Irreversible Processes and Entropy

- · Irreversible processes are associated with an increase in entropy. We will illustrate this with examples
- First consider a completely ordered state of N
 harmonic oscillators shown in (a). By a sequence
 of random hops transferring energy from site to site
 (see previous lectures) the system ends up in slide (b).
 It is equally to be in any of its states. It
 will never hop back to the completely ordered state
 although this is allowed energetically. The transition
 is irreversible and associated with an increase
 in the total # of possible states AS univ > 0
 (see also previous lectures)
- Next consider a gas initially on the left side (see slide)

 a container. The microstates are labelled by

 the positions and momenta of all particles

 X, P, ... XN, PN. When the plug is removed

 the available volume to each particle is increased.

 The gas will rush and fill the container, increasing
 the entropy of the system. For instance initially

 each particle was in the Left state. Afterwards

 it is either in Left or Right state. The number of

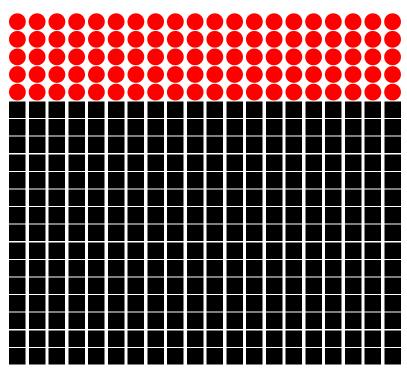
 states per particle has doubted and string state is LL.

 Left=L

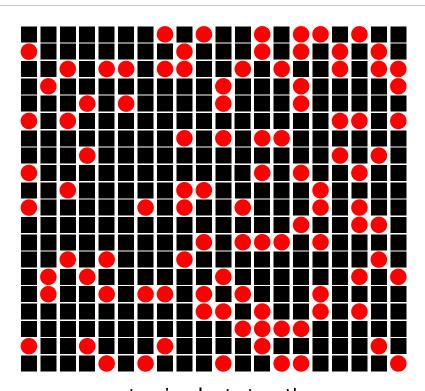
 (E.g. take two particles N=Z. The initial state is LL.

The possible final states are LL, LR, RL, RR: this is 4 times the number of initial states)

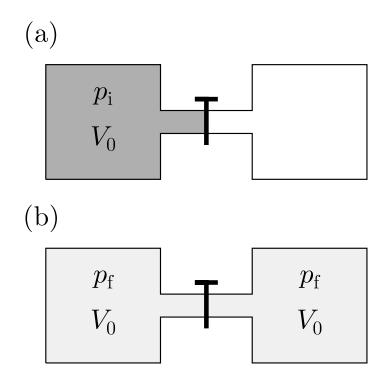
Ordered versus typical state: e^{225} states in total



Ordered state: 400 atoms, 1/4 are excited, $E=100\,\Delta$



a typical state: the energy is still, $E=100\,\Delta$



The expansion is a highly non-equilibrium process.

During the expansion no heat enters the system. Thus the energy initial equals the final energy

US = kBln Stinal - kBln Sinit = NkBln 2

We will derive this more formally later.

The particles will never go back to being on the left side (although it is not forbidden) since there a just way more configurations with the particles more equitably distributed.

· Summarizing all irreversible processes have

ASuniv > 0

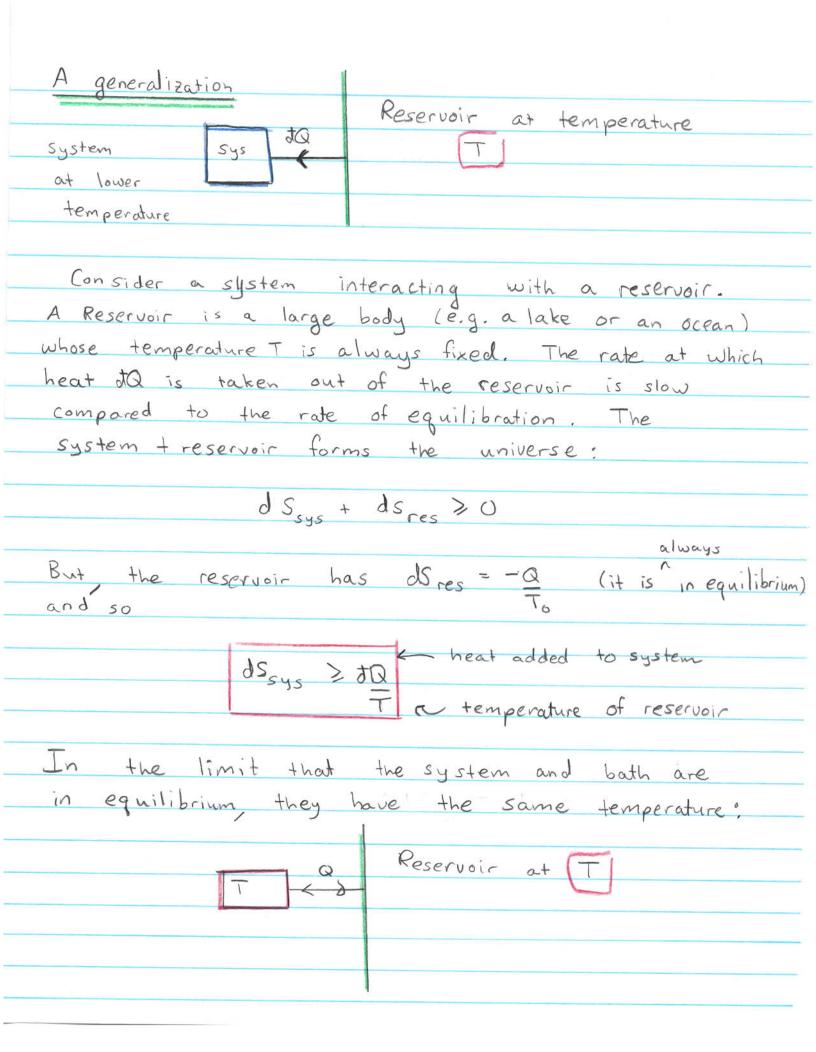
It is the weight of possibilities. There are of order 2 N more configurations with the gas completely filling the room, then with the gas on completely on the left. The gas explores these configurations for eternity, never returning to being only on the left.

When the system is fully equilibrated, S has increased as much as it can and

TR = 0

So in general:

DS univ > 0



Now heat can flow both ways (i.e. the heat transfer is reversible) without increasing the entropy of the universe

inequilibrium

flow both ways as opposed to an irreversible process where the heat flows one way 1570.

If there is more than one reservoir then we should generalize $\Delta S_{\text{sys}} \geq Q/T$. Say there are multiple reservoirs at temperature $T_1, T_2, \dots T_N$ with heat transfers to the system $Q_1, Q_2, \dots Q_N$. Then the appropriate generalization is

$$\Delta S_{\rm sys} \ge \frac{Q_1}{T_1} + \frac{Q_2}{T_2} \dots + \frac{Q_N}{T_N}$$

Sometimes this las expression is sometimes written

$$\Delta S_{\rm sys} \ge \int \frac{\mathrm{d}Q}{T}$$

But, I find the discrete case easier to interpret