4/22/2018 Problems - Codeforces

# **Educational Codeforces Round 19**

## A. k-Factorization

2 seconds, 256 megabytes

Given a positive integer n, find k integers (not necessary distinct) such that all these integers are strictly greater than 1, and their product is equal to n.

## Input

The first line contains two integers n and k ( $2 \le n \le 100000$ ,  $1 \le k \le 20$ ).

## Output

If it's impossible to find the representation of n as a product of k numbers, print -1.

Otherwise, print k integers in any order. Their product must be equal to n. If there are multiple answers, print any of them.

input	
100000 2	
output	
2 50000	

input		
100000 20		
output		
-1		

input	
1024 5	
output	
2 64 2 2 2	

B. Odd sum

1 second, 256 megabytes

You are given sequence  $a_1, a_2, ..., a_n$  of integer numbers of length n. Your task is to find such subsequence that its sum is odd and maximum among all such subsequences. It's guaranteed that given sequence contains subsequence with odd sum.

Subsequence is a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements.

You should write a program which finds sum of the best subsequence.

## Input

The first line contains integer number n ( $1 \le n \le 10^5$ ).

The second line contains n integer numbers  $a_1, a_2, ..., a_n$  ( -  $10^4 \le a_i \le 10^4$ ). The sequence contains at least one subsequence with odd sum.

## Output

Print sum of resulting subsequence.

input	
4 -2 2 -3 1	
output	
3	



In the first example sum of the second and the fourth elements is 3.

C. Minimal string

1 second, 256 megabytes

Petya recieved a gift of a string s with length up to  $10^5$  characters for his birthday. He took two more empty strings t and u and decided to play a game. This game has two possible moves:

- Extract the **first** character of *s* and append *t* with this character.
- Extract the **last** character of *t* and append *u* with this character.

Petya wants to get strings s and t empty and string u lexicographically minimal.

You should write a program that will help Petya win the game.

#### Input

First line contains non-empty string s ( $1 \le |s| \le 10^5$ ), consisting of lowercase English letters.

## Output

Print resulting string *u*.

input	
cab	
output	
abc	

input	
acdb	
output	
abdc	

# D. Broken BST

1 second, 256 megabytes

Let T be arbitrary binary tree — tree, every vertex of which has no more than two children. Given tree is rooted, so there exists only one vertex which doesn't have a parent — it's the root of a tree. Every vertex has an integer number written on it. Following algorithm is run on every value from the tree T:

- 1. Set pointer to the root of a tree.
- 2. Return success if the value in the current vertex is equal to the number you are looking for

- 3. Go to the left child of the vertex if the value in the current vertex is greater than the number you are looking for
- 4. Go to the right child of the vertex if the value in the current vertex is less than the number you are looking for
- 5. Return fail if you try to go to the vertex that doesn't exist

Here is the pseudo-code of the described algorithm:

```
bool find(TreeNode t, int x) {
   if (t == null)
      return false;
   if (t.value == x)
      return true;
   if (x < t.value)
      return find(t.left, x);
   else
      return find(t.right, x);
}
find(root, x);</pre>
```

The described algorithm works correctly if the tree is binary search tree (i.e. for each node the values of left subtree are less than the value in the node, the values of right subtree are greater than the value in the node). But it can return invalid result if tree is not a binary search tree.

Since the given tree is not necessarily a binary search tree, not all numbers can be found this way. Your task is to calculate, how many times the search will fail being running on every value from the tree.

If the tree has multiple vertices with the same values on them then you should run algorithm on every one of them separately.

# Input

First line contains integer number n ( $1 \le n \le 10^5$ ) — number of vertices in the tree.

Each of the next n lines contains 3 numbers v, l, r ( $0 \le v \le 10^9$ ) — value on current vertex, index of the left child of the vertex and index of the right child of the vertex, respectively. If some child doesn't exist then number - 1 is set instead. Note that different vertices of the tree may contain the same values.

## Output

Print number of times when search algorithm will fail.

input		
3		
15 -1 -1		
10 1 3 5 -1 -1		
5 -1 -1		
output		
2		

```
input

8
6 2 3
3 4 5
12 6 7
1 -1 8
4 -1 -1
5 -1 -1
14 -1 -1
2 -1 -1

output

1
```

In the example the root of the tree in vertex 2. Search of numbers 5 and 15 will return fail because on the first step algorithm will choose the subtree which doesn't contain numbers you are looking for.

# E. Array Queries

2 seconds, 256 megabytes

a is an array of n positive integers, all of which are not greater than n.

You have to process q queries to this array. Each query is represented by two numbers p and k. Several operations are performed in each query; each operation changes p to  $p+a_p+k$ . There operations are applied until p becomes greater than n. The answer to the query is the number of performed operations.

## Input

The first line contains one integer n ( $1 \le n \le 100000$ ).

The second line contains n integers — elements of a ( $1 \le a_i \le n$  for each i from 1 to n).

The third line containts one integer q ( $1 \le q \le 100000$ ).

Then q lines follow. Each line contains the values of p and k for corresponding query  $(1 \le p, k \le n)$ .

## Output

Print *q* integers, *i*th integer must be equal to the answer to *i*th query.

```
input

3
1 1 1 1
3
1 1 1
2 1
3 1

output

2
1
1
```

Consider first example:

In first query after first operation p = 3, after second operation p = 5.

In next two queries p is greater than n after the first operation.

# F. Mice and Holes

1.5 seconds, 256 megabytes

One day Masha came home and noticed n mice in the corridor of her flat. Of course, she shouted loudly, so scared mice started to run to the holes in the corridor.

The corridor can be represeted as a numeric axis with n mice and m holes on it. ith mouse is at the coordinate  $x_i$ , and jth hole — at coordinate  $p_j$ . jth hole has enough room for  $c_i$  mice, so not more than  $c_i$  mice can enter this hole.

What is the minimum sum of distances that mice have to go through so that they all can hide in the holes? If ith mouse goes to the hole j, then its distance is  $|x_i - p_j|$ .

Print the minimum sum of distances.

#### Input

The first line contains two integer numbers n, m ( $1 \le n$ ,  $m \le 5000$ ) — the number of mice and the number of holes, respectively.

The second line contains n integers  $x_1, x_2, ..., x_n$  ( -  $10^9 \le x_i \le 10^9$ ), where  $x_i$  is the coordinate of ith mouse.

Next m lines contain pairs of integer numbers  $p_j, c_j$  ( -  $10^9 \le p_j \le 10^9, \ 1 \le c_j \le 5000$ ), where  $p_j$  is the coordinate of jth hole, and  $c_j$  is the maximum number of mice that can hide in the hole j.

## Output

Print one integer number — the minimum sum of distances. If there is no solution, print -1 instead.

```
input

4 5
6 2 8 9
3 6
2 1
3 6
4 7
4 7

output

11
```

```
input
7 2
10 20 30 40 50 45 35
-1000000000 10
1000000000 1

output
7000000130
```

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