

# Naive Bayes Spam Filtering

## Using Word-Position-Based Attributes

Johan Hovold

Dejun Qian

# Outline

- 1 Introduction
- 2 Naive Bayes Using Word-Position-Based Attributes
- 3 Experimental Results
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## Introduction

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  - Waste resources on the Internet
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  - May expose children to unsuitable contents (e.g. pronography)
- The solution to the spam problem
  - Automatic spam filter

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- Naive Bayes classifier in this paper

## Naive Bayes Using Word-Position-Based Attributes

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- Estimate  $P(a_i = w_k|c_j)$  with  $P(w_k|c_j)$
- $$P(w_k|c_j) = \frac{C_j(w_k)+1}{n_j+|\text{Vocabulary}|}$$

## Benchmark Corpora

corpus	messages	spam ratio
PU1	1099	44%
PU2	721	20%
PU3	4139	44%
PUA	1142	50%
SA	6047	31%

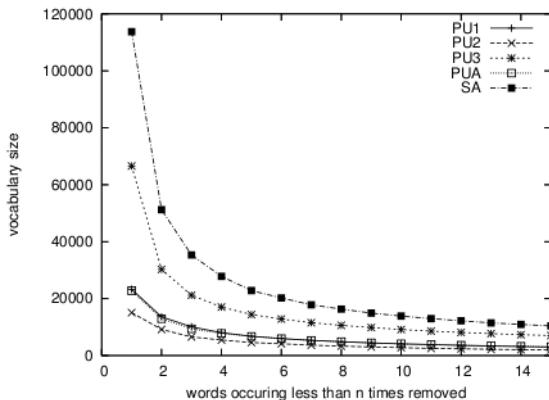
- PU corpora<sup>1</sup>
- SpamAssassin corpus<sup>2</sup>

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<sup>1</sup><http://www.iit.demokritos.gr/skel/i-config/>

<sup>2</sup><http://spamassassin.org/publiccorpus/>

## Attribute Selection - Infrequent



**Figure 1:** Impact on vocabulary size when removing infrequent words (from nine tenths of each corpora).

- Slightly increased precision at the expense of slightly reduced recall as  $n$  grew

# Attribute Selection - Frequent

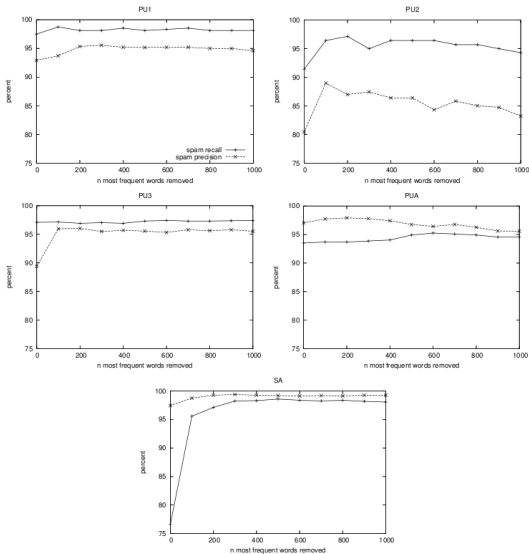


Figure 2: Impact on spam precision and recall when removing the most frequent words.



## n-grams

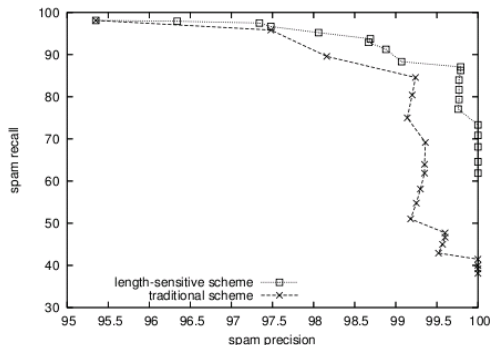
**Table 2:** Comparison of classification results when using only unigram attributes and uni-, bi- and trigram attributes, respectively. In the experiment n-grams occurring less than three times and the 200 most frequent n-grams were removed. The second n-gram row for the SA corpus shows the result when the 5000 most frequent n-grams were removed.

<i>n</i> -grams	<i>R</i>	<i>P</i>	<i>Acc</i>
PU1			
<i>n</i> = 1	98.12	95.35	97.06
<i>n</i> = 1, 2, 3	99.17	96.19	97.89
PU2			
<i>n</i> = 1	97.14	87.00	96.20
<i>n</i> = 1, 2, 3	95.00	93.12	96.90
PU3			
<i>n</i> = 1	96.92	96.02	96.83
<i>n</i> = 1, 2, 3	96.59	97.83	97.53
PUA			
<i>n</i> = 1	93.68	97.91	95.79
<i>n</i> = 1, 2, 3	94.74	97.75	96.23
SA			
<i>n</i> = 1	97.12	99.25	98.95
<i>n</i> = 1, 2, 3	92.26	98.70	97.42
<i>n</i> = 1, 2, 3	98.46	99.66	99.46

# Cost-Sensitive Classification

$$\frac{P(spam|d)}{P(legit|d)} > \lambda,$$

$$\frac{P(spam|d)}{P(legit|d)} > w^{|d|}.$$



**Figure 4:** Example recall/precision curves of the two weighting schemes from cost-sensitive classification on the PU1 corpus.

# Conclusion

- Possible to achieve very good classification performance using a word-position-based variant of naive Bayes
- Attribute selection has been stressed: memory requirements may be lowered and classification performance increased
- By extending the attribute set with bi- and trigrams, better classification performance may be achieved
- Simple weighting scheme boost precision further

Question?