Natoms connected by springs.

- · As a simple picture of ld solid, might
- consist of N oscillators. For simplicity take.

 each of the oscillators to be independent

 integer q>>>

 Then the total Energy is U = 9 two.

 q is the total number of quanta of
 energy to be shared or partitioned amongst

 the N atoms

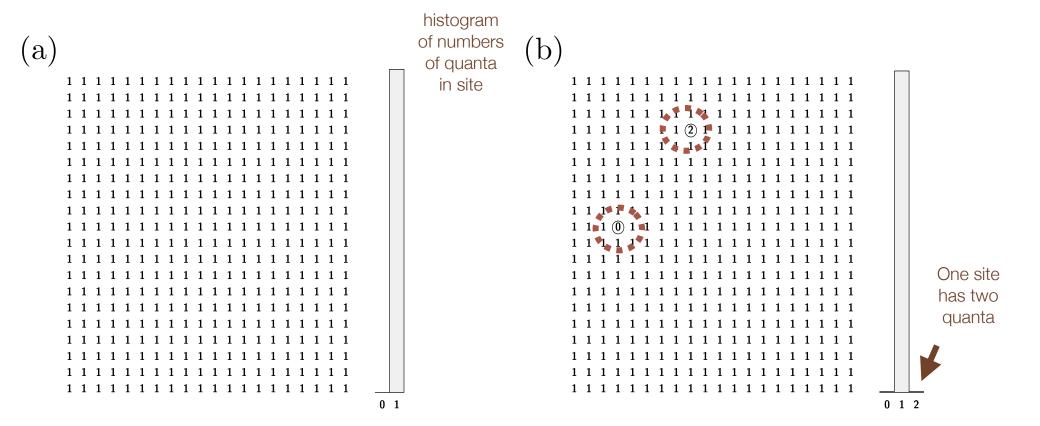
 For definiteness take 400 atoms and 400 quanta
 of energy. I quanta = I two.
 - - One possible configuration is that each atom has one quanta of energy:

This is shown on the slide below.

Now pick one oscillator at random and transfer one quanta' of energy to another randomly chosen site.

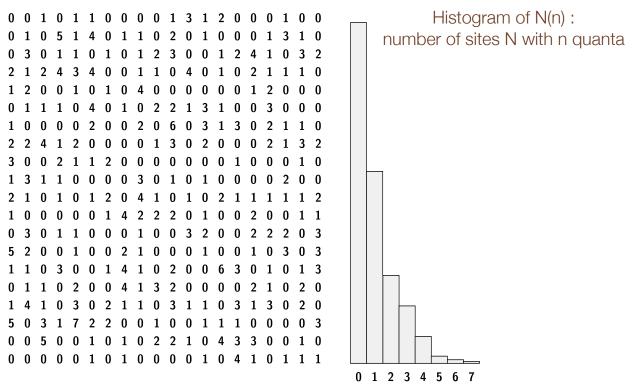
We get another possible state see slide:

20x20 oscillators (sites), with 20x20 quanta of energy, one per site

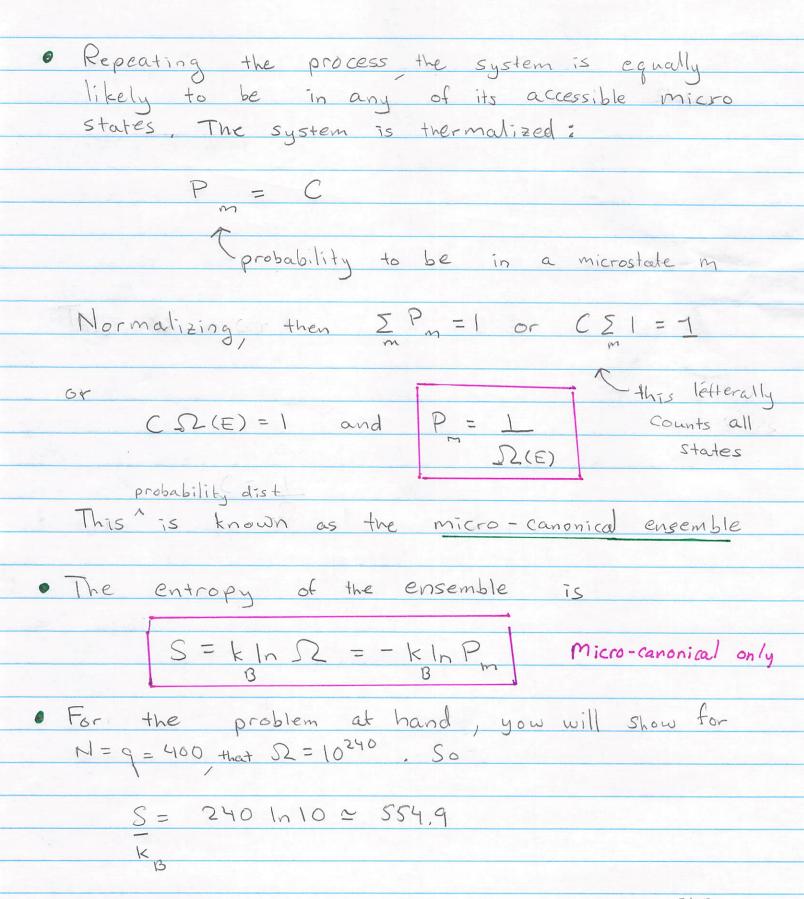


Start with initial state (a), pick two oscillators randomly, and transfer an energy quanta between the two sites. You find (b).

Now repeat the process: there are 10^{240} ways to share the energy (c)

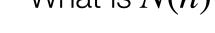


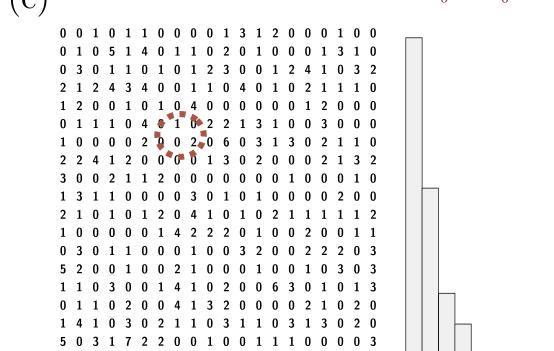
A typical distribution distribution is shown above: What is N(n)?



You will count the states and find $\Omega = 10^{240}$ in homework.

What is N(n)?





 $\begin{smallmatrix}0&0&5&0&0&1&0&1&0&2&2&1&0&4&3&3&0&0&1&0\\0&0&0&0&0&1&0&1&0&0&0&1&0&4&1&0&1&1&1\end{smallmatrix}$

Histogram of energies

in units of $\epsilon_0 = \hbar \omega_0$

0 1 2 3 4 5 6 7

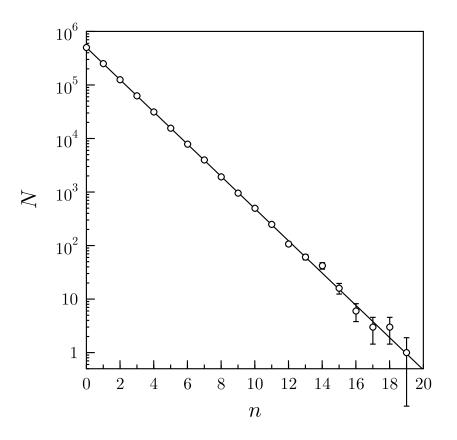
Pick a site: The remaining sites are the reservoir

Expect the probability for a site to have n quanta to be

$$P(\epsilon_n) \propto e^{-\beta \epsilon_n} = e^{-n\beta \epsilon_0}$$

The histogram N(n) is the number of sites with n quanta, and should be P_n up to normalization

Numerical verification: number of sites, N(n), with n quanta on 1000x1000 grid



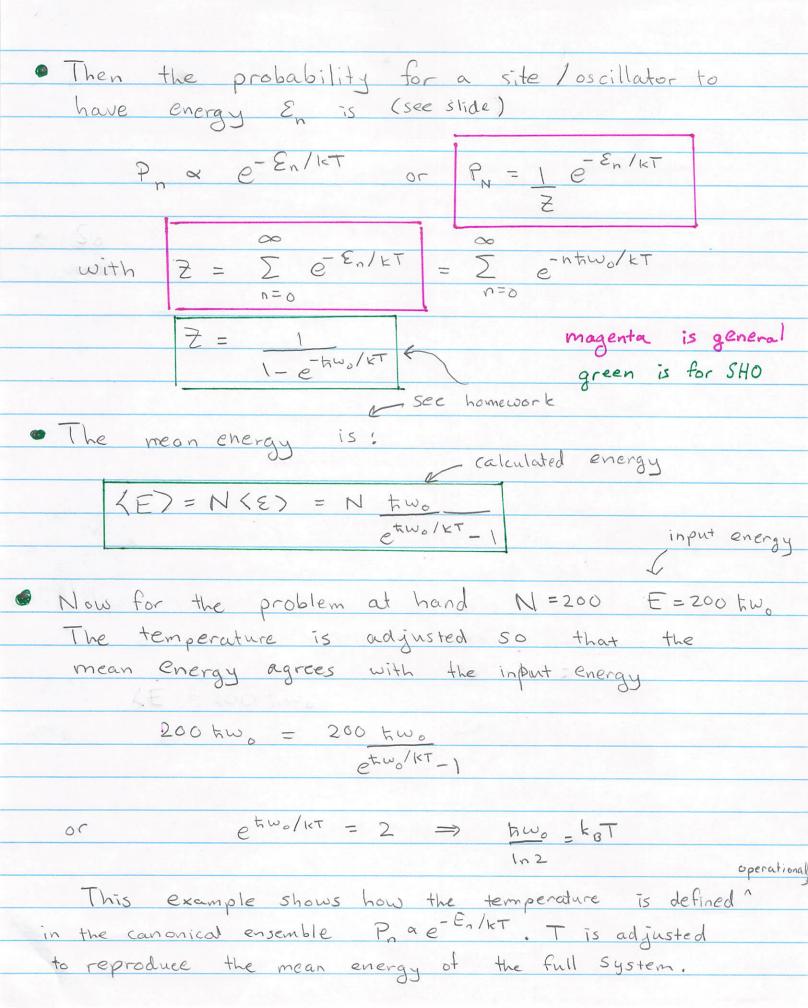
What you are seeing (on a log scale) is

$$N(n) = C_1 e^{-C_2 n}$$

The log of N(n) is

$$ln N(n) = ln C_1 - C_2 n$$

The constant $C_2 = \beta \epsilon_0$ determines the temperature



The Einstein model gives a successful phenomenology o at constant vol of solids dQ = dE + pdV So at constant volume dV = 0 $(\partial E) = dQ_v \leftarrow this$ is C_v $C_V = (\partial E) - N (\beta \hbar \omega)^2 \frac{e^{-\beta \hbar \omega_0}}{(1 - e^{-\beta \hbar \omega_0})^2}$ You will do this in homework. In fact you did it already! We did it here in 10. Specific Heat $C_{\gamma} = 3N (\beta h w_0)^2 e^{-\beta h w_0}$ $(1 - e^{-\beta h w_0})^2$ mode! of Einstein dimensions, each atom can oscillate in XyZ This is a one parameter model for the specific

heats of solids. two is adjusted to reproduce the

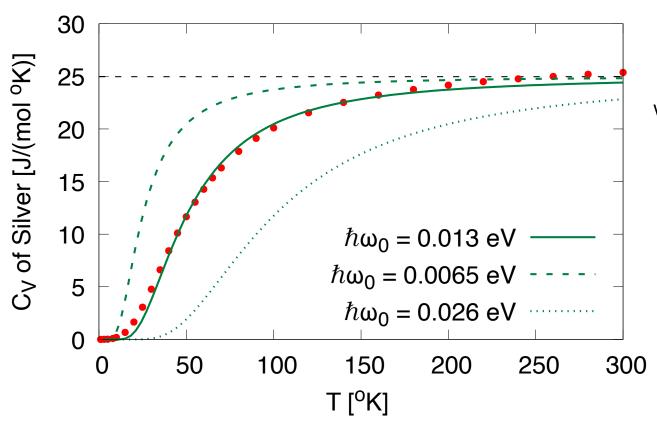
data

- The Specific Heat of silver is shown on the slide. It is reasonably fit by taking tw = 0.013eV
- In the high temperature limit find

Indeed at high temperatures the specific heats of solids approach 3R (see slide)

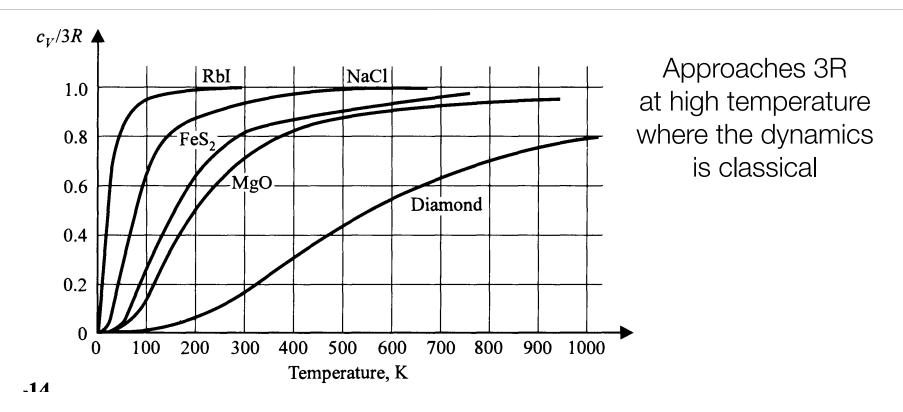
Classically one finds Cy=3R and that the result is independent of temperature. Betting the specific heat to drop with temperature was a great early success of quatium mechanics

Specific Heat of Silver



Approaches 3R at high temperature where the dynamics is classical

Specific Heats of Solids: (Taken from Zemansky and Dittman)



The general shape of these curves agrees with the Einstein Model!