

Quantitative patterns in drone wars

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Abstract

Attacks by drones (i.e., unmanned combat air vehicles) continue to generate heated political and ethical debates. Here we examine instead the quantitative nature of drone attacks, focusing on how their intensity and frequency compares to other forms of human conflict. Instead of the power-law distribution found recently for insurgent and terrorist attacks, the severity of attacks is more akin to lognormal and exponential distributions, suggesting that the dynamics underlying drone attacks lie beyond these other forms of human conflict. Meanwhile the pattern in the timing of attacks is consistent with one side having almost complete control. We show that these novel features can be reproduced and understood using a generative mathematical model in which resource allocation to the dominant side is regulated through a feedback loop.

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1 Introduction

2 Dating back to physicist L. F. Richardson’s pioneering work nearly 100
3 years ago [1], the quantitative analysis of human conflict has attracted research
4 interest from across the social, biological, economic, mathematical and phys-
5 ical sciences [2, 3, 4, 5, 6, 7]. As in other human activities [8, 9], power
6 laws have been identified in the severity distribution of individual attacks
7 in insurgencies and terrorism [10, 4, 5, 6], and in the temporal trend in
8 events [10, 11, 5]. These studies found that across a wide range of insur-
9 gent wars in which a relatively small opponent such as an insurgency (Red
10 Queen [11]) fights a larger one such as a state (Blue King [11]), the proba-
11 bility distribution for the severity s —the number of fatalities—of an event
12 (i.e., clash or attack) is given by $P(s) \propto s^{-\alpha}$ where $\alpha \sim 2.5$, while the trend
13 in the timing of attacks is given by $\tau_n = \tau_1 n^{-b}$, where τ_n is the time interval
14 between events n and $n + 1$, $n = 1, 2, \dots$ and b is the escalation parameter.
15 When $b = 0$, the Blue King and Red Queen are evenly matched, with both
16 effectively running on the same spot—hence the terminology surrounding
17 the Red Queen [11]. When $b \neq 0$, there is an escalation in the frequency of
18 attacks which can be interpreted as a relative advantage between the Red
19 Queen and the Blue King [11]. The power-law finding for the distribution of
20 event severities is consistent with the Red Queen (i.e., insurgent force) evolv-
21 ing dynamically as a self-organizing system composed of cells (i.e., clusters)
22 that sporadically either fragment under the pressure of the Blue King (e.g.,
23 state) or coalesce to create larger cells, and taking the severity of attacks as
24 proportional to the sizes of the resulting cells [6].

25 This paper examines, for the first time, event patterns in the new form of
26 human conflict offered by unmanned combat air vehicles (drones) [12]. We
27 focus on Pakistan and Yemen because of their association with drone strike
28 campaigns, using data from the New America Foundation and the South
29 Asia Terrorism Portal databases. The situation of drone wars differs from
30 the typical situation for insurgencies and terrorism in that the attacks are
31 now carried out by the Blue King on the Red Queen. Moreover, the sophis-
32 tication of the action-at-a-distance technology means that any delay in the
33 Blue King’s next attack is likely to have come from a constraint within Blue
34 itself (e.g., political opposition) as opposed to any direct counter-adaptation
35 by the Red Queen. Our findings show that drone attacks tend to deviate

36 from the universal patterns observed in the severity and timing for insur-
37 gencies and terrorism, and instead suggest a new regime in which the Blue
38 King has almost complete control over the conflict. We develop a generative
39 model in which the timing of attacks is determined solely by the resources of
40 the Blue King, but are regulated by a positive feedback loop due to the Blue
41 King’s internal sociopolitical and economic constraints. We show that this
42 simple model reproduces the main features of the original data and hence
43 yields novel insight into the unique nature of drone warfare.

44 **Results and Discussion**

45 Figs. 1A–B shows the complementary cumulative distribution function
46 (CCDF) of the severity of drone attacks using the New America Foundation
47 database. We fit power-law and lognormal distributions (dashed green and
48 solid black lines respectively; see methods) for attacks in Pakistan (Figs. 1A)
49 and Yemen (Figs. 1B). We find that the severity of the strikes is approximate-
50 ly described by lognormal distributions, particularly in the case of Pakistan.
51 In the case of Yemen, for which we have far less data, the lognormal is more
52 tentative with the larger events deviating most. This finding of approximate
53 log-normality is consistent with the notion that a drone has a specific design
54 and targets (predominantly houses and vehicles) and hence a pre-determined
55 order of magnitude of the range of destruction and likely severity. This con-
56 trasts with attacks by terrorist or insurgent clusters whose size and hence
57 lethality crosses multiple scales, yielding scale-free (power-law) severity dis-
58 tributions. In drone attacks, an approximate lognormal distribution can
59 arise through at least two mechanisms: First, the fact that the severity of the
60 attack is the result of many independent processes (e.g., successful reporting,
61 good visibility, compact target group, etc.) will itself produce a lognormal
62 distribution in the attack size. Second, if we take the uncertainty in the casu-
63 alty number to scale with the target size, this also produce an approximate
64 lognormal distribution for many underlying distributions of target sizes. For
65 example, suppose attacks target the largest known or available Red group,
66 drawn from a power-law distribution. Setting the mean and standard devi-
67 ation of a zero-truncated normal distribution to this value, then reproduces
68 the approximate lognormal distribution (Figs. 1C). Similarly, we can imagine
69 that most attacks target small groups, where the chances of civilian casual-
70 ties is lower, and that the probability of targeting larger groups decreases
71 exponentially. Setting the mean and standard deviation to a random value

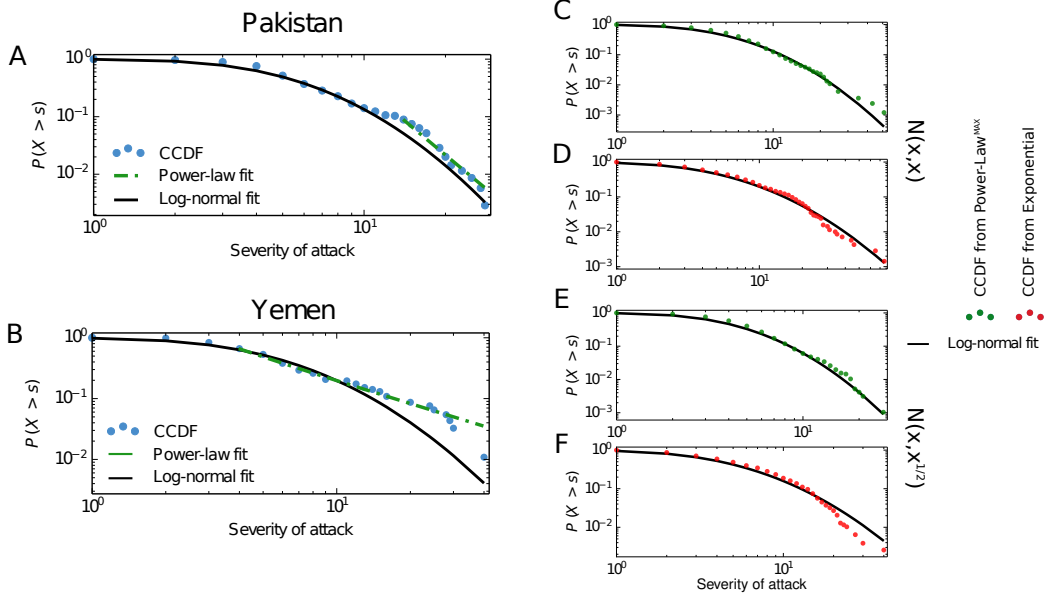


Figure 1: **The severity of drone attacks approximately follows a lognormal distribution.** Complementary Cumulative Distribution Function (CCDF) of the severity of attacks (blue dots and solid line) and best fits to power-law (solid black) and lognormal (dashed green) distributions for drone attacks in Pakistan (A) and Yemen (B). The optimal parameters for each distribution are (A) Power-law: $\alpha = 4.82$, Log-normal: $\mu = 1.60$ and $\sigma = 0.64$, (B) Power-law: $\alpha = 2.21$, Log-normal: $\mu = 1.65$ and $\sigma = 0.77$. (C-F) CCDFs of the severity of attacks and best fits to log-normal distributions. (C-D) The attack size is drawn from a normal distribution ($N(\mu, \sigma)$) with μ and σ corresponding to (C) the largest value in 100 random numbers drawn from a power-law ($\alpha = 4$) and (D) a random value from a exponential distribution ($\lambda = 5$). (E-F) The attack size is drawn from a normal distribution with μ and σ^2 corresponding to (E) the largest value in 100 random numbers drawn from a power-law ($\alpha = 4$) and (F) a random value from a exponential distribution ($\lambda = 5$). The maximum likelihood parameters for the lognormal fits are (C) $\mu = 1.48$ and $\sigma = 0.73$, (D) $\mu = 1.51$ and $\sigma = 0.93$, (E) $\mu = 1.33$ and $\sigma = 0.63$, (F) $\mu = 1.44$ and $\sigma = 0.86$.

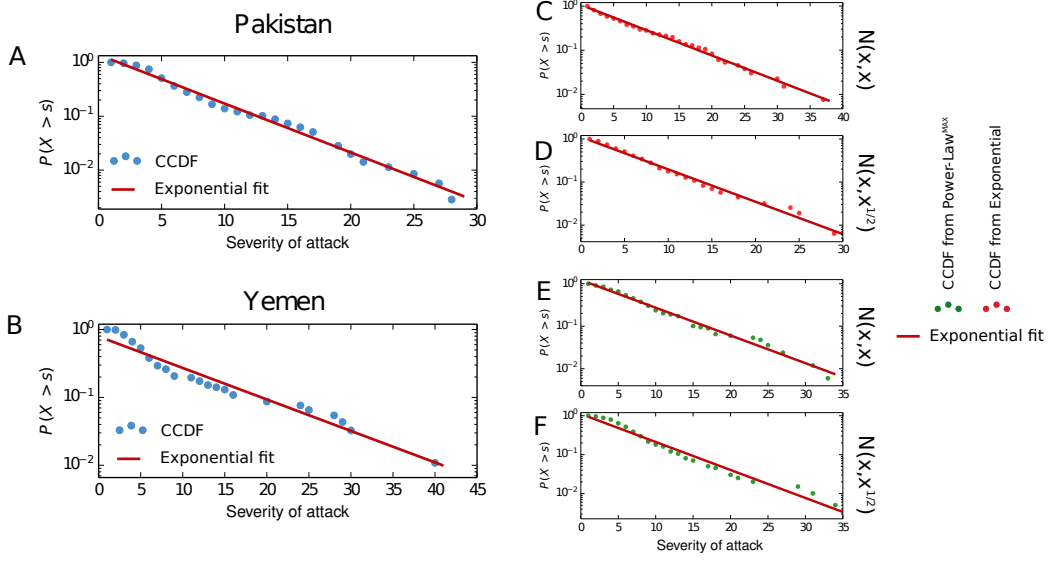


Figure 2: **The severity of drone attacks approximately follows an exponential distribution.** Complementary Cumulative Distribution Function (CCDF) of the severity of attacks (blue dots and solid line) and best fits to power-law (solid black) and exponential (solid red) distributions for drone attacks in Pakistan (A) and Yemen (B). The optimal parameters for each distribution are (A) $\lambda = -0.21$ (B) $\lambda = -0.11$. (C-F) CCDFs of the severity of attacks and best fits to exponential distributions. (C-D) The attack size is drawn from a normal distribution with μ and σ (σ^2 for D) corresponding to a random value from an exponential distribution ($\lambda = 5$). (E-F) The attack size is drawn from a normal distribution with μ and σ (σ for F) corresponding to the largest value in 100 random numbers drawn from a power-law ($\alpha = 4$). λ is measured from the slope of the least squared fit in semi-log scale and corresponds to (C) $\lambda = -0.13$, (D) $\lambda = -0.17$, (E) $\lambda = -0.15$, (F) $\lambda = -0.17$.

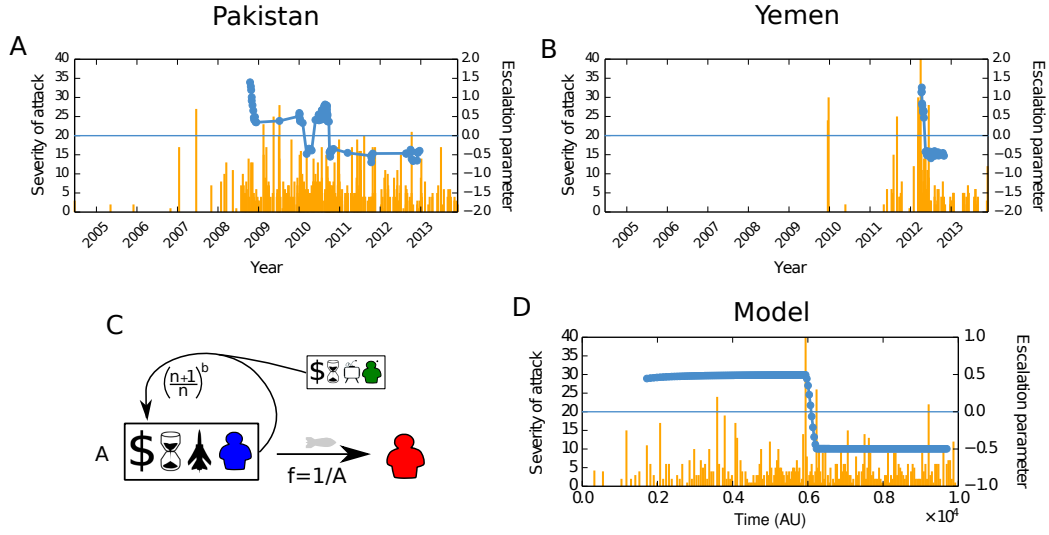


Figure 3: The timing between attacks reveals power-law relationships. (A-B) The severity of the attacks (vertical lines, left axis) and their escalation parameter b (right axis) are plotted for a moving window of 50 attacks in (A) Pakistan and (B) Yemen. (C) A simple model of the process. The Blue King's resources (funding, units, experience, etc.) influence the frequency of attacks. Resources are invested and create a positive feedback loop. The civilian population and other variables influence the strength of this positive feedback. The amount of resources available corresponds to A , the advantage of the Blue side. (D) Symmetric plot to (A-B) using data generated by the model. For the severity of attacks, the size was assumed to be drawn from the largest known group, where the group size is distributed as a power-law with $\alpha = 4$.

from an exponential distribution again yields an approximate lognormal distribution (Figs. 1D). The same pattern is recovered if the standard deviation is set to scale with the square root of the mean (Figs. 1E–F). We note that further reduction in the uncertainty of group size increases the weight of the underlying distribution: For the case where the largest known group is targeted, this can explain the fat tail observed for the Yemen data.

Although we have chosen to focus on fitting lognormal distributions as the alternative to power laws, other distributions can also provide good fits. For example, the data agrees well with an exponential distribution (see Fig. 2A–B). Scenarios where the size of the Red groups is exponentially distributed, as is the case if the probability of joining a group is constant and independent of the number of members, would naturally yield exponential distributions (Fig. 2C–D). Approximate exponential distributions can also be achieved if the groups are power-law distributed (Fig. 2E–F). Our purpose is not to identify the best alternative to a power-law distribution, but to show that in contrast with conventional warfare and terrorism, the data does not follow a power-law distribution and hence feedback processes are not present across all scales.

We now turn to the timing of attacks in order to gain insight into the temporal dynamics of the Blue King-versus-Red Queen activity. Following previous work [10], we plot the time interval between consecutive attacks τ_n as a function of the cardinal number of the attack $n = 1, 2, 3, \dots$. The escalation parameter b is the exponent of the power-law fit $\tau_n = \tau_1 n^{-b}$, which will be the slope of the best-fit line on a double logarithmic plot. In the organizational development literature in which subsequent events are related to production, this is referred to as a development curve while in the psychology literature, where subsequent events correspond to completing a certain task, it is referred to as a learning curve [11]. In this sense, the ‘production’ or ‘completion’ of drone attacks has a natural connection to human activity in these wider fields. For both Pakistan and Yemen, we find that the parameter b fails to stabilize around zero (Figs. 3A–B), which is the expected value in a steady state where both sides are adapting well to the opponent’s advances. Instead, the drone attacks exhibit a large initial escalation (i.e., large positive b) which then transitions to a de-escalation (i.e., large negative b). Given the difficulty for a Red Queen without air defenses to thwart drone attacks directly, Figs. 3A–B suggest that one side (Blue King) effectively holds complete control for an extended period of time, and that some internal constraints then arise within the Blue King entity that

eventually de-escalate drone attacks. This is consistent with the decrease in the escalation rate following the closure of a main drone base in 2011 [13]. Interestingly, there is some evidence of Red adaptation to Blue attacks in a recent report by “The Bureau of Investigative Journalism”, which shows a decrease in Red vehicle usage after 2011 corresponding to a peak in attacks on vehicles <http://wherethedronesstrike.com/report/76>. This suggests that the Red Queen may be able to limit the severity of attacks.

Fig. 3C shows our simple model for explaining these drone attack patterns. This model is of course over-simplified given the wealth of unknowns, yet we believe it is a plausible first step in explaining the empirical observations. We regard the Blue King as possessing certain resources, for example experience, units, and funding. These resources degrade over time if no investment is made in the Blue King’s activity, i.e. if the government does not invest in its own drone development or information research. We assume that if there exists investment (i.e., funding, time, etc.) then the available resources increase due to a positive feedback loop, according to the escalation observed $A \propto n^b$, where A corresponds to the advantage of the Blue King over the Red Queen. Similar feedback loops has been proposed in models of conventional terrorism [14], and can be affected by external agents, for example public opinion or budget changes. For simplicity we take the frequency of attacks as directly proportional to the resource level, while the severity of the attack is independent of resources.

These minimal features are able to replicate the drone strike data (Figs. 1C–F, Figs. 1D, is achieved if the resources increase as a power-law — hence this is only sustainable for short periods of time. A constant $b < 0$, corresponding to the frequency of attacks decreasing continuously, is achieved if the resources decrease continuously, i.e. when there is little or no investment. Assuming that each drone acts individually, that the attack severity varies slowly with the available resources (which is in turn consistent with some form of adaptation by the Red side) and that an increase in precision requires significant amounts of development effort, we are able to recreate approximate lognormal and exponential distributions for the severity of attacks.

In summary, our analysis reveals and helps explain patterns in the severity and timing of attacks in drone wars, which themselves represent a new form of action-at-a-distance human conflict. We have purposely stepped aside from issues of ethics or technology, choosing instead to focus on the event data since they represent a quantitative measure of drone war impact. We have shown that a simple model, in which the production of drones evolves from a

148 shared pool of resources controlled by a feedback loop, is able to recreate the
 149 original data and therefore explain the overall dynamics of the Blue King’s
 150 drone campaign. Going forward, our model could be also used to explore how
 151 wars might unfold when drones are used by two or more sides in conflicts.

152 **Methods**

153 We obtained all data from the New America database: <http://securitydata.newamerica.net/.newamerica.net/> and crosschecked with the South Asia
 154 Terrorism Portal database: <http://www.satp.org/satporgtp/countries/pakistan/>.

157 We obtained the best fit to power-law distributions following Clauset
 158 et al. [4]. We fitted lognormal distributions using the maximum likelihood
 159 estimators. For the escalation rate analysis, $\tau_n = \tau_1 n^{-b}$, we plotted the
 160 number of attack vs. the time between attacks on a log-log scale. We used a
 161 rolling window of 50 attacks and accepted every value of b that allowed for
 162 a correlation greater than 20%, which allows us to measure fast transitions.

163 We simulated 200 attacks with our model. The initial advantage was set
 164 to 1. The time to the next attack is equal to $323 \cdot A^{-1}$, where the 323 mimics
 165 t_0 for the Pakistan conflict. At every step (attack) the advantage of the Blue
 166 King changed by the factor $((n+1)/n)^b$, where n is the attack number. For
 167 the first 50 attacks $b = 0.5$; for the last 50 attacks $b = -0.5$.

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