

1 Introduction

2 Model

Due that the proplyds cusp is the only part that is directly exposed to the radiation field of $\theta^1\text{C}$ this is the brightest part of the proplyd at least in Ha and ions of high and medium ionization. The diffuse radiation of the nebulae is negligible in comparison with the $\theta^1\text{C}$ in the cusp at least for those proplyds that are very close to $\theta^1\text{C}$. For those far from $\theta^1\text{C}$, we take into account the diffuse radiation as a fraction of the main radiation field.

In this first step of the model we constructed a model for only the proplyd cusp with the influence of the main radiation field, $\theta^1\text{C}$, and the diffuse radiation as a $\theta^1\text{C}$ fraction.

We follow the analytic model of a photoevaporated wind described in Henney & Arthur (1998).

The simplest assumption is that there is a static spherical distribution of gas about the central lowmass star. This gas is being evaporated and ionizing by the radiation coming from $\theta^1\text{C}$

- Ionizing radiation incident parallel to the proplyd.
- Assuming a cylindrical geometry with symmetry in the coordinate Φ
- Semi-spheric ionization front. $S_\theta = S_0(\cos \theta)$
- The photoionized gas flows radially from the border of ionization
- The gas flow is not isothermic
- Collisional deexcitation are not negligibles – mas que una suposicion es una consecuencia, cierto?

We construct Cloudy models of a series of individual radial cuts from the center of the proplyd, at different angles θ from the proplyd axis. For each angle we reduce the flux by a factor of $\cos\theta$.

2.1 Geometry

Δ is the ionization front width in terms of the mean free path at 1 Rydberg. That is, $\Delta = W / n_0 \sigma_0$ where n_0 is the density at the sonic point, σ_0 is the H cross section and W is the number of the mean free paths.

For simplicity and clarity of the model we chose to use a dimensionless radial coordinate $R r / r_0$ where r is the radial coordinate in cm starting in the low-mass star inside the proplyd and r_0 is the distance between the proplyd center and the sonic point.

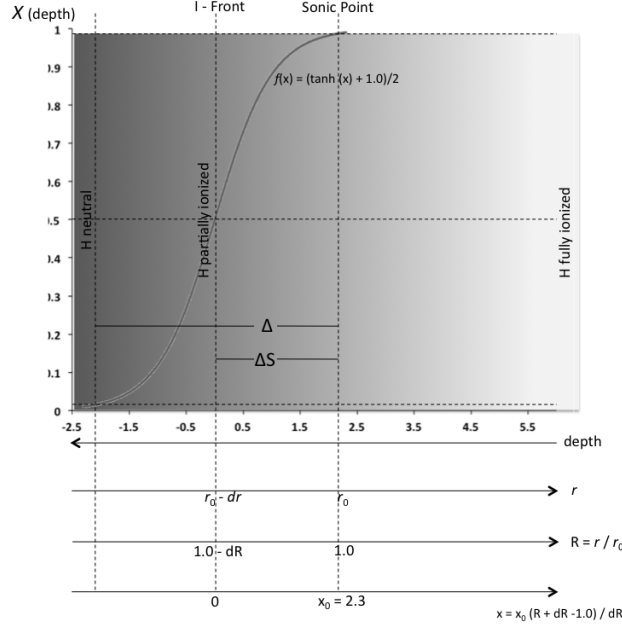


Figure 1: A sketched geometry of the 1D Cloudy model.

2.2 Radial Density Structure

As we mentioned above one way to develop models that take into account both, the radiative transfer and the hydrodynamics of the gas, is to introduce an approximate hydrodynamics in the radiative models that are available and such are stable. This is our case and the way to introduce the hydrodynamics of the gas is using the electron density structure that is a result of the hydrodynamic theoretical models.

We divide the proplyd flow into two zones:

- $r > r_0$: An outer, fully ionized flow.
- $r < r_0$: An inner, partially ionized flow.

This is equivalent to say that the behavior of the physical conditions are different in both zones. We suppose that the flow in the partially ionized zone, that correspond to the thin ionization front, is a subsonic flow. This is accelerated to be a supersonic flow in the outer fully ionized zone. The boundary between them are exactly the sonic point. The conditions there, and in every point of the proplyd, are fixed by continuity, it means that the electron density change as the gas-phase velocity change and viceversa.

$$n_e(X) = \begin{cases} f_1(X) & 1 \geq X \geq 0.98 \\ f_2(X) & 0.02 \geq X \leq 0.98 \end{cases} \quad (1)$$

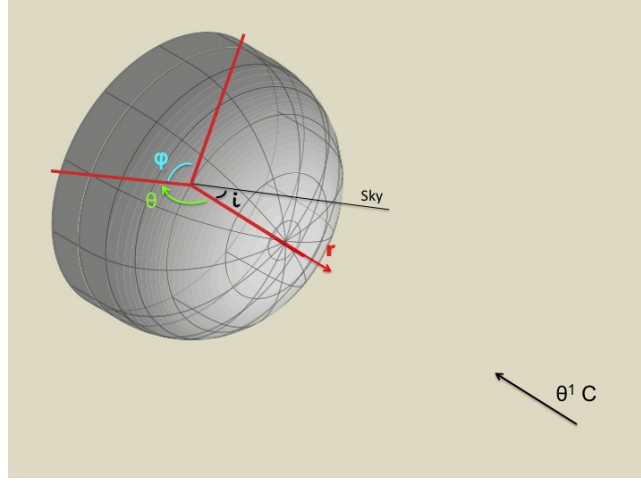


Figure 2: A sketched geometry of the semi-3D model.

2.2.1 The outer zone

This is similar to what Will did in (Henney et al., 2002)

In the outer zone we assume an isothermal, supersonic, complete ionized flow. From mass conservation, in spherical geometry and In the steady state, radial velocity of the ionized gas, $v(r)$

Gas velocity is given by Dyson solution (Dyson, 1968)

$$R = U^{(-1/2)} \exp \left[\frac{1}{4} (U^2 - 1) \right] \quad (2)$$

where $U(R) = v/c_0$ with $v(R)$ is the gas velocity and $c(R)$ is the sound speed which is calculated *in situ* by Cloudy for each step. Due we can not have an analytic solution for U as a function of R , from this equation generate a table of values for U and R and interpolate this table for each R that is necessary in the Cloudy model.

At each point the density is calculated by the continuity equation:

$$\rho(R) = \rho(R_{max}) \left(\frac{U(R_{max})}{U(R)} \right) \left(\frac{R_{max}}{R} \right)^2 \quad (3)$$

2.2.2 The boundary

Because the gas velocity is the property that determines the behavior of other physical properties of the proplyd, the logical boundary between the regions is exactly the sonic point.

This point is also where the criterion of Stromgren for a density bounded region is met. That is, where the photoionization balance is broken and the recombination start to overcome the photoionization.

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$$r = r_0$$

$$X_H \simeq 0.99$$

$$u_0 = c_0 \text{ by definition of the boundary}$$

$$c_0 = c_{max} \text{ at least a local maximum}$$

2.2.3 The inner zone

Partially ionized region: Density is function of sound speed

In this zone, we follow the simplified analytic model for weak-D ionization front described in Appendix of the Henney et al. (2005) paper. Even when this model is for a plane-parallel ionization front (the momentum conservation assumes plane parallel geometry) and this is not our case (we have an divergent geometry) this is an approximation that could give us a good idea of the advection effects on the I-front.

Following the A8 equation,

$$c(X) = c_0 \left[\frac{T(X)}{T_0} \frac{1+X}{1+X_0} \right]^{1/2} \quad (4)$$

If we see the electronic temperature behavior for the weak-D solutions, Fig.18 from Henney et al. (2005), we can see that the temperature could be assume constant in first approximation, at least in $0.25 \leq X \leq 1.0$. This is our case, then the sound speed will be:

$$c(X) = c_0 \left[\frac{1+X}{1+X_0} \right]^{1/2} \quad (5)$$

As in the Cloudy models the temperature is one of the physical quantities that are calculated in each zone, we can not use it for calculate the sound speed in each zone. Then, we made an approximation for the behavior of X in the recombination zone, for calculate the sound speed. We approximate the H ionization fraction by a function of R :

$$ifrac = 0.5(\tanh(x) + 1.0) \quad (6)$$

where $x = x_0 \frac{R+dR-1.0}{dR}$. x_0 is where the H ionization fraction is 0.99, i.e. in the sonic point where $R = 1$ ($ifrac_0 = 0.5(\tanh(x_0) + 1.0)$).

Making use of the Mach number $M = v/c$ and the fact of $c_0/c = \frac{1}{2}(M + M^{-1})$. Then, once more by continuity, the electronic density in this zone is:

$$\rho = \rho_0 / 1.0 - \sqrt{1.0 - \left[\frac{1+X}{1+X_0} \right]} \quad (7)$$

in contrast to the static case where the density is: $\rho \sim 1/c^2$

3 Results and Predictions

3.1 Physical properties

- Electron Density: It has an almost constant increase reaching the maximum value in the i-front (after the sonic point) where the H is partially ionized. In this zone,

the electron density reach the critical electron density for some ions, making the collisional deexcitation a process that need to take into account.

This could be negligible in the outer parts of the flow since they are highly ionized, which means that [O III] is the dominant coolant. The critical density of this ion is about 10^6 cm^{-3} , which is reached just near of the sonic point, that is, where the [O III] emission is less than the 10% of the total [O III] emission. (See Sect. 3.3).

- **Temperature:** The electron temperature is almost constant in the outer zone. As we approach to the He recombination front the Te increase reaching the maximum value just before the i-front, where the He is neutral and the H still fully ionized.

It is due for two reasons: The first one is that as the radiation field goes into the gas-phase of the proplyd, the less energy photons are absorbed. This cause a hardening of the radiation field increasing the mean electron kinetic energy. That is, increasing the photoelectric heating per recombination. The second one is the electron density increase. It causes collisional deexcitation of the main cooling lines.

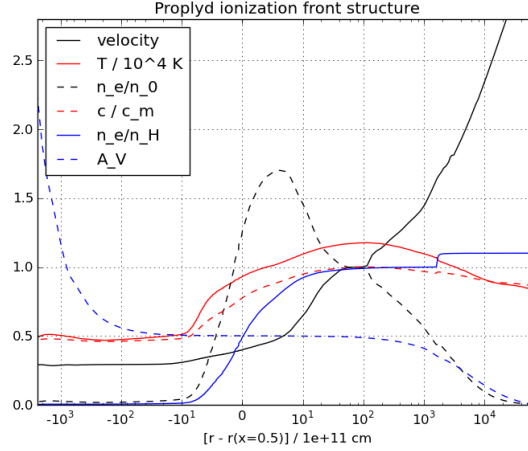


Figure 3: 1D model structure.

3.2 Ionization structure

3.3 Emissivities

All the high ionization lines are all wholly outside the sonic point.

[Ne II], $H\alpha$, [N II] and [O II] have almost the 90% of their emission in the super-sonic zone and the 10% in the sub-sonic zone.

[S II] is about 70% outside the sonic point and 30% inside.

[O I] is about 20% outside and 80% inside the sonic point.

So if we take into account the full emission of the proplyd, and the sub-sonic zone is not well modelated, the efect of this should be not very important since it is only going to affect two lines. Nevertheless, if we want to compare the model predictions with observations that takes only a little aperture of the proplyd and it is near of the center (near the i-front), the sub-sonic zone will be very important.

There are a clear separation of 3 km/s (about 15%) between the median velocity of the [O III] 5007 and 4363 lines.

Discutir tambien la diferencia que hay entre la linea auroral y la nebular de [N II] para ver la importancia de las desexcitaciones colisionales. Una es mas afectada que la otra y por lo tanto conforme vamos a las zonas de mayor densidad la razon entre ellas debe ir cambiando, aumentando de hecho.

4 Conclusion

We will construct Cloudy models of a series of individual radial cuts from the center of the proplyd, at different angles θ from the proplyd axis.

References

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