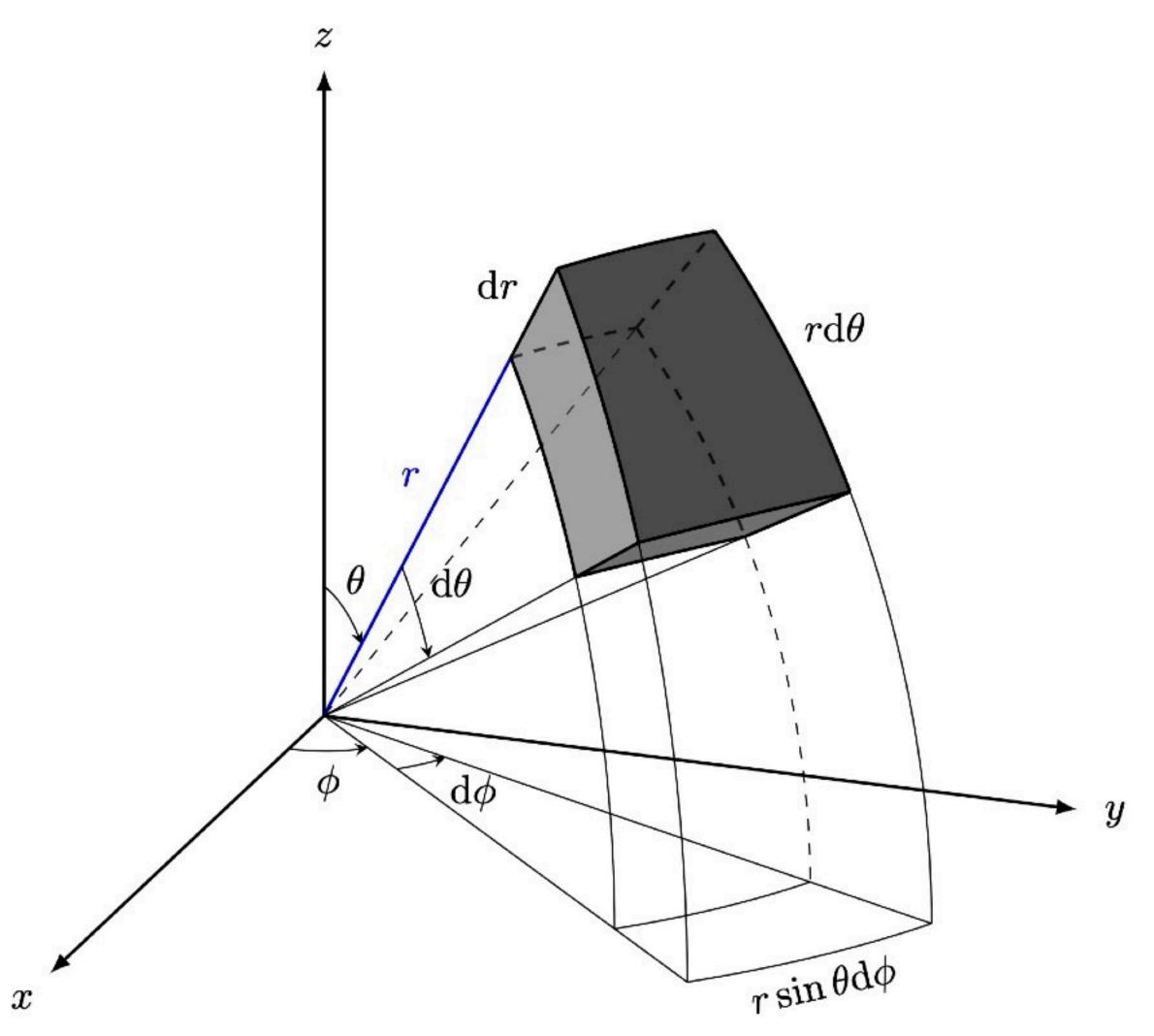
Spherical Coordinates

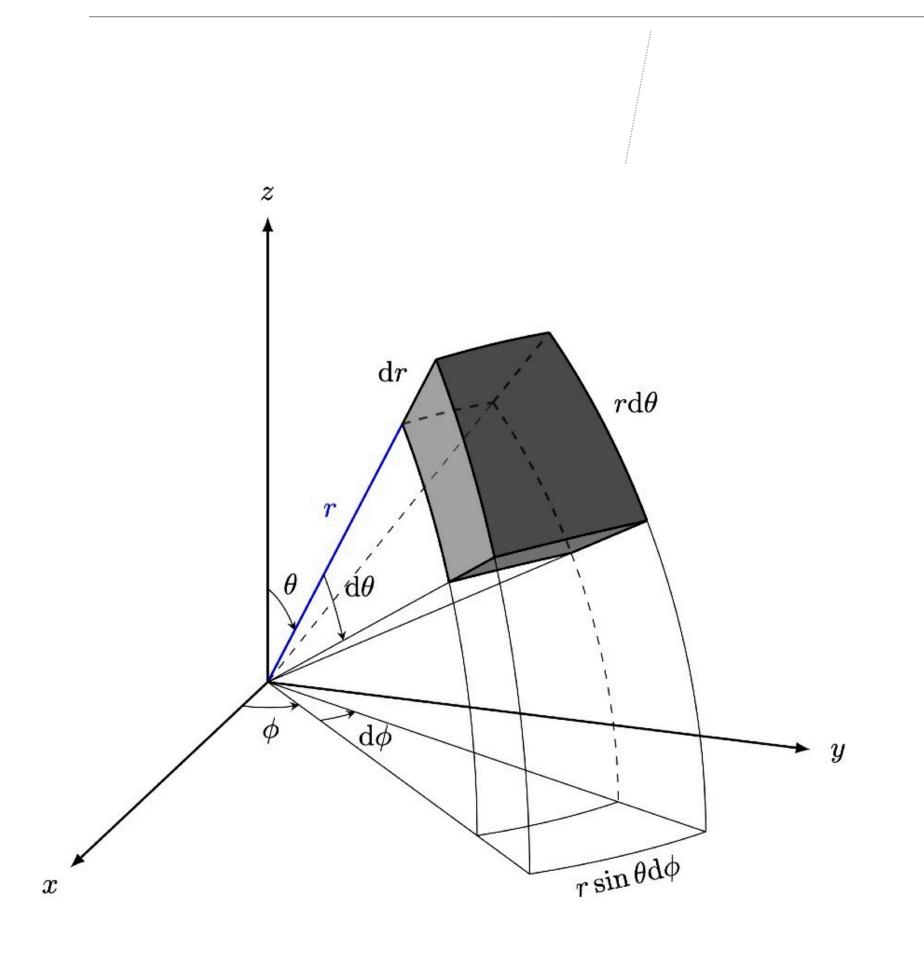


Volume and area elements

$$dV = dA dr = (rd\theta) (r \sin \theta d\phi) (dr)$$
$$= r^{2} \sin \theta dr d\theta d\phi$$

$$dA = (rd\theta)(r\sin\theta d\phi)$$
$$= r^2 \sin(\theta) d\theta d\phi$$

Jacobian Determinant



$$x = r \sin \theta \cos \phi$$
$$y = r \sin \theta \sin \phi$$
$$z = r \cos \theta$$

$$\begin{vmatrix} \frac{\partial x}{\partial r} & \frac{\partial x}{\partial \theta} & \frac{\partial x}{\partial \phi} \\ \frac{\partial y}{\partial r} & \frac{\partial y}{\partial \theta} & \frac{\partial y}{\partial \phi} \\ \frac{\partial z}{\partial r} & \frac{\partial z}{\partial \theta} & \frac{\partial z}{\partial \phi} \end{vmatrix} = \begin{vmatrix} \sin \theta \cos \phi & r \cos \theta \cos \phi & -r \sin \theta \sin \phi \\ \sin \theta \cos \phi & r \cos \theta \sin \phi & r \sin \theta \cos \phi \end{vmatrix} = r^2 \sin \theta$$