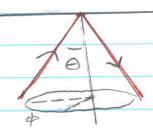
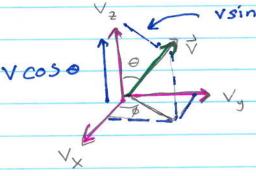
Pressure and Effusion



- Particles bounce of the walls with a variety of angles θ , ϕ a variety of speeds V each second. This gives a net force per area. We need the distribution of angles and speeds
- Then the velocity distribution is

$$dP = \left(\frac{m}{2\pi k_BT}\right)^{3/2} e^{-\frac{1}{2}mV^2/kT} dv_x dv_y dv_z$$

So we can change variables to speeds and angles $V = |\vec{V}| \quad V_{\pm} = V\cos\theta \quad V_{\pm} = V\sin\theta\cos\phi \quad \text{etc} \quad \text{like}$ before



sinodo do

$$d\mathcal{P} = \left(\frac{m}{2\pi k_{o}T}\right)^{3/2} e^{-\frac{1}{2}mV^{2}/kt} V^{2} dV dS^{2}$$

$$P(V) = \frac{m}{2\pi kT}$$

$$e^{-mv^{2}/2kT}$$

$$distribution of$$

$$speeds discussed$$

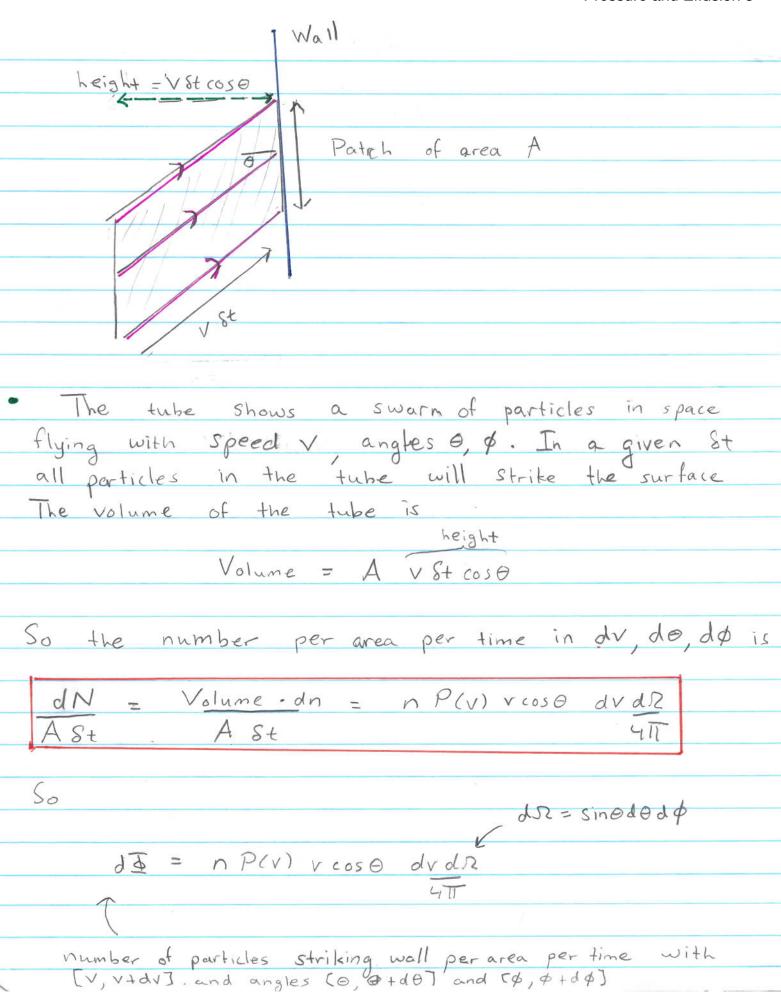
$$before.$$

This gives the distribution of speeds and angles. The angular part is uniformly distributed over the sphere do = sin 0 d0 dp / 41T, as: we could have hoped.

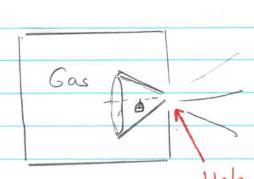
To find the density of particles with speed [v, dv] and angles [0,0+d0] [d, d+dq] we multiply by the adensity of the system N=N V

$$dn = n dP = n P(v) dv d\Omega$$

Now consider a small patch of area A on the wall. We want to work out the flux P of particles striking the surface per dv, do, dp







· For example a slow bicycle leak. This is gas escaping through A

Hole of area A

Find the total number escaping per area

$$\overline{\Phi} = \int d\overline{\Phi} = \int dv \int d\theta \int d\theta n P(v) v \cos\theta \sin\theta$$
from d)

· You will do the angular integrals in

homework

$$\overline{\phi} = \int_{0}^{\infty} dv \ v P(v) \int_{0}^{\pi/2} \cos \theta \ 1 \sin \theta \ d\theta \int_{0}^{2\pi} d\phi$$

14 from homework

$$\overline{\Phi} = I n \langle v \rangle$$

$$\overline{\Phi} = D \left(\frac{k_B T}{m}\right)^{\frac{1}{2}} \frac{1}{\sqrt{2\pi}}$$

$$\sqrt{2\pi}$$

$$\sqrt{2\pi}$$

$$\sqrt{2\pi}$$

$$\sqrt{2\pi}$$

$$\sqrt{2\pi}$$

$$\langle v \rangle = \left(\frac{8 k_B T}{T m} \right)^{1/2}$$

units: Number x m = number / Area time