Derek Hughes Assignment #5 Predict 410 – Sec 57

INTRODUCTION:

Here we are conducting an EDA analysis on a data set that has a dichotomous response variable. We will explore the data using EDA and try to estimate the single variable that will give us the highest probability to predict whether our response variable is positive or negative. Next, we will use the proc logistic procedure with the score selection method to determine which variable the procedure selects compared to the one we selected with our EDA. Next we will evaluate the goodness of fit metrics for a logistic regression to determine if the model does a good job determining the probability of the different response variables. Finally, we will explore the ROC curve with our model and then compare it to a model with an additional variable.

RESULTS:

Our EDA begins by looking at the categories in each categorical variable. We are looking at the frequency amounts of each category to determine which categories can be lumped into a base category. For example, in categorical variable A6, we can lump the category j and r into a base category because each has a very low frequency amount that's too low to use as a reasonable predictor. For the remaining categories (non-base categories) we create dummy variables for each category. Again, this is to provide us with more predictive and evaluative effectiveness when doing our EDA.

| A1 | Frequency | Percent | | Cumulative Percent |
|-----------|-----------|---------|-----|-----------------------|
| a | 203 | 31.09 | 203 | 31.09 |
| b | 450 | 68.91 | 653 | 100.00 |

| A4 | Frequency | Percent | | Cumulative Percent |
|-----------|-----------|---------|-----|-----------------------|
| 1 | 2 | 0.31 | 2 | 0.31 |
| u | 499 | 76.42 | 501 | 76.72 |
| y | 152 | 23.28 | 653 | 100.00 |

| A5 | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|----|-----------|---------|-------------------------|-----------------------|
| g | 499 | 76.42 | 499 | 76.42 |
| gg | 2 | 0.31 | 501 | 76.72 |
| p | 152 | 23.28 | 653 | 100.00 |

| | | _ | Cumulative | Cumulative |
|-----------|-----------|---------|------------|------------|
| A6 | Frequency | Percent | Frequency | Percent |
| aa | 52 | 7.96 | 52 | 7.96 |
| c | 133 | 20.37 | 185 | 28.33 |
| cc | 40 | 6.13 | 225 | 34.46 |
| d | 26 | 3.98 | 251 | 38.44 |
| e | 24 | 3.68 | 275 | 42.11 |
| ff | 50 | 7.66 | 325 | 49.77 |
| i | 55 | 8.42 | 380 | 58.19 |
| j | 10 | 1.53 | 390 | 59.72 |
| k | 48 | 7.35 | 438 | 67.08 |
| m | 38 | 5.82 | 476 | 72.89 |
| q | 75 | 11.49 | 551 | 84.38 |
| r | 3 | 0.46 | 554 | 84.84 |
| w | 63 | 9.65 | 617 | 94.49 |
| X | 36 | 5.51 | 653 | 100.00 |

| A 7 | E | D4 | Cumulative | |
|-----|-----------|---------|------------|---------|
| A7 | Frequency | Percent | Frequency | Percent |
| bb | 53 | 8.12 | 53 | 8.12 |
| dd | 6 | 0.92 | 59 | 9.04 |
| ff | 54 | 8.27 | 113 | 17.30 |
| h | 137 | 20.98 | 250 | 38.28 |
| j | 8 | 1.23 | 258 | 39.51 |
| n | 4 | 0.61 | 262 | 40.12 |
| 0 | 2 | 0.31 | 264 | 40.43 |
| v | 381 | 58.35 | 645 | 98.77 |
| Z | 8 | 1.23 | 653 | 100.00 |

| A9 | Frequency | Percent | | Cumulative Percent |
|----|-----------|---------|-----|-----------------------|
| f | 304 | 46.55 | 304 | 46.55 |
| t | 349 | 53.45 | 653 | 100.00 |

| A10 | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|-----|-----------|---------|-------------------------|-----------------------|
| f | 366 | 56.05 | 366 | 56.05 |
| t | 287 | 43.95 | 653 | 100.00 |

| A12 | Frequency | Percent | | Cumulative Percent |
|-----|-----------|---------|-----|-----------------------|
| f | 351 | 53.75 | 351 | 53.75 |
| t | 302 | 46.25 | 653 | 100.00 |

| A13 | Frequency | Percent | | Cumulative Percent |
|-----|-----------|---------|-----|-----------------------|
| g | 598 | 91.58 | 598 | 91.58 |
| p | 2 | 0.31 | 600 | 91.88 |
| s | 53 | 8.12 | 653 | 100.00 |

| A16 | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|-----|-----------|---------|-------------------------|-----------------------|
| + | 296 | 45.33 | 296 | 45.33 |
| - | 357 | 54.67 | 653 | 100.00 |

Below we have the PROC MEANS summary statistics for the continuous variables. We use this table to determine effective "cut off" points to divide up the values of each continuous variable into discrete values that represent a range of values. This allows us to analyze the results more effectively. Generally we try to divide the values up into quantiles but the goal is to produce discrete ranges of values that can predict the binary response variable categories with a high degree of probability. This means that we want each discrete category to have a mean either close to 0 or close to 1, as a probability closer to 1 means that particular category has a stronger chance of making a correct prediction that the response variable will be 1 and vice versa if the value is close to 0. We want to avoid discrete categories with means close to .5, as that indicates it doesn't have any more predictive power than the probability of guessing between two numbers. Through trial and error, we try different "cut off" points within each continuous variable to create discrete categories that have more predictive power (away from a mean of .5), although sometimes an effective "cut off" point isn't possible with some variables (which indicates they should not be used in our predictive model).

| | N | | | | | | | | |
|---|-----|----------|------------|------------|-------------|-------------|-------------|-------------|-------------|
| Y | Obs | Variable | 5th Pctl | 10th Pctl | 25th Pctl | 50th Pctl | 75th Pctl | 90th Pctl | 95th Pctl |
| 0 | 357 | A2 | 17.0800000 | 18.4200000 | 21.9200000 | 26.9200000 | 34.8300000 | 44.2500000 | 51.9200000 |
| | | A3 | 0.1700000 | 0.3750000 | 0.8350000 | 2.2100000 | 5.0000000 | 11.0000000 | 12.7500000 |
| | | A8 | 0 | 0 | 0.1250000 | 0.4550000 | 1.5000000 | 3.3350000 | 5.0000000 |
| | | A11 | 0 | 0 | 0 | 0 | 0 | 2.0000000 | 3.0000000 |
| | | A14 | 0 | 0 | 100.0000000 | 160.0000000 | 260.0000000 | 360.0000000 | 454.0000000 |
| | | A15 | 0 | 0 | 0 | 1.0000000 | 67.0000000 | 400.0000000 | 1000.00 |
| 1 | 296 | A2 | 18.8300000 | 20.4200000 | 23.2500000 | 31.0400000 | 41.4600000 | 52.8300000 | 58.4200000 |
| | | A3 | 0.2050000 | 0.4600000 | 1.5000000 | 4.4800000 | 9.5825000 | 13.0000000 | 16.0000000 |
| | | A8 | 0.0400000 | 0.0850000 | 0.7500000 | 2.0000000 | 5.0000000 | 8.5000000 | 13.8750000 |
| | | A11 | 0 | 0 | 0 | 3.0000000 | 7.0000000 | 12.0000000 | 14.0000000 |
| | | A14 | 0 | 0 | 0 | 120.0000000 | 280.0000000 | 400.0000000 | 480.0000000 |
| | | A15 | 0 | 0 | 0 | 210.5000000 | 1223.00 | 4159.00 | 8000.00 |

The following tables show the means of the categories we created of each continuous variable using the cut off points we selected for each variable. Here I created at least four categories within each continuous variable. Hence, we changed each continuous variable into a discrete variable with four categories that represent the continuous range of values for that particular continuous variable.

| A 3 | E 7 • | 11 37 |
|-------------------------------|--|--|
| Analysis | | ble : Y |
| A2 discrete | N Obs | Mean |
| | | |
| 1 | 83 | 0.2891566 |
| 2 | 275 | 0.4290909 |
| 3 | 158 | 0.4303797 |
| 4 | 137 | 0.6277372 |
| Analysis | Varia | ble : Y |
| 42 11 | N | 24 |
| A3_discrete | Obs | Mean |
| 1 | 154 | 0.3766234 |
| 2 | 224 | 0.3392857 |
| 3 | 117 | 0.5470085 |
| 4 | 158 | 0.6202532 |
| Analysis | Varia | ble : Y |
| | N | |
| A8 discrete | Obs | Mean |
| 110_41501 000 | Obs | |
| 1 | 308 | 0.2662338 |
| 1 2 | | 0.2662338 0.5422222 |
| 1 | 308 | 0.2662338 |
| 1 2 | 308 225 | 0.2662338 0.5422222 |
| 1 2 3 | 308 225 79 41 | 0.2662338 0.5422222 0.7468354 0.8048780 |
| 1 2 3 4 Analysis | 308 225 79 41 Varia | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y |
| 1 2 3 4 | 308 225 79 41 Varia | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y |
| 1 2 3 4 Analysis | 308 225 79 41 Varia | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y |
| 1 2 3 4 Analysis A11_discrete | 308 225 79 41 Varia N Obs | 0.2662338 0.5422222 0.7468354 0.8048780 hble : Y Mean 5 0.2896552 |
| 1 2 3 4 Analysis A11_discrete | 308 225 79 41 Varia N Obs 1 43: | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y Mean 5 0.2896552 4 0.5833333 |
| 1 2 3 4 Analysis A11_discrete | 308 225 79 41 Varia N Obs 1 433 2 84 | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y Mean 5 0.2896552 4 0.5833333 5 0.9200000 |
| 1 2 3 4 Analysis A11_discrete | 308 225 79 41 Varia N Obs 1 433 2 84 3 73 4 59 | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y Mean 5 0.2896552 4 0.5833333 5 0.9200000 9 0.8813559 |
| 1 2 3 4 Analysis A11_discrete | 308 225 79 41 Varia N Obs 1 433 2 84 3 73 4 59 | 0.2662338 0.5422222 0.7468354 0.8048780 able : Y Mean 5 0.2896552 4 0.5833333 5 0.9200000 9 0.8813559 able : Y |
| 1 2 3 4 Analysis A11_discrete | 308 225 79 41 Varia N Obs 1 433 2 84 3 73 4 59 Varia | 0.2662338 0.5422222 0.7468354 0.8048780 hble : Y Mean 5 0.2896552 4 0.5833333 5 0.9200000 9 0.8813559 hble : Y |

0.2748092

0.3800000

104 0.5384615

131

100

3

4

| Analysis Variable : Y | | | |
|-----------------------|----------|-----------|--|
| A15 discrete | N Obs | Mean | |
| <u>1</u> | 302 | 0.3642384 | |
| 2 | 156 | 0.2628205 | |
| 3 | 98 | 0.6530612 | |
| 4 | 97 | 0.8350515 | |

The following frequency tables can be used to evaluate our cut off points for the continuous variables and how those cut off points change the percentage of categorical values associated with the respective response variable categories.

| Table of Y by A11_discrete | | | | | |
|--|--------------------------------|--------------------------------|-------------------------------|-------------------------------|---------------|
| Y | A11_discrete | | | | |
| Frequency Percent Row Pct | | | | | |
| Col Pct | 1 | 2 | 3 | 4 | Total |
| 0 | 309 47.32 | 35 5.36 | 6 0.92 | 7 1.07 | 357 54.67 |
| | 86.55 71.03 | 9.80 41.67 | 1.68 8.00 | 1.96 11.86 | |
| 1 | 126 19.30 42.57 28.97 | 49 7.50 16.55 58.33 | 69 10.57 23.31 92.00 | 52 7.96 17.57 88.14 | 296 45.33 |
| Total | 435 66.62 | 84 12.86 | 75 11.49 | 59 9.04 | 653 100.00 |
| Tak | ole of Y | by A | 15_dis | crete | |
| Y | | A1 | 5_disc | rete | |
| Frequency Percent Row Pct Col Pct | 1 | 2 | 3 | 4 | Total |
| 0 | 192 29.40 53.78 63.58 | 115 17.61 32.21 73.72 | 34 5.21 9.52 34.69 | 16 2.45 4.48 16.49 | 357 54.67 |
| 1 | 110 16.85 37.16 36.42 | 41 6.28 13.85 26.28 | 64 9.80 21.62 65.31 | 81 12.40 27.36 83.51 | 296 45.33 |
| Total | 302 46.25 | 156 23.89 | 98 15.01 | 97 14.85 | 653 100.00 |

We can also use PROC MEANS to evaluate the means of all of our discrete and categorical variables. The mean values found here are similar to those found on the frequency tables we created above. In particular, the mean values for each category are the equivalent to the percent of observations that are found when the response variable is 1. For example, for A15_discrete in the frequency table the percentage of category 1 observations that were also Y = 1 was 36.42%. In the PROC MEANS table for A15_discrete, for category 1 the means is .3642, which says that 36.42% of the time when the category is 1 for A15_discrete that the response variable is 1.

Below we have the means for each dummy variable. We are looking for a variable that shows a large difference in means for each response category. Also, we want these means to be either very close to 0 or 1 but opposing each other. For example, A9_t shows that it predicts a response of 1 almost 80% of the time and a response of 0 almost 95% of the time. Thus, it would be a reliable predictor of the response variable Y.

| Analysis Variable : Y | | |
|------------------------------|-----|-----------|
| N | | |
| A1_b | Obs | Mean |
| 0 | 203 | 0.4679803 |
| 1 | 450 | 0.4466667 |

Analysis Variable: Y

| N | | |
|------|-----|-----------|
| A4_u | Obs | Mean |
| 0 | 154 | 0.3051948 |
| 1 | 499 | 0.4989980 |

Analysis Variable : Y

| | N | |
|------|-----|-----------|
| A5_g | Obs | Mean |
| 0 | 154 | 0.3051948 |
| 1 | 499 | 0.4989980 |

Analysis Variable : Y

| | N | |
|-------|-----|-----------|
| A6_aa | Obs | Mean |
| 0 | 601 | 0.4608985 |
| 1 | 52 | 0.3653846 |

Analysis Variable : Y

| N | | |
|-------------|-----|-----------|
| A6_c | Obs | Mean |
| 0 | 520 | 0.4538462 |
| 1 | 133 | 0.4511278 |

Analysis Variable : Y

| A6_cc | N Obs | Mean |
|-------|----------|-----------|
| 0 | 613 | 0.4355628 |
| 1 | 40 | 0.7250000 |

Analysis Variable : Y

| | N | |
|-------|-----|-----------|
| A6_ff | Obs | Mean |
| 0 | 603 | 0.4792703 |
| 1 | 50 | 0.1400000 |

Analysis Variable :

| A6_i | N Obs | Mean |
|------|----------|-----------|
| 0 | 598 | 0.4715719 |
| 1 | 55 | 0.2545455 |

Analysis Variable: Y

| A6 k | N Obs | Mean |
|------|----------|-----------|
| 0 | 605 | 0.4677686 |
| 1 | 48 | 0.2708333 |

Analysis Variable : Y

| | N Obs | A6_m |
|-----------|----------|------|
| 0.4552846 | 615 | 0 |
| 0.4210526 | 38 | 1 |

Analysis Variable : Y

| | N | |
|-------------|-----|-----------|
| A6_q | Obs | Mean |
| 0 | 578 | 0.4273356 |
| 1 | 75 | 0.6533333 |

Analysis Variable : Y

| | N | |
|-------------|-----|-----------|
| A6_w | Obs | Mean |
| 0 | 590 | 0.4457627 |
| 1 | 63 | 0.5238095 |

Analysis Variable : Y

| | N | |
|-------------|-----|-----------|
| A6_x | Obs | Mean |
| 0 | 617 | 0.4311183 |
| 1 | 36 | 0.8333333 |

Analysis Variable : Y

| | N | |
|-------|-----|-----------|
| A7_bb | Obs | Mean |
| 0 | 600 | 0.4533333 |
| 1 | 53 | 0.4528302 |

Analysis Variable : Y

| | N | |
|-------|-----|------|
| A7_ff | Obs | Mean |

| Analysis Variable : Y | | |
|-----------------------|-----|-----------|
| | N | |
| A1_b | Obs | Mean |
| 0 | 599 | 0.4808013 |
| 1 | 54 | 0.1481481 |

Analysis Variable : Y

| | N | |
|------|-----|-----------|
| A7_h | Obs | Mean |
| 0 | 516 | 0.4050388 |
| 1 | 137 | 0.6350365 |

Analysis Variable : Y

| | N | |
|------|-----|-----------|
| A7_v | Obs | Mean |
| 0 | 272 | 0.4889706 |
| 1 | 381 | 0.4278215 |

Analysis Variable: Y

| | N | |
|------|-----|-----------|
| A9_t | Obs | Mean |
| 0 | 304 | 0.0592105 |
| 1 | 349 | 0.7965616 |

Analysis Variable : Y

| A10_f | N Obs | Mean |
|-------|----------|-----------|
| 0 | 287 | 0.7073171 |
| 1 | 366 | 0.2540984 |

Analysis Variable : Y

| A12_f | N Obs | Mean |
|-------|----------|-----------|
| 0 | 302 | 0.4801325 |
| 1 | 351 | 0.4301994 |

| Analysis Variable : Y | | | |
|-----------------------|-----------------------|-----------|--|
| | N | | |
| A13_g | Obs | Mean | |
| 0 | 55 | 0.2909091 | |
| 1 | 598 | 0.4682274 | |
| Analys | Analysis Variable : Y | | |
| | N | | |
| A13_s | Obs | Mean | |
| 0 | 600 | 0.4683333 | |
| 1 | 53 | 0.2830189 | |

From our EDA I've concluded that A11_discrete and A15_discrete were the best continuous variables to predict the correct response value. I concluded that A9_t was the best dummy_variable created from the categorical variables. Overall I felt A9_t was the best for predicting the correct response variable value. I selected each of these variables based on the relatively high mean values each variable had in regard to the response variable value of 1 or the low mean value when the response variable value is 0.

----- PART 2 -----

I selected A9_t for the best predictor variable for the response variable values. I fit the model and the results are shown below.

| Model Information | | | |
|---------------------------|------------------|--|--|
| Data Set | WORK.TEMPFILE | | |
| Response Variable | Y | | |
| Number of Response Levels | 2 | | |
| Model | binary logit | | |
| Optimization Technique | Fisher's scoring | | |

| Number of Observations Read | 653 |
|------------------------------------|-----|
| Number of Observations Used | 653 |

| Response Profile | | |
|------------------|---|-----------|
| Ordered Tota | | |
| Value | Y | Frequency |
| 1 | 1 | 296 |
| 2 | 0 | 357 |

Probability modeled is Y=1.

Model Convergence Status

| Model Fit Statistics | | | |
|-----------------------------|--------------|------------|--|
| | Intercept ar | | |
| Criterion | Only | Covariates | |
| AIC | 901.544 | 493.254 | |
| SC | 906.025 | 502.218 | |
| -2 Log L | 899.544 | 489.254 | |

| Testing Global Null Hypothesis: BETA=0 | | | |
|--|----------|---|--------|
| Test Chi-Square DF Pr > ChiS | | | |
| Likelihood Ratio | 410.2891 | 1 | <.0001 |
| Score | 356.4519 | 1 | <.0001 |
| Wald | 222.3474 | 1 | <.0001 |

| Analysis of Maximum Likelihood Estimates | | | | | |
|--|----|---------------|--------|------------|------------|
| | | Standard Wald | | | |
| Parameter | DF | Estimate | Error | Chi-Square | Pr > ChiSq |
| Intercept | 1 | -2.7656 | 0.2430 | 129.5239 | <.0001 |
| A9_t | 1 | 4.1306 | 0.2770 | 222.3474 | <.0001 |

| Odds Ratio Estimates | | | |
|----------------------|------------------------------------|--------|-----------|
| | Point 95% Wald | | |
| Effect | fect Estimate Confidence Limit | | ce Limits |
| A9_t | 62.213 | 36.148 | 107.071 |

| Association of Predicted Probabilities and Observed Responses | | | | |
|--|--------|-------|-------|--|
| Percent Concordant75.2Somers' D0.74 | | | | |
| Percent Discordant | 1.2 | Gamma | 0.968 | |
| Percent Tied | 23.6 | Tau-a | 0.367 | |
| Pairs | 105672 | c | 0.870 | |

Now, I used the selection "score" procedure to select the best variable. By looking for the variable with the highest chisquares values, we can determine the best single variable for this model using the score selection procedure.

| Model Information | | | |
|---------------------------|------------------|--|--|
| Data Set | WORK.TEMPFILE | | |
| Response Variable | Y | | |
| Number of Response Levels | 2 | | |
| Model | binary logit | | |
| Optimization Technique | Fisher's scoring | | |

| Number of Observations Read | 653 |
|-----------------------------|-----|
| Number of Observations Used | 653 |

| Response Profile | | |
|------------------|---|-----------|
| Ordered | | Total |
| Value | Y | Frequency |
| 1 | 1 | 296 |
| 2 | 0 | 357 |

Probability modeled is Y=1.

Note: The following variables are not used in the SCORE selection since they are a linear combination of other variables as shown.

$$\mathbf{A5}_{\mathbf{g}} = \mathbf{A4}_{\mathbf{u}}$$

As we can see from the Chi-square score, similar to what we selected from our EDA, A9_t is also selected by the score procedure as the best individual variable for this regression model. When a dummy variable is dropped from the model, it is simply included in the base category from that point forward.

| Regress | Regression Models Selected by Score Criterion | | |
|------------------------|---|-----------------------------|--|
| Number of Variables | Score Chi-Square | Variables Included in Model | |
| 1 | 356.4519 | A9_t | |
| 1 | 133.3312 | A10_f | |
| 1 | 107.6653 | A11 | |
| 1 | 72.2924 | A8 | |
| 1 | 28.0037 | A3 | |
| 1 | 23.1084 | A7_h | |
| 1 | 22.2053 | A6_x | |
| 1 | 22.1186 | A7_ff | |
| 1 | 21.4453 | A6_ff | |
| 1 | 21.2165 | A2 | |
| 1 | 19.4908 | A15 | |
| 1 | 17.8360 | A4_u | |
| 1 | 13.6820 | A6_q | |
| 1 | 12.6935 | A6_cc | |
| 1 | 9.5729 | A6_i | |
| 1 | 6.9598 | A6_k | |
| 1 | 6.7484 | A13_s | |
| 1 | 6.3903 | A13_g | |
| 1 | 4.7420 | A14 | |
| 1 | 2.3946 | A7_v | |
| 1 | 1.7618 | A6_aa | |
| 1 | 1.6332 | A12_f | |
| 1 | 1.3991 | A6_w | |
| 1 | 0.2564 | A1_b | |
| 1 | 0.1692 | A6_m | |

| Regression Models Selected by Score Criterion | | | |
|---|--------|-----------------------------|--|
| Number of Score Variables Chi-Square | | Variables Included in Model | |
| 1 | 0.0032 | A6_c | |
| 1 | 0.0000 | A7_bb | |

| Model Information | | | |
|----------------------------------|------------------|--|--|
| Data Set | WORK.TEMPFILE | | |
| Response Variable | Y | | |
| Number of Response Levels | 2 | | |
| Model | binary logit | | |
| Optimization Technique | Fisher's scoring | | |

| Number of Observations Read | |
|------------------------------------|-----|
| Number of Observations Used | 653 |

| Response Profile | | | |
|------------------|---|-----------------|--|
| Ordered Value | Y | Total Frequency | |
| 1 | 1 | 296 | |
| 2 | 0 | 357 | |

Probability modeled is Y=1.

Model Convergence Status

| Model Fit Statistics | | | |
|----------------------|-------------------|-------------------|--|
| | | Intercept | |
| Criterion | Intercept Only | and Covariates | |
| AIC | 901.544 | 493.254 | |
| SC | 906.025 | 502.218 | |
| -2 Log L | 899.544 | 489.254 | |

The model fit statistics can be used to assess how well the model fits. In this case we are looking for the lowest value of the three, which is -2LogL.

| Testing Global Null Hypothesis: BETA=0 | | | |
|--|------------|----|------------|
| Test | Chi-Square | DF | Pr > ChiSq |
| Likelihood Ratio | 410.2891 | 1 | <.0001 |
| Score | 356.4519 | 1 | <.0001 |
| Wald | 222.3474 | 1 | <.0001 |

When testing if the model is significant, we must check if each of the three values (Likelihood ratio, score, and Wald) is significant. If so, then we can say that the model has more statistically significant predictive power with the variable(s) than without the variables. As we can see, each metric has a probability of less than .0001 which says that the model is statistically significant.

| Analysis of Maximum Likelihood Estimates | | | | | |
|--|----|----------|-------------------|--------------------|------------|
| Parameter | DF | Estimate | Standard Error | Wald Chi-Square | Pr > ChiSq |
| Intercept | 1 | -2.7656 | 0.2430 | 129.5239 | <.0001 |
| A9_t | 1 | 4.1306 | 0.2770 | 222.3474 | <.0001 |

The maximum likelihood estimates are used to determine the coefficients/estimates, the odd-ratio, probability or fitted values, and the test statistics to assess each parameter and the model. We can test if the individual variables have significant predictive power, which is significant in this case because p<.0001 for A9 t.

The g(x) or logit or log-odds or estimate of the logistic regression equation can be found from this table and is as follows: $g(x) = -2.7656 + 4.1306*A9_t$. This numeric coefficient of the variable A9_t can be interpreted as the expected change in the logit for every unit change in A9_t with the other variables held constant.

| Odds Ratio Estimates | | | |
|----------------------|-----------------------------------|--------|---------|
| | Point 95% Wald | | |
| Effect | Estimate Confidence Limits | | |
| A9_t | 62.213 | 36.148 | 107.071 |

The odds-ratio for A9_t is interpreted as the odds that the response value is 1 is 62.213 times greater when the predictor variable A9_t is 1 than when it is zero. It is calculated from the estimate or coefficient of the predictor variable A9_t... $e^{4.1306} = 62.213$.

| Association of Predicted Probabilities and Observed Responses | | | |
|--|--------|-----------|-------|
| Percent Concordant | 75.2 | Somers' D | 0.740 |
| Percent Discordant | 1.2 | Gamma | 0.968 |
| Percent Tied | 23.6 | Tau-a | 0.367 |
| Pairs | 105672 | c | 0.870 |

These measures are used to evaluate the association between the predicted values versus the observed values. These measures rely on concordant and discordant pairs. Concordant pairs are those pairs where the lower ordered response value (often 0) has a lower predicted mean score than the observation with the higher ordered response value. In other words, it is the percent of correctly classified pairs. This is desirable, while discordant pairs have a higher predicted mean score for lower order response values (less desirable).

Somers' D is used to determine the strength and direction of relation between pairs of variables. It has a value of -1 to +1 with +1 meaning that all pairs agree or are concordant. A Somers' D value of .740 shows fairly strong concordance with between the predicted and observed responses.

Gamma is similar to Somers' D except that it does not penalize for ties and therefore (using the same scale of -1 to +1) is usually higher value than Somers' D, which is what we see here as well.

Tau-a is similar to a generalized value of R-square that is derived from the likelihood ratio. It is defined to be the ratio of the difference between the number of concordant pairs minus the discordant pairs divided by the total number of possible pairs.

C is used to determine how well the model can discriminate the response. It's value ranges from 0.5 to 1, where 0.5 is randomly guessing (no predictive power). Thus we want a higher number and our number of .870 shows us that our model is strong at discriminating the response value.

Thus, we can see that, taken together, based on our concordant/discordant values, Somers' D, Gamma, Tau-a, and c values that we have a fairly strong model for predicting the response variable values correctly.

-----PART 3 -----

Here we evaluate our model with a ROC curve and then compare it to another model with an additional variable using the ROC curve. The area under the ROC curve ranges from 0.5 to 1.0. This provides a measure of the model's ability to discriminate between those subjects who experience the "outcome of interest" versus those who do not. We would like to use a cutpoint that maximizes both sensitivity (probability of detecting a true value) and specificity (the probability of detecting a false value). We also use an arbitrary cutoff point, above which we consider the test to be abnormal and below to be normal. This cutoff point determines how many true positives, true negatives, false positives, and false negatives are shown. There is a tradeoff between sensitivity and specificity so different cutoff points will affect the sensitivity and specificity values. Also, the closer the curve comes to the 45-degree diagonal, the less accurate the test. The closer the curve follows the left-hand border and then the top border of the ROC space, the more accurate the test.

| Model Information | | |
|----------------------------------|------------------|--|
| Data Set | WORK.TEMPFILE | |
| Response Variable | Y | |
| Number of Response Levels | 2 | |
| Model | binary logit | |
| Optimization Technique | Fisher's scoring | |

| Number of Observations Read | 653 |
|------------------------------------|-----|
| Number of Observations Used | 653 |

| Response Profile | | | |
|------------------|---|--------------------|--|
| Ordered Value | Y | Total Frequency | |
| 1 | 1 | 296 | |
| 2 | 0 | 357 | |

Probability modeled is Y=1.

Model Convergence Status

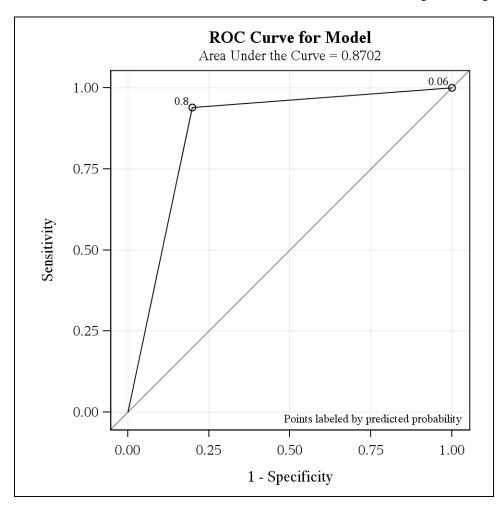
| Model Fit Statistics | | | | | |
|----------------------|-----------|------------|--|--|--|
| | | Intercept | | | |
| | Intercept | and | | | |
| Criterion | Only | Covariates | | | |
| AIC | 901.544 | 493.254 | | | |
| SC | 906.025 | 502.218 | | | |
| -2 Log L | 899.544 | 489.254 | | | |

| Testing Global Null Hypothesis: BETA=0 | | | | | |
|--|------------|----|------------|--|--|
| Test | Chi-Square | DF | Pr > ChiSq | | |
| Likelihood Ratio | 410.2891 | 1 | <.0001 | | |
| Score | 356.4519 | 1 | <.0001 | | |
| Wald | 222.3474 | 1 | <.0001 | | |

| Analysis of Maximum Likelihood Estimates | | | | | | |
|--|----|---------------|--------|------------|------------|--|
| _ | | Standard Wald | | | | |
| Parameter | DF | Estimate | Error | Chi-Square | Pr > ChiSq | |
| Intercept | 1 | -2.7656 | 0.2430 | 129.5239 | <.0001 | |
| A9_t | 1 | 4.1306 | 0.2770 | 222.3474 | <.0001 | |

| Odds Ratio Estimates | | | | | |
|----------------------|----------|----------------------|---------|--|--|
| Point 95% Wald | | | | | |
| Effect | Estimate | te Confidence Limits | | | |
| A9_t | 62.213 | 36.148 | 107.071 | | |

| Association of Predicted Probabilities and Observed Responses | | | | | |
|---|--------|-----------|-------|--|--|
| Percent Concordant | 75.2 | Somers' D | 0.740 | | |
| Percent Discordant | 1.2 | Gamma | 0.968 | | |
| Percent Tied | 23.6 | Tau-a | 0.367 | | |
| Pairs | 105672 | c | 0.870 | | |



| Obs | _PROB_ | _POS_ | _NEG_ | _FALPOS_ | _FALNEG_ | _SENSIT_ | _1MSPEC_ |
|-----|---------|-------|-------|----------|----------|----------|----------|
| 1 | 0.79656 | 278 | 286 | 71 | 18 | 0.93919 | 0.19888 |
| 2 | 0.05921 | 296 | 0 | 357 | 0 | 1.00000 | 1.00000 |

In this case the cutoff points are 0.8 and 0.06 which coincide with the mean values associated with our predictor variable A9_t with each response variable value (1 and 0). We can also see that the total area under the curve is .8702. This measures how well the test separates the variable being testing into those with and without the response value in question. Thus, the more area under the curve covered the better the test, while an area coverage of 0.5 indicates a completely useless test (same as guessing).

| Model Information | | | | |
|----------------------------------|------------------|--|--|--|
| Data Set | WORK.TEMPFILE | | | |
| Response Variable | Y | | | |
| Number of Response Levels | 2 | | | |
| Model | binary logit | | | |
| Optimization Technique | Fisher's scoring | | | |

| Number of Observations Read | 653 |
|------------------------------------|-----|
| Number of Observations Used | 653 |

| Response Profile | | | | |
|------------------|---|--------------------|--|--|
| Ordered Value | Y | Total Frequency | | |
| 1 | 1 | 296 | | |
| 2 | 0 | 357 | | |

Probability modeled is Y=1.

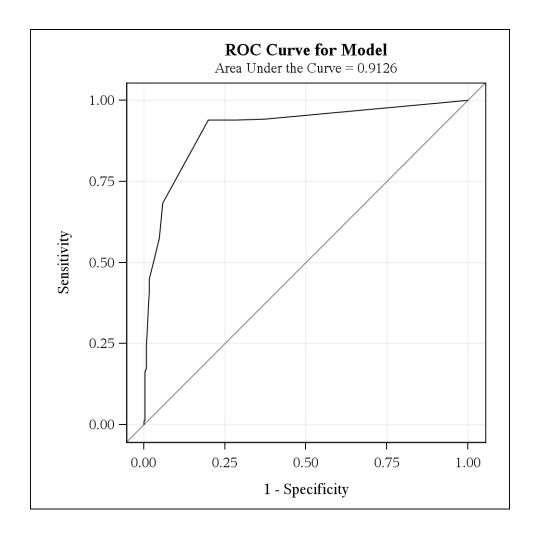
Model Convergence Status

| Model Fit Statistics | | | | | |
|----------------------|-----------|------------|--|--|--|
| | Interc | | | | |
| | Intercept | and | | | |
| Criterion | Only | Covariates | | | |
| AIC | 901.544 | 461.750 | | | |
| SC | 906.025 | 475.195 | | | |
| -2 Log L | 899.544 | 455.750 | | | |

| Testing Global Null Hypothesis: BETA=0 | | | | | |
|--|------------|----|------------|--|--|
| Test | Chi-Square | DF | Pr > ChiSq | | |
| Likelihood Ratio | 443.7932 | 2 | <.0001 | | |
| Score | 368.6614 | 2 | <.0001 | | |
| Wald | 211.9953 | 2 | <.0001 | | |

| Analysis of Maximum Likelihood Estimates | | | | | | |
|--|----|----------|-------------------|--------------------|------------|--|
| Parameter | DF | Estimate | Standard Error | Wald Chi-Square | Pr > ChiSq | |
| Intercept | 1 | -2.9245 | 0.2500 | 136.8938 | <.0001 | |
| A9_t | 1 | 3.7048 | 0.2837 | 170.4803 | <.0001 | |
| A11 | 1 | 0.2076 | 0.0426 | 23.8107 | <.0001 | |

| Odds Ratio Estimates | | | | | | |
|----------------------|----------------|--------------------------|--------|--|--|--|
| T. 00 | Point 95% Wald | | | | | |
| Effect | Estimate | Confidence Limits | | | | |
| A9_t | 40.641 | 23.305 | 70.874 | | | |
| A11 | 1.231 | 1.132 | 1.338 | | | |



ROC Model: omit a11

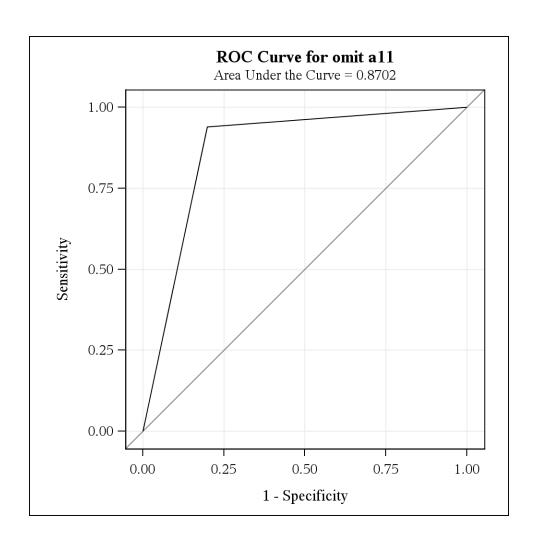
Model Convergence Status

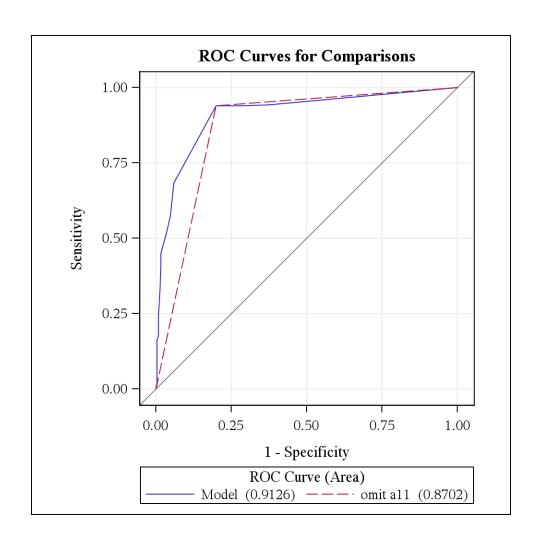
| Model Fit Statistics | | | | | | |
|----------------------|-----------|------------|--|--|--|--|
| | Intercept | | | | | |
| | Intercept | and | | | | |
| Criterion | Only | Covariates | | | | |
| AIC | 901.544 | 493.254 | | | | |
| SC | 906.025 | 502.218 | | | | |
| -2 Log L | 899.544 | 489.254 | | | | |

| Testing Global Null Hypothesis: BETA=0 | | | | | | | |
|--|----------|---|--------|--|--|--|--|
| Test Chi-Square DF Pr > Chi-Square | | | | | | | |
| Likelihood Ratio | 410.2891 | 1 | <.0001 | | | | |
| Score | 356.4519 | 1 | <.0001 | | | | |
| Wald | 222.3474 | 1 | <.0001 | | | | |

| Analysis of Maximum Likelihood Estimates | | | | | | | | |
|--|----|----------|--------|------------|------------|--|--|--|
| Standard Wald | | | | | | | | |
| Parameter | DF | Estimate | Error | Chi-Square | Pr > ChiSq | | | |
| Intercept | 1 | -2.7656 | 0.2430 | 129.5239 | <.0001 | | | |
| A9_t | 1 | 4.1306 | 0.2770 | 222.3474 | <.0001 | | | |

| Odds Ratio Estimates | | | | | | |
|----------------------|----------------|--------------------------|---------|--|--|--|
| | Point 95% Wald | | | | | |
| Effect | Estimate | Confidence Limits | | | | |
| A9_t | 62.213 | 36.148 | 107.071 | | | |





| ROC Association Statistics | | | | | | | | | |
|----------------------------|--------------|----------|--------------------------|--------|-----------|--------|--------|--|--|
| | Mann-Whitney | | | | | | | | |
| | | Standard | 95% | Wald | Somers' D | | | | |
| ROC Model | Area | Error | Confidence Limits | | (Gini) | Gamma | Tau-a | | |
| Model | 0.9126 | 0.0116 | 0.8899 | 0.9353 | 0.8253 | 0.8930 | 0.4097 | | |
| omit a11 | 0.8702 | 0.0127 | 0.8453 | 0.8950 | 0.7403 | 0.9684 | 0.3675 | | |

| ROC Contrast Test Results | | | | | | |
|---------------------------|----|------------|------------|--|--|--|
| Contrast | DF | Chi-Square | Pr > ChiSq | | | |
| Reference = Model | 1 | 31.0489 | <.0001 | | | |

| ROC Contrast Estimation and Testing Results by Row | | | | | | | | |
|--|----------|-------------------|-------------------------------|--------|------------|------------|--|--|
| Contrast | Estimate | Standard Error | 95% Wald Confidence Limits | | Chi-Square | Pr > ChiSq | | |
| Model - omit a11 | 0.0425 | 0.00762 | 0.0275 | 0.0574 | 31.0489 | <.0001 | | |

We can see when comparing the models that the model that includes both variables (A9 t and A11) encompasses more area under the ROC curve comparatively speaking. This indicates that it is a better model for our purposes. We can also see that it is further to the left-hand side of the graph and almost exactly on the same plane at the top of the graph. As with any ROC analysis, if we want more specificity then we will sacrifice sensitivity which can change how much the model is preferred.

CONCLUSION----

Using the EDA and PROC LOGISTIC with the score selection procedure we determined that A9 t was the best single variable we could use to predict the values of the response variable. Initially, we selected $\overline{A9}$ t via EDA by comparing the difference between its mean values for each response variable value. Then we discovered that the selection score procedure selected the same variable so we fit our model and evaluated the results. We found that it was statistically significant as an individual variable and the model was statistically significant for predictive power as well. Finally, we created a ROC curve from which we could determine the sensitivity and specificity of the model and, again, found that it had strong predictive power. We also compared it to another model that included an additional variable and found the new model was slightly better in terms of its measures of area under the curve, specificity, and sensitivity.

```
CODE -----
* creating the macro for data set;
%let PATH = /courses/u northwestern.edu1/i 833463/c 3505/SAS Data/;
%let NAME = MYDATA;
%let LIB = &NAME..;
libname &NAME. "&PATH." access=readonly;
%let INFILE = &LIB.credit approval;
%let TEMPFILE = TEMPFILE;
* setting database to temp data file;
data &TEMPFILE.;
set &INFILE.;
      * set target variable;
      if A16='+' then Y=1;
```

```
else if A16='-' then Y=0;
       else Y = .;
* subsection 2 - discretize continuous variables;
       if (A2<20) then A2 discrete=1;
       else if (A2<30) then A2 discrete=2;
       else if (A2<40) then A2 discrete=3;
       else A2 discrete=4;
       if (A3<1) then A3 discrete=1;
       else if (A3<4) then A3 discrete=2;
       else if (A3<8) then A3 discrete=3;
       else A3 discrete=4;
       if (A8<1) then A8 discrete=1;
       else if (A8<4) then A8 discrete=2;
       else if (A8<8) then A8 discrete=3;
       else A8 discrete=4;
       if (A11<2) then A11 discrete=1;
       else if (A11<5) then A11 discrete=2;
       else if (A11<10) then A11 discrete=3;
       else A11 discrete=4;
       if (A14<150) then A14 discrete=1;
       else if (A14<225) then A14 discrete=2;
       else if (A14<325) then A14 discrete=3;
       else A14_discrete=4;
       if (A15 < 1.5) then A15 discrete=1;
       else if (A15 < 250) then A15 discrete=2;
       else if (A15 < 1001) then A15 discrete=3;
       else A15 discrete=4;
* subsection 3 - change variables to appropriate formats
       (continuous to discrete and categorical to dummy variables)
  I'm combining any category with less than 30 observations and
       using them for the base;
  if (A1 ='b') then A1 b=1; else A1 b=0;
  if (A4 = 'u') then A4 u=1; else A4 u=0;
  if (A5 = 'g') then A5 g=1; else A5 g=0;
  if (A6 ='aa') then A6 aa=1; else A6 aa=0;
```

```
if (A6 = c) then A6 c=1; else A6 c=0;
       if (A6 = 'cc') then A6 cc=1; else A6 cc=0;
       if (A6 = 'ff') then A6 ff=1; else A6 ff=0;
       if (A6 = 'i') then A6 i=1; else A6 i=0;
       if (A6 = 'k') then A6 k=1; else A6 k=0;
       if (A6 = 'm') then A6 m=1; else A6 m=0;
       if (A6 = 'g') then A6 g=1; else A6 g=0;
       if (A6 = 'w') then A6 w=1; else A6 w=0;
       if (A6 = 'x') then A6 x=1; else A6 x=0;
       if (A7 = 'bb') then A7 bb=1; else A7 bb=0;
       if (A7 = 'ff') then A7 ff=1; else A7 ff=0;
       if (A7 ='h') then A7 h=1; else A7 h=0;
       if (A7 = 'v') then A7 v=1; else A7 v=0;
       if (A9 = t) then A9 t=1; else A9 t=0;
       if (A10 ='f') then A10 f=1; else A10 f=0;
       if (A12 ='f') then A12 f=1; else A12 f=0;
       if (A13 = 'g') then A13 g=1; else A13 g=0;
       if (A13 = 's') then A13 s=1; else A13 s=0;
* subsection 4 - delete missing values;
       if (a1='?') or (a4='?') or (a5='?') or (a6='?') or (a7='?') or (a9='?') or (a10='?') or (a12='?') or (a13='?')
       or (a2=.) or (a3=.) or (a8=.) or (a11=.) or (a14=.) or (a15=.)
              then delete;
* to "fix" this data we could create some code that takes the mean or median values and substitutes it for these
variables:
run; quit;
* subsection 1 - proc freq to view details of categorical variables;
proc freq data=&TEMPFILE.;
tables A1 A4 A5 A6 A7 A9 A10 A12 A13 A16;
run:
* subsection 1 - proc means to view details of continuous variables:
proc means data=&TEMPFILE. p5 p10 p25 p50 p75 p90 p95;
```

class y;

```
var A2 A3 A8 A11 A14 A15;
run;
* subsection 5 - macro for class mean(c);
%macro class mean(c);
proc means data=&tempfile. mean;
*class a1 a4 a5 a6 a7 a8 a10 a12 a13;
class &c.;
var Y;
run;
%mend class mean;
* discretized continuous variables;
%class mean(c=a2 discrete);
%class mean(c=a3 discrete);
%class mean(c=a8 discrete);
%class mean(c=a11 discrete);
%class mean(c=a14 discrete);
%class mean(c=a15 discrete);
* I selected A15 discrete and a11 discretes as best variables from continuous variables;
proc freq data=&tempfile.;
tables Y*a11 discrete;
run;
proc freq data=&tempfile.;
tables y*a15 discrete;
run;
* categorical variables;
%class mean(c=a1 b);
%class mean(c=a4 u);
%class mean(c=a5 g);
%class mean(c=a6 aa);
%class mean(c=a6 c);
%class mean(c=a6 cc);
%class mean(c=a6 ff);
%class mean(c=a6 i);
%class mean(c=a6 k);
%class mean(c=a6 m);
%class mean(c=a6 q);
%class mean(c=a6 w);
%class mean(c=a6 x);
```

```
%class mean(c=a7 bb);
%class mean(c=a7 ff);
%class mean(c=a7 h);
%class mean(c=a7 v);
%class mean(c=a9 t);
%class mean(c=a10 f);
%class mean(c=a12 f);
%class mean(c=a13 g);
%class mean(c=a13 s);
* I selected A9 as best variable from categorical variables;
* I selected A9 as best categorical variable and a11 discrete and a15 discrete as best dummy variables;
* fit logistic regression model to the variables- each dummy variable must be included;
* subsection 1 - proc logistic on variable selected from EDA;
proc logistic data=&tempfile. descending;
model Y = A9 t;
run;
* subsection 2 - proc logistic on all variables;
proc logistic data=&tempfile. descending;
model Y = a2 a3 a8 a11 a14 a15
      al ba4 ua5 g
      a6 aa a6 c a6 cc a6 ff a6 i a6 k a6 m a6 q a6 w a6 x
      a7 bb a7 ff a7 h a7 v
      a9 t a10 f a12 f a13 g a13 s/selection=score start=1 stop=1;
run;
* model selects A9 t as best predictive variables;
proc logistic data=&tempfile. descending;
model y = a9 t;
run:
****** PART 3 *********
ods graphics on;
proc logistic data=&tempfile. descending plots(only)=roc(id=prob);
model Y = A9 t / outroc = roc1;
ods graphics off;
```

```
proc print data=roc1;
run; quit;
*** comparison model ****;
ods graphics on;
proc logistic data=&tempfile. descending;
model y = a9_t a11;
roc 'omit a11' a9_t;
roccontrast/ estimate=allpairs;
ods graphics off;
```