CSC 211: Object Oriented Programming Recursion

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Spring 2020



Recursion

- Problem solving technique in which we solve a task by reducing it to smaller tasks (of the same kind)
 - ✓ then use same approach to solve the smaller tasks
- · Technically, a recursive function is one that calls itself
- · General form:
 - ✓ base case
 - solution for a **trivial case**
 - it can be used to stop the recursion (prevents "stack overflow")
 - every recursive algorithm needs at least one base case
 - ✓ recursive call(s)
 - divide problem into **smaller instance(s)** of the **same structure**

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General form

```
function() {
    if (this is the base case) {
        calculate trivial solution
    } else {
        break task into subtasks solve each task recursively combine solutions if necessary
    }
}
```

Why recursion?

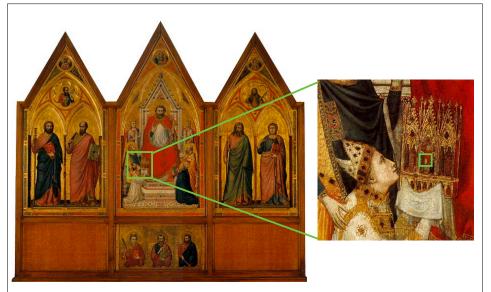
- Can we live without it?
 - ✓ yes, you can write "any program" with arrays, loops, and conditionals
- · However ...
 - √ some formulas are explicitly recursive
 - ✓ some problems exhibit a natural recursive solution







https://courses.cs.washington.edu/courses/cse120/17sp/labs/11/tree.html



The Stefaneschi Altarpiece is a triptych by the Italian medieval painter Giotto, commissioned by Cardinal Giacomo Stefaneschi to serve as an altarpiece for one of the altars of Old St.

Peter's Basilica in Rome. It is now at the Pinacoteca Vaticana, Rome. Circa 1320.

https://en.wikipedia.org/wiki/Stefaneschi_Triptych

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Example: factorial

$$n! = 1 \cdot 2 \cdot \ldots \cdot n = \prod_{k=1}^{n} k$$

$$n! = \begin{cases} 1 & \text{if } n = 0\\ (n-1)! \cdot n & \text{if } n > 0 \end{cases}$$

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Example: factorial

 Apply the recursive definition of factorial to calculate:

$$n! = \begin{cases} 1 & \text{if } n = 0\\ (n-1)! \cdot n & \text{if } n > 0 \end{cases}$$

· 5!

· 3!

General form

```
function() {
    if (this is the base case) {
        calculate trivial solution
    } else {
        break task into subtasks solve each task recursively combine solutions if necessary
    }
}
```

. .

int fact(int n) { // base case if (n < 2) { return 1; } // recursive call return fact(n-1) * n; }</pre>

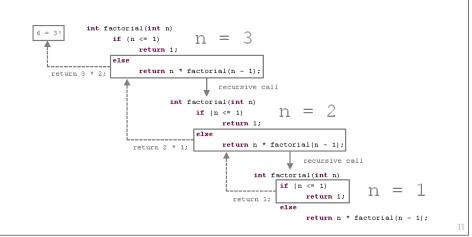
Recursion call tree (tracing recursion)

```
fact(3)

int fact(int n) {
    if (n < 2) {
        return 1;
    }
    return fact(n-1) * n;
}</pre>
```

Example

Factorial



Question

• Given f(n) = f(n-1) + 2n - 1, what is the value of f(3)?

Must have base case and make progress towards base case

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Rules of the game

- Your code must have at least one base case for a trivial solution
 - ✓ that is, for a non-recursive solution
- Recursive calls should make progress towards the base case
- Your code must break a larger problem into smaller problems
 - ' each smaller problem should be of the same 'nature' as the larger problem

Example: power of a number

```
b^n = b \cdot b \cdot \dots \cdot b base case?

n times recursive case?

double power(double b, int n) {

// base case
if (n == 0) {
    return 1;
    }

// recursive call
    return b * power(b, n-1);
}
```

Recursion call tree (tracing recursion)

```
power(2, 4) return 2*8

b = 2 \quad n = 4
b * power(2, 3) return 2*4
b = 2 \quad n = 3
b * power(2, 2) return 2*2
b = 2 \quad n = 2
b * power(2, 1) return 2*1
b = 2 \quad n = 1
b * power(2, 0) return 1
b = 2 \quad n = 0
```

What is the output of foo (1234)?

```
int foo(int n) {
    if (n < 10) {
        return n;
    }
    int b = n % 10;
    return b + foo(n/10);
}</pre>
```

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Write a function to print this pattern?

for any n > 0

n = 2

```
***
```

n = 4

Write a function to print this pattern?

for any n > 0

n = 2

** *** *** *** *** ** n = 4

What is the output of mystery(7)?

```
void mystery(unsigned int n) {
    if (n < 2) {
         std::cout << n;</pre>
    } else {
         mystery(n/2);
         std::cout << n % 2;</pre>
```

Indirect Recursion

```
void f2(int n);
                            f1(1) ?
void f1(int n) {
    if (n > 1) {
                            f1(2) ?
        std::cout << "1";
        f2(n - 1);
                            f1(4) ?
                            f1(7) ?
void f2(int n) {
    std::cout << "0";
                            f1(10)
    f1(n - 1);
```

Final thoughts

Recursion is a powerful technique that solves problems by breaking them down into smaller subproblems of the same form, and applying the same strategy to solve the subproblems

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