

LLM Reasoning: Key Ideas and Limitations



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Google DeepMind

What do you expect for AI?

Solve the hardest math problems that humans cannot solve?

Discover new scientific theory?

Solve AGI?

...

My *little* expectation for AI

AI should be able to **learn from just a few examples**, like what humans usually do

Does ML meet this expectation?

Semi-supervised learning

Bayesian nonparametric

Kernel machines

Sparsity

Low rank

Active learning

...



What is missing in ML?

Reasoning

Humans can learn from just a few examples
because humans can reason

Let's start from a toy problem

“Make things as simple as possible but no simpler”

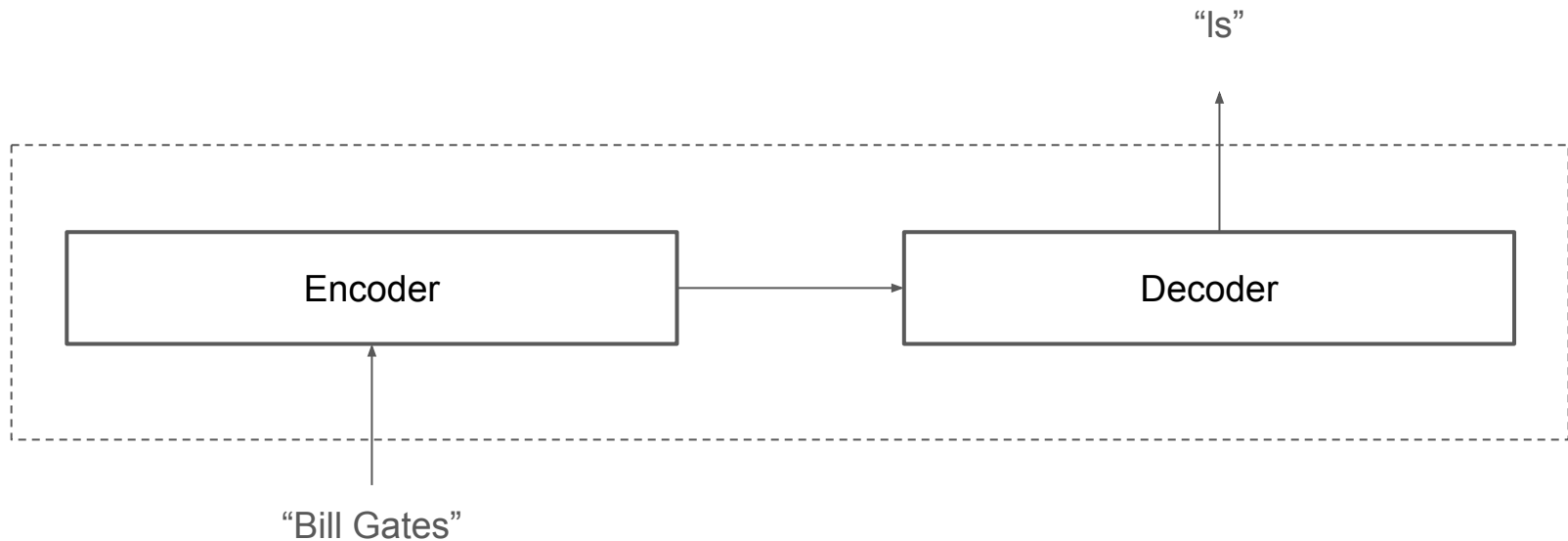
— Albert Einstein

Last Letter Concatenation

Input	Output
“Elon Musk”	“nk”
“Bill Gates”	“ls”
“Barack Obama”	“?”

Rule: Take the last letter of each word, and then concatenate them

Solve it by ML? Tons of labeled data needed!



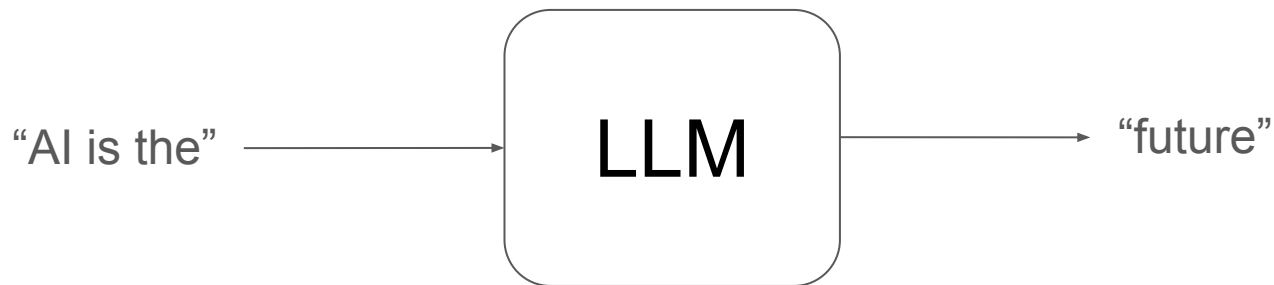
Would you still refer to ML as AI when it requires vast amounts of labeled data to learn such a “simple” task?

Let's see how this problem can
be solved by using large
language models (LLMs)!

What are Large Language Models (LLMs)?

LLM is a “transformer” model trained to predict the next word

Eg “AI is the future”

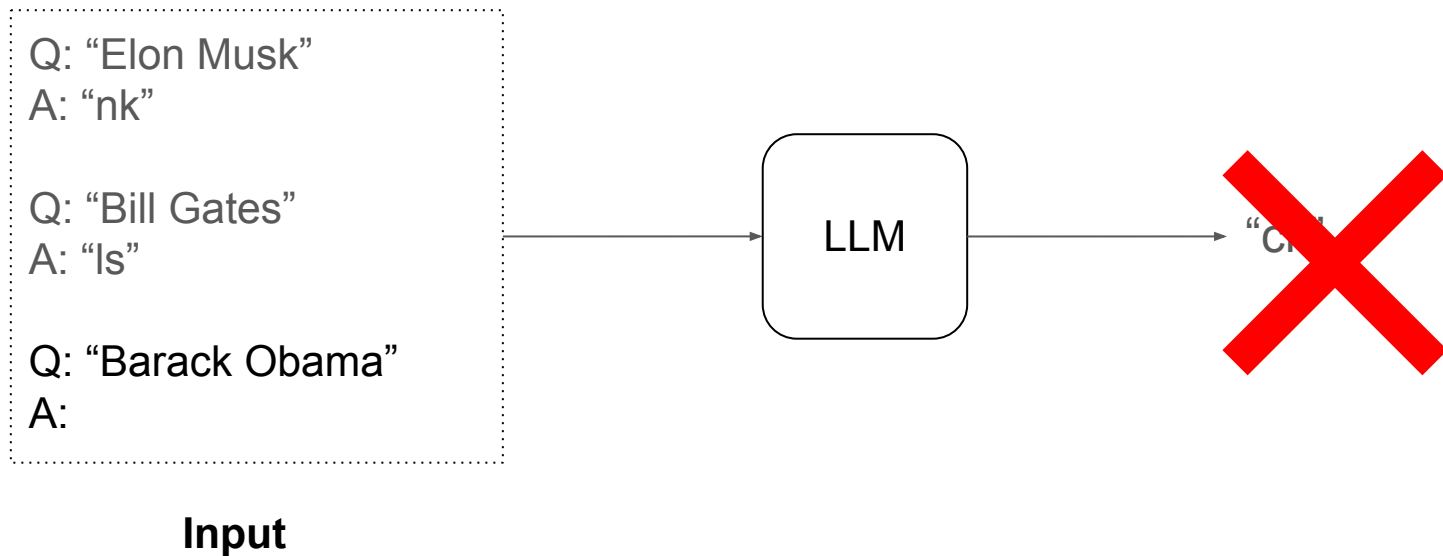


Trained with many sentences, e.g. all texts from the Internet

You can think of training LLMs
as training parrots to mimic
human languages



Few-shot prompting for last-letter-concatenation



Brown, T.B., 2020. Language models are few-shot learners. *arXiv preprint arXiv:2005.14165*.

Let's add “reasoning process” before “answer”

Q: “Elon Musk”

A: the last letter of "Elon" is "n". the last letter of "Musk" is "k". Concatenating "n", "k" leads to "nk". so the output is "nk".

reasoning process

Q: “Bill Gates”

A: the last letter of "Bill" is "l". the last letter of "Gates" is "s". Concatenating "l", "s" leads to "ls". so the output is "ls".

Q: “Barack Obama”

A:

Let's add “reasoning process” before “answer”

Q: “Elon Musk”

A: the last letter of "Elon" is "n". the last letter of "Musk" is "k". Concatenating "n", "k" leads to "nk". so the output is "nk".

reasoning process

Q: “Bill Gates”

A: the last letter of "Bill" is "l". the last letter of "Gates" is "s". Concatenating "l", "s" leads to "ls". so the output is "ls".

Q: “Barack Obama”

A: the last letter of "Barack" is "k". the last letter of "Obama" is "a". Concatenating "k", "a" leads to "ka". so the output is "ka".

One demonstration is enough, like humans

Q: "Elon Musk"

A: the last letter of "Elon" is "n". the last letter of "Musk" is "k". Concatenating "n", "k" leads to "nk". so the output is "nk".

Q: "Barack Obama"

A: the last letter of "Barack" is "k". the last letter of "Obama" is "a". Concatenating "k", "a" leads to "ka". so the output is "ka".

100% accuracy with only one demonstration example

Key Idea: Derive the Final Answer through Intermediate Steps

[Ling et al 2017](#) in DeepMind pioneered using **natural language rationale** to solve math problems by “... **derive the final answer through a series of small steps**”. Trained a sequence-to-sequence model from scratch.

Problem 1:

Question: Two trains running in opposite directions cross a man standing on the platform in 27 seconds and 17 seconds respectively and they cross each other in 23 seconds. The ratio of their speeds is:

Options: A) $3/7$ B) $3/2$ C) $3/88$ D) $3/8$ E) $2/2$

Rationale: Let the speeds of the two trains be x m/sec and y m/sec respectively. Then, length of the first train = $27x$ meters, and length of the second train = $17y$ meters. $(27x + 17y) / (x + y) = 23 \rightarrow 27x + 17y = 23x + 23y \rightarrow 4x = 6y \rightarrow x/y = 3/2$.

Correct Option: B



Ling et al. [Program Induction by Rationale Generation: Learning to Solve and Explain Algebraic Word Problems](#). ACL 2017

GSM8K: <Problem, **Intermediate Steps**, Answer>

Following the work by Ling et al 2017, Cobbe et al 2021 in OpenAI built a much larger math word problem dataset (GSM8K) with natural language rationales, and used it to finetune GPT3

Problem: Ali is a dean of a private school where he teaches one class. John is also a dean of a public school. John has two classes in his school. Each class has $\frac{1}{8}$ the capacity of Ali's class which has the capacity of 120 students. What is the combined capacity of both schools?

Solution: Ali's class has a capacity of 120 students. Each of John's classes has a capacity of $120/8 = 15$ students. The total capacity of John's two classes is $15 \text{ students} * 2 \text{ classes} = 30 \text{ students}$. The combined capacity of the two schools is $120 \text{ students} + 30 \text{ students} = 150 \text{ students}$.

Final answer: 150



Cobbe et al. Training Verifiers to Solve Math Word Problems. [arXiv:2110.14168](https://arxiv.org/abs/2110.14168) [cs.LG]. 2021

Show Your Work: Scratchpads for Intermediate Computation with Language Models

Input:

2 9 + 5 7

Target:

<scratch>

2 9 + 5 7 , C: 0

2 + 5 , 6 C: 1 # added 9 + 7 = 6 carry 1

, 8 6 C: 0 # added 2 + 5 + 1 = 8 carry 0

0 8 6

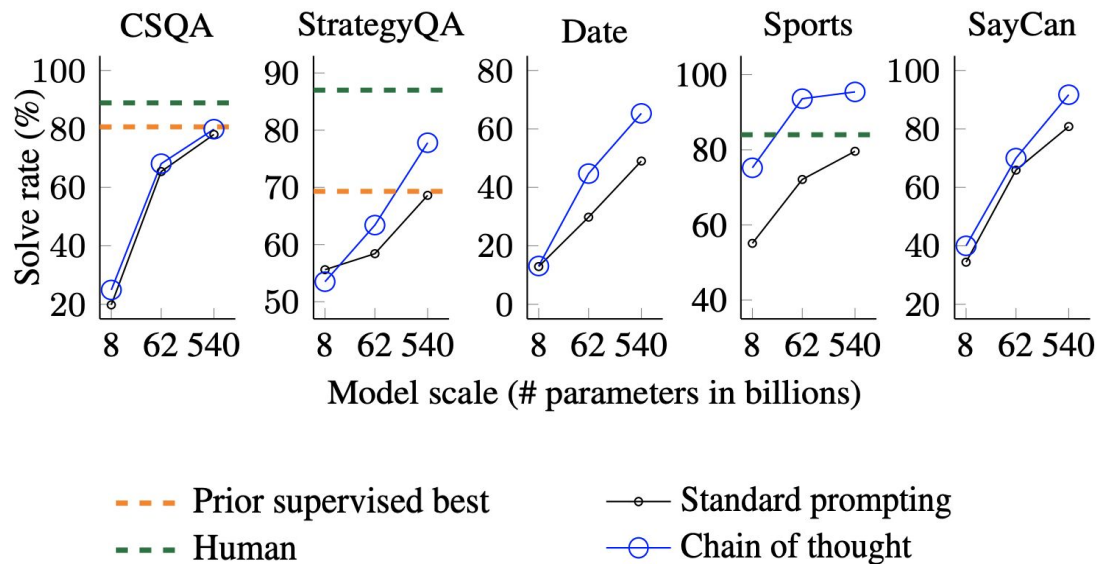
</scratch>

8 6



Nye et al. Show Your Work: Scratchpads for Intermediate Computation with Language Models. [arXiv:2112.00114](https://arxiv.org/abs/2112.00114) [cs.LG], 2021

Chain-of-Thought (CoT) Prompting



Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten Bosma, Brian Ichter, Fei Xia, Ed Chi, Quoc Le, and Denny Zhou.
[Chain-of-thought prompting elicits reasoning in large language models](#). NeurIPS 2022

Training with intermediate steps (Ling et al 2017)



Training with intermediate steps (Cobbe et al 2021, Nye et al 2021)

Pre-training with intermediate steps (Nye et al 2021, Wei et al 2022)

This is what really matters!

Regardless of training, fine-tuning, or prompting, when provided with examples that include intermediate steps, LLMs will respond with intermediate steps

Is it also helpful to add reasoning strategies in demonstration examples?

Least-to-Most Prompting

Enable easy-to-hard generalization by decomposition

Denny Zhou, Nathanael Schärli, Le Hou, Jason Wei, Nathan Scales, Xuezhi Wang, Dale Schuurmans, Claire Cui, Olivier Bousquet, Quoc Le, Ed Chi. [Least-to-Most Prompting Enables Complex Reasoning in Large Language Models](#). ICLR 2023.



How to Solve It

a new aspect of
mathematical method

*With a new foreword
by John H. Conway*

G. POLYA

Decomposing and recombining are important operations of the mind.

differently. You decompose the whole into its parts, and you recombine the parts into a more or less different whole.

1. If you go into detail you may lose yourself in details. Too many or too minute particulars are a burden on the mind. They may prevent you from giving sufficient attention to the main point, or even from seeing the main point at all. Think of the man who cannot see the forest for the trees.

Elsa has 3 apples. Anna has 2 more apples than Elsa. How many apples do they have together?

Let's break down this problem: 1. How many apples does Anna have? 2. How many apples do Elsa and Anna have together?

1. Anna has 2 more apples than Elsa. So Anna has $2 + 3 = 5$ apples.
 2. Anna has 5 apples. Elsa and Anna have $3 + 5 = 8$ apples together.
- The answer is 8.

SCAN (Compositional Generalization)

Command	Action Sequence
“look thrice after jump”	JUMP LOOK LOOK LOOK
“run left and walk”	TURN_LEFT RUN WALK
“look opposite right”	TURN_RIGHT TURN_RIGHT LOOK

Method	Standard prompting	Chain-of-Thought	Least-to-Most
code-davinci-002	16.7	16.2	99.7
text-davinci-002	6.0	0.0	76.0
code-davinci-001	0.4	0.0	60.7

Using just 0.1% demonstration examples achieves perfect generalization

CFQ (Compositional Generalization): Text-to-Code

	MCD1	MCD2	MCD3	Ave.
Fully Supervised				
T5-base (Herzig et al., 2021)	58.5	27.0	18.4	34.6
T5-large (Herzig et al., 2021)	65.1	32.3	25.4	40.9
T5-3B (Herzig et al., 2021)	65.0	41.0	42.6	49.5
HPD (Guo et al., 2020)	79.6	59.6	67.8	69.0
T5-base + IR (Herzig et al., 2021)	85.8	64.0	53.6	67.8
T5-large + IR (Herzig et al., 2021)	88.6	79.2	72.7	80.2
T5-3B + IR (Herzig et al., 2021)	88.4	85.3	77.9	83.9
LeAR (Liu et al., 2021)	91.7	89.2	91.7	90.9
Prompting				
(Ours) Dynamic Least-to-Most	94.3	95.3	95.5	95.0

Using just 1% data!

Andrew Drozdov, Nathanael Schärli, Ekin Akyürek, Nathan Scales, Xinying Song, Xinyun Chen, Olivier Bousquet, Denny Zhou. [Compositional Semantic Parsing with Large Language Models](#). ICLR 2023.

Why intermediate steps are helpful?

“There is nothing more practical than a good theory.”

— Kurt Lewin

- **Constant-depth transformers** can solve any inherently serial problem as long as it generates sufficiently long intermediate reasoning steps
- **Transformers which directly generate final answers** either requires a huge depth to solve or cannot solve at all

Zhiyuan Li, Hong Liu, Denny Zhou, and Tengyu Ma. [Chain of Thought Empowers Transformers to Solve Inherently Serial Problems](#). ICLR 2024.

Tons of practical implications of this theory

Generating more intermediate steps (think longer)

Too long to generate? Calling external tools e.g. MCTS

Distill test-time search? You will need a huge depth!

Which to choose: transformer vs RNN/SSM

...

Is it possible to trigger step by step reasoning without using demonstration examples?

Let's think step by step

Q: A juggler can juggle 16 balls. Half of the balls are golf balls, and half of the golf balls are blue. How many blue golf balls are there?

A: The answer (arabic numerals) is

(Output) 8 ✗

Q: A juggler can juggle 16 balls. Half of the balls are golf balls, and half of the golf balls are blue. How many blue golf balls are there?

A: **Let's think step by step.**

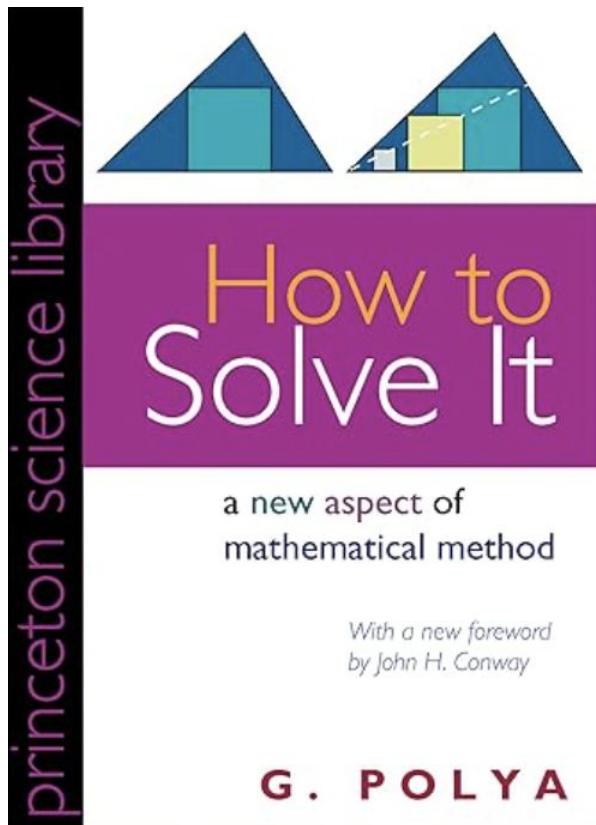
(Output) *There are 16 balls in total. Half of the balls are golf balls. That means that there are 8 golf balls. Half of the golf balls are blue. That means that there are 4 blue golf balls. ✓*

Kojima, T., Gu, S.S., Reid, M., Matsuo, Y. and Iwasawa, Y. Large language models are zero-shot reasoners. NeurIPS 2022.

Hmm, zero-shot is cool but usually significantly worse than few-shot ...

LLMs as Analogical Reasoners

Michihiro Yasunaga, Xinyun Chen, Yujia Li, Panupong Pasupat, Jure Leskovec, Percy Liang, Ed H. Chi, Denny Zhou. [Large Language Models as Analogical Reasoners](#). ICLR 2024.



Do you know a related problem? We can scarcely imagine a problem absolutely new, unlike and unrelated to any formerly solved problem; but, if such a problem could exist, it would be insoluble. In fact, when solving a problem, we always profit from previously solved problems, using their result, or their method, or the experience we acquired solving them. And, of course, the problems from which we profit must be in some way related to our present problem. Hence the question: *Do you know a related problem?*

There is usually no difficulty at all in recalling formerly solved problems which are more or less related

“A mathematician is a person who can find analogies between theorems; a better mathematician is one who can see analogies between proofs and the best mathematician can notice analogies between theories. One can imagine that the **ultimate mathematician is one who can see analogies between analogies.**”

— Stefan Banach

What is the area of the square with the four vertices at $(-2, 2)$, $(2, -2)$, $(-2, -6)$, and $(-6, -2)$? Recall a related problem, and then solve this one.

LLM

The related problem is finding the distance between two points on a coordinate plane. To find the distance between two points, we use the distance formula: $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$.

In this problem, we have four points: $(-2, 2)$, $(2, -2)$, $(-2, -6)$, and $(-6, -2)$. Let's choose $(-2, 2)$ and $(2, -2)$ to find the distance d between them: $d = \sqrt{((2 - (-2)))^2 + (-2 - 2)^2} = \sqrt{(4)^2 + (-4)^2} = \sqrt{(16 + 16)} = \sqrt{32}$. We know that the distance between two opposite sides of a square is equal. So, the length of each side of the square is $\sqrt{32}$. To find the area of the square, we square the length of one side: $\text{Area} = (\sqrt{32})^2 = 32$.

Analogical reasoner vs zero-shot / few-shot CoT

Prompting Method	GSM8K Accuracy			MATH Accuracy	
	GPT3.5-turbo	text-davinci-003	PaLM2	GPT3.5-turbo	PaLM2
0-shot	75.0%	14.8%	60.8%	33.0%	27.1%
0-shot CoT	75.8%	50.3%	78.2%	33.9%	29.8%
5-shot CoT	76.7%	54.0%	80.7%	34.9%	34.3%
Ours: Self-generated Exemplars	77.8%	61.0% [†]	81.7%	37.3%	34.8%

Analogical reasoner vs zero-shot / few-shot CoT

Prompting Method	Word sorting	Logical deduction five objects	Temporal sequences	Reasoning about colored objects	Formal fallacies
0-shot	66.8%	30.0%	40.4%	50.4%	53.6%
0-shot CoT	67.6%	35.2%	44.8%	61.6%	55.6%
3-shot CoT	68.4%	36.4%	58.0%	62.0%	55.6%
Ours: Self-generated Exemplars	75.2%	41.6%	57.6%	68.0%	58.8%

google/**BIG-bench**

Analogical reasoner vs zero-shot / few-shot CoT

Prompting Method	GPT3.5-turbo-16k		GPT4	
	Acc@1	Acc@10	Acc@1	Acc@10
0-shot	8%	24%	16%	30%
0-shot CoT	9%	27%	16%	29%
3-shot CoT	11%	27%	17%	31%
Ours: Self-generated Exemplars	13%	25%	17%	32%
Ours: Self-generated Knowledge + Exemplars	15%	29%	19%	37%

Analogical reasoning:
adaptively generate relevant
examples and knowledge,
rather than just using a fix set of
examples



Is it possible to trigger step by step reasoning even without using any prompt like “let’s think step by step”?

Chain-of-Thought Reasoning without Prompting

Xuezhi Wang and Denny Zhou. [Chain-of-Thought Reasoning Without Prompting](#).
arXiv preprint arXiv:2402.10200 (2024).

I have 3 apples, my dad has 2 more apples than me, how many apples do we have in total?

Decoding at step 0	Full generation after continuing greedy decoding
Top-1: 5	5 apples.
Top-2: I	I have 3 apples, my dad has 2 more apples than me, so he has 5 apples. $3+5=8$.
Top-3: We	We have 8 apples in total.
Top-4: You	You have 3 apples, your dad has 2 more apples than you, so he has 5 apples. $3+5=8$.
Top-5: The	The answer is 5.

Chain-of-Thought Decoding

Was Nicolas Cage born in an even or odd year?

Top-1: Nicolas	Nicolas Cage was born in an odd year.
Top-2: Even	Even.
Top-3: Odd	Odd.
Top-4: 1964	1964, an even year.
Top-5: He	He was born in an even year.
Top-6: Cage	Cage was born in 1964, an even year.

Chain-of-Thought Decoding

Probability for the answer token

1	Nicolas Cage was born in an odd year.	0.117
2	Even.	0.207
3	Odd.	0.198
4	1964, an even year.	0.949
5	He was born in an even year.	0.000
6	Cage was born in 1964, an even year.	0.978

Chain-of-Thought Decoding

Key takeaways

1. Pre-trained LLMs, without further finetuning, has been ready for step-by-step reasoning, but we need a non-greedy decoding strategy to elicit it
2. When a step-by-step reasoning path is present, LLMs have much higher confidence in decoding the final answer than direct-answer decoding

		PaLM-2 Pre-trained				PaLM-2 Inst-tuned
		X-Small	Small	Medium	Large	Large
GSM8K	greedy	9.0	14.3	21.0	34.8	67.8
	CoT-decoding	17.7 (+8.7)	35.1 (+20.8)	39.7 (+18.7)	61.5 (+26.7)	81.3 (+13.5)
MultiArith	greedy	7.5	15.8	36.8	75.0	93.7
	CoT-decoding	34.8 (+27.3)	43.5 (+27.7)	52.5 (+15.7)	86.7 (+11.7)	98.7 (+5.0)

Greedy Decoding vs Chain-of-Thought Decoding

Generating intermediate steps
are helpful, but ...

Any concern on generating intermediate steps instead of direct answers?



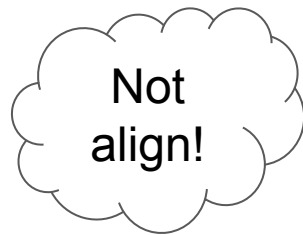
Always keep in mind that LLMs are probabilistic models of generating next tokens. **They are not humans.**

What LLM does in decoding:

$$\arg \max \mathbb{P}(\text{reasoning path, final answer} | \text{problem})$$

What we want:

$$\arg \max \mathbb{P}(\text{final answer} | \text{problem})$$



One-step further

$$\begin{aligned} & \arg \max \mathbb{P}(\text{final answer}|\text{problem}) \\ = & \sum_{\text{reasoning path}} \mathbb{P}(\text{ reasoning path, final answer}|\text{problem}) \end{aligned}$$

How to compute the sum then? Sampling!

Self-Consistency

Greatly improves step-by-step reasoning

Xuezhi Wang, Jason Wei, Dale Schuurmans, Quoc Le, Ed Chi, Sharan Narang, Aakanksha Chowdhery, Denny Zhou.
[Self-Consistency Improves Chain of Thought Reasoning in Language Models](#). ICLR 2023.

[Question] Janet's ducks lay 16 eggs per day. She eats three for breakfast every morning and bakes muffins for her friends every day with four. She sells the remainder for \$2 per egg. How much does she make every day?

Sampled responses:

Response 1: She has $16 - 3 - 4 = 9$ eggs left. So she makes $\$2 * 9 = \18 per day.

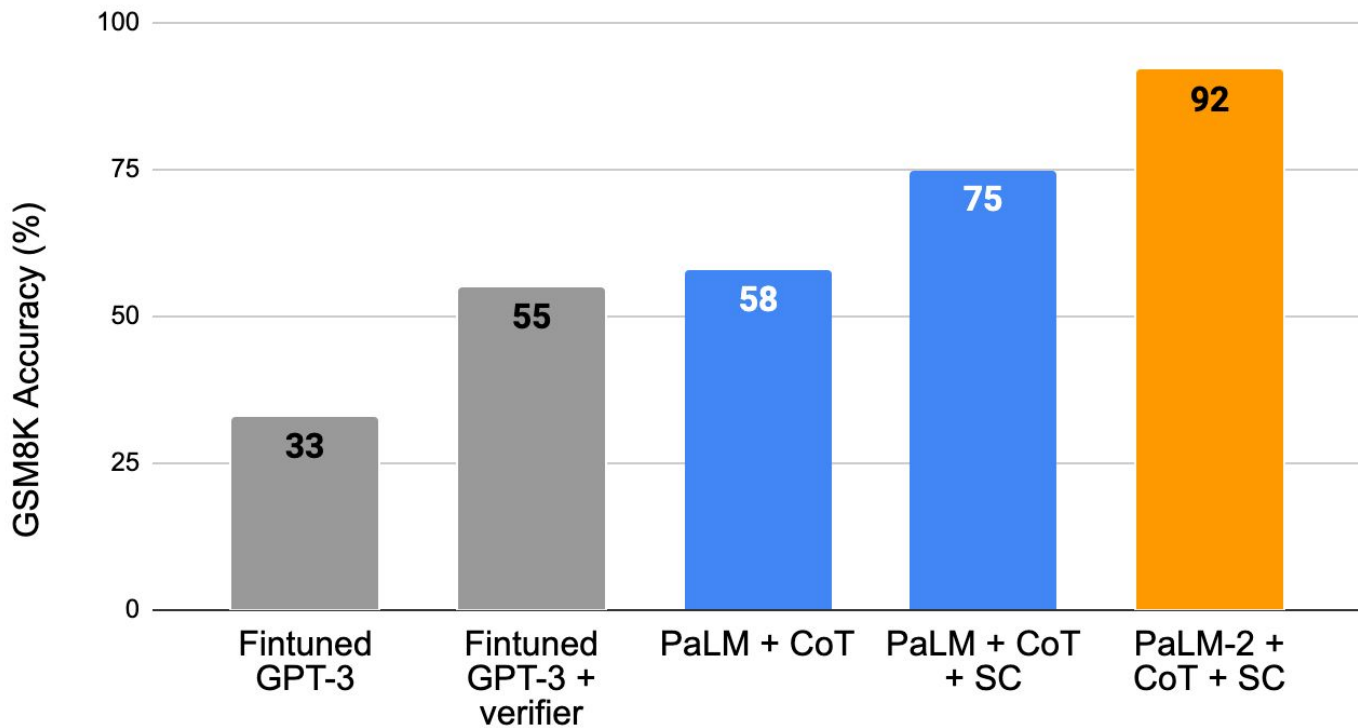
Response 2: This means she she sells the remainder for $\$2 * (16 - 4 - 3) = \26 per day.

Response 3: She eats 3 for breakfast, so she has $16 - 3 = 13$ left. Then she bakes muffins, so she has $13 - 4 = 9$ eggs left. So she has $9 \text{ eggs} * \$2 = \18 .

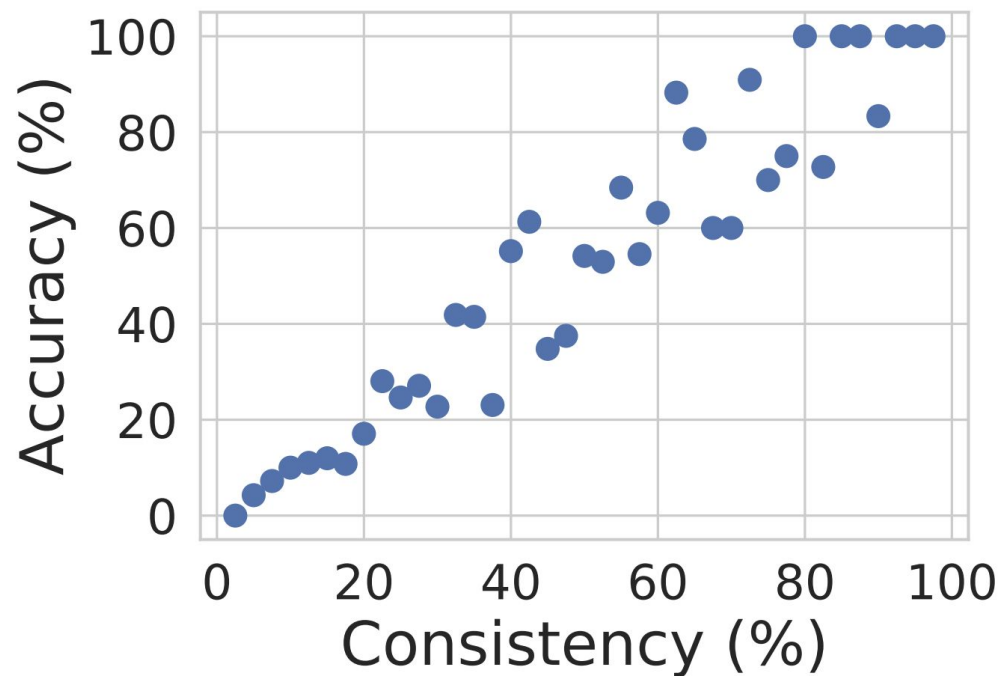
Most frequent answer is: 18
(Not most frequent reasoning path!)



Crushed GSM8K SOTA with only 8 examples



More consistent, more likely to be correct



QUIZ

[Q1] When the LLM outputs a direct answer without intermediate steps, will you still sample several times, and then choose the most common answer?

[Q2] Change self-consistency by letting LLM generate multiple responses, instead of sampling multiple times, and then choosing the most common answer. Does this make sense?



$$\arg \max \mathbb{P}(\text{final answer} | \text{problem})$$

How about free-from answers?

Universal Self-Consistency (USC)

Ask LLMs to self-select the most consistent answer

Xinyun Chen, Renat Aksitov, Uri Alon, Jie Ren, Kefan Xiao, Pengcheng Yin, Sushant Prakash, Charles Sutton, Xuezhi Wang, Denny Zhou.
[Universal Self-Consistency for Large Language Model Generation](#). arXiv:2311.17311 [cs.CL], 2023.

[Question] Where do people drink less coffee than they do in Mexico?

Response 1: ... Some examples include Japan, China and the United Kingdom.

It is important to note that coffee consumption can vary among individuals within these countries, and preferences can change depending on different factors such as...

Response 2: People in countries like Japan, China, and India typically drink less coffee than they do in Mexico...

Response 3: There are several countries where people generally drink less coffee compared to Mexico. Some of these countries include:

1. Japan:...
2. China...
3. Saudi Arabia...
4. India...

...

The most consistent response: 2

Limitations

LLMs Can Be Easily Distracted by Irrelevant Context

Freda Shi, Xinyun Chen, Kanishka Misra, Nathan Scales, David Dohan, Ed Chi, Nathanael Schärli, and Denny Zhou. [Large Language Models Can Be Easily Distracted by Irrelevant Context](#). **ICML 2023**.

Humans may be easily distracted by irrelevant context

Psychology studies show that irrelevant information may significantly decrease some children and even adults problem-solving accuracy

... inattentive children's difficulties in problem solving are partially due to an inability to inhibit irrelevant information ...

Does this observation
hold for LLMs?

Marzocchi, G.M., Lucangeli, D., De Meo, T., Fini, F. and Cornoldi, C., 2002. The disturbing effect of irrelevant information on arithmetic problem solving in inattentive children. *Developmental neuropsychology*, 21(1), pp.73-92.

Adding irrelevant contexts to GSM8K leads to 20+ points performance drop

Lucy has \$65 in the bank. She made a \$15 deposit and then followed by a \$4 withdrawal. Maria's monthly rent is \$10. What is Lucy's bank balance?

LLM

Lucy's bank balance is $\$65 + \$15 - \$4 - \$10 = \$66$. The answer is \$66.

Prompting LLMs to Ignore irrelevant context can take some performance back

Lucy has \$65 in the bank. She made a \$15 deposit and then followed by a \$4 withdrawal.
Maria's monthly rent is \$10. What is Lucy's bank balance? Ignore irrelevant context.

LLM

Lucy has \$65 in the bank. After making a \$15 deposit and then a \$4 withdrawal, her bank balance is \$76. Maria's monthly rent is not relevant to this question, so it can be ignored. The answer is \$76.

We can simply add many irrelevant sentences

The sky is blue. The sky is blue. The sky is blue. The sky is blue.

Lucy has \$65 in the bank. ... The sky is blue. The grass is green.

The grass is green. **She made a \$15 deposit and then followed**

by a \$4 withdrawal. ... The sky is blue. The sky is blue. The sky is

blue. The sky is blue. The grass is green. The grass is green. The sky

is blue. The grass is green. ... **What is Lucy's bank balance?**

LLMs Cannot Self-Correct Reasoning Yet

Jie Huang, Xinyun Chen, Swaroop Mishra, Huaixiu Steven Zheng, Adams Wei Yu, Xinying Song, Denny Zhou. [Large Language Models Cannot Self-Correct Reasoning Yet](#). ICLR 2024.

Christina is planning a birthday party and needs .75 gift bags per invited guest, because $\frac{1}{4}$ of attendees don't show up. She invited 16 friends. Gift bags are \$2 each. How much will she spend?

... $0.75 * 12 = 9$ gift bags ... Christina will spend a total of $2 * 9 = \$8$... (wrong)

Review your previous answer and find problems with your answer.

Upon reviewing my previous answer, I recognize a mistake. I incorrectly stated that Christina needs 0.75 gift bags per invited guest. The given information states that $\frac{1}{4}$ of the attendees won't show up...

Based on the problems you found, improve your answer.

... $16 * (\frac{3}{4}) = 12$ gift bags ... Christina will spend $12 * \$2 = \24 ... (Correct)

Terry eats 2 yogurts a day. They are currently on sale at 4 yogurts for \$5.00. How much does he spend on yogurt over 30 days?

... So, Terry spends \$75 on yogurt over 30 days. (Correct)

Review your previous answer and find problems with your answer.

Upon reviewing my previous answer, I realized that I made a mistake in calculating Terry's spending on yogurt over 30 days. I incorrectly stated that Terry spends \$2.50 per day for 30 days...

Based on the problems you found, improve your answer.

... the final answer is Terry spends \$37.5 on yogurt over 30 days. (wrong)

While allowing LLMs to review their generated responses can help correct inaccurate answers, it may also risk changing correct answers into incorrect ones

Self-correcting results in worse results

		# calls	GSM8K	CommonSenseQA	HotpotQA
GPT-3.5	Standard Prompting	1	75.9	75.8	26.0
	Self-Correct (round 1)	3	75.1	38.1	25.0
	Self-Correct (round 2)	5	74.7	41.8	25.0
GPT-4	Standard Prompting	1	95.5	82.0	49.0
	Self-Correct (round 1)	3	91.5	79.5	49.0
	Self-Correct (round 2)	5	89.0	80.0	43.0

Reported improvements need oracle answers

		GSM8K	CommonSenseQA	HotpotQA
GPT-3.5	Standard Prompting	75.9	75.8	26.0
	Self-Correct (Oracle)	84.3	89.7	29.0
GPT-4	Standard Prompting	95.5	82.0	49.0
	Self-Correct (Oracle)	97.5	85.5	59.0

Oracle: Let LLMs self correct only when the answer is wrong

Multi-LLM debate? Worse than self-consistency!

	# responses	GSM8K
Standard Prompting	1	76.7
Self-Consistency	3	82.5
Multi-Agent Debate (round 1)	6	83.2
Self-Consistency	6	85.3
Multi-Agent Debate (round 2)	9	83.0
Self-Consistency	9	88.2

Lesson learned

Oracle feedback needed for LLM
to self-correct

Self-debug naturally leverage unit tests as oracle

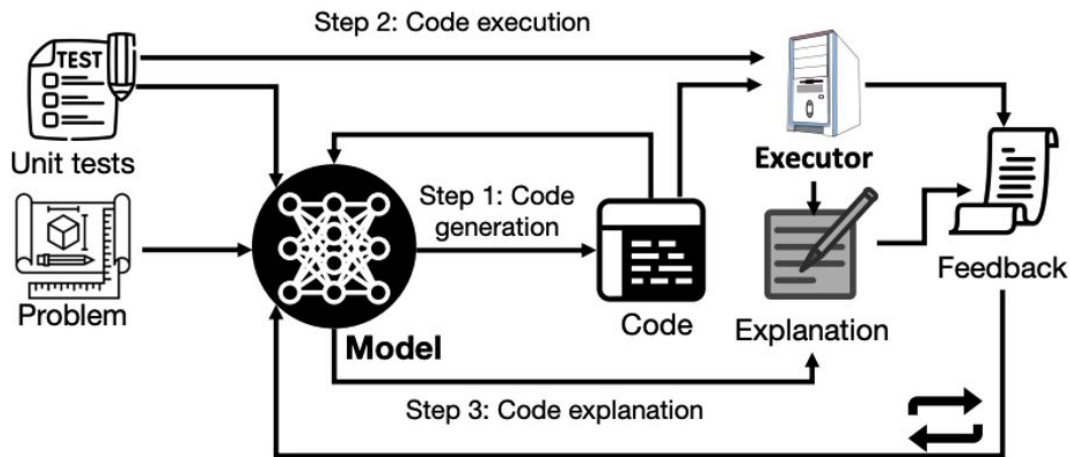


Figure 1: SELF-DEBUGGING for iterative debugging using a large language model. At each debugging step, the model first generates new code, then the code is executed and the model explains the code. The code explanation along with the execution results constitute the feedback message, which is then sent back to the model to perform more debugging steps. When unit tests are not available, the feedback can be purely based on code explanation.

Premise Order Matters in LLM Reasoning

Xinyun Chen, Ryan A Chi, Xuezhi Wang, Denny Zhou. [Premise Order Matters in Reasoning with Large Language Models](#). ICML 2024.

[Original GSM8K Problem] Thomas withdraws \$1000 in 20 dollar bills from the bank account. He loses 10 bills while getting home. After that, he uses half of the remaining bills to pay for a bill. Thomas then triples his money. He then converts all his bills to 5 dollar bills. How many 5 dollar bills does he have?

[Reordered GSM8K Problem] Thomas withdraws \$1000 in 20 dollar bills from the bank account. After getting home, he uses half of the remaining bills to pay for a bill. Thomas then triples his money. He then converts all his bills to 5 dollar bills. He loses 10 bills while getting home. How many 5 dollar bills does he have?

About 10 points drop on solving rates across all frontier LLMs

Response for original

1. Thomas withdraws \$1000 in \$20 bills. $\$1000 / \$20 = 50$ bills
2. He loses 10 of those bills. 50 bills - 10 bills = 40 bills
3. He uses half of the remaining bills to pay for a bill. Half of 40 bills is 20 bills. 40 bills - 20 bills = 20 bills remaining
4. Thomas then triples his money. He has 20 bills of \$20, which is $20 * \$20 = \400 . Tripling \$400 gives us $\$400 * 3 = \1200 .
5. He converts all his money to \$5 bills. $\$1200 / \$5 = 240$ bills

Response for reordered

1. Thomas withdraws \$1000 in \$20 bills from the bank. $\$1000 / \$20 = 50$ bills
2. He uses half of the remaining bills to pay for a bill. Half of 50 bills is 25 bills. So, he uses 25 bills and has 25 bills left.
3. Thomas then triples his money. Since he had 25 bills of \$20 each, he had $25 * \$20 = \500 before tripling his money. Tripling \$500 gives him $\$500 * 3 = \1500 .
4. He then converts all his bills to \$5 bills. $\$1500 / \$5 = 300$ bills
5. He lost 10 bills while getting home. 300 bills - 10 bills = 290 bills

Rules: If duve, then dax. If kere and riff, then tess. If feg and tess, then rabe. If wozz, then riff. If rabe, then thoxe. If ag and riff and kere, then hepe. If thoxe, then vepe. If nife and hume and ag, then dax. If feg and thoxe, then ire. If rebe and ene and heff, then kone. If ire and dax, then wope. If tess and vepe, then nup. If rabe and vide and nife, then ag. If nup and ag and vide, then duve. If zeck and hepe and dax, then riff. If nup, then hepe. If sene, then hume. If hepe and tess and ag, then kere. If fum, then vide. If kere and wope, then fum. If jag and kone, then thoxe. If fum, then wozz.

Facts: Alice is cote. Alice is kone. Alice is duve. Alice is ag. Alice is jag. Alice is tess. Alice is riff. Alice is feg. Alice is vide.

Query: Is Alice wozz? In each step, indicate whether you are using a fact, or a rule.

Logical inference task: The rules are ordered according to their use in the inference process, though not all rules are necessary for the query

Rules: If nup, then hepe. If kere and riff, then tess. If feg and tess, then rabe. If wozz, then riff. If tess and vepe, then nup. If ag and riff and kere, then hepe. If feg and thoxe, then ire. If nife and hume and ag, then dax. If ire and dax, then wope. If rebe and ene and heff, then kone. If hepe and tess and ag, then kere. If rabe, then thoxe. If rabe and vide and nife, then ag. If fum, then wozz. If zeck and hepe and dax, then riff. If kere and wope, then fum. If sene, then hume. If thoxe, then vepe. If fum, then vide. If duve, then dax. If jag and kone, then thoxe. If nup and ag and vide, then duve.

Facts: Alice is cote. Alice is kone. Alice is duve. Alice is ag. Alice is jag. Alice is tess. Alice is riff. Alice is feg. Alice is vide.

Query: Is Alice wozz? In each step, indicate whether you are using a fact, or a rule.

Logical inference task: The rules relevant to the query are **randomly** ordered, 30+ points performance drop across all frontier LLMs

Summary

- Generating intermediate steps improves LLM performance
 - Training / finetuning / prompting with intermediate steps
 - Zero-shot, analogical reasoning, special decoding
- Self-consistency greatly improves step-by-step reasoning
- Limitation: irrelevant context, self-correction, premise order

What is next?

“If I were given one hour to save the planet, I would spend 59 minutes defining the problem and one minute resolving it.”

— Albert Einstein

1. Define a right problem to work on
2. Solve it from the first principles

Develop a model that autonomously
learns all the reasoning techniques
we have introduced while addressing
all the limitations we have identified

An aerial photograph of Philadelphia, Pennsylvania, featuring the University of Pennsylvania campus in the foreground, the Schuylkill River winding through the city, and the downtown skyline in the background. The text is overlaid on the image.

CONFERENCE ON LANGUAGE MODELING

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Philadelphia, PA
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THE END

"The best way to predict the future is to invent it." — Alan Kay