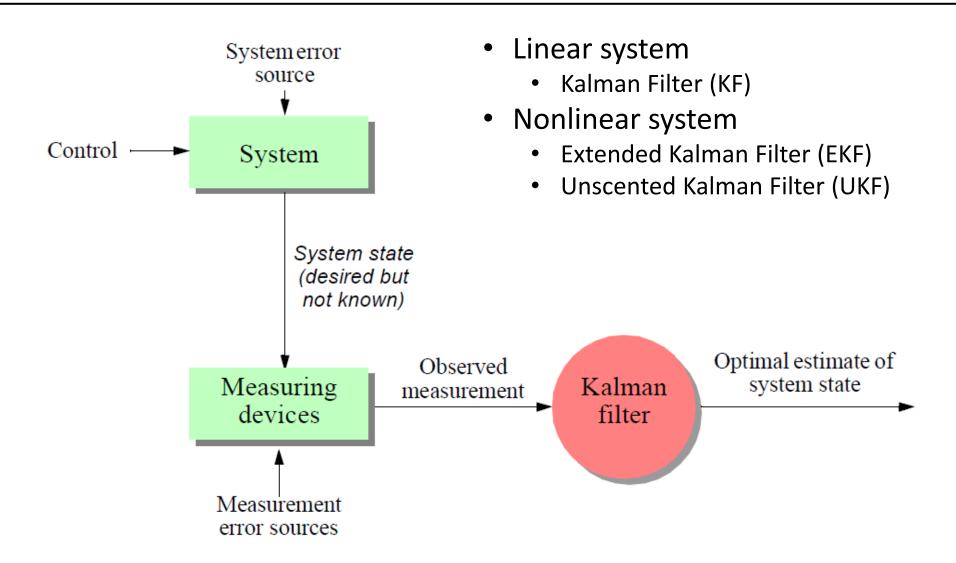
Disadvantages

- Complete nature of Markov Localisation is violated by sampling approaches
- Still requires large computation resources



Kalman Filter Localisation

Kalman filter localisation

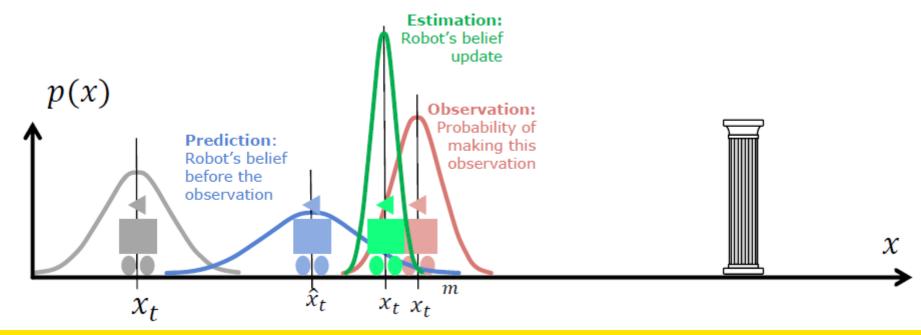




Rudolf Emil Kalman (1930 - 2016)

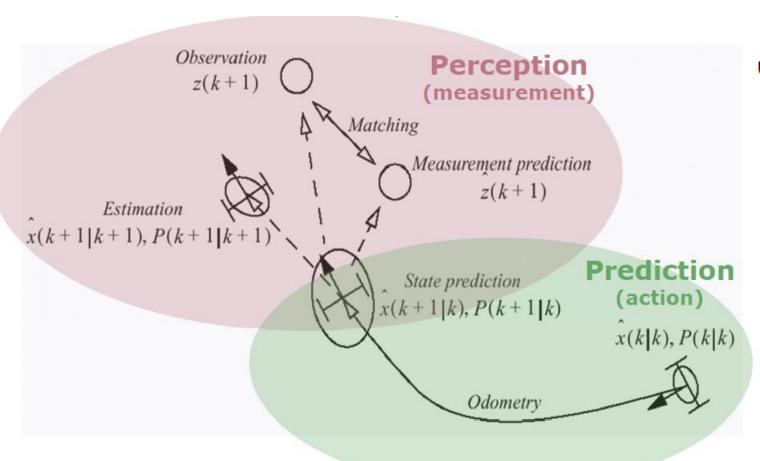
Kalman filter localisation

- Prediction update
 - Applying the theorem of total probability and using previous estimate and odometry
- Measurement update
 - Observation with on-board sensors
 - Measurement prediction based on prediction and map
 - Matching of observation and map
 - Estimation: position update





Kalman filter localisation



Predict [edit]

Predicted (a priori) state estimate

Predicted (a priori) error covariance

$$egin{aligned} \hat{\mathbf{x}}_{k|k-1} &= \mathbf{F}_k \hat{\mathbf{x}}_{k-1|k-1} + \mathbf{B}_k \mathbf{u}_k \ \mathbf{P}_{k|k-1} &= \mathbf{F}_k \mathbf{P}_{k-1|k-1} \mathbf{F}_k^\mathsf{T} + \mathbf{Q}_k \end{aligned}$$

Update [edit]

Innovation or measurement pre-fit

residual

Innovation (or pre-fit residual)

covariance

Optimal Kalman gain

Updated (a posteriori) state estimate

Updated (a posteriori) estimate

covariance

Measurement post-fit residual

$$\tilde{\mathbf{y}}_k = \mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_{k|k-1}$$

$$\mathbf{S}_k = \mathbf{H}_k \mathbf{P}_{k|k-1} \mathbf{H}_k^\mathsf{T} + \mathbf{R}_k$$

$$\mathbf{K}_k = \mathbf{P}_{k|k-1} \mathbf{H}_k^\mathsf{T} \mathbf{S}_k^{-1}$$

$$\hat{\mathbf{x}}_{k|k} = \hat{\mathbf{x}}_{k|k-1} + \mathbf{K}_k \tilde{\mathbf{y}}_k$$

$$\mathbf{P}_{k|k} = \left(\mathbf{I} - \mathbf{K}_k \mathbf{H}_k\right) \mathbf{P}_{k|k-1}$$

$$ilde{\mathbf{y}}_{k|k} = \mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_{k|k}$$



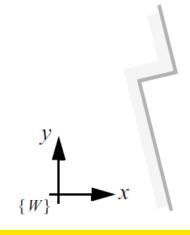
• 1. Position prediction – Based on odometry model

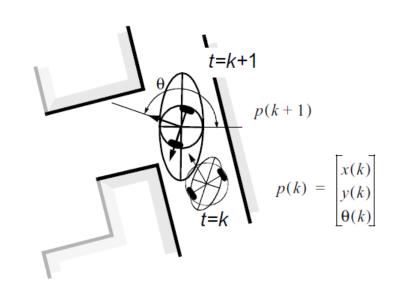
$$\hat{p}(k+1|k) = \hat{p}(k|k) + u(k) = \hat{p}(k|k) + \frac{\Delta s_r + \Delta s_l}{2} \sin\left(\theta + \frac{\Delta s_r - \Delta s_l}{2b}\right)$$

$$\frac{\Delta s_r + \Delta s_l}{2} \sin\left(\theta + \frac{\Delta s_r - \Delta s_l}{2b}\right)$$

$$\frac{\Delta s_r - \Delta s_l}{b}$$

$$\Sigma_{p}(k+1|k) = \nabla_{p} f \cdot \Sigma_{p}(k|k) \cdot \nabla_{p} f^{T} + \nabla_{u} f \cdot \Sigma_{u}(k) \cdot \nabla_{u} f^{T}$$







• 2. Measurement prediction – Based on map and predicted position

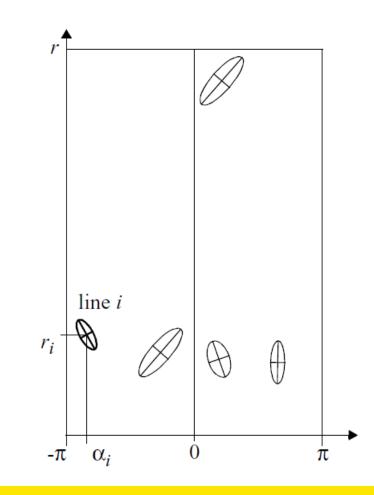
$$\hat{z}_{i}(k+1) = \begin{bmatrix} \alpha_{t,i} \\ r_{t,i} \end{bmatrix} = h_{i}(z_{t,i}, \hat{p}(k+1|k))$$

$$= \begin{bmatrix} w_{\alpha_{t,i}} - w_{\theta}(k+1|k) \\ w_{r_{t,i}} - (w_{x}(k+1|k)\cos(w_{\alpha_{t,i}}) + w_{y}(k+1|k)\sin(w_{\alpha_{t,i}})) \end{bmatrix}$$

$$\theta(k+1)$$

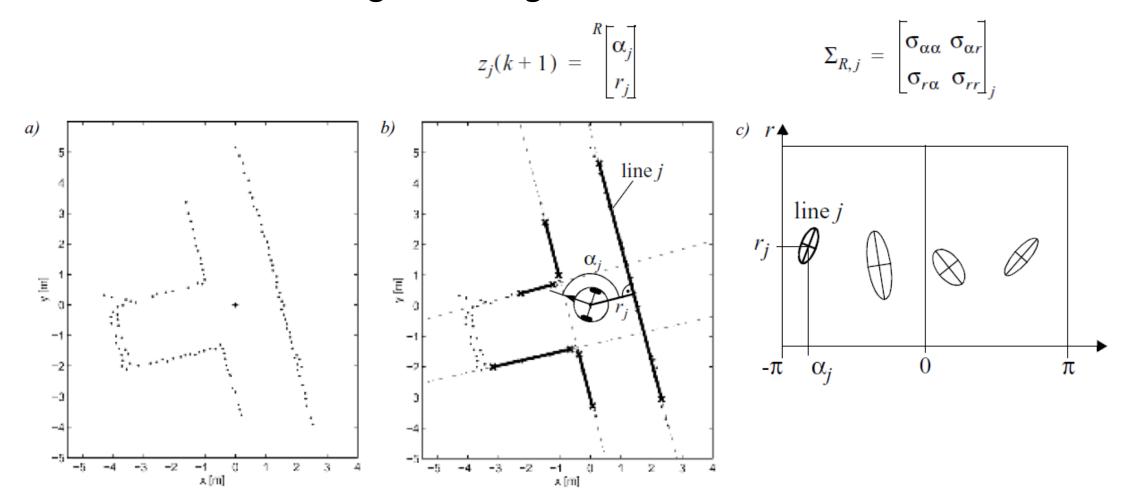
$$\{R\}$$

$$\{R$$



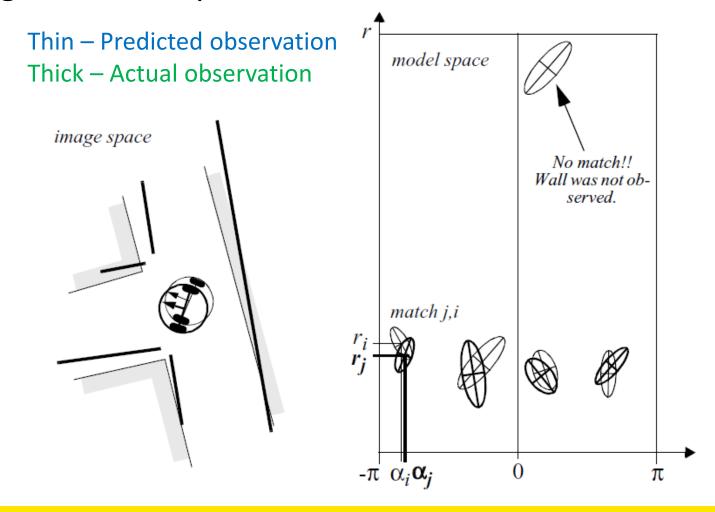


• 3. Observation – Using laser rangefinder



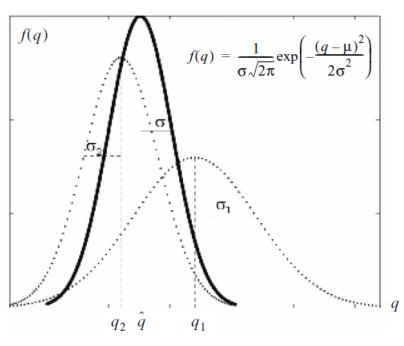


• 4. Matching – Between predicted and actual observation





• 5. Estimation – Applying the Bayes rule

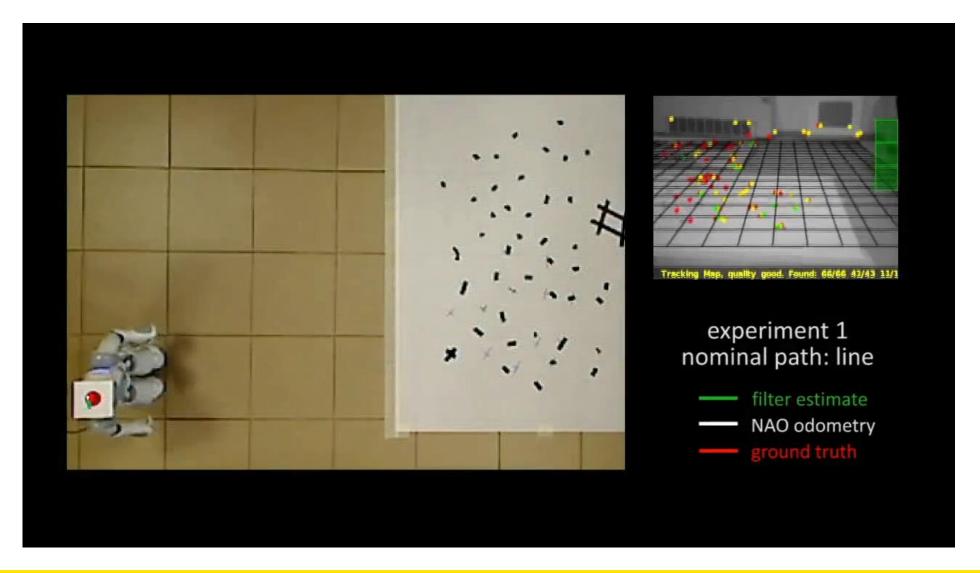




Thin – Prediction of robot position
Thick – Position Measurement
Very thick – updated estimate of
the robot position



Kalman filter localisation – Example





Kalman filter localisation – Summary

Advantages

- Inherently very precise
 - Accurate mathematical formulation
- Very efficient
 - Compact representation of the probability distribution (Gaussian assumption)

Disadvantages

- Not suited for discrete map representation (not an analytic model, e.g., occupancy grid)
- Not suited for global localisation problem as the Gaussian assumption for the probability distribution taken by Kalman filter is violated
- If the uncertainty of the robot becomes too large (e.g., collision with an object), the Kalman filter will fail and the position is definitively lost.



slido

Which of these probabilistic map-based localisation methods do you think are suited for a REAL Micromouse? (select one or more)

(i) Start presenting to display the poll results on this slide.

What if the map is unknown?

SLAM

What is **SLAM** (Simultaneous Localisation and Mapping)?

- Problem statement
 - The computational problem of constructing or updating a map of an unknown environment while simultaneously keeping track of an agent's location within it.

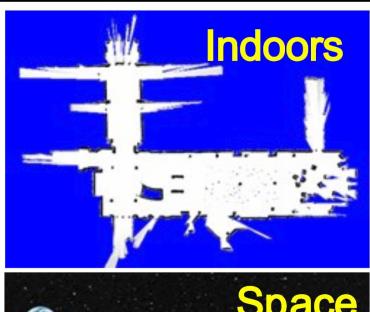
- When is it necessary?
 - When there is no prior knowledge about the environment (in contrast to mapbased localisation), and
 - When the localisation of the robot cannot be determined exclusively on external positioning systems like GPS (in contrast to pure mapping or localisation without mapping)

One of the essential competences of a truly autonomous mobile robot.



What is **SLAM** (Simultaneous Localisation and Mapping)?

- Wide applications:
 - Field robots
 - UGV, UAV, AUV, selfdriving cars, planetary rovers...
 - Medical robots
 - e.g., SLAM inside body
 - VR
 - AR
 - •











SLAM

 One of the most challenging problems in mobile robotics.

- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.
- Loop closure
 - The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



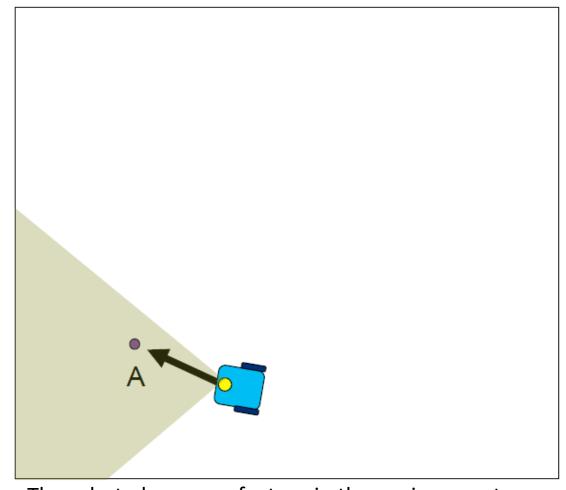
The robot starts with no knowledge about the environment.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

 The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



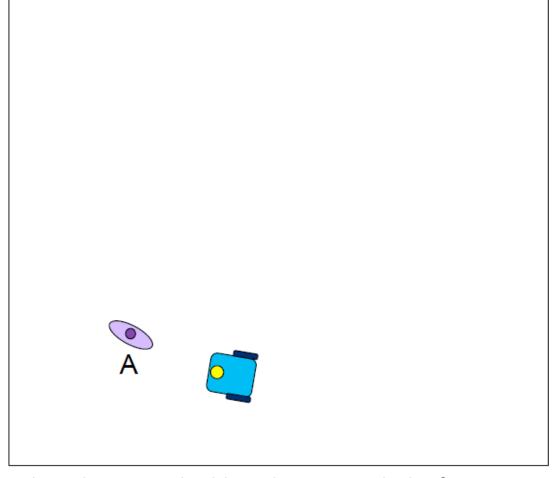
The robot observes a feature in the environment.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

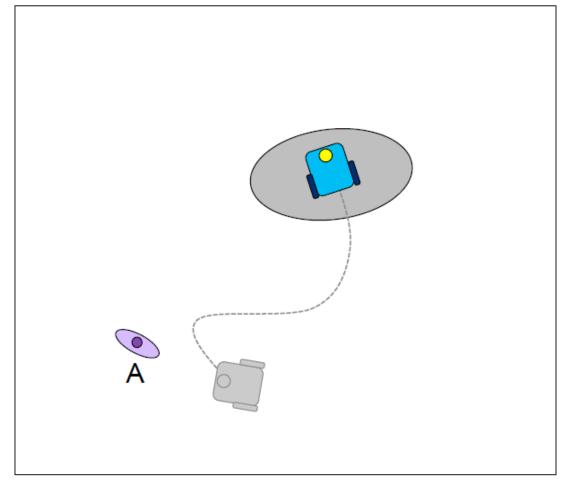
 The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



The robot starts building the map with the feature.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.
- Loop closure
 - The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



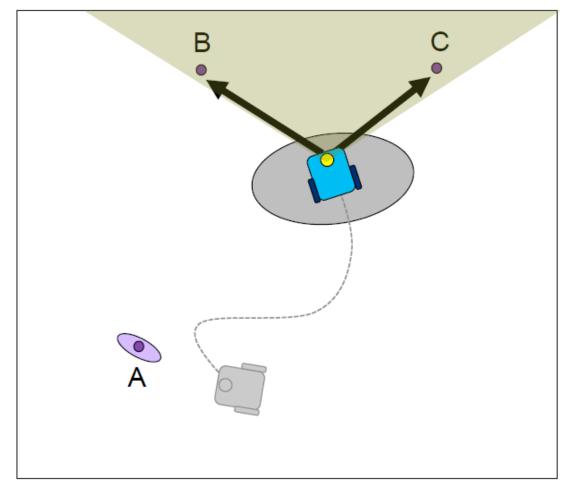
The robot travels for a distance and tracks its location with some uncertainty.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

 The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



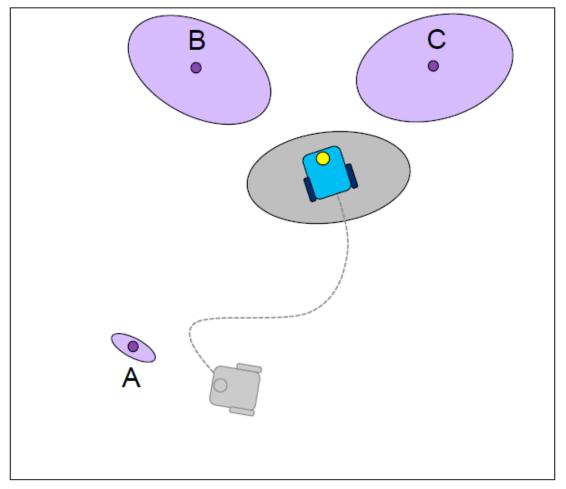
The robot observes two additional features in the environment.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

 The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



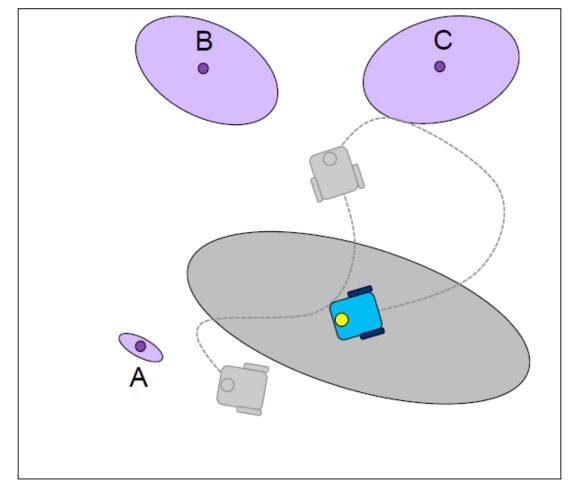
The robot maps these two features with larger uncertainty due to the uncertainty of its own pose.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

• The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



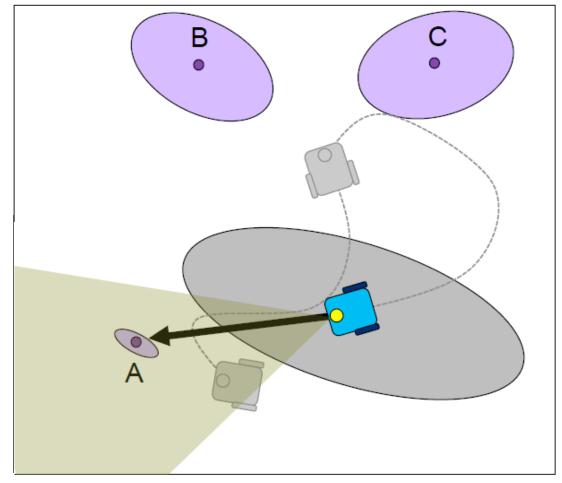
The robot continues moving and the uncertainty of its location accumulates.



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

• The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



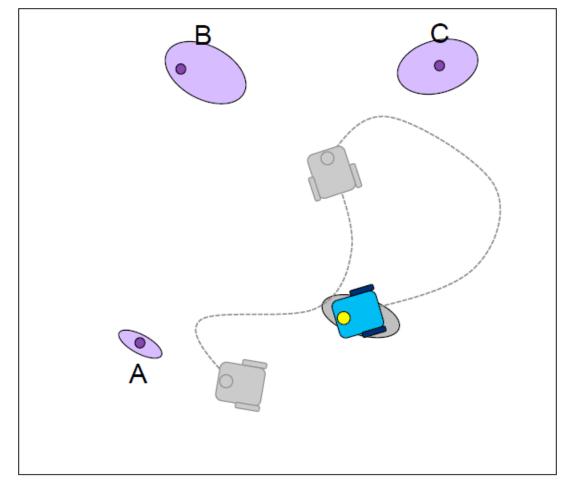
The robot observes a feature that has been observed before (location known in its belief space).



- The *chicken-or-egg* dilemma
 - For localisation the robot needs to know the map;
 - For mapping the robot needs to know its location.

Loop closure

 The uncertainty keeps accumulating until the robot observes features whose location has already been estimated.



The uncertainty of the robot's location and the other features shrinks (loop closure).



SLAM - Methods

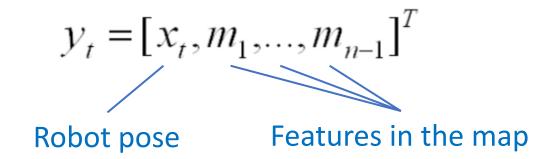
- Three main paradigms
 - Extended Kalman Filter (EKF) SLAM
 - Graph-based SLAM
 - Particle filter SLAM



Extended Kalman Filter (EKF) SLAM

Proceeds exactly like the standard EKF that is used for robot localisation

 Only differentiated in that it uses an extended state vector that consists of both the robot pose and all the features in the map:





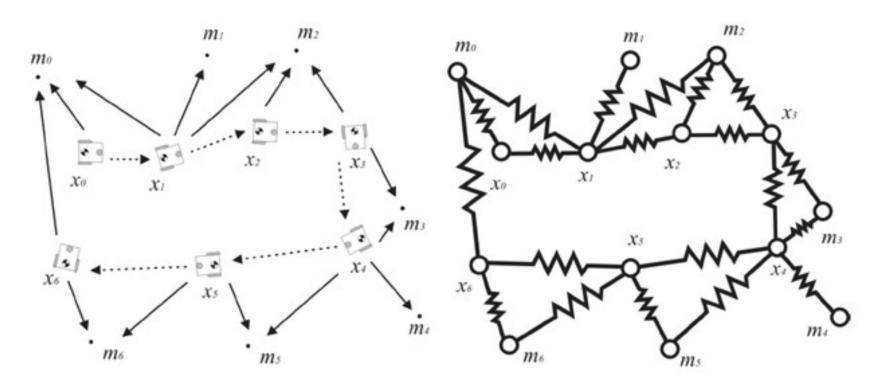
EKF SLAM – Example: MonoSLAM

Real-Time Camera Tracking in Unknown Scenes



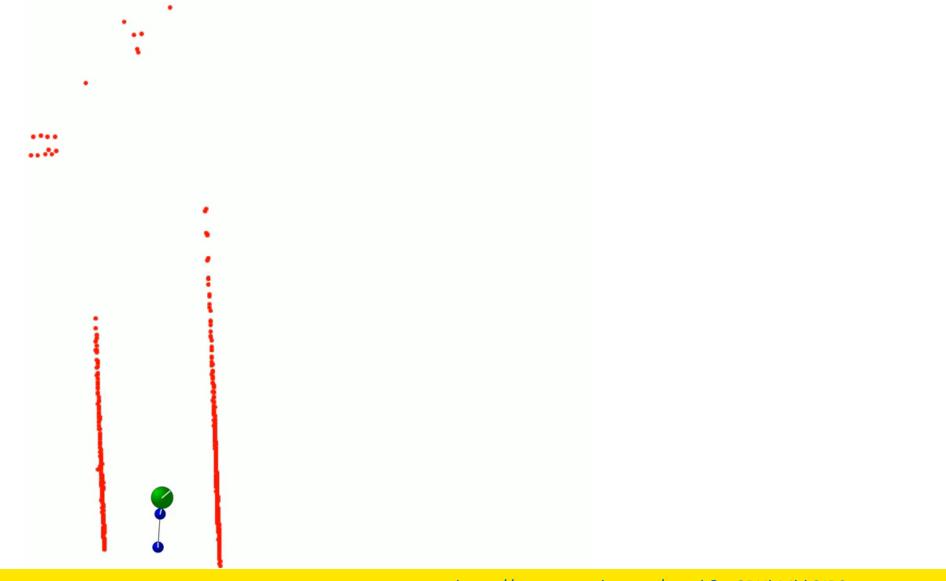
Graph-based SLAM

- Treat the FULL SLAM problem as a graph optimization
- Solve for the constraints between poses and landmarks
- Globally consistent solution, but infeasible for large-scale SLAM



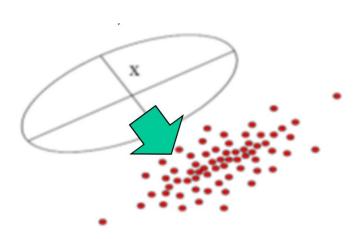


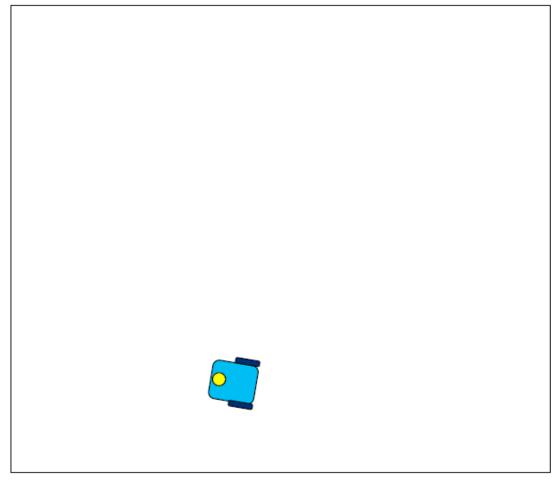
Graph-based SLAM - Example





Uses particles to represent the uncertainty

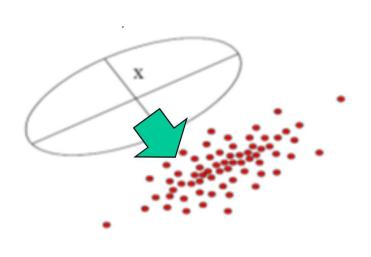


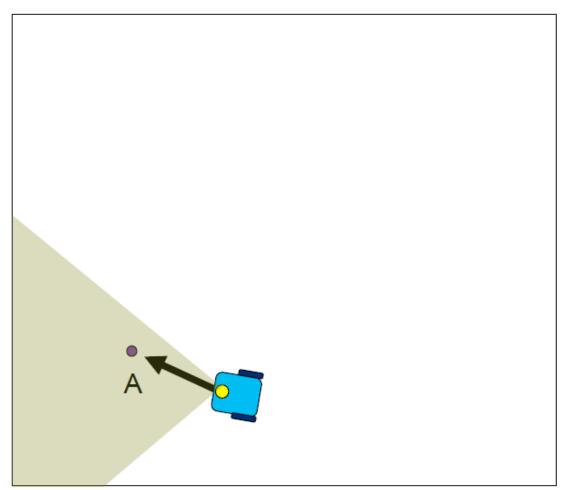


The robot starts with no knowledge about the environment.



Uses particles to represent the uncertainty

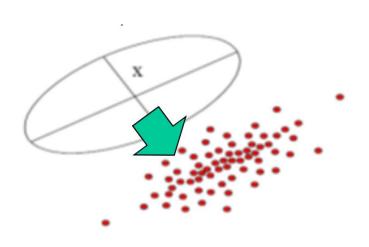


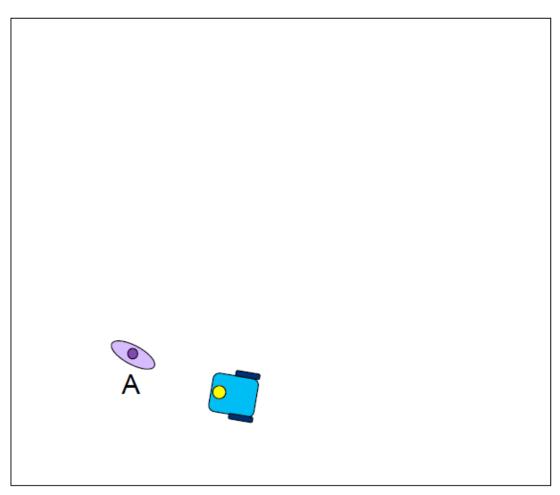


The robot observes a feature in the environment.



Uses particles to represent the uncertainty

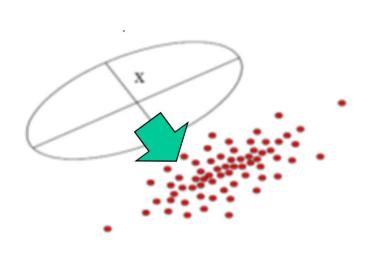


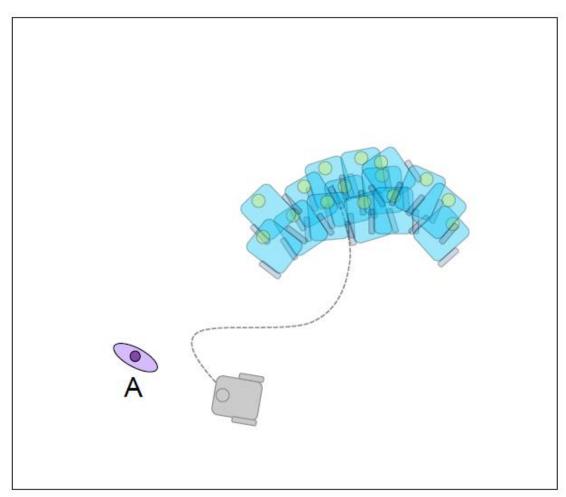


The robot starts building the map with the feature.



Uses particles to represent the uncertainty

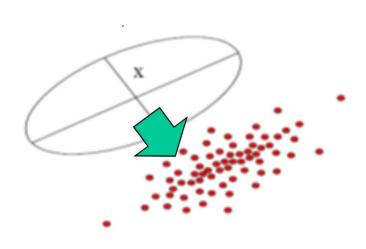


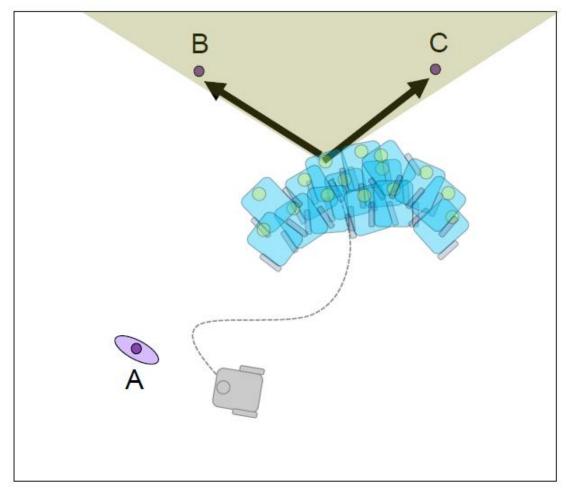


The robot travels for a distance. Particles are used to represent the uncertainty.



Uses particles to represent the uncertainty

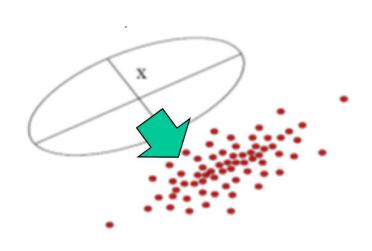


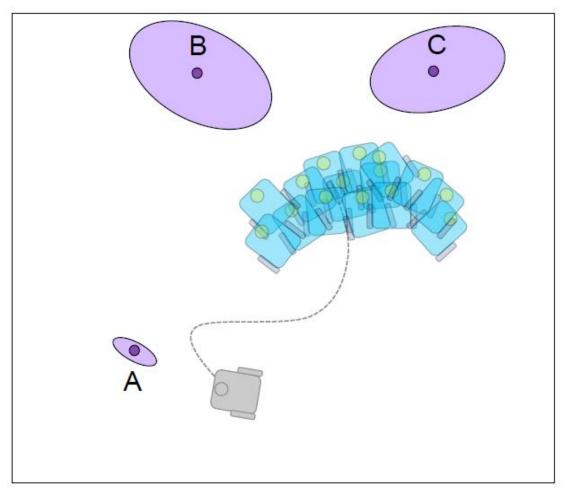


The robot observes two additional features in the map.



Uses particles to represent the uncertainty

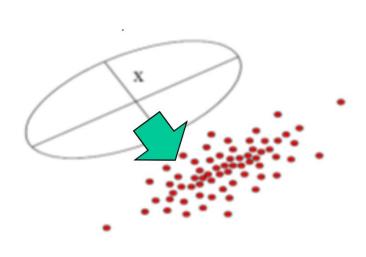


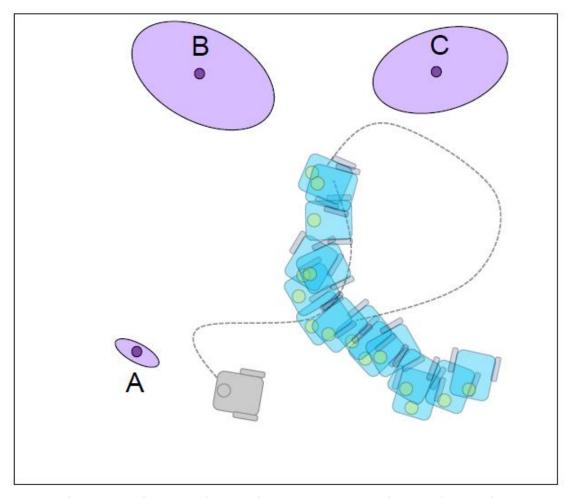


Each particle makes an estimation of the measurements.



Uses particles to represent the uncertainty

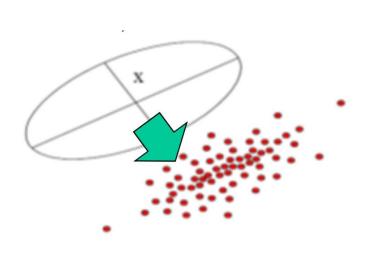


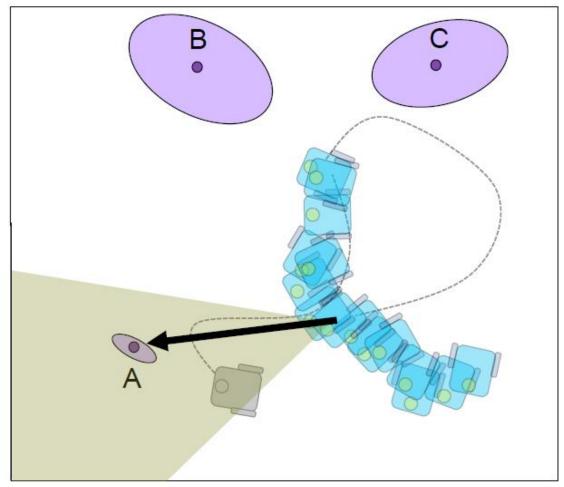


Each particle predicts the next pose based on the motion model.



Uses particles to represent the uncertainty

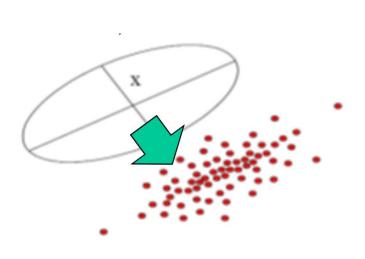


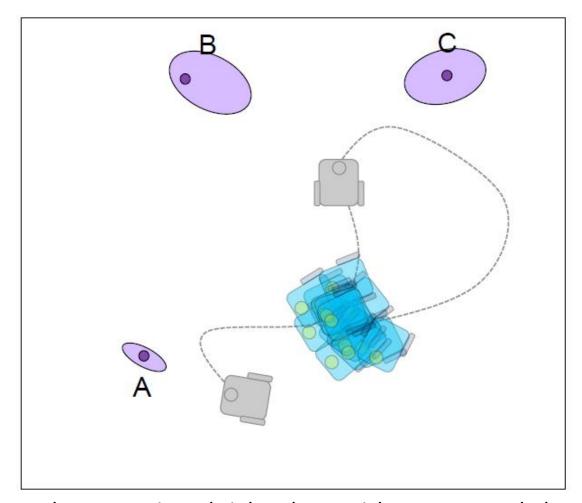


Loop closure. The particles with better match get higher weights.



Uses particles to represent the uncertainty

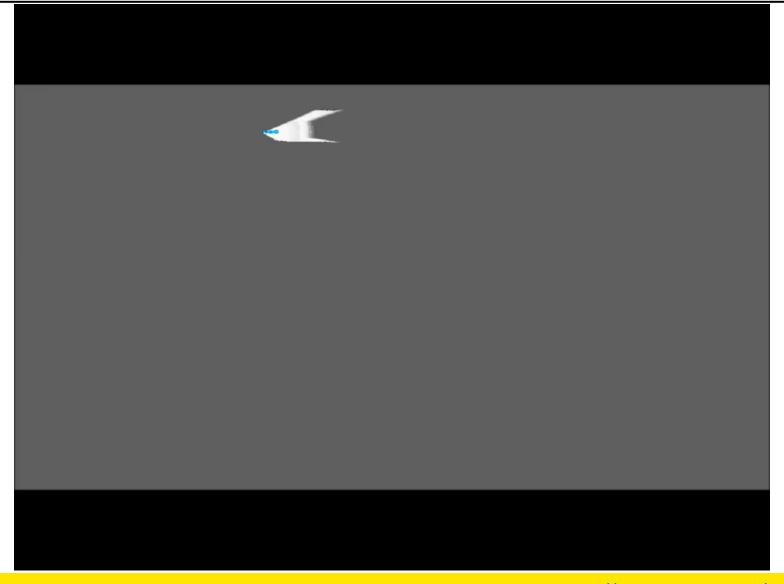




The uncertainty shrinks. The particles are resampled based on weights assigned to the previous particles.



Particle filter SLAM – Example: FastSLAM





SLAM - Summary

EKF SLAM

- Pros
 - Can run online
 - Works for problems with perturbations
- Cons
 - Unimodal estimate
 - States must be well approximated by a Gaussian
 - Computationally expensive for largescale SLAM

Graph-based SLAM

- Pros
 - Information can move backward in time
 - Best possible (most likely) estimate given the data and models
- Cons
 - Computationally demanding
 - Difficult to provide the online estimates for a controller

Particle Filter SLAM

- Pros
 - Noise densities can be from any distribution
 - Works for multi-modal distributions
 - Easy to implement
- Cons
 - Does not scale to highdimensional problems
 - Requires many particles to have good convergence

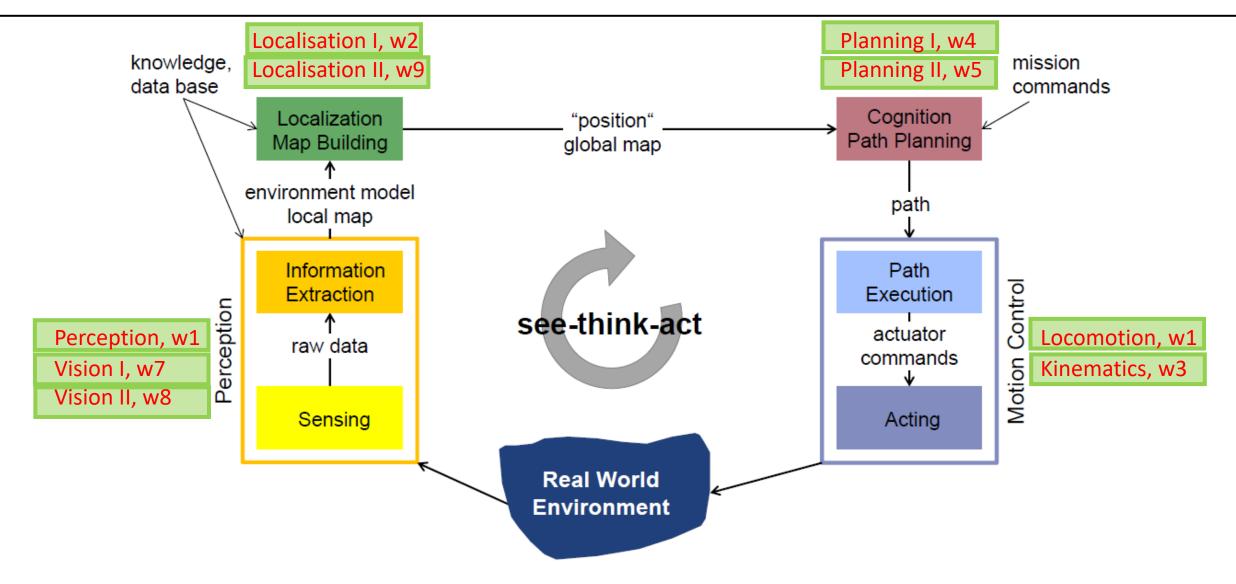


Keyframe-based SLAM – Example: ORB-SLAM on KITTI Dataset





The See-Think-Act cycle





Lecture 10: What's next?