

Study Material

Downloaded from Vedantu

About Vedantu

Vedantu is India's largest **LIVE online teaching platform** with best teachers from across the country.

Vedantu offers Live Interactive Classes for **JEE, NEET, KVPY, NTSE, Olympiads, CBSE, ICSE, IGCSE, IB & State Boards** for Students Studying in **6-12th Grades** and Droppers.

FREE LIVE ONLINE
MASTER CLASSES
FREE Webinars by Expert Teachers



Register for **FREE**

Awesome Master Teachers



Anand Prakash
B.Tech, IIT Roorkee
Co-Founder, Vedantu



Pulkit Jain
B.Tech, IIT Roorkee
Co-Founder, Vedantu



Vamsi Krishna
B.Tech, IIT Bombay
Co-Founder, Vedantu



“ My mentor is approachable and **guides me in my future aspirations as well.** ”

Student - **Ayushi**



“ My son loves the sessions and **I can already see the change.** ”

Parent - **Sreelatha**

 **10,04,600+**
Hours of LIVE Learning



9,49,900+
Happy Students



95%
Top Results

95% Students of Regular Tuitions on Vedantu scored above **90%** in exams!

Vedantu

FREE MASTER CLASS SERIES

- For **Grades 6-12th** targeting **JEE, CBSE, ICSE** & much more
- Free 60 Minutes Live Interactive** classes everyday
- Learn from the **Master Teachers** - India's best

Register for **FREE**

Limited Seats!

Download Vedantu's App & Get



All Study Material
with Solution



LIVE
Doubt Solving



Daily
LIVE Classes



FREE Tests and
Reports

GET IT ON
Google Play

Have a Doubt? **Ask Now!**



TAKE A PIC

OR

Enter your doubt as text

MY DOUBTS >



ASK



CLASSROOM



STUDY



COURSES



TESTS

DOWNLOAD THE APP

Answers & Solutions For JEE MAIN 2017

(Code-D)

Time Duration: 3 hrs.

Maximum Marks: 360

(Mathematics, Physics and Chemistry)

Important Instructions :

1. The test is of 3 hours duration.
2. The Test Booklet consists of 90 questions. The maximum marks are 360.
3. There are three parts in the question paper A, B, C consisting of Mathematics, Physics and Chemistry having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for each correct response.
4. Candidates will be awarded marks as stated above in Instructions No. 3 for correct response of each question. $\frac{1}{4}$ (one-fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
5. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 4 above.
6. For writing particulars/marking responses on Side-1 and Side-2 of the Answer Sheet use only Blue/Black Ball Point Pen provided by the Board.
7. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. except the Admit Card inside the examination hall/room.



Study Materials

[NCERT Solutions for Class 6 to 12 \(Math & Science\)](#)

[Revision Notes for Class 6 to 12 \(Math & Science\)](#)

[RD Sharma Solutions for Class 6 to 12 Mathematics](#)

[RS Aggarwal Solutions for Class 6, 7 & 10 Mathematics](#)

[Important Questions for Class 6 to 12 \(Math & Science\)](#)

[CBSE Sample Papers for Class 9, 10 & 12 \(Math & Science\)](#)

[Important Formula for Class 6 to 12 Math](#)

[CBSE Syllabus for Class 6 to 12](#)

[Lakhmir Singh Solutions for Class 9 & 10](#)

[Previous Year Question Paper](#)

[CBSE Class 12 Previous Year Question Paper](#)

[CBSE Class 10 Previous Year Question Paper](#)

[JEE Main & Advanced Question Paper](#)

[NEET Previous Year Question Paper](#)

PART-A : MATHEMATICS

1. If S is the set of distinct values of b for which the following system of linear equations

$$x + y + z = 1$$

$$x + ay + z = 1$$

$$ax + by + z = 0$$

has no solution, then S is

- (1) An empty set
- (2) An infinite set
- (3) A finite set containing two or more elements
- (4) A singleton

Answer (4)

Sol.
$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & a & 1 \\ a & b & 1 \end{vmatrix} = 0$$

$$\Rightarrow -(1 - a)^2 = 0$$

$$\Rightarrow a = 1$$

For $a = 1$

Eq. (1) & (2) are identical i.e., $x + y + z = 1$

To have no solution with $x + by + z = 0$.

$$b = 1$$

2. The following statement $(p \rightarrow q) \rightarrow [(\neg p \rightarrow q) \rightarrow q]$ is

- (1) A tautology
- (2) Equivalent to $\neg p \rightarrow q$
- (3) Equivalent to $p \rightarrow \neg q$
- (4) A fallacy

Answer (1)

Sol.
$$\begin{array}{|c|c|c|c|c|c|c|} \hline p & q & p \rightarrow q & (\neg p \rightarrow q) & (\neg p \rightarrow q) \rightarrow q & (p \rightarrow q) \rightarrow [(\neg p \rightarrow q) \rightarrow q] \\ \hline T & T & T & T & T & T \\ \hline T & F & F & T & F & T \\ \hline F & T & T & T & T & T \\ \hline F & F & T & F & T & T \\ \hline \end{array}$$

(a tautology)

3. If $5(\tan^2 x - \cos^2 x) = 2\cos 2x + 9$, then the value of $\cos 4x$ is

(1) $-\frac{3}{5}$

(2) $\frac{1}{3}$

(3) $\frac{2}{9}$

(4) $-\frac{7}{9}$

Answer (4)

Sol. $5 \tan^2 x = 9 \cos^2 x + 7$

$$5 \sec^2 x - 5 = 9 \cos^2 x + 7$$

Let $\cos^2 x = t$

$$\frac{5}{t} = 9t + 12$$

$$9t^2 + 12t - 5 = 0$$

$$t = \frac{1}{3} \quad \text{as} \quad t \neq -\frac{5}{3}$$

$$\cos^2 x = \frac{1}{3}, \quad \cos 2x = 2\cos^2 x - 1$$

$$= -\frac{1}{3}$$

$$\cos 4x = 2 \cos^2 2x - 1$$

$$= \frac{2}{9} - 1$$

$$= -\frac{7}{9}$$

4. For three events A , B and C , P (Exactly one of A or B occurs) = P (Exactly one of B or C occurs)

$$= P(\text{Exactly one of } C \text{ or } A \text{ occurs}) = \frac{1}{4} \text{ and}$$

$$P(\text{All the three events occur simultaneously}) = \frac{1}{16}.$$

Then the probability that at least one of the events occurs, is

(1) $\frac{7}{32}$ (2) $\frac{7}{16}$

(3) $\frac{7}{64}$ (4) $\frac{3}{16}$

Answer (2)

Sol. $P(A) + P(B) - P(A \cap B) = \frac{1}{4}$

$$P(B) + P(C) - P(B \cap C) = \frac{1}{4}$$

$$P(C) + P(A) - P(A \cap C) = \frac{1}{4}$$

$$P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C) - P(A \cap C) = \frac{3}{8}$$

$$\therefore P(A \cap B \cap C) = \frac{1}{16}$$

$$\therefore P(A \cup B \cup C) = \frac{3}{8} + \frac{1}{16} = \frac{7}{16}$$

5. Let ω be a complex number such that $2\omega + 1 = z$ where $z = \sqrt{-3}$. If

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -\omega^2 - 1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k, \text{ then } k \text{ is equal to}$$

- (1) $-z$ (2) z
 (3) -1 (4) 1

Answer (1)

Sol. $2\omega + 1 = z, z = \sqrt{3}i$

$$\omega = \frac{-1 + \sqrt{3}i}{2} \rightarrow \text{Cube root of unity.}$$

$$C_1 \rightarrow C_1 + C_2 + C_3$$

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -1 - \omega^2 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ 1 & \omega & \omega^2 \\ 1 & \omega^2 & \omega \end{vmatrix} = \begin{vmatrix} 3 & 1 & 1 \\ 0 & \omega & \omega^2 \\ 0 & \omega^2 & \omega \end{vmatrix}$$

$$= 3(\omega^2 - \omega^4)$$

$$= 3 \left[\left(\frac{-1 - \sqrt{3}i}{2} \right) - \left(\frac{-1 + \sqrt{3}i}{2} \right) \right]$$

$$= -3\sqrt{3}i$$

$$= -3z$$

$$\therefore k = -z$$

6. Let k be an integer such that the triangle with vertices $(k, -3k)$, $(5, k)$ and $(-k, 2)$ has area 28 sq. units. Then the orthocentre of this triangle is at the point

- (1) $\left(2, -\frac{1}{2}\right)$ (2) $\left(1, \frac{3}{4}\right)$
 (3) $\left(1, -\frac{3}{4}\right)$ (4) $\left(2, \frac{1}{2}\right)$

Answer (4)

$$\text{Sol. Area} = \left| \begin{vmatrix} k & -3k & 1 \\ 5 & k & 1 \\ -k & 2 & 1 \end{vmatrix} \right| = 28$$

$$\begin{vmatrix} k-5 & -4k & 0 \\ 5+k & k-2 & 0 \\ -k & 2 & 1 \end{vmatrix} = \pm 56$$

$$(k^2 - 7k + 10) + 4k^2 + 20k = \pm 56$$

$$5k^2 + 13k + 10 = \pm 56$$

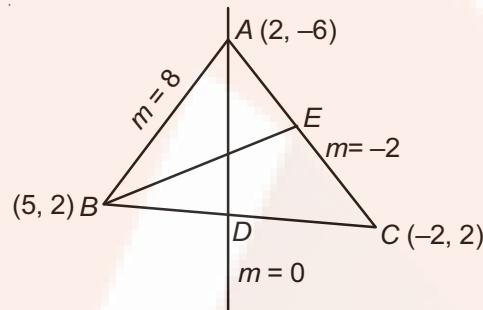
$$5k^2 + 13k - 46 = 0 \quad | \quad 5K^2 + 13K + 66 = 0$$

$$5k^2 + 13k - 46 = 0$$

$$k = \frac{-13 \pm \sqrt{169 + 920}}{10}$$

$$= 2, -4.6 \\ \text{reject}$$

For $k = 2$



Equation of AD ,

$$x = 2 \quad \dots(i)$$

Also equation of BE ,

$$y - 2 = \frac{1}{2}(x - 5)$$

$$2y - 4 = x - 5$$

$$x - 2y - 1 = 0 \quad \dots(ii)$$

Solving (i) & (ii), $2y = 1$

$$y = \frac{1}{2}$$

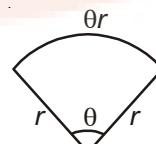
Orthocentre is $\left(2, \frac{1}{2}\right)$

7. Twenty meters of wire is available for fencing off a flower-bed in the form of a circular sector. Then the maximum area (in sq. m) of the flower-bed, is

- (1) 12.5 (2) 10
 (3) 25 (4) 30

Answer (3)

Sol.



$$2r + \theta r = 20 \quad \dots(i)$$

$$A = \text{area} = \frac{\theta}{2\pi} \times \pi r^2 = \frac{\theta r^2}{2} \quad \dots \text{(ii)}$$

$$A = \frac{r^2}{2} \left(\frac{20 - 2r}{r} \right)$$

$$A = \left(\frac{20r - 2r^2}{2} \right) = 10r - r^2$$

A to be maximum

$$\frac{dA}{dr} = 10 - 2r = 0 \Rightarrow r = 5$$

$$\frac{d^2A}{dr^2} = -2 < 0$$

Hence for $r = 5$, A is maximum

Now, $10 + \theta \cdot 5 = 20 \Rightarrow \theta = 2$ (radian)

$$\text{Area} = \frac{2}{2\pi} \times \pi(5)^2 = 25 \text{ sq m}$$

8. The area (in sq. units) of the region

$$\{(x, y) : x \geq 0, x + y \leq 3, x^2 \leq 4y \text{ and } y \leq 1 + \sqrt{x}\}$$

is

(1) $\frac{59}{12}$

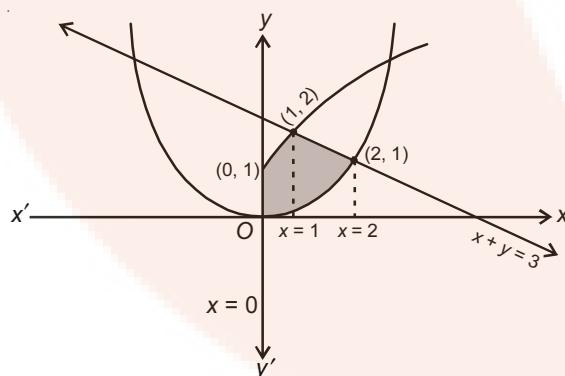
(2) $\frac{3}{2}$

(3) $\frac{7}{3}$

(4) $\frac{5}{2}$

Answer (4)

Sol.



Area of shaded region

$$= \int_0^1 \left(\sqrt{x} + 1 - \frac{x^2}{4} \right) dx + \int_1^2 \left((3-x) - \frac{x^2}{4} \right) dx$$

$$= \frac{5}{2} \text{ sq. unit}$$

9. If the image of the point $P(1, -2, 3)$ in the plane, $2x + 3y - 4z + 22 = 0$ measured parallel to the line, $\frac{x}{1} = \frac{y}{4} = \frac{z}{5}$ is Q, then PQ is equal to

(1) $3\sqrt{5}$

(2) $2\sqrt{42}$

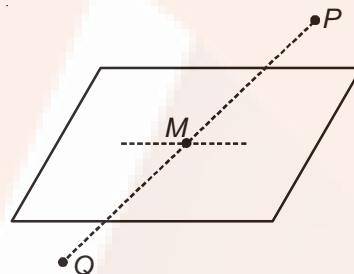
(3) $\sqrt{42}$

(4) $6\sqrt{5}$

Answer (2)

Sol. Equation of PQ , $\frac{x-1}{1} = \frac{y+2}{4} = \frac{z-3}{5}$

Let M be $(\lambda + 1, 4\lambda - 2, 5\lambda + 3)$



As it lies on $2x + 3y - 4z + 22 = 0$

$$\lambda = 1$$

For Q, $\lambda = 2$

$$\text{Distance } PQ = 2\sqrt{1^2 + 4^2 + 5^2} = 2\sqrt{42}$$

10. If for $x \in \left(0, \frac{1}{4}\right)$, the derivative of $\tan^{-1}\left(\frac{6x\sqrt{x}}{1-9x^3}\right)$ is $\sqrt{x} \cdot g(x)$, then $g(x)$ equals

(1) $\frac{9}{1+9x^3}$

(2) $\frac{3x\sqrt{x}}{1-9x^3}$

(3) $\frac{3x}{1-9x^3}$

(4) $\frac{3}{1+9x^3}$

Answer (1)

Sol. $f(x) = 2\tan^{-1}(3x\sqrt{x})$ For $x \in \left(0, \frac{1}{4}\right)$

$$f'(x) = \frac{9\sqrt{x}}{1+9x^3}$$

$$g(x) = \frac{9}{1+9x^3}$$

11. If $(2 + \sin x) \frac{dy}{dx} + (y + 1)\cos x = 0$ and $y(0) = 1$, then $y\left(\frac{\pi}{2}\right)$ is equal to

- (1) $\frac{1}{3}$ (2) $-\frac{2}{3}$
 (3) $-\frac{1}{3}$ (4) $\frac{4}{3}$

Answer (1)

Sol. $(2 + \sin x) \frac{dy}{dx} + (y + 1)\cos x = 0$

$$y(0) = 1, y\left(\frac{\pi}{2}\right) = ?$$

$$\frac{1}{y+1} dy + \frac{\cos x}{2 + \sin x} dx = 0$$

$$\ln|y+1| + \ln(2 + \sin x) = \ln C$$

$$(y+1)(2 + \sin x) = C$$

$$\text{Put } x = 0, y = 1$$

$$(1+1) \cdot 2 = C \Rightarrow C = 4$$

$$\text{Now, } (y+1)(2 + \sin x) = 4$$

$$\text{For, } x = \frac{\pi}{2}$$

$$(y+1)(2+1) = 4$$

$$y+1 = \frac{4}{3}$$

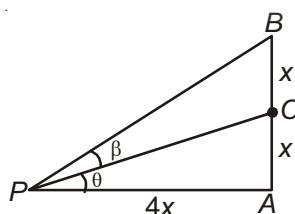
$$y = \frac{4}{3} - 1 = \frac{1}{3}$$

12. Let a vertical tower AB have its end A on the level ground. Let C be the mid-point of AB and P be a point on the ground such that $AP = 2AB$. If $\angle BPC = \beta$ then $\tan \beta$ is equal to

- (1) $\frac{6}{7}$ (2) $\frac{1}{4}$
 (3) $\frac{2}{9}$ (4) $\frac{4}{9}$

Answer (3)

Sol.



$$\tan \theta = \frac{1}{4}$$

$$\tan(\theta + \beta) = \frac{1}{2}$$

$$\therefore \frac{\frac{1}{4} + \tan \beta}{1 - \frac{1}{4} \tan \beta} = \frac{1}{2}$$

$$\text{Solving } \tan \beta = \frac{2}{9}$$

13. If $A = \begin{bmatrix} 2 & -3 \\ -4 & 1 \end{bmatrix}$, then adj $(3A^2 + 12A)$ is equal to

$$(1) \begin{bmatrix} 72 & -84 \\ -63 & 51 \end{bmatrix} \quad (2) \begin{bmatrix} 51 & 63 \\ 84 & 72 \end{bmatrix}$$

$$(3) \begin{bmatrix} 51 & 84 \\ 63 & 72 \end{bmatrix} \quad (4) \begin{bmatrix} 72 & -63 \\ -84 & 51 \end{bmatrix}$$

Answer (2)

Sol. $A = \begin{bmatrix} 2 & -3 \\ -4 & 1 \end{bmatrix}$

$$|A - \lambda I| = \begin{vmatrix} 2 - \lambda & -3 \\ -4 & 1 - \lambda \end{vmatrix}$$

$$= (2 - 2\lambda - \lambda + \lambda^2) - 12$$

$$f(\lambda) = \lambda^2 - 3\lambda - 10$$

$\therefore A$ satisfies $f(\lambda)$

$$\therefore A^2 - 3A - 10I = 0$$

$$A^2 - 3A = 10I$$

$$3A^2 - 9A = 30I$$

$$3A^2 + 12A = 30I + 21A$$

$$= \begin{bmatrix} 30 & 0 \\ 0 & 30 \end{bmatrix} + \begin{bmatrix} 42 & -63 \\ -84 & 21 \end{bmatrix}$$

$$= \begin{bmatrix} 72 & -63 \\ -84 & 51 \end{bmatrix}$$

$$\text{adj}(3A^2 + 12A) = \begin{bmatrix} 51 & 63 \\ 84 & 72 \end{bmatrix}$$

14. For any three positive real numbers a, b and c ,

$$9(25a^2 + b^2) + 25(c^2 - 3ac) = 15b(3a + c).$$

Then

- (1) b, c and a are in G.P.
- (2) b, c and a are in A.P.
- (3) a, b and c are in A.P.
- (4) a, b and c are in G.P.

Answer (2)

Sol. $9(25a^2 + b^2) + 25(c^2 - 3ac) = 15b(3a + c)$

$$\Rightarrow (15a)^2 + (3b)^2 + (5c)^2 - 45ab - 15bc - 75ac = 0$$

$$\Rightarrow (15a - 3b)^2 + (3b - 5c)^2 + (15a - 5c)^2 = 0$$

It is possible when

$$15a - 3b = 0 \text{ and } 3b - 5c = 0 \text{ and } 15a - 5c = 0$$

$$15a = 3b = 5c$$

$$\frac{a}{1} = \frac{b}{5} = \frac{c}{3}$$

$\therefore b, c, a$ are in A.P.

15. The distance of the point $(1, 3, -7)$ from the plane passing through the point $(1, -1, -1)$, having normal

perpendicular to both the lines $\frac{x-1}{1} = \frac{y+2}{-2} = \frac{z-4}{3}$

and $\frac{x-2}{2} = \frac{y+1}{-1} = \frac{z+7}{-1}$, is

(1) $\frac{20}{\sqrt{74}}$ (2) $\frac{10}{\sqrt{83}}$

(3) $\frac{5}{\sqrt{83}}$ (4) $\frac{10}{\sqrt{74}}$

Answer (2)

Sol. Let the plane be

$$a(x-1) + b(y+1) + c(z+1) = 0$$

It is perpendicular to the given lines

$$a - 2b + 3c = 0$$

$$2a - b - c = 0$$

Solving, $a : b : c = 5 : 7 : 3$

\therefore The plane is $5x + 7y + 3z + 5 = 0$

Distance of $(1, 3, -7)$ from this plane = $\frac{10}{\sqrt{83}}$

16. Let $I_n = \int \tan^n x dx, (n > 1)$. If

$I_4 + I_6 = a \tan^5 x + bx^5 + C$, where C is a constant of integration, then the ordered pair (a, b) is equal to

(1) $\left(-\frac{1}{5}, 1\right)$ (2) $\left(\frac{1}{5}, 0\right)$

(3) $\left(\frac{1}{5}, -1\right)$ (4) $\left(-\frac{1}{5}, 0\right)$

Answer (2)

Sol. $I_n = \int \tan^n x dx, n > 1$

$$I_4 + I_6 = \int (\tan^4 x + \tan^6 x) dx$$

$$= \int \tan^4 x \sec^2 x dx$$

Let $\tan x = t$

$$\sec^2 x dx = dt$$

$$= \int t^4 dt$$

$$= \frac{t^5}{5} + C$$

$$= \frac{1}{5} \tan^5 x + C$$

$$a = \frac{1}{5}, b = 0$$

17. The eccentricity of an ellipse whose centre is at the

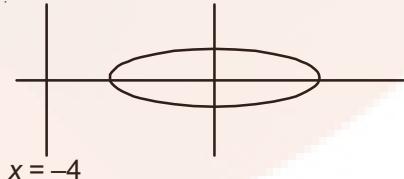
origin is $\frac{1}{2}$. If one of its directrices is $x = -4$, then

the equation of the normal to it at $\left(1, \frac{3}{2}\right)$ is

- (1) $2y - x = 2$
- (2) $4x - 2y = 1$
- (3) $4x + 2y = 7$
- (4) $x + 2y = 4$

Answer (2)

Sol.



$$e = \frac{1}{2}$$

$$\frac{-a}{e} = -4$$

$$-a = -4 \times e$$

$a = 2$

$$\text{Now, } b^2 = a^2(1-e^2) = 3$$

Equation to ellipse

$$\frac{x^2}{4} + \frac{y^2}{3} = 1$$

Equation of normal is

$$\frac{x-1}{\frac{1}{4}} = \frac{y-\frac{3}{2}}{\frac{3}{2 \times 3}} \Rightarrow 4x - 2y - 1 = 0$$

18. A hyperbola passes through the point $P(\sqrt{2}, \sqrt{3})$ and has foci at $(\pm 2, 0)$. Then the tangent to this hyperbola at P also passes through the point

- (1) $(3\sqrt{2}, 2\sqrt{3})$ (2) $(2\sqrt{2}, 3\sqrt{3})$
 (3) $(\sqrt{3}, \sqrt{2})$ (4) $(-\sqrt{2}, -\sqrt{3})$

Answer (2)

$$\text{Sol. } \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

$$a^2 + b^2 = 4$$

$$\text{and } \frac{2}{a^2} - \frac{3}{b^2} = 1$$

$$\frac{2}{4-b^2} - \frac{3}{b^2} = 1$$

$$\Rightarrow b^2 = 3$$

$$\therefore a^2 = 1$$

$$\therefore x^2 - \frac{y^2}{3} = 1$$

\therefore Tangent at $P(\sqrt{2}, \sqrt{3})$ is $\sqrt{2}x - \frac{y}{\sqrt{3}} = 1$

Clearly it passes through $(2\sqrt{2}, 3\sqrt{3})$

19. The function $f : R \rightarrow \left[-\frac{1}{2}, \frac{1}{2}\right]$ defined as

$$f(x) = \frac{x}{1+x^2}, \text{ is}$$

- (1) Invertible
 (2) Injective but not surjective
 (3) Surjective but not injective
 (4) Neither injective nor surjective

Answer (3)

$$\text{Sol. } f(x) = \frac{x}{1+x^2}$$

$$f'(x) = \frac{(1+x^2) \cdot 1 - x \cdot 2x}{(1+x^2)^2} = \frac{1-x^2}{(1+x^2)^2}$$

$f'(x)$ changes sign in different intervals.

\therefore Not injective.

$$y = \frac{x}{1+x^2}$$

$$yx^2 - x + y = 0$$

For $y \neq 0$

$$D = 1 - 4y^2 \geq 0 \Rightarrow y \in \left[-\frac{1}{2}, \frac{1}{2}\right] - \{0\}$$

For, $y = 0 \Rightarrow x = 0$

\therefore Part of range

$$\therefore \text{Range : } \left[-\frac{1}{2}, \frac{1}{2}\right]$$

\therefore Surjective but not injective.

20. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\cot x - \cos x}{(\pi - 2x)^3}$ equals

$$(1) \frac{1}{24} \quad (2) \frac{1}{16}$$

$$(3) \frac{1}{8} \quad (4) \frac{1}{4}$$

Answer (2)

$$\text{Sol. } \lim_{x \rightarrow \frac{\pi}{2}} \frac{\cot x - \cos x}{(\pi - 2x)^3}$$

$$\text{Put, } \frac{\pi}{2} - x = t$$

$$\lim_{t \rightarrow 0} \frac{\tan t - \sin t}{8t^3}$$

$$= \lim_{t \rightarrow 0} \frac{\sin t \cdot 2 \sin^2 \frac{t}{2}}{8t^3}$$

$$= \frac{1}{16}.$$

21. Let $\vec{a} = 2\hat{i} + \hat{j} - 2\hat{k}$ and $\vec{b} = \hat{i} + \hat{j}$. Let \vec{c} be a vector such that $|\vec{c} - \vec{a}| = 3$, $|(\vec{a} \times \vec{b}) \times \vec{c}| = 3$ and the angle between \vec{c} and $\vec{a} \times \vec{b}$ be 30° . Then $\vec{a} \cdot \vec{c}$ is equal to

(1) $\frac{25}{8}$

(2) 2

(3) 5

(4) $\frac{1}{8}$

Answer (2)

Sol. $|(\vec{a} \times \vec{b}) \times \vec{c}| = 3$

$$\vec{a} \times \vec{b} = 2\hat{i} - 2\hat{j} + \hat{k}$$

$$\Rightarrow |\vec{a} \times \vec{b}| |\vec{c}| \sin 30^\circ = 3 \quad |\vec{a}| = 3 = |\vec{a} \times \vec{b}|$$

$$\Rightarrow |\vec{c}| = 2$$

$$|\vec{c} - \vec{a}| = 3$$

$$\Rightarrow |\vec{c}|^2 + |\vec{a}|^2 - 2(\vec{a} \cdot \vec{c}) = 9$$

$$\vec{a} \cdot \vec{c} = \frac{9 - 3 - 2}{2} = 2$$

22. The normal to the curve $y(x-2)(x-3) = x+6$ at the point where the curve intersects the y -axis passes through the point

(1) $\left(-\frac{1}{2}, -\frac{1}{2}\right)$

(2) $\left(\frac{1}{2}, \frac{1}{2}\right)$

(3) $\left(\frac{1}{2}, -\frac{1}{3}\right)$

(4) $\left(\frac{1}{2}, \frac{1}{3}\right)$

Answer (2)

Sol. $y(x-2)(x-3) = x+6$

At y -axis, $x = 0$, $y = 1$

Now, on differentiation.

$$\frac{dy}{dx}(x-2)(x-3) + y(2x-5) = 1$$

$$\frac{dy}{dx}(6) + 1(-5) = 1$$

$$\frac{dy}{dx} = \frac{6}{6} = 1$$

Now slope of normal = -1

Equation of normal $y - 1 = -1(x - 0)$

$$y + x - 1 = 0 \quad \dots \text{(i)}$$

Line (i) passes through $\left(\frac{1}{2}, \frac{1}{2}\right)$

23. If two different numbers are taken from the set $\{0, 1, 2, 3, \dots, 10\}$; then the probability that their sum as well as absolute difference are both multiple of 4, is

(1) $\frac{6}{55}$

(2) $\frac{12}{55}$

(3) $\frac{14}{45}$

(4) $\frac{7}{55}$

Answer (1)

Sol. Total number of ways = ${}^{11}C_2$

$$= 55$$

Favourable ways are

(0, 4), (0, 8), (4, 8), (2, 6), (2, 10), (6, 10)

$$\text{Probability} = \frac{6}{55}$$

24. A man X has 7 friends, 4 of them are ladies and 3 are men. His wife Y also has 7 friends, 3 of them are ladies and 4 are men. Assume X and Y have no common friends. Then the total number of ways in which X and Y together can throw a party inviting 3 ladies and 3 men, so that 3 friends of each of X and Y are in this party, is

(1) 485

(2) 468

(3) 469

(4) 484

Answer (1)

Sol. $X(4 \text{ L } 3 \text{ G}) \quad Y(3 \text{ L } 4 \text{ G})$

3 L 0 G

0 L 3 G

2 L 1 G

1 L 2 G

1 L 2 G

2 L 1 G

0 L 3 G

3 L 0 G

Required number of ways

$$={}^4C_3 \cdot {}^4C_3 + ({}^4C_2 \cdot {}^3C_1)^2 + ({}^4C_1 \cdot {}^3C_2)^2 + ({}^3C_3)^2$$

$$= 16 + 324 + 144 + 1$$

$$= 485$$

25. The value of

$$({}^{21}C_1 - {}^{10}C_1) + ({}^{21}C_2 - {}^{10}C_2) + ({}^{21}C_3 - {}^{10}C_3) +$$

$$({}^{21}C_4 - {}^{10}C_4) + \dots + ({}^{21}C_{10} - {}^{10}C_{10}) \text{ is}$$

(1) $2^{21} - 2^{11}$

(2) $2^{21} - 2^{10}$

(3) $2^{20} - 2^9$

(4) $2^{20} - 2^{10}$

Answer (4)

Sol. ${}^{21}C_1 + {}^{21}C_2 + \dots + {}^{21}C_{10} = \frac{1}{2} \{ {}^{21}C_0 + {}^{21}C_1 + \dots + {}^{21}C_{21} \} - 1$
 $= 2^{20} - 1$

$$\left({}^{10}C_1 + {}^{10}C_2 + \dots + {}^{10}C_{10} \right) = 2^{10} - 1$$

$$\therefore \text{Required sum} = (2^{20} - 1) - (2^{10} - 1)
= 2^{20} - 2^{10}$$

26. A box contains 15 green and 10 yellow balls. If 10 balls are randomly drawn, one-by-one, with replacement, then the variance of the number of green balls drawn is

(1) $\frac{12}{5}$

(2) 6

(3) 4

(4) $\frac{6}{25}$

Answer (1)

Sol. $n = 10$

$$p(\text{Probability of drawing a green ball}) = \frac{15}{25}$$

$$\therefore p = \frac{3}{5}, q = \frac{2}{5}$$

$$\text{var}(X) = n.p.q$$

$$= 10 \cdot \frac{6}{25} = \frac{12}{5}$$

27. Let $a, b, c \in R$. If $f(x) = ax^2 + bx + c$ is such that $a + b + c = 3$ and

$$f(x+y) = f(x) + f(y) + xy, \forall x, y \in R,$$

then $\sum_{n=1}^{10} f(n)$ is equal to

(1) 330

(2) 165

(3) 190

(4) 255

Answer (1)

Sol. As, $f(x+y) = f(x) + f(y) + xy$

$$\text{Given, } f(1) = 3$$

$$\text{Putting, } x = y = 1 \Rightarrow f(2) = 2f(1) + 1 = 7$$

$$\text{Similarly, } x = 1, y = 2 \Rightarrow f(3) = f(1) + f(2) + 2 = 12$$

$$\text{Now, } \sum_{n=1}^{10} f(n) = f(1) + f(2) + f(3) + \dots + f(10)$$

$$= 3 + 7 + 12 + 18 + \dots = S \text{ (let)}$$

$$\text{Now, } S_n = 3 + 7 + 12 + 18 + \dots + t_n$$

$$\text{Again, } S_n = 3 + 7 + 12 + \dots + t_{n-1} + t_n$$

$$\text{We get, } t_n = 3 + 4 + 5 + \dots n \text{ terms}$$

$$= \frac{n(n+5)}{2}$$

$$\text{i.e., } S_n = \sum_{n=1}^n t_n$$

$$= \frac{1}{2} \{ \sum n^2 + 5 \sum n \}$$

$$= \frac{n(n+1)(n+8)}{6}$$

$$\text{So, } S_{10} = \frac{10 \times 11 \times 18}{6} = 330$$

28. The radius of a circle, having minimum area, which touches the curve $y = 4 - x^2$ and the lines, $y = |x|$ is

(1) $2(\sqrt{2} + 1)$

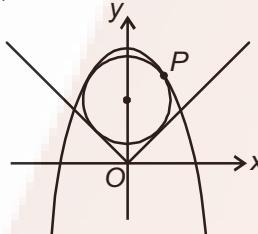
(2) $2(\sqrt{2} - 1)$

(3) $4(\sqrt{2} - 1)$

(4) $4(\sqrt{2} + 1)$

Answer (3)

Sol.



$$x^2 = -(y - 4)$$

Let a point on the parabola $P\left(\frac{t}{2}, 4 - \frac{t^2}{4}\right)$

Equation of normal at P is

$$y + \frac{t^2}{4} - 4 = \frac{1}{t} \left(x - \frac{t}{2} \right)$$

$$\Rightarrow x - ty - \frac{t^3}{4} + \frac{7}{2}t = 0$$

It passes through centre of circle, say $(0, k)$

$$-tk - \frac{t^3}{4} + \frac{7}{2}t = 0 \quad \dots(i)$$

$$t = 0, t^2 = 14 - 4k$$

$$\text{Radius } r = \frac{|0-k|}{\sqrt{2}} \quad (\text{Length of perpendicular from } (0, k) \text{ to } y = x)$$

$$\Rightarrow r = \frac{k}{\sqrt{2}}$$

$$\text{Equation of circle is } x^2 + (y-k)^2 = \frac{k^2}{2}$$

It passes through point P

$$\frac{t^2}{4} + \left(4 - \frac{t^2}{4} - k\right)^2 = \frac{k^2}{2}$$

$$t^4 + t^2(8k - 28) + 8k^2 - 128k + 256 = 0 \quad \dots(\text{ii})$$

$$\text{For } t = 0 \Rightarrow k^2 - 16k + 32 = 0$$

$$k = 8 \pm 4\sqrt{2}$$

$$\therefore r = \frac{k}{\sqrt{2}} = 4(\sqrt{2} - 1) \quad (\text{discarding } 4(\sqrt{2} + 1)) \dots(\text{iii})$$

$$\text{For } t = \pm\sqrt{14-4k}$$

$$(14-4k)^2 + (14-4k)(8k-28) + 8k^2 - 128k + 256 = 0$$

$$2k^2 + 4k - 15 = 0$$

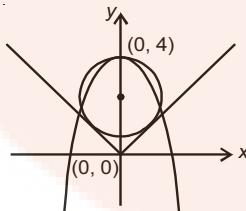
$$k = \frac{-2 \pm \sqrt{34}}{2}$$

$$\therefore r = \frac{k}{\sqrt{2}} = \frac{\sqrt{17} - \sqrt{2}}{2} \quad (\text{Ignoring negative value of } r) \dots(\text{iv})$$

From (iii) & (iv),

$$r_{\min} = \frac{\sqrt{17} - \sqrt{2}}{2}$$

But from options, $r = 4(\sqrt{2} - 1)$



29. If, for a positive integer n , the quadratic equation,
 $x(x+1) + (x+1)(x+2) + \dots + (x+n-1)(x+n) = 10n$
has two consecutive integral solutions, then n is equal to

(1) 12

(2) 9

(3) 10

(4) 11

Answer (4)

Sol. Rearranging equation, we get

$$nx^2 + \{1+3+5+\dots+(2n-1)\}x$$

$$+ \{1 \cdot 2 + 2 \cdot 3 + \dots + (n-1)n\} = 10n$$

$$\Rightarrow nx^2 + n^2x + \frac{(n-1)n(n+1)}{3} = 10n$$

$$\Rightarrow x^2 + nx + \left(\frac{n^2 - 31}{3}\right) = 0$$

Given difference of roots = 1

$$\Rightarrow |\alpha - \beta| = 1$$

$$\Rightarrow D = 1$$

$$\Rightarrow n^2 - \frac{4}{3}(n^2 - 31) = 1$$

$$\text{So, } n = 11$$

30. The integral $\int_{\frac{\pi}{4}}^{3\pi} \frac{dx}{1 + \cos x}$ is equal to

(1) -2

(2) 2

(3) 4

(4) -1

Answer (2)

$$\text{Sol. } \int_{\frac{\pi}{4}}^{3\pi} \frac{dx}{2\cos^2 \frac{x}{2}} = \frac{1}{2} \int_{\frac{\pi}{4}}^{3\pi} \sec^2 \frac{x}{2} dx$$

$$= \frac{1}{2} \left[\frac{\tan \frac{x}{2}}{\frac{1}{2}} \right]_{\frac{\pi}{4}}^{3\pi}$$

$$= \tan \frac{3\pi}{8} - \tan \frac{\pi}{8}$$

$$\tan \frac{\pi}{8} = \sqrt{\frac{1 - \cos \frac{\pi}{4}}{1 + \cos \frac{\pi}{4}}} = \sqrt{\frac{\sqrt{2} - 1}{\sqrt{2} + 1}} = \frac{\sqrt{2} - 1}{1}$$

$$\tan \frac{3\pi}{8} = \sqrt{\frac{1 - \cos \frac{3\pi}{4}}{1 + \cos \frac{3\pi}{4}}} = \sqrt{\frac{\sqrt{2} + 1}{\sqrt{2} - 1}} = \sqrt{2} + 1$$

$$= (\sqrt{2} + 1) - (\sqrt{2} - 1)$$

$$= 2$$

PART-B : PHYSICS

31. A radioactive nucleus A with a half life T , decays into a nucleus B . At $t = 0$, there is no nucleus B . At sometime t , the ratio of the number of B to that of A is 0.3. Then, t is given by

$$(1) \quad t = \frac{T}{\log(1.3)}$$

$$(2) \quad t = \frac{T}{2} \frac{\log 2}{\log 1.3}$$

$$(3) \quad t = T \frac{\log 1.3}{\log 2}$$

$$(4) \quad t = T \log(1.3)$$

Answer (3)

$$\text{Sol. } \frac{N_0 - N_0 e^{-\lambda t}}{N_0 e^{-\lambda t}} = 0.3$$

$$\Rightarrow e^{\lambda t} = 1.3$$

$$\therefore \lambda t = \ln 1.3$$

$$\left(\frac{\ln 2}{T} \right) t = \ln 1.3$$

$$t = T \cdot \frac{\ln(1.3)}{\ln 2}$$

$$t = T \frac{\log(1.3)}{\log 2}$$

32. The following observations were taken for determining surface tension T of water by capillary method:

diameter of capillary, $D = 1.25 \times 10^{-2}$ m

rise of water, $h = 1.45 \times 10^{-2}$ m.

Using $g = 9.80 \text{ m/s}^2$ and the simplified relation

$$T = \frac{rhg}{2} \times 10^3 \text{ N/m}, \text{ the possible error in surface}$$

tension is closest to

- | | |
|----------|-----------|
| (1) 10% | (2) 0.15% |
| (3) 1.5% | (4) 2.4% |

Answer (3)

$$\text{Sol. } \frac{\Delta T}{T} \times 100 = \frac{\Delta D}{D} \times 100 + \frac{\Delta h}{h} \times 100$$

$$= \frac{0.01}{1.25} \times 100 + \frac{0.01}{1.45} \times 100$$

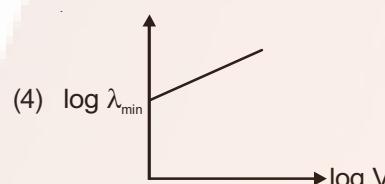
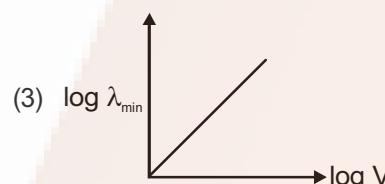
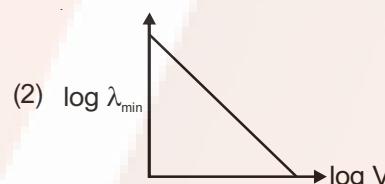
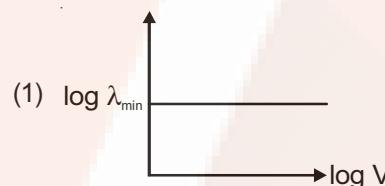
$$= \frac{100}{125} + \frac{100}{145}$$

$$= 0.8 + 0.689$$

$$= 1.489$$

$$1.5\%$$

33. An electron beam is accelerated by a potential difference V to hit a metallic target to produce X-rays. It produces continuous as well as characteristic X-rays. If λ_{\min} is the smallest possible wavelength of X-ray in the spectrum, the variation of $\log \lambda_{\min}$ with $\log V$ is correctly represented in



Answer (2)

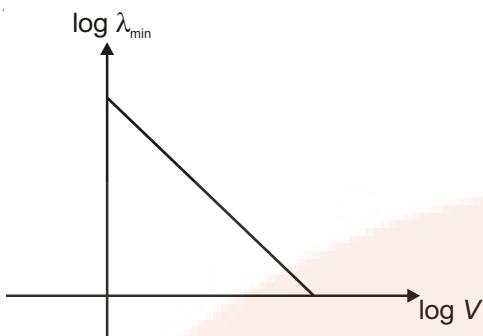
Sol. In X-ray tube

$$\lambda_{\min} = \frac{hc}{eV}$$

$$\ln \lambda_{\min} = \ln \left(\frac{hc}{e} \right) - \ln V$$

Slope is negative

Intercept on y -axis is positive



$$\pi R^2 \ell = \frac{2\pi\ell^3}{3}$$

$$\frac{\ell^2}{R^2} = \frac{3}{2}$$

$$\frac{\ell}{R} = \sqrt{\frac{3}{2}}$$

34. The moment of inertia of a uniform cylinder of length ℓ and radius R about its perpendicular bisector is I .

What is the ratio $\frac{\ell}{R}$ such that the moment of inertia is minimum?

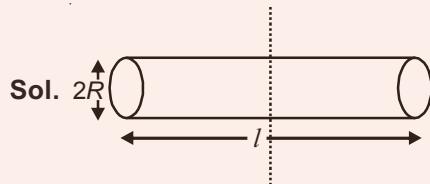
(1) $\frac{3}{\sqrt{2}}$

(2) $\sqrt{\frac{3}{2}}$

(3) $\frac{\sqrt{3}}{2}$

(4) 1

Answer (2)



$$I = \frac{mR^2}{4} + \frac{m\ell^2}{12}$$

$$I = \frac{m}{4} \left[R^2 + \frac{\ell^2}{3} \right]$$

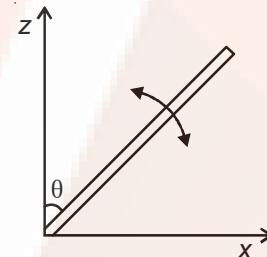
$$= \frac{m}{4} \left[\frac{v}{\pi\ell} + \frac{\ell^2}{3} \right]$$

$$\frac{dI}{d\ell} = \frac{m}{4} \left[\frac{-v}{\pi\ell^2} + \frac{2\ell}{3} \right] = 0$$

$$\frac{v}{\pi\ell^2} = \frac{2\ell}{3}$$

$$v = \frac{2\pi\ell^3}{3}$$

35. A slender uniform rod of mass M and length ℓ is pivoted at one end so that it can rotate in a vertical plane (see figure). There is negligible friction at the pivot. The free end is held vertically above the pivot and then released. The angular acceleration of the rod when it makes an angle θ with the vertical is



(1) $\frac{2g}{3\ell} \cos\theta$

(2) $\frac{3g}{2\ell} \sin\theta$

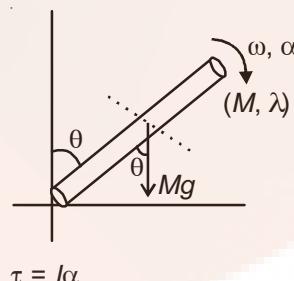
(3) $\frac{2g}{3\ell} \sin\theta$

(4) $\frac{3g}{2\ell} \cos\theta$

Answer (2)

Sol. Torque at angle θ

$$\tau = Mg \sin\theta \cdot \frac{\ell}{2}$$



$$I\alpha = Mg \sin\theta \frac{\ell}{2}$$

$$\therefore I = \frac{M\ell^2}{3}$$

$$\frac{M\ell^2}{3} \cdot \alpha = Mg \sin\theta \frac{\ell}{2}$$

$$\frac{\ell\alpha}{3} = g \frac{\sin\theta}{2}$$

$$\alpha = \frac{3g \sin\theta}{2\ell}$$

36. C_p and C_v are specific heats at constant pressure and constant volume respectively. It is observed that

$C_p - C_v = a$ for hydrogen gas

$C_p - C_v = b$ for nitrogen gas

The correct relation between a and b is

(1) $a = 28b$

(2) $a = \frac{1}{14}b$

(3) $a = b$

(4) $a = 14b$

Answer (4)

Sol. Let molar heat capacity at constant pressure = X_p

and molar heat capacity at constant volume = X_v

$$X_p - X_v = R$$

$$MC_p - MC_v = R$$

$$C_p - C_v = \frac{R}{M}$$

For hydrogen; $a = \frac{R}{2}$

For N_2 ; $b = \frac{R}{28}$

$$\frac{a}{b} = 14$$

$$a = 14b$$

37. A copper ball of mass 100 gm is at a temperature T . It is dropped in a copper calorimeter of mass 100 gm, filled with 170 gm of water at room temperature. Subsequently, the temperature of the system is found to be 75°C. T is given by :

(Given : room temperature = 30°C, specific heat of copper = 0.1 cal/gm°C)

(1) 825°C

(2) 800°C

(3) 885°C

(4) 1250°C

Answer (3)

Sol. $100 \times 0.1 \times (t - 75) = 100 \times 0.1 \times 45 + 170 \times 1 \times 45$

$$10t - 750 = 450 + 7650$$

$$10t = 1200 + 7650$$

$$10t = 8850$$

$$t = 885^\circ\text{C}$$

38. In amplitude modulation, sinusoidal carrier frequency used is denoted by ω_c and the signal frequency is denoted by ω_m . The bandwidth ($\Delta\omega_m$) of the signal is such that $\Delta\omega_m \ll \omega_c$. Which of the following frequencies is not contained in the modulated wave?

(1) $\omega_c - \omega_m$

(2) ω_m

(3) ω_c

(4) $\omega_m + \omega_c$

Answer (2)

Sol. Modulated wave has frequency range.

$$\omega_c \pm \omega_m$$

∴ Since $\omega_c \gg \omega_m$

∴ ω_m is excluded.

39. The temperature of an open room of volume 30 m³ increases from 17°C to 27°C due to the sunshine. The atmospheric pressure in the room remains 1×10^5 Pa. If n_i and n_f are the number of molecules in the room before and after heating, then $n_f - n_i$ will be

(1) -2.5×10^{25}

(2) -1.61×10^{23}

(3) 1.38×10^{23}

(4) 2.5×10^{25}

Answer (1)

Sol. n_1 = initial number of moles

$$n_1 = \frac{P_1 V_1}{R T_1} = \frac{10^5 \times 30}{8.3 \times 290} \approx 1.24 \times 10^3$$

n_2 = final number of moles

$$= \frac{P_2 V_2}{R T_2} = \frac{10^5 \times 30}{8.3 \times 300} \approx 1.20 \times 10^3$$

Change of number of molecules :

$$n_f - n_i = (n_2 - n_1) \times 6.023 \times 10^{23}$$

$$\approx -2.5 \times 10^{25}$$

40. In a Young's double slit experiment, slits are separated by 0.5 mm, and the screen is placed 150 cm away. A beam of light consisting of two wavelengths, 650 nm and 520 nm, is used to obtain interference fringes on the screen. The least distance from the common central maximum to the point where the bright fringes due to both the wavelengths coincide is
- 15.6 mm
 - 1.56 mm
 - 7.8 mm
 - 9.75 mm

Answer (3)

Sol. For λ_1

$$y = \frac{m\lambda_1 D}{d}$$

$$\Rightarrow \frac{m}{n} = \frac{\lambda_2}{\lambda_1} = \frac{4}{5}$$

For λ_1

$$y = \frac{m\lambda_1 D}{d}, \lambda_1 = 650 \text{ nm}$$

$$= 7.8 \text{ mm}$$

41. A particle A of mass m and initial velocity v collides with a particle B of mass $\frac{m}{2}$ which is at rest. The collision is head on, and elastic. The ratio of the de-Broglie wavelengths λ_A to λ_B after the collision is

$$(1) \frac{\lambda_A}{\lambda_B} = \frac{1}{2}$$

$$(2) \frac{\lambda_A}{\lambda_B} = \frac{1}{3}$$

$$(3) \frac{\lambda_A}{\lambda_B} = 2$$

$$(4) \frac{\lambda_A}{\lambda_B} = \frac{2}{3}$$

Answer (3)

Sol. $v_1 = \frac{(m_1 - m_2)v}{m_1 + m_2} + 0$

$$= \frac{v}{3}$$

$$\begin{aligned} m_1 &= m \\ m_2 &= \frac{m}{2} \end{aligned}$$

$$\therefore p_1 = m \left[\frac{v}{3} \right]$$

$$\begin{aligned} v_2 &= \frac{2m_1 v}{m_1 + m_2} + 0 \\ &= \frac{4v}{3} \end{aligned}$$

$$p_2 = \frac{m}{2} \left[\frac{4v}{3} \right] = \frac{2mv}{3}$$

$$\therefore \text{de-Broglie wavelength } \frac{\lambda_A}{\lambda_B} = \frac{p_2}{p_1} = 2 : 1$$

42. A magnetic needle of magnetic moment $6.7 \times 10^{-2} \text{ Am}^2$ and moment of inertia $7.5 \times 10^{-6} \text{ kg m}^2$ is performing simple harmonic oscillations in a magnetic field of 0.01 T. Time taken for 10 complete oscillations is

- 8.76 s
- 6.65 s
- 8.89 s
- 6.98 s

Answer (2)

$$\text{Sol. } T = 2\pi \sqrt{\frac{I}{MB}}$$

$$= 2\pi \sqrt{\frac{7.5 \times 10^{-6}}{6.7 \times 10^{-2} \times 0.01}} = \frac{2\pi}{10} \times 1.06$$

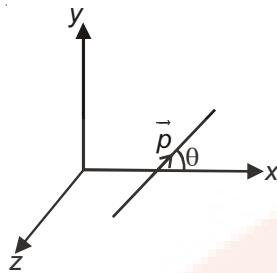
For 10 oscillations,

$$\begin{aligned} t &= 10T = 2\pi \times 1.06 \\ &= 6.6568 \approx 6.65 \text{ s} \end{aligned}$$

43. An electric dipole has a fixed dipole moment \vec{p} , which makes angle θ with respect to x-axis. When subjected to an electric field $\vec{E}_1 = E\hat{i}$, it experiences a torque $\vec{T}_1 = \tau\hat{k}$. When subjected to another electric

field $\vec{E}_2 = \sqrt{3}E\hat{j}$ it experiences a torque $\vec{T}_2 = -\vec{T}_1$. The angle θ is

- 90°
- 30°
- 45°
- 60°

Answer (4)
Sol.


$$\vec{p} = p \cos \theta \hat{i} + p \sin \theta \hat{j}$$

$$\vec{E}_1 = E \hat{i}$$

$$\vec{T}_1 = \vec{p} \times \vec{E}_1$$

$$= (p \cos \theta \hat{i} + p \sin \theta \hat{j}) \times E (\hat{i})$$

$$\tau \hat{k} = p E \sin \theta (-\hat{k}) \quad \dots(i)$$

$$\vec{E}_2 = \sqrt{3} E_1 \hat{j}$$

$$\vec{T}_2 = (p \cos \theta \hat{i} + p \sin \theta \hat{j}) \times \sqrt{3} E_1 \hat{j}$$

$$-\tau \hat{k} = \sqrt{3} p E_1 \cos \theta \hat{k} \quad \dots(ii)$$

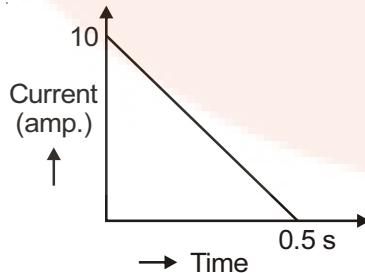
From (i) and (ii)

$$p E \sin \theta = \sqrt{3} p E \cos \theta$$

$$\tan \theta = \sqrt{3}$$

$$\theta = 60^\circ$$

44. In a coil of resistance 100Ω , a current is induced by changing the magnetic flux through it as shown in the figure. The magnitude of change in flux through the coil is



- (1) 275 Wb (2) 200 Wb
 (3) 225 Wb (4) 250 Wb

Answer (4)

$$\text{Sol. } \varepsilon = \frac{d\phi}{dt}$$

$$iR = \frac{d\phi}{dt}$$

$$\int d\phi = R \int i dt$$

Magnitude of change in flux = $R \times (\text{area under current vs time graph})$

$$= 100 \times \frac{1}{2} \times \frac{1}{2} \times 10 \\ = 250 \text{ Wb}$$

45. A time dependent force $F = 6t$ acts on a particle of mass 1 kg. If the particle starts from rest, the work done by the force during the first 1 second will be

- (1) 18 J (2) 4.5 J
 (3) 22 J (4) 9 J

Answer (2)

$$\text{Sol. } 6t = 1 \cdot \frac{dv}{dt}$$

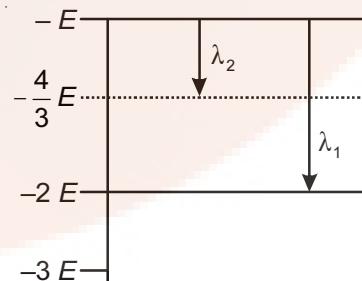
$$\int_0^v dv = \int 6t dt$$

$$v = 6 \left[\frac{t^2}{2} \right]_0^1$$

$$= 3 \text{ ms}^{-1}$$

$$W = \Delta KE = \frac{1}{2} \times 1 \times 9 = 4.5 \text{ J}$$

46. Some energy levels of a molecule are shown in the figure. The ratio of the wavelengths $r = \lambda_1 / \lambda_2$, is given by



- (1) $r = \frac{1}{3}$ (2) $r = \frac{4}{3}$
 (3) $r = \frac{2}{3}$ (4) $r = \frac{3}{4}$

Answer (1)

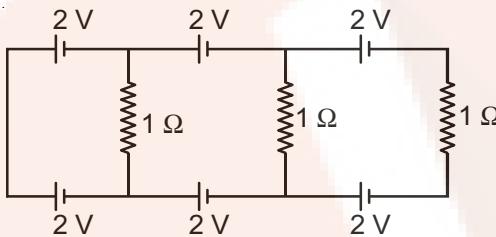
Sol. From energy level diagram

$$\lambda_1 = \frac{hc}{E}$$

$$\lambda_2 = \frac{hc}{\left(\frac{E}{3}\right)}$$

$$\therefore \frac{\lambda_1}{\lambda_2} = \frac{1}{3}$$

47.



In the above circuit the current in each resistance is

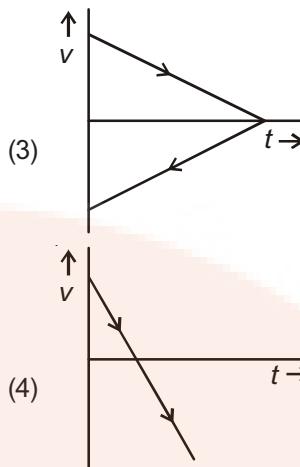
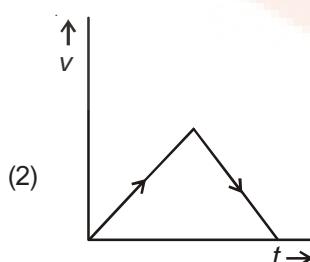
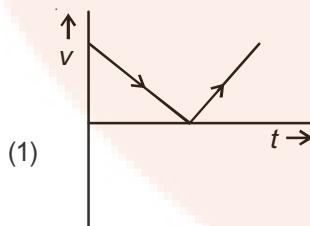
- (1) 0 A (2) 1 A
 (3) 0.25 A (4) 0.5 A

Answer (1)

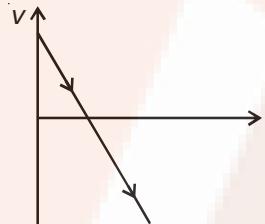
Sol. The potential difference in each loop is zero.

∴ No current will flow.

48. A body is thrown vertically upwards. Which one of the following graphs correctly represent the velocity vs time?


Answer (4)

Sol. Acceleration is constant and negative



49. A capacitance of $2 \mu\text{F}$ is required in an electrical circuit across a potential difference of 1.0 kV . A large number of $1 \mu\text{F}$ capacitors are available which can withstand a potential difference of not more than 300 V .

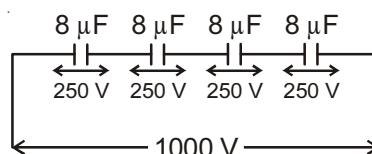
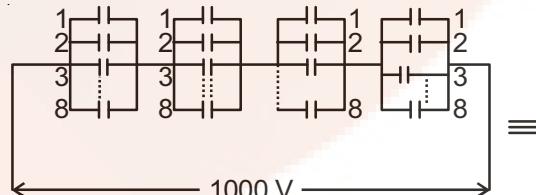
The minimum number of capacitors required to achieve this is

- (1) 32 (2) 2
 (3) 16 (4) 24

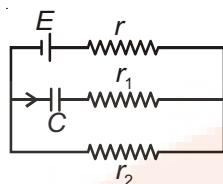
Answer (1)

Sol. Following arrangement will do the needful :

8 capacitors of $1 \mu\text{F}$ in parallel with four such branches in series.



50. In the given circuit diagram when the current reaches steady state in the circuit, the charge on the capacitor of capacitance C will be :



(1) $CE \frac{r_1}{(r_1 + r)}$

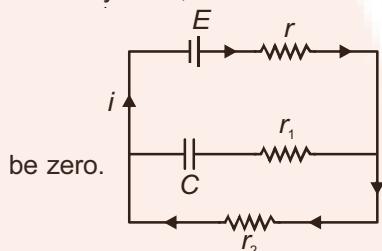
(2) CE

(3) $CE \frac{r_1}{(r_2 + r)}$

(4) $CE \frac{r_2}{(r + r_2)}$

Answer (4)

Sol. In steady state, flow of current through capacitor will



$$i = \frac{E}{r + r_2}$$

$$V_C = i r_2 C = \frac{Er_2 C}{r + r_2}$$

$$V_C = CE \frac{r_2}{r + r_2}$$

51. In a common emitter amplifier circuit using an n-p-n transistor, the phase difference between the input and the output voltages will be

(1) 180°

(2) 45°

(3) 90°

(4) 135°

Answer (1)

Sol. In common emitter configuration for n-p-n transistor, phase difference between output and input voltage is 180° .

52. Which of the following statements is false?

(1) Kirchhoff's second law represents energy conservation

(2) Wheatstone bridge is the most sensitive when all the four resistances are of the same order of magnitude

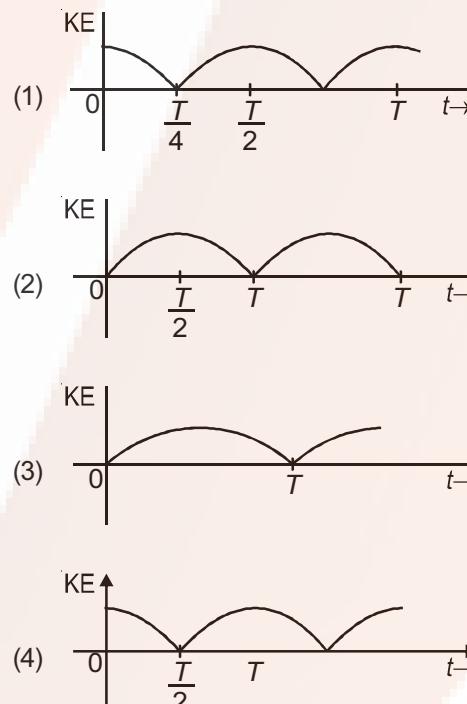
(3) In a balanced Wheatstone bridge if the cell and the galvanometer are exchanged, the null point is disturbed

(4) A rheostat can be used as a potential divider

Answer (3)

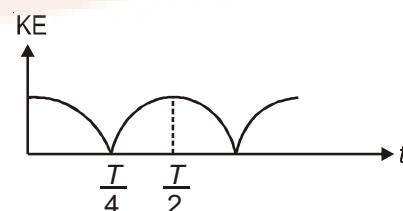
Sol. In a balanced Wheatstone bridge, the null point remains unchanged even if cell and galvanometer are interchanged.

53. A particle is executing simple harmonic motion with a time period T . At time $t = 0$, it is at its position of equilibrium. The kinetic energy-time graph of the particle will look like :



Answer (1)

Sol. $K.E = \frac{1}{2} m \omega^2 A^2 \cos^2 \omega t$



54. An observer is moving with half the speed of light towards a stationary microwave source emitting waves at frequency 10 GHz. What is the frequency of the microwave measured by the observer? (speed of light = $3 \times 10^8 \text{ ms}^{-1}$)

- (1) 15.3 GHz (2) 10.1 GHz
 (3) 12.1 GHz (4) 17.3 GHz

Answer (4)

Sol. For relativistic motion

$$f = f_0 \sqrt{\frac{c+v}{c-v}} ; v = \text{relative speed of approach}$$

$$f = 10 \sqrt{\frac{c + \frac{v}{2}}{c - \frac{v}{2}}} = 10\sqrt{3} = 17.3 \text{ GHz}$$

55. A man grows into a giant such that his linear dimensions increase by a factor of 9. Assuming that his density remains same, the stress in the leg will change by a factor of

- (1) $\frac{1}{81}$ (2) 9
 (3) $\frac{1}{9}$ (4) 81

Answer (2)

$$\text{Sol. } \frac{V_f}{V_i} = 9^3$$

\therefore Density remains same

So, mass \propto Volume

$$\frac{m_f}{m_i} = 9^3$$

$$\frac{(\text{Area})_f}{(\text{Area})_i} = 9^2$$

$$\text{Stress} = \frac{(\text{Mass}) \times g}{\text{Area}}$$

$$\frac{\sigma_2}{\sigma_1} = \left(\frac{m_f}{m_i} \right) \left(\frac{A_i}{A_f} \right)$$

$$= \frac{9^3}{9^2} = 9$$

56. When a current of 5 mA is passed through a galvanometer having a coil of resistance 15 Ω , it shows full scale deflection. The value of the resistance to be put in series with the galvanometer to convert it into a voltmeter of range 0-10 V is

- (1) $4.005 \times 10^3 \Omega$
 (2) $1.985 \times 10^3 \Omega$
 (3) $2.045 \times 10^3 \Omega$
 (4) $2.535 \times 10^3 \Omega$

Answer (2)

Sol. $i_g = 5 \times 10^{-3} \text{ A}$

$$G = 15 \Omega$$

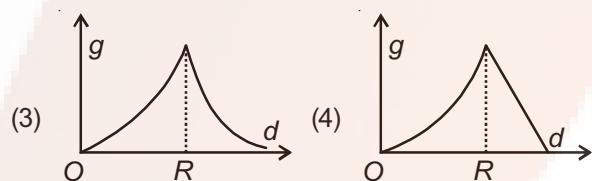
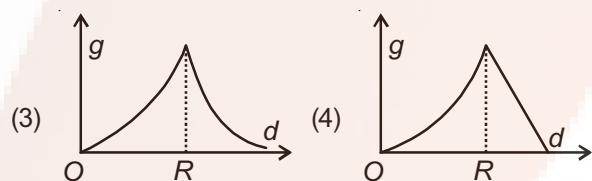
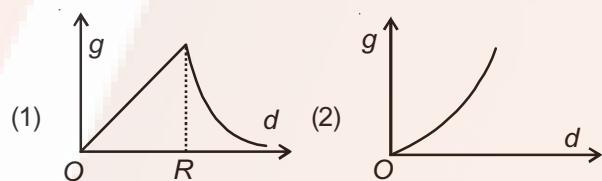
Let series resistance be R .

$$V = i_g (R + G)$$

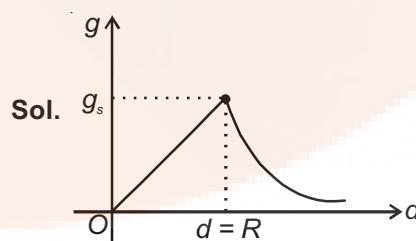
$$10 = 5 \times 10^{-3} (R + 15)$$

$$R = 2000 - 15 = 1985 = 1.985 \times 10^3 \Omega$$

57. The variation of acceleration due to gravity g with distance d from centre of the earth is best represented by (R = Earth's radius)



Answer (1)



Variation of g inside earth surface

$$d < R = g = \frac{Gm}{R^2} \cdot d$$

$$d = R = g_s = \frac{Gm}{R^2}$$

$$d > R = g = \frac{Gm}{d^2}$$

58. An external pressure P is applied on a cube at 0°C so that it is equally compressed from all sides. K is the bulk modulus of the material of the cube and α is its coefficient of linear expansion. Suppose we want to bring the cube to its original size by heating. The temperature should be raised by

(1) $3PK\alpha$

(2) $\frac{P}{3\alpha K}$

(3) $\frac{P}{\alpha K}$

(4) $\frac{3\alpha}{PK}$

Answer (2)

Sol. $K = \frac{\Delta P}{\left(-\frac{\Delta V}{V}\right)}$

$$\frac{\Delta V}{V} = \frac{P}{K}$$

$$\therefore V = V_0 (1 + \gamma \Delta t)$$

$$\frac{\Delta V}{V_0} = \gamma \Delta t$$

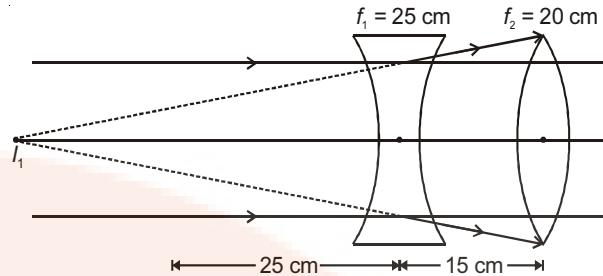
$$\therefore \frac{P}{K} = \gamma \Delta t \Rightarrow \Delta t = \frac{P}{\gamma K} = \frac{P}{3\alpha K}$$

59. A diverging lens with magnitude of focal length 25 cm is placed at a distance of 15 cm from a converging lens of magnitude of focal length 20 cm. A beam of parallel light falls on the diverging lens. The final image formed is

- (1) Real and at a distance of 6 cm from the convergent lens
- (2) Real and at a distance of 40 cm from convergent lens
- (3) Virtual and at a distance of 40 cm from convergent lens
- (4) Real and at a distance of 40 cm from the divergent lens

Answer (2)

Sol.



For converging lens

$$u = -40 \text{ cm} \text{ which is equal to } 2f$$

∴ Image will be real and at a distance of 40 cm from convergent lens.

60. A body of mass $m = 10^{-2} \text{ kg}$ is moving in a medium and experiences a frictional force $F = -kv^2$. Its initial speed is $v_0 = 10 \text{ ms}^{-1}$. If, after 10 s, its energy is $\frac{1}{8}mv_0^2$, the value of k will be

(1) $10^{-1} \text{ kg m}^{-1} \text{ s}^{-1}$ (2) $10^{-3} \text{ kg m}^{-1}$

(3) $10^{-3} \text{ kg s}^{-1}$ (4) $10^{-4} \text{ kg m}^{-1}$

Answer (4)

Sol. $\frac{k_f}{k_i} = \frac{\frac{1}{8}mv_0^2}{\frac{1}{2}mv_0^2} = \frac{1}{4}$

$$\frac{v_f}{v_i} = \frac{1}{2}$$

$$v_f = \frac{v_0}{2}$$

$$-kv^2 = \frac{mdv}{dt}$$

$$\int_{v_0}^{\frac{v_0}{2}} \frac{dv}{v^2} = \int_0^{t_0} \frac{-kdt}{m}$$

$$\left[-\frac{1}{v} \right]_{v_0}^{\frac{v_0}{2}} = \frac{-k}{m} t_0$$

$$\frac{1}{v_0} - \frac{2}{v_0} = -\frac{k}{m} t_0$$

$$-\frac{1}{v_0} = -\frac{k}{m} t_0$$

$$k = \frac{m}{v_0 t_0}$$

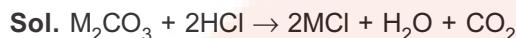
$$= \frac{10^{-2}}{10 \times 10} = 10^{-4} \text{ kg m}^{-1}$$

PART-C : CHEMISTRY

61. 1 gram of a carbonate (M_2CO_3) on treatment with excess HCl produces 0.01186 mole of CO_2 . The molar mass of M_2CO_3 in g mol^{-1} is

- (1) 84.3
- (2) 118.6
- (3) 11.86
- (4) 1186

Answer (1)



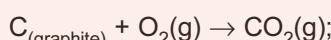
$$n_{M_2CO_3} = n_{CO_2}$$

$$\frac{1}{M_{M_2CO_3}} = 0.01186$$

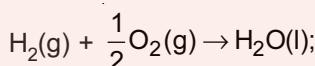
$$M_{M_2CO_3} = \frac{1}{0.01186}$$

$$= 84.3 \text{ g/mol}$$

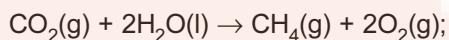
62. Given



$$\Delta_rH^\circ = -393.5 \text{ kJ mol}^{-1}$$

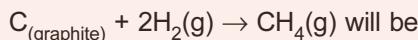


$$\Delta_rH^\circ = -285.8 \text{ kJ mol}^{-1}$$



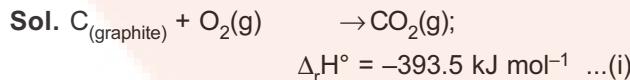
$$\Delta_rH^\circ = +890.3 \text{ kJ mol}^{-1}$$

Based on the above thermochemical equations, the value of Δ_rH° at 298 K for the reaction

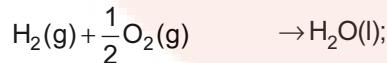


- (1) +144.0 kJ mol^{-1}
- (2) -74.8 kJ mol^{-1}
- (3) -144.0 kJ mol^{-1}
- (4) +74.8 kJ mol^{-1}

Answer (2)



$$\Delta_rH^\circ = -393.5 \text{ kJ mol}^{-1} \dots(i)$$



$$\Delta_rH^\circ = -285.8 \text{ kJ mol}^{-1} \dots(ii)$$



$$\Delta_rH^\circ = 890.3 \text{ kJ mol}^{-1} \dots(iii)$$

By applying the operation

(i) + 2 × (ii) + (iii), we get



$$\begin{aligned}\Delta_rH^\circ &= -393.5 - 285.8 \times 2 + 890.3 \\ &= -74.8 \text{ kJ mol}^{-1}\end{aligned}$$

63. The freezing point of benzene decreases by 0.45°C when 0.2 g of acetic acid is added to 20 g of benzene. If acetic acid associates to form a dimer in benzene, percentage association of acetic acid in benzene will be

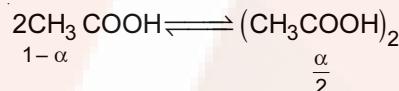
$$(K_f \text{ for benzene} = 5.12 \text{ K kg mol}^{-1})$$

- (1) 80.4%
- (2) 74.6%
- (3) 94.6%
- (4) 64.6%

Answer (3)

Sol. $0.45 = i(5.12) \frac{0.2 / 60}{20} \times 1000$

$$\Rightarrow i = 0.527$$



$$\Rightarrow i = 1 - \frac{\alpha}{2}$$

$$\Rightarrow 0.527 = 1 - \frac{\alpha}{2}$$

$$\Rightarrow \frac{\alpha}{2} = 0.473$$

$$\Rightarrow \alpha = 0.946$$

$$\therefore \% \text{ association} = 94.6\%$$

64. The most abundant elements by mass in the body of a healthy human adult are :

Oxygen (61.4%); Carbon (22.9%); Hydrogen (10.0%) and Nitrogen (2.6%).

The weight which a 75 kg person would gain if all 1H atoms are replaced by 2H atoms is

- (1) 37.5 kg
- (2) 7.5 kg
- (3) 10 kg
- (4) 15 kg

Answer (2)

Sol. Mass of hydrogen = $\frac{10}{100} \times 75 = 7.5 \text{ kg}$

Replacing 1H by 2H would replace 7.5 kg with 15 kg

$$\therefore \text{Net gain} = 7.5 \text{ kg}$$

65. ΔU is equal to

- (1) Isobaric work
- (2) Adiabatic work
- (3) Isothermal work
- (4) Isochoric work

Answer (2)

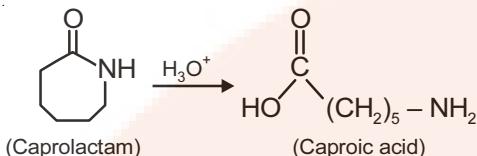
Sol. For adiabatic process, $q = 0$

\therefore As per 1st law of thermodynamics,
 $\Delta U = W$

66. The formation of which of the following polymers involves hydrolysis reaction?
- Bakelite
 - Nylon 6, 6
 - Terylene
 - Nylon 6

Answer (4)

Sol. Caprolactam is hydrolysed to produce caproic acid which undergoes condensation to produce Nylon-6.



67. Given

$$E^\circ_{\text{Cl}_2/\text{Cl}^-} = 1.36 \text{ V}, E^\circ_{\text{Cr}^{3+}/\text{Cr}} = -0.74 \text{ V}$$

$$E^\circ_{\text{Cr}_2\text{O}_7^{2-}/\text{Cr}^{3+}} = 1.33 \text{ V}, E^\circ_{\text{MnO}_4^-/\text{Mn}^{2+}} = 1.51 \text{ V}$$

Among the following, the strongest reducing agent is

- Mn^{2+}
- Cr^{3+}
- Cl^-
- Cr

Answer (4)

Sol. For Cr^{3+} , $E^\circ_{\text{Cr}^{3+}/\text{Cr}_2\text{O}_7^{2-}} = -1.33 \text{ V}$

For Cl^- , $E^\circ_{\text{Cl}^-/\text{Cl}_2} = -1.36 \text{ V}$

For Cr, $E^\circ_{\text{Cr}/\text{Cr}^{3+}} = 0.74 \text{ V}$

For Mn^{2+} , $E^\circ_{\text{Mn}^{2+}/\text{MnO}_4^-} = -1.51 \text{ V}$

Positive E° is for Cr, hence it is strongest reducing agent.

68. The Tyndall effect is observed only when following conditions are satisfied

- The diameter of the dispersed particles is much smaller than the wavelength of the light used.
 - The diameter of the dispersed particle is not much smaller than the wavelength of the light used
 - The refractive indices of the dispersed phase and dispersion medium are almost similar in magnitude
 - The refractive indices of the dispersed phase and dispersion medium differ greatly in magnitude
- (b) and (d)
 - (a) and (c)
 - (b) and (c)
 - (a) and (d)

Answer (1)

Sol. For Tyndall effect refractive index of dispersion phase and dispersion medium must differ significantly. Secondly, size of dispersed phase should not differ much from wavelength used.

69. In the following reactions, ZnO is respectively acting as a/an



- Base and base

- Acid and acid

- Acid and base

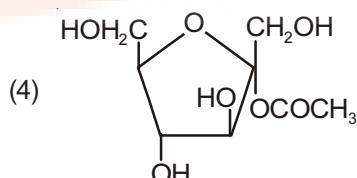
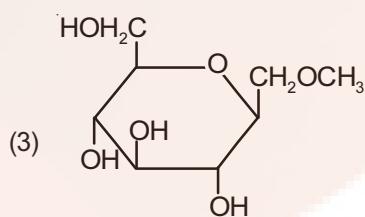
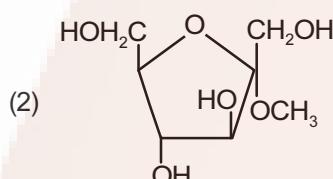
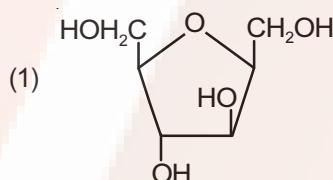
- Base and acid

Answer (3)

Sol. In (a), ZnO acts as acidic oxide as Na_2O is basic oxide.

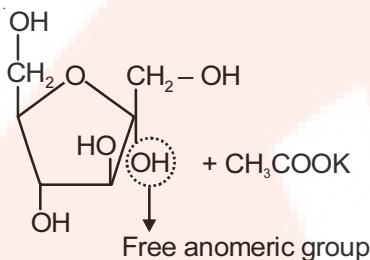
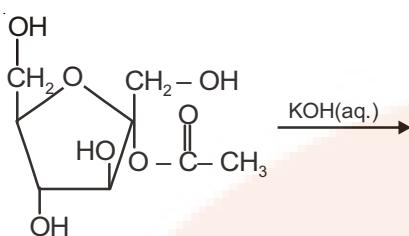
In (b), ZnO acts as basic oxide as CO_2 is acidic oxide.

70. Which of the following compounds will behave as a reducing sugar in an aqueous KOH solution?

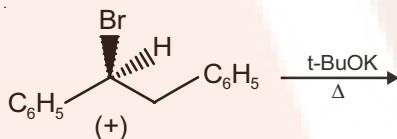


Answer (4)

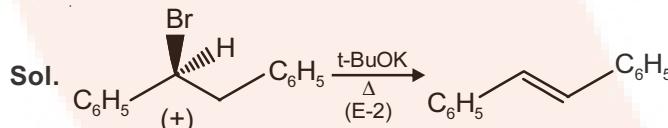
Sol. Sugars in which there is free anomeric $-\text{OH}$ group are reducing sugars



71. The major product obtained in the following reaction is



- (1) $\text{C}_6\text{H}_5\text{CH}=\text{CHC}_6\text{H}_5$
- (2) $(+)\text{C}_6\text{H}_5\text{CH(O}^t\text{Bu})\text{CH}_2\text{C}_6\text{H}_5$
- (3) $(-\text{C}_6\text{H}_5\text{CH(O}^t\text{Bu})\text{CH}_2\text{C}_6\text{H}_5$
- (4) $(\pm)\text{C}_6\text{H}_5\text{CH(O}^t\text{Bu})\text{CH}_2\text{C}_6\text{H}_5$

Answer (1)


72. Which of the following species is not paramagnetic?
- (1) CO
 - (2) O₂
 - (3) B₂
 - (4) NO

Answer (1)

Sol. CO has 14 electrons (even) \therefore it is diamagnetic

NO has 15e⁻ (odd) \therefore it is paramagnetic and has 1 unpaired electron in $\pi^*2\text{p}$ molecular orbital.

B₂ has 10e⁻ (even) but still paramagnetic and has two unpaired electrons in $\pi 2\text{p}_x$ and $\pi 2\text{p}_y$ (s-p mixing).

O₂ has 16 e⁻ (even) but still paramagnetic and has two unpaired electrons in $\pi^*2\text{p}_x$ and $\pi^*2\text{p}_y$ molecular orbitals.

73. On treatment of 100 mL of 0.1 M solution of $\text{CoCl}_3 \cdot 6\text{H}_2\text{O}$ with excess AgNO_3 ; 1.2×10^{22} ions are precipitated. The complex is

- (1) $[\text{Co}(\text{H}_2\text{O})_3\text{Cl}_3] \cdot 3\text{H}_2\text{O}$
- (2) $[\text{Co}(\text{H}_2\text{O})_6]\text{Cl}_3$
- (3) $[\text{Co}(\text{H}_2\text{O})_5\text{Cl}]\text{Cl}_2 \cdot \text{H}_2\text{O}$
- (4) $[\text{Co}(\text{H}_2\text{O})_4\text{Cl}_2]\text{Cl} \cdot 2\text{H}_2\text{O}$

Answer (3)

Sol. Millimoles of $\text{AgNO}_3 = \frac{1.2 \times 10^{22}}{6 \times 10^{23}} \times 1000 = 20$

Millimoles of $\text{CoCl}_3 \cdot 6\text{H}_2\text{O} = 0.1 \times 100 = 10$

\therefore Each mole of $\text{CoCl}_3 \cdot 6\text{H}_2\text{O}$ gives two chloride ions.

$\therefore [\text{Co}(\text{H}_2\text{O})_5\text{Cl}]\text{Cl}_2 \cdot \text{H}_2\text{O}$

74. pK_a of a weak acid (HA) and pK_b of a weak base (BOH) are 3.2 and 3.4, respectively. The pH of their salt (AB) solution is

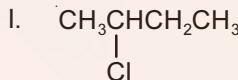
- (1) 6.9
- (2) 7.0
- (3) 1.0
- (4) 7.2

Answer (1)

$$\text{Solt. pH} = 7 + \frac{1}{2} (\text{pK}_a - \text{pK}_b)$$

$$= 7 + \frac{1}{2} (3.2 - 3.4) \\ = 6.9$$

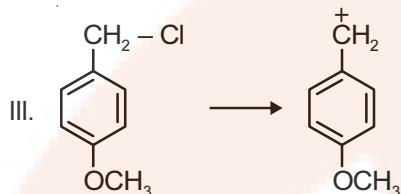
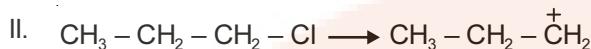
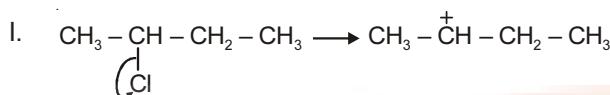
75. The increasing order of the reactivity of the following halides for the $\text{S}_{\text{N}}1$ reaction is



- (1) (II) < (I) < (III)
- (2) (I) < (III) < (II)
- (3) (II) < (III) < (I)
- (4) (III) < (II) < (I)

Answer (1)

Sol. Rate of S_N1 reaction \propto stability of carbocation



So, II < I < III

Increase stability of carbocation and hence increase reactivity of halides.

76. Both lithium and magnesium display several similar properties due to the diagonal relationship, however, the one which is incorrect, is

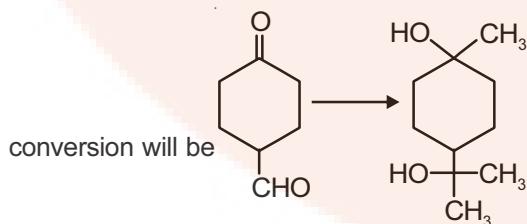
- (1) Both form soluble bicarbonates
- (2) Both form nitrides
- (3) Nitrates of both Li and Mg yield NO₂ and O₂ on heating
- (4) Both form basic carbonates

Answer (4)

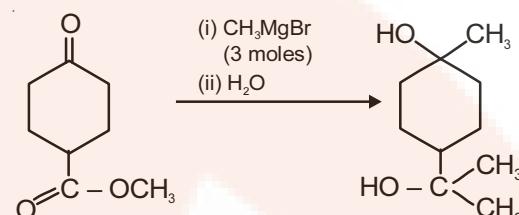
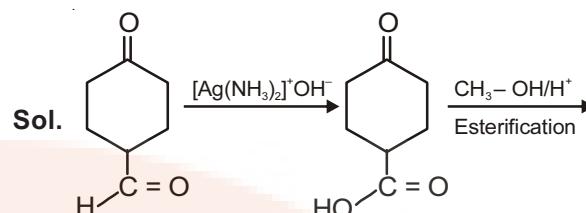
Sol. Mg forms basic carbonate

$3\text{MgCO}_3 \cdot \text{Mg}(\text{OH})_2 \cdot 3\text{H}_2\text{O}$ but no such basic carbonate is formed by Li.

77. The correct sequence of reagents for the following

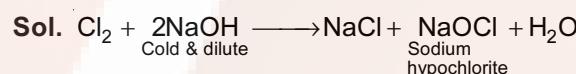


- (1) $\text{CH}_3\text{MgBr}, \text{H}^+/\text{CH}_3\text{OH}, [\text{Ag}(\text{NH}_3)_2]^+\text{OH}^-$
- (2) $\text{CH}_3\text{MgBr}, [\text{Ag}(\text{NH}_3)_2]^+\text{OH}^-, \text{H}^+/\text{CH}_3\text{OH}$
- (3) $[\text{Ag}(\text{NH}_3)_2]^+\text{OH}^-, \text{CH}_3\text{MgBr}, \text{H}^+/\text{CH}_3\text{OH}$
- (4) $[\text{Ag}(\text{NH}_3)_2]^+\text{OH}^-, \text{H}^+/\text{CH}_3\text{OH}, \text{CH}_3\text{MgBr}$

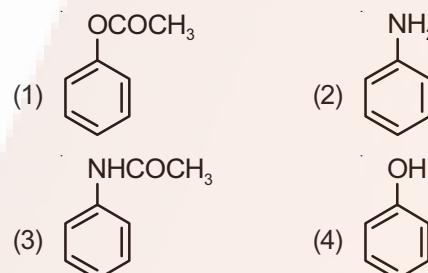
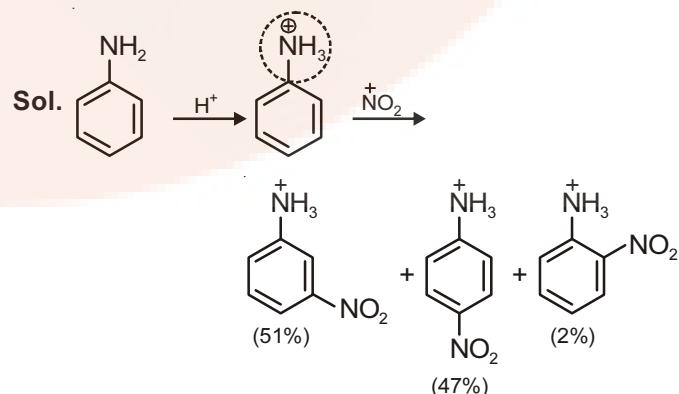
Answer (4)


78. The products obtained when chlorine gas reacts with cold and dilute aqueous NaOH are

- (1) ClO_2^- and ClO_3^-
- (2) Cl^- and ClO^-
- (3) Cl^- and ClO_2^-
- (4) ClO^- and ClO_3^-

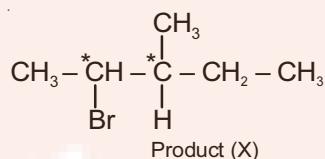
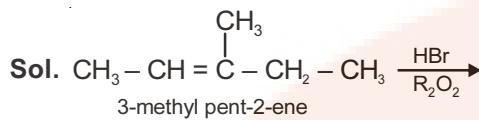
Answer (2)


79. Which of the following compounds will form significant amount of *meta* product during mono-nitration reaction?


Answer (2)


80. 3-Methyl-pent-2-ene on reaction with HBr in presence of peroxide forms an addition product. The number of possible stereoisomers for the product is
- Zero
 - Two
 - Four
 - Six

Answer (3)



Since product (X) contains two chiral centres and it is unsymmetrical.

So, its total stereoisomers = $2^2 = 4$.

81. Two reactions R_1 and R_2 have identical pre-exponential factors. Activation energy of R_1 exceeds that of R_2 by 10 kJ mol^{-1} . If k_1 and k_2 are rate constants for reactions R_1 and R_2 respectively at 300 K , then $\ln(k_2/k_1)$ is equal to

$$(R = 8.314 \text{ J mole}^{-1} \text{ K}^{-1})$$

- 12
- 6
- 4
- 8

Answer (3)

Sol. $k_1 = A e^{-E_{a_1}/RT}$

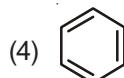
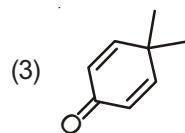
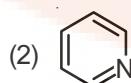
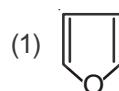
$k_2 = A e^{-E_{a_2}/RT}$

$$\frac{k_2}{k_1} = e^{\frac{1}{RT}(E_{a_1} - E_{a_2})}$$

$$\ln \frac{k_2}{k_1} = \frac{E_{a_1} - E_{a_2}}{RT}$$

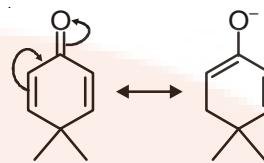
$$= \frac{10 \times 10^3}{8.314 \times 300} \approx 4$$

82. Which of the following molecules is least resonance stabilized?



Answer (3)

Sol. However, all molecules given in options are stabilised by resonance but compound given in option (3) is least resonance stabilised (other three are aromatic)



83. The group having isoelectronic species is

- O^- , F^- , Na^+ , Mg^{2+}
- O^{2-} , F^- , Na^+ , Mg^{2+}
- O^- , F^- , Na^+ , Mg^{2+}
- O^{2-} , F^- , Na^+ , Mg^{2+}

Answer (4)

Sol. Mg^{2+} , Na^+ , O^{2-} and F^- all have 10 electrons each.

84. The radius of the second Bohr orbit for hydrogen atom is

(Planck's Const. $h = 6.6262 \times 10^{-34} \text{ Js}$;
mass of electron = $9.1091 \times 10^{-31} \text{ kg}$;
charge of electron $e = 1.60210 \times 10^{-19} \text{ C}$;
permittivity of vacuum

$$\epsilon_0 = 8.854185 \times 10^{-12} \text{ kg}^{-1} \text{ m}^{-3} \text{ A}^2$$

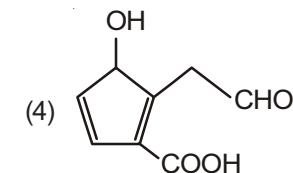
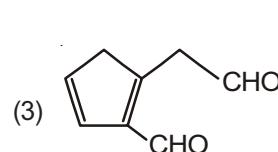
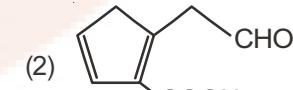
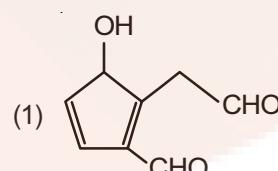
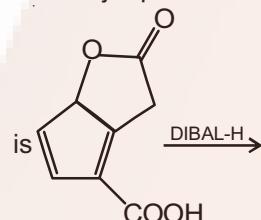
- 4.76 Å
- 0.529 Å
- 2.12 Å
- 1.65 Å

Answer (3)

Sol. $r = a_0 \frac{n^2}{Z} = 0.529 \times 4$

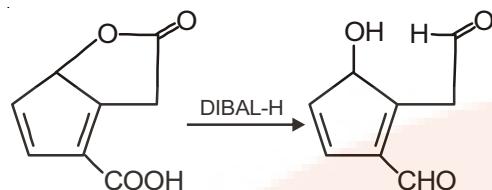
$$= 2.12 \text{ Å}$$

85. The major product obtained in the following reaction



Answer (1)

Sol. DIBAL — H reduces esters and carboxylic acids into aldehydes



86. Which of the following reactions is an example of a redox reaction?

- (1) $\text{XeF}_2 + \text{PF}_5 \rightarrow [\text{XeF}]^+ \text{PF}_6^-$
- (2) $\text{XeF}_6 + \text{H}_2\text{O} \rightarrow \text{XeOF}_4 + 2\text{HF}$
- (3) $\text{XeF}_6 + 2\text{H}_2\text{O} \rightarrow \text{XeO}_2\text{F}_2 + 4\text{HF}$
- (4) $\text{XeF}_4 + \text{O}_2\text{F}_2 \rightarrow \text{XeF}_6 + \text{O}_2$

Answer (4)

Sol. Xe is oxidised from +4(in XeF_4) to +6(in XeF_6)

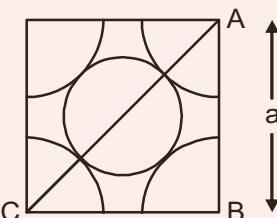
Oxygen is reduced from +1 (in O_2F_2) to zero (in O_2)

87. A metal crystallises in a face centred cubic structure. If the edge length of its unit cell is 'a', the closest approach between two atoms in metallic crystal will be

- (1) $2\sqrt{2}a$
- (2) $\sqrt{2}a$
- (3) $\frac{a}{\sqrt{2}}$
- (4) $2a$

Answer (3)

Sol. In FCC, one of the face is like



By ΔABC ,

$$2a^2 = 16r^2$$

$$\Rightarrow r^2 = \frac{1}{8}a^2$$

$$\Rightarrow r = \frac{1}{2\sqrt{2}}a$$

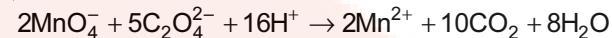
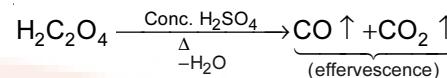
$$\text{Distance of closest approach} = 2r = \frac{a}{\sqrt{2}}$$

88. Sodium salt of an organic acid 'X' produces effervescence with conc. H_2SO_4 . 'X' reacts with the acidified aqueous CaCl_2 solution to give a white precipitate which decolourises acidic solution of KMnO_4 . 'X' is

- (1) HCOONa
- (2) CH_3COONa
- (3) $\text{Na}_2\text{C}_2\text{O}_4$
- (4) $\text{C}_6\text{H}_5\text{COONa}$

Answer (3)

Sol. $\text{Na}_2\text{C}_2\text{O}_4 + \text{H}_2\text{SO}_4 \xrightarrow[\text{Conc.}]{(X)} \text{Na}_2\text{SO}_4 + \text{H}_2\text{C}_2\text{O}_4$
oxalic acid



89. A water sample has ppm level concentration of following anions

$$\text{F}^- = 10; \text{SO}_4^{2-} = 100; \text{NO}_3^- = 50$$

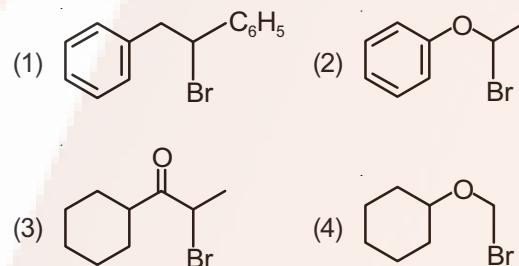
The anion/anions that make/makes the water sample unsuitable for drinking is/are

- (1) Both SO_4^{2-} and NO_3^-
- (2) Only F^-
- (3) Only SO_4^{2-}
- (4) Only NO_3^-

Answer (2)

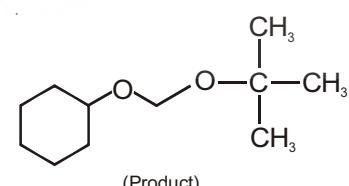
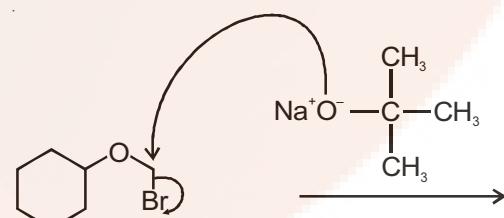
Sol. Permissible limit of F^- in drinking water is upto 1 ppm. Excess concentration of $\text{F}^- > 10$ ppm causes decay of bones.

90. Which of the following, upon treatment with *tert*-BuONa followed by addition of bromine water, fails to decolorize the colour of bromine?



Answer (4)

Sol.



The above product does not have any $\text{C}=\text{C}$ or $\text{C}\equiv\text{C}$ bond, so, it will not give Br_2 -water test.

Thank You

for downloading the PDF

FREE  LIVE ONLINE

MASTER CLASSES

FREE Webinars by Expert Teachers



Vedantu

FREE MASTER CLASS SERIES

- For **Grades 6-12th** targeting **JEE, CBSE, ICSE** & much more
- Free 60 Minutes Live Interactive** classes everyday
- Learn from the **Master Teachers** - India's best

Register for **FREE**

Limited Seats!