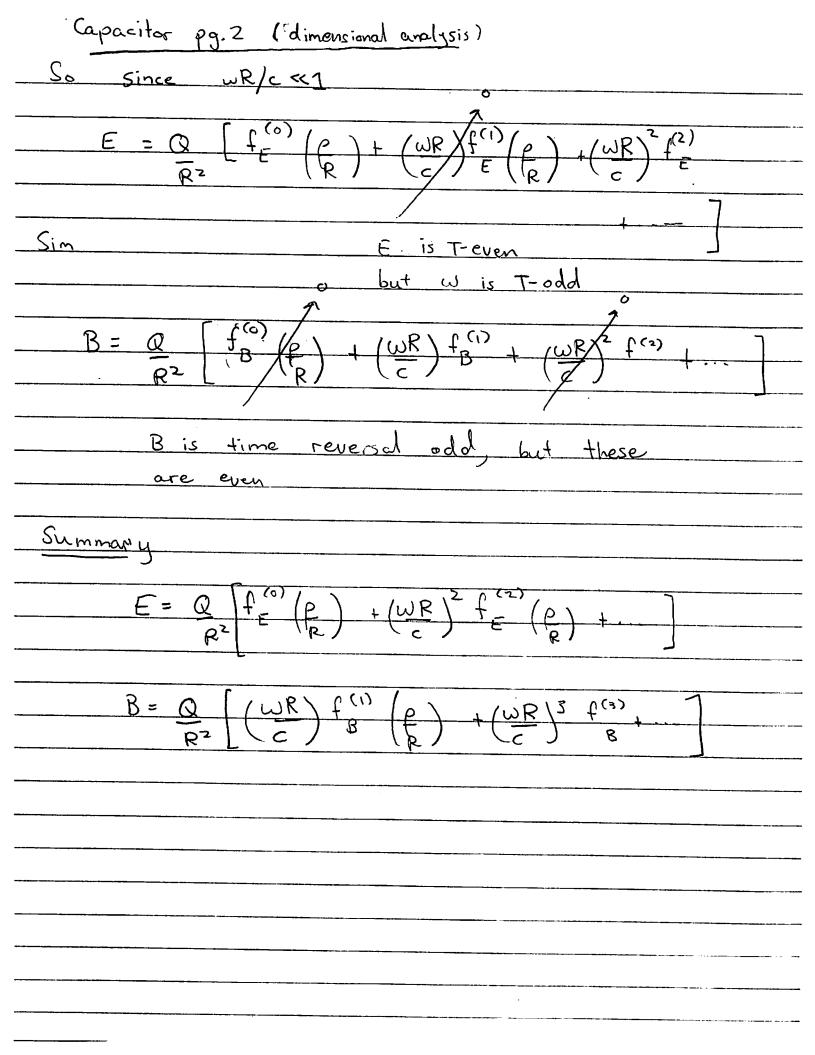
Last Time Talked about inductance VxH = jext/c + 12t5 $\nabla \cdot \mathcal{B} = \mathcal{O}$ -VxE=12R $\nabla \times E^{(o)} = 0$ Vx H(1) = jext/c + 1 2 D(0) 1st D.B., 0 - Vx E (2) = 1 2, B(1) 2nd So concluded H·SB =

Potentials Pg.1 Can also express in terms of potentials · VxB=j/c+1),Ē V.B=0 -0xE = 12+B So from B E = - 12 + A - PYfrom (9) from $\nabla \left(-1 \partial_t \vec{A} - \nabla \varphi \right) = \rho \implies \left(-\nabla^2 \varphi \right) \left(\nabla \cdot \vec{A} \right) = \rho$ $\left(\frac{1}{C^2}\frac{\partial^2}{\partial t^2} - \nabla^2\right)\Psi - \frac{1}{C}\frac{\partial}{\partial t}\left(\frac{+1}{2}Q + \nabla \cdot \vec{A}\right)$ - 12+ (12+ V.A) $= -\frac{1}{2} \frac{\partial}{\partial t^2} + \frac{\nabla^2}{2} = \frac{d'Alembertian}{dt}$

Capacitor pg. 1 (dimensional analysis) An important example Q=Q cos wt the dimension ful parameters: $Q, (d, z), (\rho, R) (\omega, c)$ What are the dimensionless parameters? $\frac{WR \ll 1}{C}$ and $\frac{d}{R} \stackrel{?}{R} \stackrel{?}{R} \stackrel{?}{R}$



Capacitor pg.3
Ok How do we solve;
$\frac{O+h}{\nabla \cdot E^{(\bullet)}} = 0$
$\nabla \times E^{(\circ)} = 0$
$11111 = 0. \cos \omega + 2$
TI R2
1st The PxB(1) = 13, E(0)
These tollow trom
2nd - Vx E(2) = 12 B(1) VxB = 1 2 E
C ,
-DXE=12B
1st Order
The displacement current = 2 E(c) sources B:
$\nabla_{x} B^{(1)} = \int a_{t} E^{(\alpha)}$
∫B·dl = 1∫2, E(°) aπρ dp
ar salve

E(0) = 00 cosmt

with

Capa	ecitor	pg.4

Solving this equation we find $\frac{B}{R^2} = -Q_0 \text{ sinut } \left(\frac{\omega P}{2c} \right) + \frac{C(P)}{R^2}$

In solving this equation we have discarded an irregular solution $\propto 1/p$. We see that $B_0^{(1)} \ll E_2^{(0)}$ since $wp/2c \ll 1$.

2nd Order

$$-\nabla x E^{(2)} = \int_{C} \partial_{t} \mathcal{B}_{0}^{(1)} \hat{\phi}$$

Using the expression $\nabla \times E = -\partial E^2/\partial \rho \hat{\rho}$ assuming that only E^2 is non-zero, we have

$$\frac{+\partial E_{2}^{(2)}}{\partial \rho} = \frac{1}{C} \frac{\partial_{b} B_{b}^{(17)}}{\partial \rho}$$

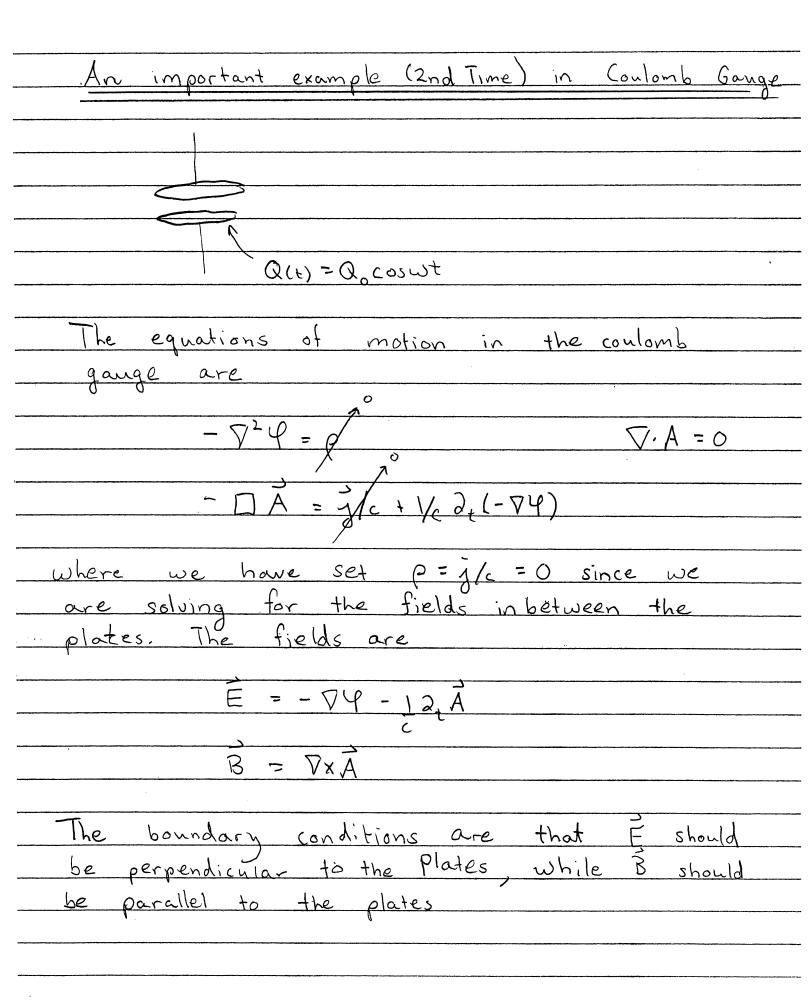
Integrating this expression we have

$$E^{(2)} = -Q_{o}\cos\omega t \qquad \omega^{2}\rho^{2} + Const(t)$$

$$\overline{\Pi}R^{2} \qquad \overline{\Pi}C^{2}$$

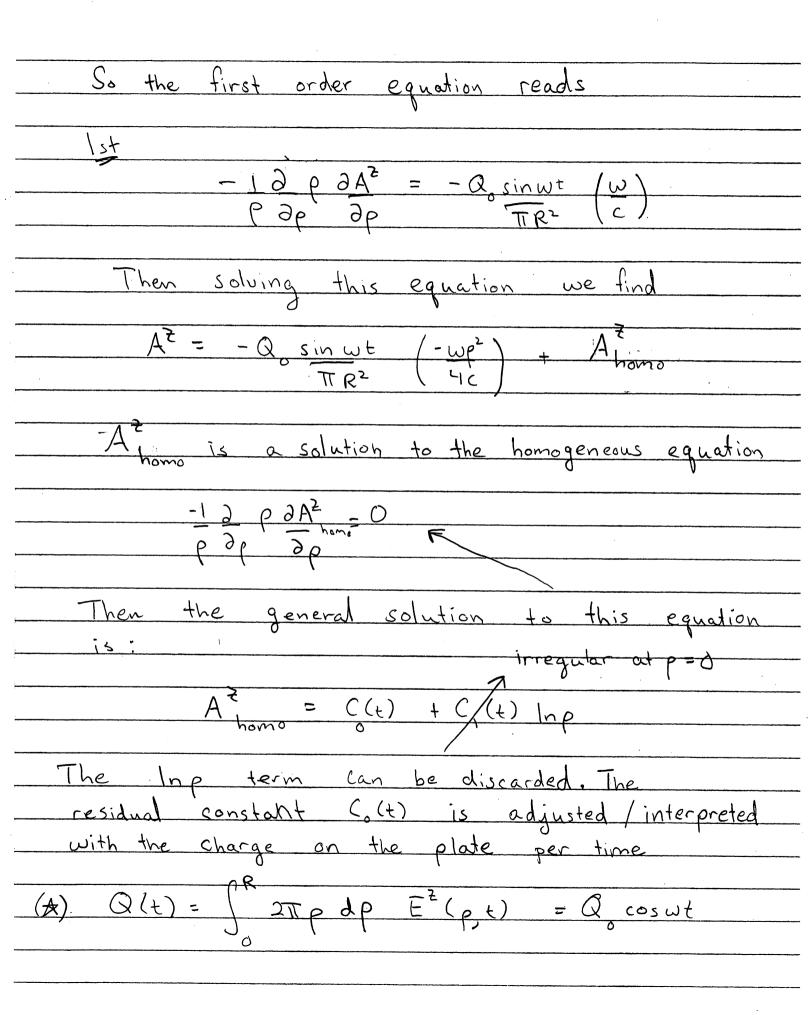
The constant is fixed by the fact that the total charge on the plate is Q coswt

Capacitor Pg.5
Integrating
$Q(t) = \left(2\pi\rho d\rho \sigma(\rho, t)\right)$
$\frac{\sqrt{2}}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} $
$Q_0 coswt = \begin{cases} 2\pi p dp \left[E_2^{(0)} + E_2^{(2)} + \right] \end{cases}$
COSWI - JAMP LEZ FEZ F.
0
2.2
We find that Const (t) is Q coswt wR2
TR2 8C2
1 hus
$E^{2}(t,p) = Q_{0}\cos\omega t \left[1 + \omega^{2}R^{2}(1 - 2p^{2}) +\right]$
TTR2 8c2 R2
By (tp) = - Q sinwt wp
$B_{\rho}(t,p) = -Q_{0} \sin \omega t \left[\frac{\omega p}{2c} \right]$
Notes:
. The second correction to E is of order
wiri/cz relative to Qo/TIRZ
The next correction to \vec{B} is $\sim (\omega R)^3 \vec{Q}_o$
$\frac{1}{C}$
$\frac{1}{2} = \frac{1}{2} = \frac{1}$
i.e it is $\sim (\omega R)^3$ smaller than Q_0/TR^2



Solving the Laplace Equation for 4 at zeroth
order
O+1/2 :
$\mathcal{L} = \mathcal{L}_{o}(t) + \mathcal{L}_{i}(t) \neq \hat{A} = 0$
The coefficient Co(t) (an be taken to be zero
and C(t) must be adjusted to so that the
and ((t) must be adjusted to so that the charge on the plate must be Q(t) = Q coswt
this fixes
Y = - Q coswt Z
$ \varphi = -Q_{o} \cos \omega t = Z $ $ \pi R^{2} $
Actually this is the solution for 4 to all
orders. We will now set up an approximation
scheme for A(tp)
Noting that the electric field must remain
I to the plate we must take A in the
7-direction. Thus we try
$A(t,p) = A(t,p) \hat{z}$
And note that the gange condition is satisfied
3 0
$\nabla \cdot A = 0$

Then	we approximate	
	$A = A^{(1)} + A^{(2)} + A^{(3)} + \dots$	
So u	e find from	
	$\frac{1}{2} \left(- \nabla^2 \right) \vec{A} = \frac{1}{2} \partial_{\xi} \left(- \nabla \Psi \right)$	
The s	ystems	
\st 	$-\nabla^2 \vec{A}^{(1)} = \frac{1}{2} \partial_{\xi} (-\nabla \Psi)$	
2 ml	$-\nabla^2 A^{(2)} = 0$	A(5) = 0
3 rd	$-\nabla^{2}A^{(3)} = -L \partial_{2}^{2}A^{(1)}$	
So		



This yields

$$E^{2}(t,p) = -\nabla \Psi - 1\partial_{1}A$$

$$= Q_{1} \cos \omega t - Q_{0} \cos \omega t \left(\omega^{2}\rho^{2}\right) + \frac{1}{C}O(t)$$

$$= \frac{1}{\pi}R^{2} - \frac{1}{\pi}R^{2} \left(\frac{\omega^{2}}{\pi}C^{2}\right) + \frac{1}{C}O(t)$$
So we find by demanding Eq. At is sortified

$$A^{2} = Q_{0} \sin \omega t \left(-\frac{\omega\rho^{2}}{\pi}C^{2} - \frac{\omega R^{2}}{8C}\right)$$
And thus we can compute E

$$B^{(1)} = \nabla x A^{(1)} \Rightarrow B_{0} = -\partial A^{2}$$

$$\Rightarrow B_{0} = -\partial A^{2}$$