Lecture 9: Hardware and Software

Assignment 3 Released

Assignment 3 is released! It covers:

- Fully-connected networks
- Dropout
- Update rules: SGD+Momentum, RMSprop, Adam
- Convolutional networks
- Batch normalization

Due Friday October 9, 11:59pm

(Website originally said 10/16 – this was a typo!)

Deep Learning Hardware

Inside a computer



Inside a computer

GPU: "Graphics Processing Unit"



This image is in the public domain



This image copyright 2017, Justin Johnson

Inside a computer

CPU: "Central Processing Unit"



This image is licensed under CC-BY 2.0

GPU: "Graphics Processing Unit"



This image is in the public domain



inis image copyright 2017, Justin Johnson

NVIDIA

VS

AMD

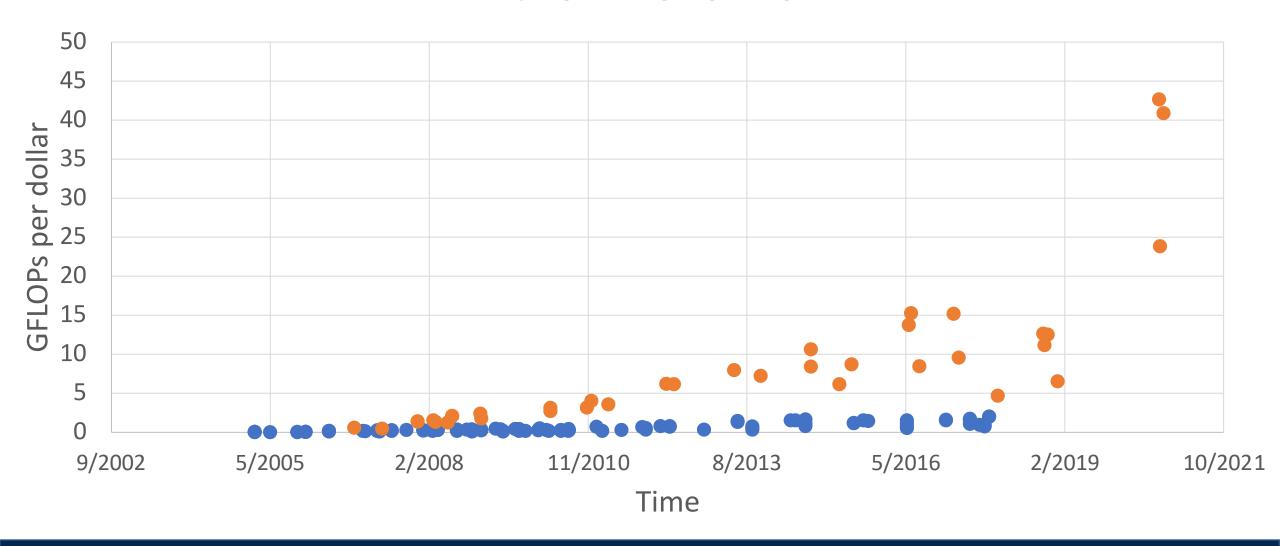
NVIDIA

VS

AMD

GFLOPs per Dollar

• CPU • GPU FP32



CPU vs GPU

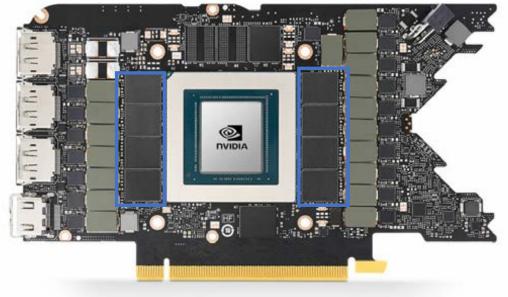
	Cores	Clock Speed (GHz)	Memory	Price	TFLOP/sec
CPU Ryzen Threadripper 3970X	64 (128 threads with hyperthreading)	3.7 (4.5 boost)	System RAM	\$1999	~6.9 FP32
GPU NVIDIA RTX 3090	10496	1.4 (1.7 boost)	24 GB GDDR6X	\$1499	~35.6 FP32

CPU: Fewer cores, but each core is much faster and much more capable; great at sequential tasks

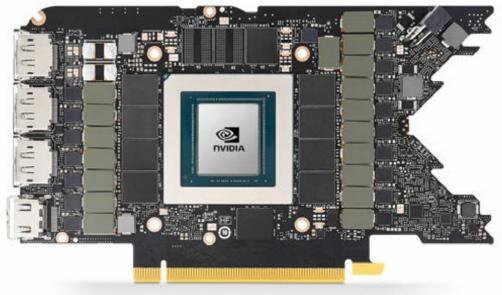
GPU: More cores, but each core is much slower and "dumber"; great for parallel tasks

12x 2GB memory modules





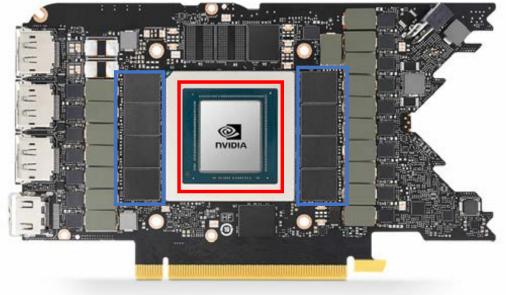




12x 2GB memory modules

Processor





Inside a GPU:

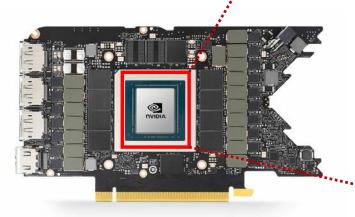
RTX 3090



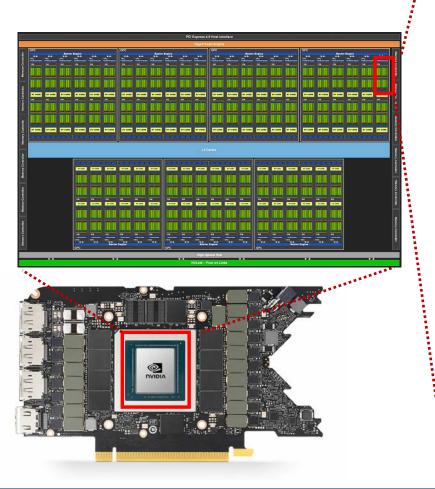
Inside a GPU:

RTX 3090

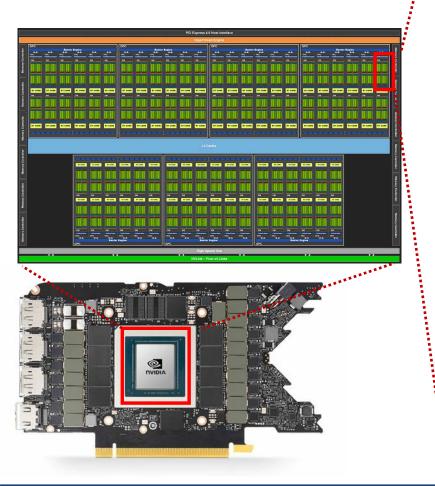
82 Streaming multiprocessors (SMs)







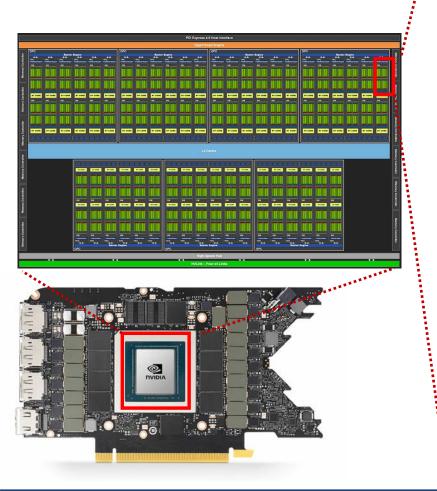






64 FP32 cores per SM

64 INT32/FP32 cores per SM





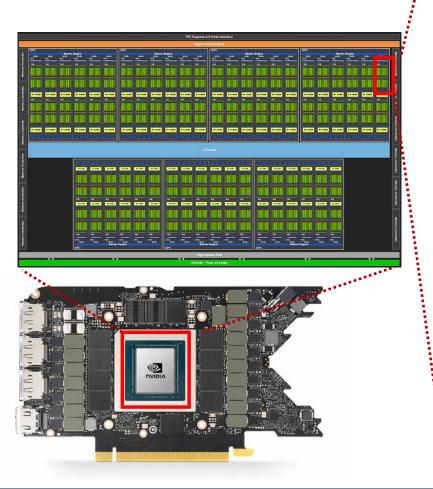
64 FP32 cores per SM

64 INT32/FP32 cores per SM

35.6 FP32 TFLOP/sec

Multiply:

- 82 SM
- 128 FP32 core/SM
- 2 FLOP/cycle
- 1.7 GCycle / sec
- = 35.6 TFLOP/sec





64 FP32 cores per SM

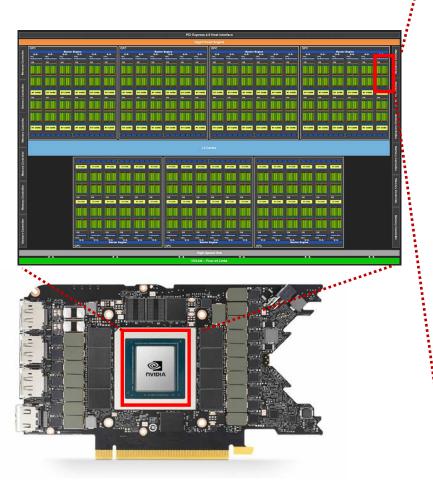
64 INT32/FP32 cores per SM

35.6 FP32 TFLOP/sec

4 Tensor Core per SM

Special hardware!

Let A, B, C be matrices (A 4x4, B,C 4x8).
Compute AB+C in one clock cycle (256 FLOP)





64 FP32 cores per SM

64 INT32/FP32 cores per SM

35.6 FP32 TFLOP/sec

4 Tensor Core per SM

35.6 FP32 TFLOP/sec

Multiply:

- 82 SM
- 4 Tensor Core/SM
- 256 FLOP/cycle
- 1.7 GCycle / sec
- = 142 TFLOP/sec

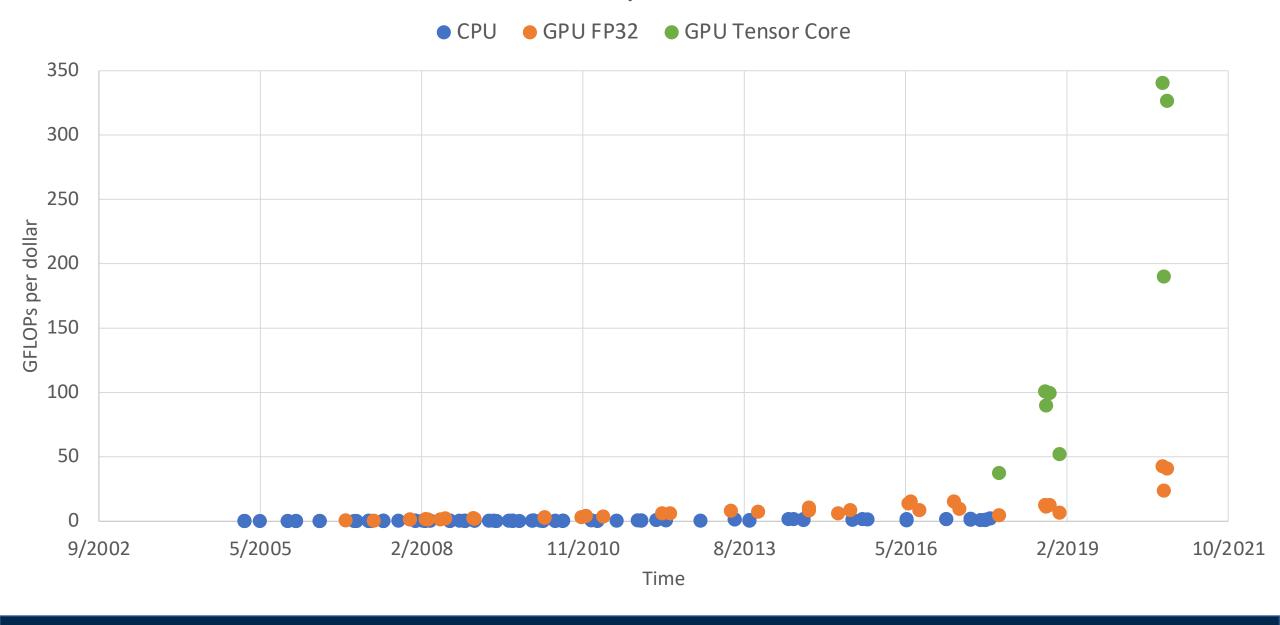
CPU vs GPU

	Cores	Clock Speed (GHz)	Memory	Price	TFLOP/sec
CPU Ryzen Threadripper 3970X	64 (128 threads with hyperthreading)	3.7 (4.5 boost)	System RAM	\$1999	~6.9 FP32
GPU NVIDIA RTX 3090	10496	1.4 (1.7 boost)	24 GB GDDR6X	\$1499	~35.6 FP32 ~142 TFLOP with Tensor core

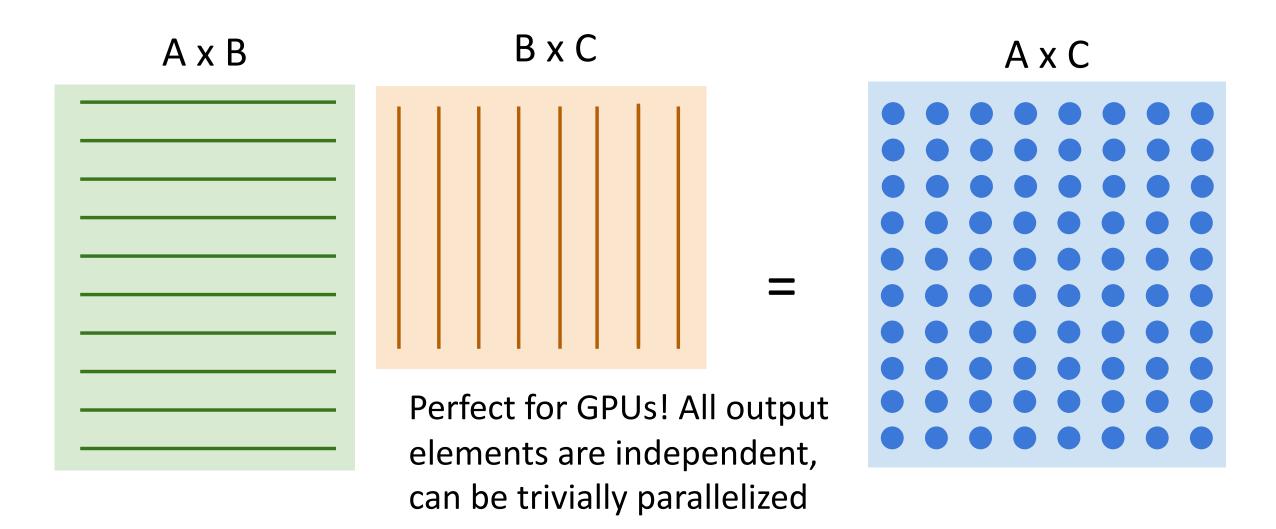
CPU: Fewer cores, but each core is much faster and much more capable; great at sequential tasks

GPU: More cores, but each core is much slower and "dumber"; great for parallel tasks

GFLOPs per Dollar



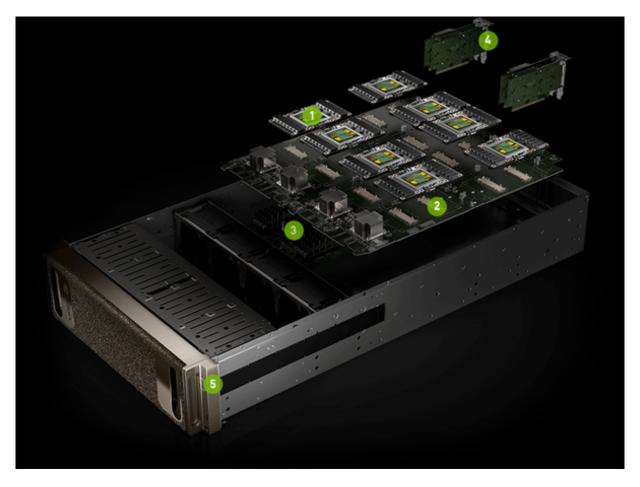
Example: Matrix Multiplication



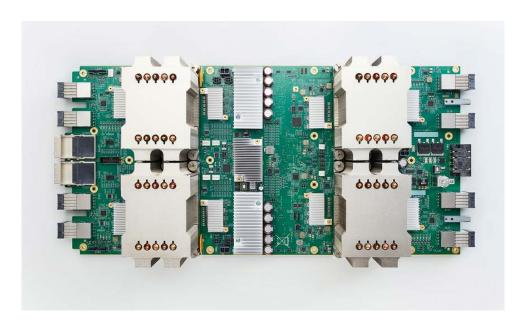
Programming GPUs

- CUDA (NVIDIA only)
 - Write C-like code that runs directly on the GPU
 - NVIDIA provides optimized APIs: cuBLAS, cuFFT, cuDNN, etc
- OpenCL
 - Similar to CUDA, but runs on anything
 - Usually slower on NVIDIA hardware
- EECS 598.009: Applied GPU Programming

Scaling up: Typically 8 GPUs per server



NVIDIA DGX-1: 8x V100 GPUs



Special hardware for matrix multiplication, similar to NVIDIA Tensor Cores; also runs in mixed precision (bfloat16)

Cloud TPU v2-8

180 TFLOP/sec

64 GB HBM memory

\$6 / hour

(free on Colab!)



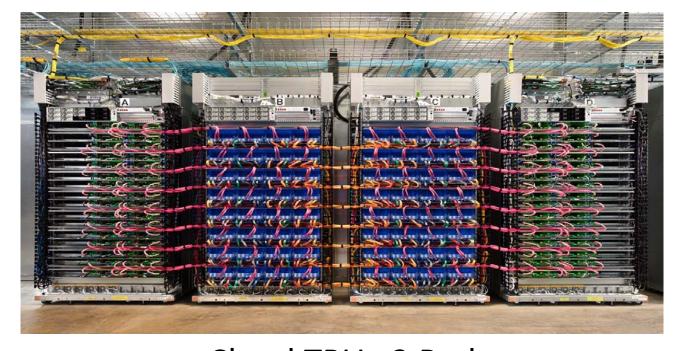
Cloud TPU v2-8

180 TFLOP/sec

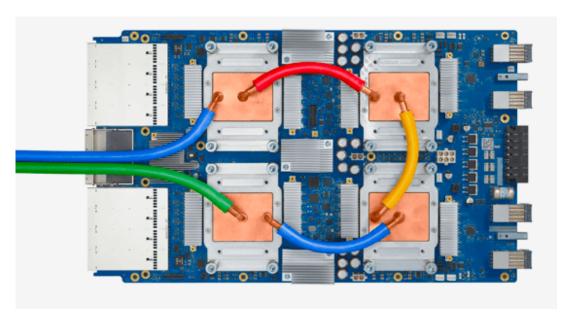
64 GB HBM memory

\$6 / hour

(free on Colab!)

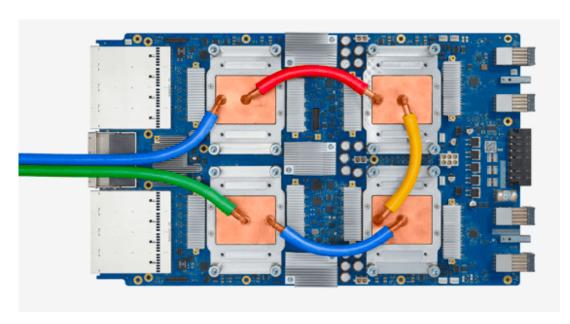


Cloud TPU v2 Pod 16x TPU-v2-8 11.5 PFLOPs \$384 / hour



Cloud TPU v3-8
420 TFLOP/sec
128 GB HBM memory
\$8 / hour

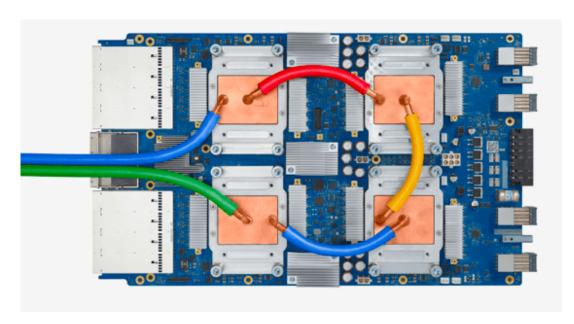
TPU-v3 image is released under a CC-SA 4.0 International license



Cloud TPU v3-8
420 TFLOP/sec
128 GB HBM memory
\$8 / hour



Cloud TPU v3 Pod 256 TPU-v3 107 PFLOPs



Cloud TPU v3-8
420 TFLOP/sec
128 GB HBM memory
\$8 / hour



Cloud TPU v3 Pod

256 TPU-v3

107 PFLOPs

Contact sales rep for pricing

Deep Learning Software

A zoo of frameworks!

Caffe Caffe2
(UC Berkeley) (Facebook)

Theano _____ TensorFlow (U Montreal) (Google)

PaddlePaddle Chainer (Baidu)

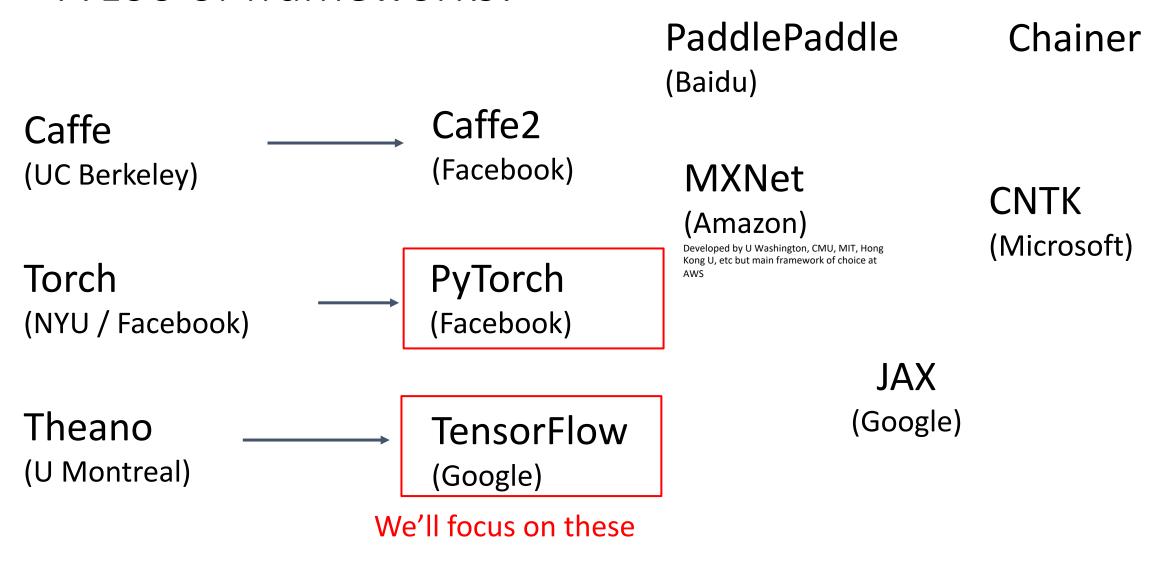
MXNet
(Amazon)

Developed by U Washington, CMU, MIT, Hong Kong U, etc but main framework of choice at

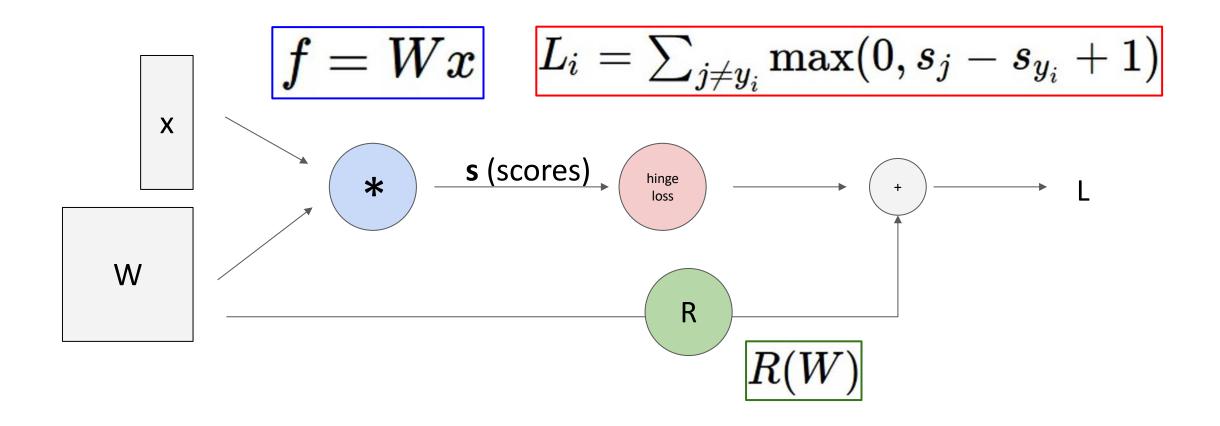
CNTK (Microsoft)

JAX (Google)

A zoo of frameworks!



Recall: Computational Graphs



The point of deep learning frameworks

- 1. Allow rapid prototyping of new ideas
- 2. Automatically compute gradients for you
- 3. Run it all efficiently on GPU (or TPU)

PyTorch

PyTorch: Versions

For this class we are using **PyTorch version 1.6** (Released July 2020)

Be careful if you are looking at older PyTorch code – the API changed a lot before 1.0 (0.3 to 0.4 had big changes!)

PyTorch: Fundamental Concepts

Tensor: Like a numpy array, but can run on GPU

Autograd: Package for building computational graphs out of Tensors, and automatically computing gradients

Module: A neural network layer; may store state or learnable weights

PyTorch: Fundamental Concepts

Tensor: Like a numpy array, but can run on GPU A1, A2, A3

Autograd: Package for building computational graphs out of Tensors, and automatically computing gradients

Module: A neural network layer; may store state or learnable weights

44, A5, A6

Running example: Train a two-layer ReLU network on random data with L2 loss

```
import torch
device = torch.device('cpu')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y pred = h relu.mm(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Create random tensors for data and weights

```
import torch
device = torch.device('cpu')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y pred = h relu.mm(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Forward pass: compute predictions and loss

```
import torch
device = torch.device('cpu')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y pred = h relu.mm(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Backward pass: manually compute gradients

```
import torch
device = torch.device('cpu')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y pred = h relu.mm(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Gradient descent step on weights

```
import torch
device = torch.device('cpu')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in, device=device)
y = torch.randn(N, D_out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h_relu = h.clamp(min=0)
    y pred = h relu.mm(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad h relu = grad y pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

To run on GPU, just use a different device!

```
import torch
device = torch.device('cuda:0')
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in, device=device)
y = torch.randn(N, D out, device=device)
w1 = torch.randn(D in, H, device=device)
w2 = torch.randn(H, D out, device=device)
learning rate = 1e-6
for t in range(500):
    h = x.mm(w1)
    h relu = h.clamp(min=0)
    y pred = h relu.mm(w2)
    loss = (y pred - y).pow(2).sum()
    grad y pred = 2.0 * (y pred - y)
    grad w2 = h relu.t().mm(grad y pred)
    grad_h_relu = grad_y_pred.mm(w2.t())
    grad h = grad h relu.clone()
    grad h[h < 0] = 0
    grad w1 = x.t().mm(grad h)
    w1 -= learning rate * grad w1
    w2 -= learning rate * grad w2
```

Creating Tensors with requires_grad=True enables autograd

Operations on Tensors with requires_grad=True cause PyTorch to build a computational graph

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

We will not want gradients (of loss) with respect to data

Do want gradients with respect to weights

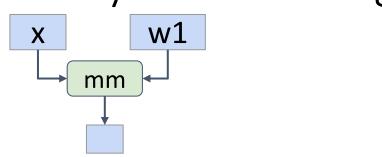
```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

Forward pass looks exactly the same as before, but we don't need to track intermediate values - PyTorch keeps track of them for us in the graph

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

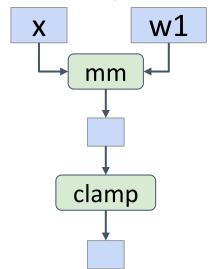
Computes gradients with respect to all inputs that have requires_grad=True!

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```



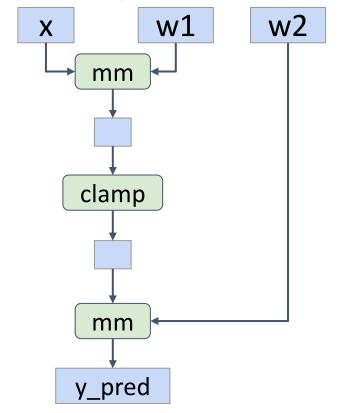
Every operation on a tensor with requires_grad=True will add to the computational graph, and the resulting tensors will also have requires_grad=True

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

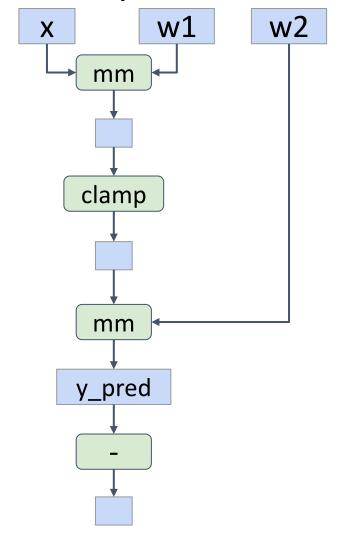


Every operation on a tensor with requires_grad=True will add to the computational graph, and the resulting tensors will also have requires grad=True

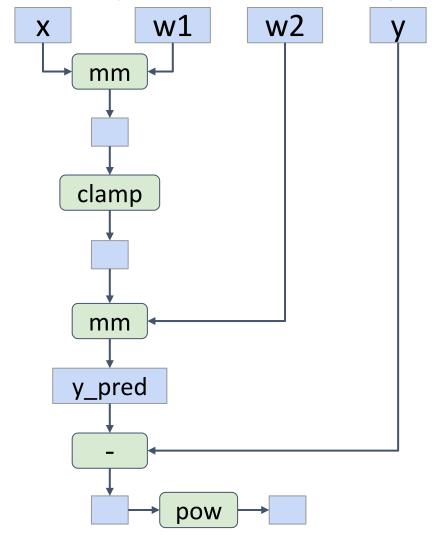
```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y_{pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```



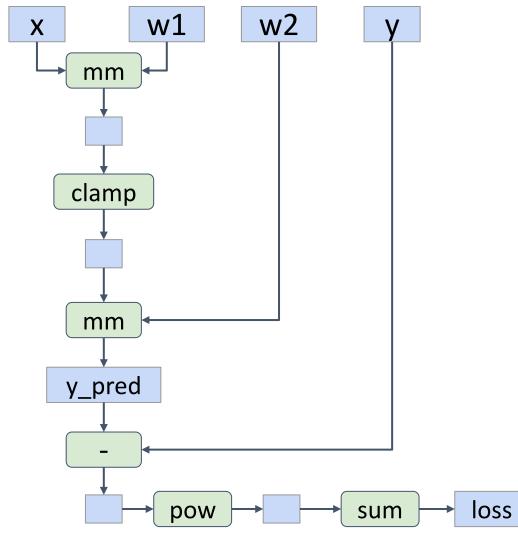
```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero_()
```



```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y_pred = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero_()
```



```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```



```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y_pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

```
w2
         w1
X
    mm
   clamp
                              Backprop to
    mm
                              all inputs that
  y_pred
                              require grad
                                  loss
           pow
                         sum
```

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

x | w1

w2

У

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

x | w1

w2

У

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

Make gradient step on weights

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no_grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

x w1

w2

У

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

Set gradients to zero – forgetting this is a common bug!

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

x w1

w2

У

After backward finishes, gradients are **accumulated** into w1.grad and w2.grad and the graph is destroyed

Tell PyTorch not to build a graph for these operations

```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
    with torch.no grad():
        w1 -= learning_rate * w1.grad
        w2 -= learning_rate * w2.grad
        wl.grad.zero ()
        w2.grad.zero ()
```

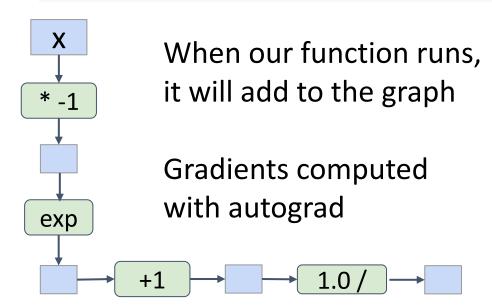
Can define new operations using Python functions

```
def sigmoid(x):
   return 1.0 / (1.0 + (-x).exp())
```

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
for t in range(500):
  y pred = sigmoid(x.mm(w1)).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  if t % 50 == 0:
    print(t, loss.item())
  with torch.no grad():
    w1 -= learning_rate * w1.grad
    w2 -= learning rate * w2.grad
    wl.grad.zero ()
    w2.grad.zero ()
```

Can define new operations using Python functions

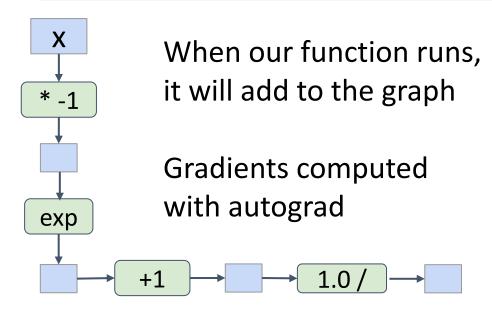
```
def sigmoid(x):
   return 1.0 / (1.0 + (-x).exp())
```



```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
y = torch.randn(N, D out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
for t in range(500):
 y pred = sigmoid(x.mm(w1)).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  if t % 50 == 0:
    print(t, loss.item())
  with torch.no grad():
    w1 -= learning rate * w1.grad
    w2 -= learning rate * w2.grad
   wl.grad.zero ()
   w2.grad.zero ()
```

Can define new operations using Python functions

```
def sigmoid(x):
   return 1.0 / (1.0 + (-x).exp())
```



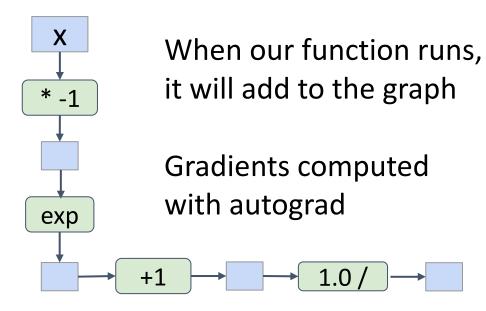
Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
  @staticmethod
  def forward(ctx, x):
    y = 1.0 / (1.0 + (-x).exp())
    ctx.save for backward(y)
    return y
  @staticmethod
  def backward(ctx, grad y):
    y, = ctx.saved tensors
    grad x = grad y * y * (1.0 - y)
    return grad x
def sigmoid(x):
  return Sigmoid.apply(x)
```

Recall:
$$\frac{\partial}{\partial x} \Big[\sigma(x) \Big] = (1 - \sigma(x)) \sigma(x)$$

Can define new operations using Python functions

```
def sigmoid(x):
   return 1.0 / (1.0 + (-x).exp())
```



Define new autograd operators by subclassing Function, define forward and backward

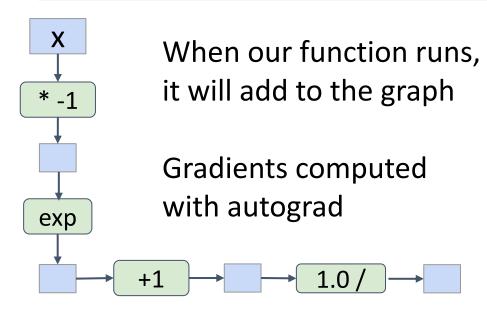
```
class Sigmoid(torch.autograd.Function):
  @staticmethod
  def forward(ctx, x):
    y = 1.0 / (1.0 + (-x).exp())
    ctx.save for backward(y)
    return y
  @staticmethod
  def backward(ctx, grad_y):
    y, = ctx.saved tensors
    grad x = grad y * y * (1.0 - y)
    return grad x
def sigmoid(x):
  return Sigmoid.apply(x)
```

Now when our function runs, it adds one node to the graph!



Can define new operations using Python functions

```
def sigmoid(x):
   return 1.0 / (1.0 + (-x).exp())
```



Define new autograd operators by subclassing Function, define forward and backward

```
class Sigmoid(torch.autograd.Function):
  @staticmethod
  def forward(ctx, x):
    y = 1.0 / (1.0 + (-x).exp())
    ctx.save for backward(y)
    return y
  @staticmethod
  def backward(ctx, grad_y):
    y, = ctx.saved tensors
    grad x = grad y * y * (1.0 - y)
    return grad x
def sigmoid(x):
  return Sigmoid.apply(x)
```

In practice this is pretty rare – in most cases Python functions are good enough

Higher-level wrapper for working with neural nets

Use this! It will make your life easier

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

Object-oriented API: Define model object as sequence of layers objects, each of which holds weight tensors

```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

Forward pass: Feed data to model and compute loss

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

Forward pass: Feed data to model and compute loss

torch.nn.functional has useful helpers like loss functions

```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning_rate * param.grad
    model.zero grad()
```

Backward pass: compute gradient with respect to all model weights (they have requires_grad=True)

```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-2
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    with torch.no grad():
        for param in model.parameters():
            param -= learning rate * param.grad
    model.zero grad()
```

Make gradient step on each model parameter (with gradients disabled)

PyTorch: optim

Use an **optimizer** for different update rules

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D_out))
<u>learning rate = 1e-4</u>
optimizer = torch.optim.Adam(model.parameters(),
                              lr=learning_rate)
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

PyTorch: optim

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
          torch.nn.Linear(D_in, H),
          torch.nn.ReLU(),
          torch.nn.Linear(H, D out))
learning rate = 1e-4
optimizer = torch.optim.Adam(model.parameters(),
                             lr=learning_rate)
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

After computing gradients, use optimizer to update and zero gradients

A PyTorch **Module** is a neural net layer; it inputs and outputs Tensors

Modules can contain weights or other modules

Very common to define your own models or layers as custom Modules

```
import torch
class TwoLayerNet(torch.nn.Module):
    def init (self, D in, H, D out):
        super(TwoLayerNet, self). init ()
        self.linear1 = torch.nn.Linear(D in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

Define our whole model as a single Module

```
import torch
class TwoLayerNet(torch.nn.Module):
    def init (self, D in, H, D_out):
        super(TwoLayerNet, self). init ()
        self.linear1 = torch.nn.Linear(D in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

Initializer sets up two children (Modules can contain modules)

```
import torch
class TwoLayerNet(torch.nn.Module):
    def init (self, D in, H, D out):
        super(TwoLayerNet, self). init ()
        self.linear1 = torch.nn.Linear(D in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

Define forward pass using child modules and tensor operations

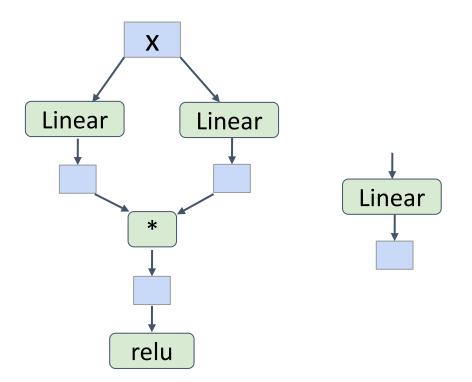
No need to define backward - autograd will handle it

```
import torch
class TwoLayerNet(torch.nn.Module):
    def init (self, D in, H, D out):
        super(TwoLayerNet, self). init ()
        self.linear1 = torch.nn.Linear(D in, H)
        self.linear2 = torch.nn.Linear(H, D out)
    def forward(self, x):
        h relu = self.linear1(x).clamp(min=0)
        y pred = self.linear2(h relu)
        return y pred
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
for t in range(500):
    y \text{ pred} = \text{model}(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

Very common to mix and match custom Module subclasses and Sequential containers

```
import torch
class ParallelBlock(torch.nn.Module):
    def init (self, D in, D out):
        super(ParallelBlock, self). init ()
        self.linear1 = torch.nn.Linear(D in, D out)
        self.linear2 = torch.nn.Linear(D in, D out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
            ParallelBlock(D in, H),
            ParallelBlock(H, H),
            torch.nn.Linear(H, D out))
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

Define network component as a Module subclass



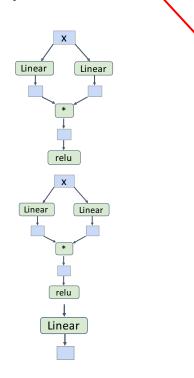
import torch

```
class ParallelBlock(torch.nn.Module):
    def __init__(self, D_in, D_out):
        super(ParallelBlock, self).__init__()
        self.linear1 = torch.nn.Linear(D_in, D_out)
        self.linear2 = torch.nn.Linear(D_in, D_out)

def forward(self, x):
    h1 = self.linear1(x)
    h2 = self.linear2(x)
    return (h1 * h2).clamp(min=0)
```

Stack multiple instances of the component in a sequential

Very easy to quickly build complex network architectures!



```
import torch
class ParallelBlock(torch.nn.Module):
    def init (self, D in, D out):
        super(ParallelBlock, self). init ()
        self.linear1 = torch.nn.Linear(D in, D out)
        self.linear2 = torch.nn.Linear(D in, D out)
    def forward(self, x):
        h1 = self.linear1(x)
        h2 = self.linear2(x)
        return (h1 * h2).clamp(min=0)
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
model = torch.nn.Sequential(
            ParallelBlock(D in, H),
            ParallelBlock(H, H),
            torch.nn.Linear(H, D out))
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
for t in range(500):
    y pred = model(x)
    loss = torch.nn.functional.mse loss(y pred, y)
    loss.backward()
    optimizer.step()
    optimizer.zero grad()
```

PyTorch: DataLoaders

A **DataLoader** wraps a **Dataset** and provides minibatching, shuffling, multithreading, for you

When you need to load custom data, just write your own Dataset class

```
import torch
from torch.utils.data import TensorDataset, DataLoader
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
loader = DataLoader(TensorDataset(x, y), batch_size=8)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-2)
for epoch in range(20):
    for x batch, y batch in loader:
        y pred = model(x batch)
        loss = torch.nn.functional.mse loss(y pred, y batch)
        loss.backward()
        optimizer.step()
        optimizer.zero grad()
```

PyTorch: DataLoaders

Iterate over loader to form minibatches

```
import torch
from torch.utils.data import TensorDataset, DataLoader
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
loader = DataLoader(TensorDataset(x, y), batch size=8)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-2)
for epoch in range(20):
    for x batch, y batch in loader:
        y pred = model(x batch)
        loss = torch.nn.functional.mse loss(y pred, y batch)
        loss.backward()
        optimizer.step()
        optimizer.zero grad()
```

PyTorch: DataLoaders

Iterate over loader to form minibatches

```
import torch
from torch.utils.data import TensorDataset, DataLoader
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
loader = DataLoader(TensorDataset(x, y), batch size=8)
model = TwoLayerNet(D in, H, D out)
optimizer = torch.optim.SGD(model.parameters(), lr=1e-2)
for epoch in range(20):
    for x batch, y batch in loader:
        y pred = model(x batch)
        loss = torch.nn.functional.mse loss(y pred, y batch)
        loss.backward()
        optimizer.step()
        optimizer.zero grad()
```

PyTorch: Pretrained Models

Super easy to use pretrained models with torchvision https://github.com/pytorch/vision

```
import torch
import torchvision

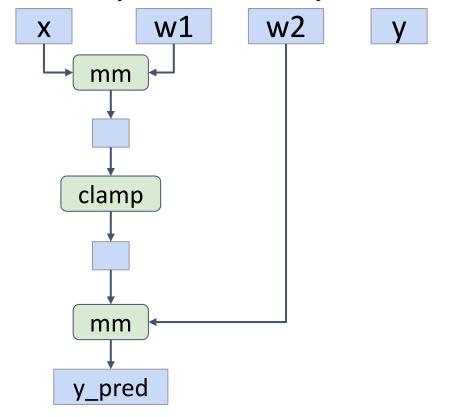
alexnet = torchvision.models.alexnet(pretrained=True)
vgg16 = torchvision.models.vgg16(pretrained=True)
resnet101 = torchvision.models.resnet101(pretrained=True)
```

```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

x w1 w2 y

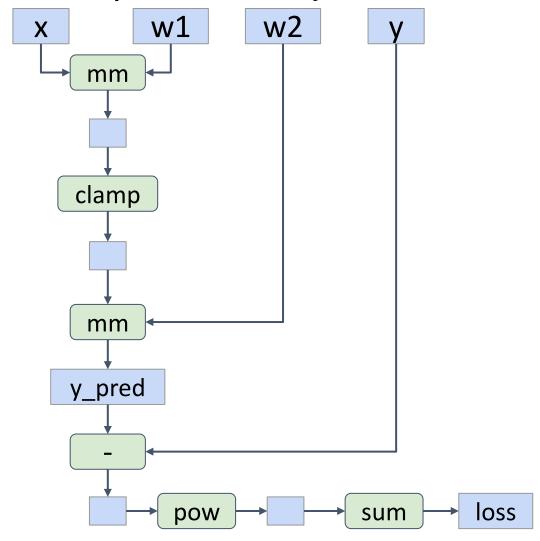
```
import torch
N, D_in, H, D_out = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Create Tensor objects



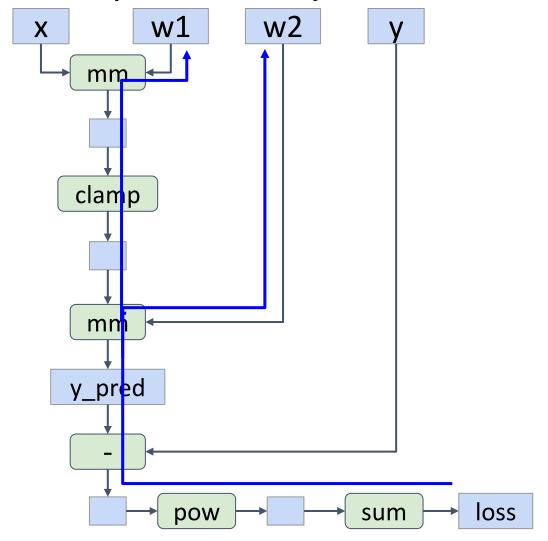
```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Build graph data structure AND perform computation



```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Build graph data structure AND perform computation



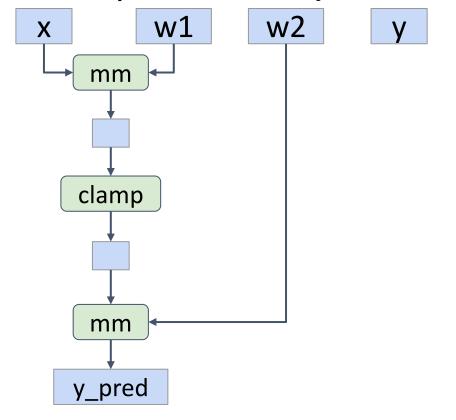
```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Perform backprop, throw away graph

x w1 w2 y

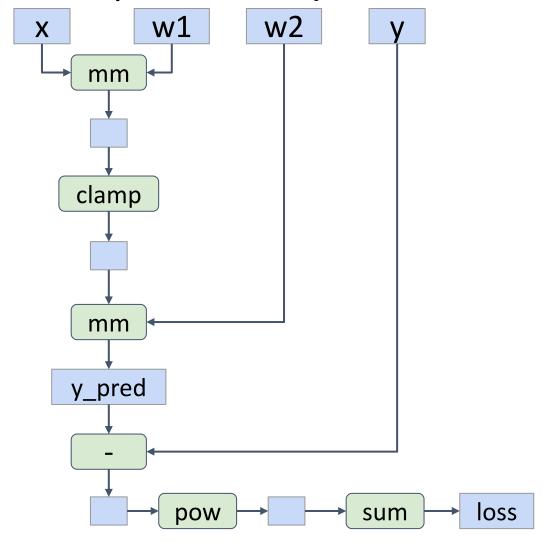
```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning_rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Perform backprop, throw away graph



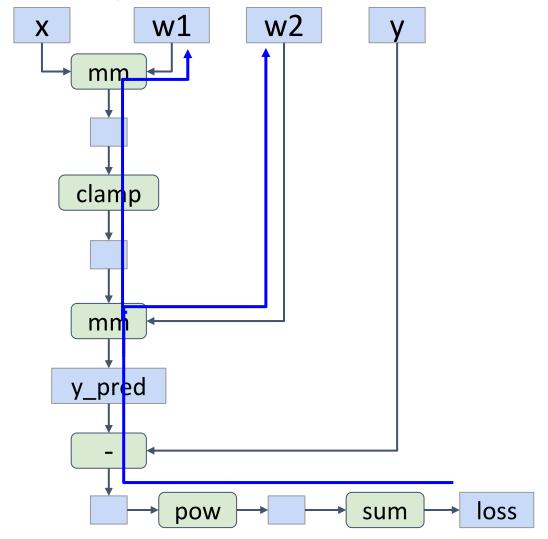
```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Build graph data structure AND perform computation



```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Build graph data structure AND perform computation



```
import torch
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D_in)
y = torch.randn(N, D_out)
w1 = torch.randn(D_in, H, requires_grad=True)
w2 = torch.randn(H, D_out, requires_grad=True)
learning rate = 1e-6
for t in range(500):
    y \text{ pred} = x.mm(w1).clamp(min=0).mm(w2)
    loss = (y pred - y).pow(2).sum()
    loss.backward()
```

Perform backprop, throw away graph

Dynamic graphs let you use regular Python control flow during the forward pass!

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
prev loss = 5.0
for t in range(500):
 w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  prev loss = loss.item()
```

Dynamic graphs let you use regular Python control flow during the forward pass!

Initialize two different weight matrices for second layer

```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D_out, requires_grad=True)
w2b = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
prev loss = 5.0
for t in range(500):
  w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  prev loss = loss.item()
```

Dynamic graphs let you use regular Python control flow during the forward pass!

Decide which one to use at each layer based on loss at previous iteration

(this model doesn't makes sense! Just a simple dynamic example)

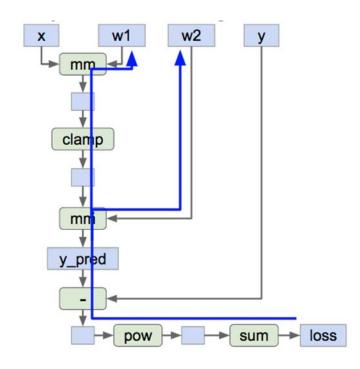
```
import torch
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires_grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
learning rate = 1e-6
prev loss = 5.0
for t in range(500):
  w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  loss.backward()
  prev loss = loss.item()
```

Alternative: Static Computation Graphs

Alternative: **Static** graphs

Step 1: Build computational graph describing our computation (including finding paths for backprop)

Step 2: Reuse the same graph on every iteration



```
graph = build_graph()

for x_batch, y_batch in loader:
   run_graph(graph, x=x_batch, y=y_batch)
```

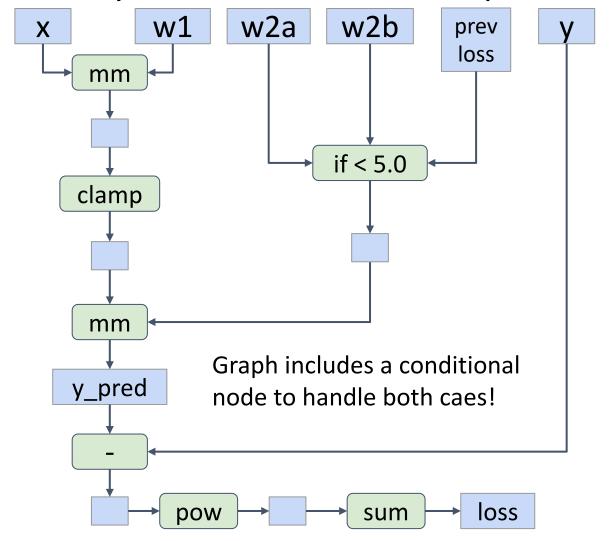
Define model as a Python function

```
import torch
def model(x, y, w1, w2a, w2b, prev loss):
  w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D_{in}, H, D_{out} = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
graph = torch.jit.script(model)
prev loss = 5.0
learning rate = 1e-6
for t in range(500):
  loss = graph(x, y, w1, w2a, w2b, prev_loss)
  loss.backward()
  prev loss = loss.item()
```

Just-In-Time compilation: Introspect the source code of the function, **compile** it into a graph object.

Lots of magic here!

```
import torch
def model(x, y, w1, w2a, w2b, prev loss):
  w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
graph = torch.jit.script(model)
prev loss = 5.0
learning rate = 1e-6
for t in range(500):
  loss = graph(x, y, w1, w2a, w2b, prev loss)
  loss.backward()
  prev loss = loss.item()
```



```
import torch
def model(x, y, w1, w2a, w2b, prev loss):
  w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
graph = torch.jit.script(model)
prev loss = 5.0
learning rate = 1e-6
for t in range(500):
  loss = graph(x, y, w1, w2a, w2b, prev loss)
  loss.backward()
  prev loss = loss.item()
```

Use our compiled graph object at each forward pass

```
import torch
def model(x, y, w1, w2a, w2b, prev loss):
  w2 = w2a if prev loss < 5.0 else w2b
  y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
graph = torch.jit.script(model)
prev loss = 5.0
learning rate = 1e-6
for t in range(500):
 loss = graph(x, y, w1, w2a, w2b, prev_loss)
  loss.backward()
  prev loss = loss.item()
```

Even easier: add **annotation** to function, Python function compiled to a graph when it is defined

Calling function uses graph

```
import torch
@torch.jit.script
def model(x, y, w1, w2a, w2b, prev loss):
  w2 = w2a if prev loss < 5.0 else w2b
 y pred = x.mm(w1).clamp(min=0).mm(w2)
  loss = (y pred - y).pow(2).sum()
  return loss
N, D in, H, D out = 64, 1000, 100, 10
x = torch.randn(N, D in)
y = torch.randn(N, D_out)
w1 = torch.randn(D in, H, requires grad=True)
w2a = torch.randn(H, D out, requires grad=True)
w2b = torch.randn(H, D out, requires grad=True)
prev loss = 5.0
learning rate = 1e-6
for t in range(500):
  loss = model(x, y, w1, w2a, w2b, prev loss)
  loss.backward()
  prev loss = loss.item()
```

Static vs Dynamic Graphs: Optimization

With static graphs, framework can **optimize** the graph for you before it runs!



Conv ReLU

Conv

ReLU

Conv

ReLU

Equivalent graph with **fused operations**

Conv+ReLU

Conv+ReLU

Conv+ReLU

Static vs Dynamic Graphs: Serialization

Static

Once graph is built, can serialize it and run it without the code that built the graph!

e.g. train model in Python, deploy in C++

Dynamic

Graph building and execution are intertwined, so always need to keep code around

Static vs Dynamic Graphs: Debugging

Static

Lots of indirection between the code you write and the code that runs – can be hard to debug, benchmark, etc

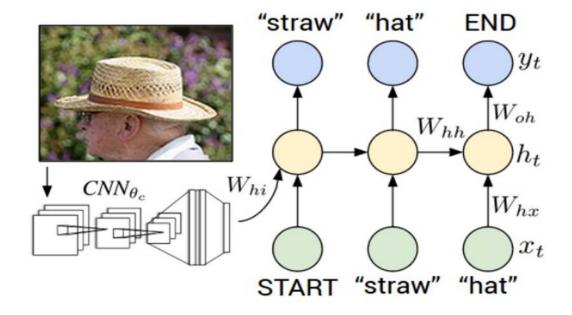
Dynamic

The code you write is the code that runs! Easy to reason about, debug, profile, etc

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks

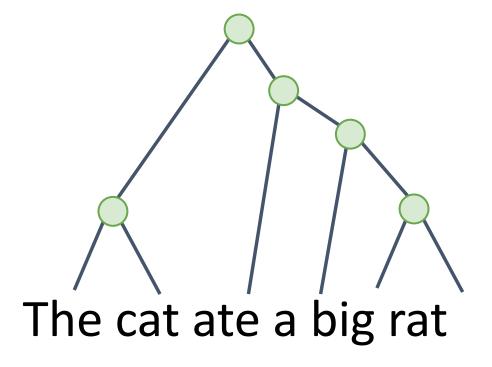


Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks
- Recursive Networks

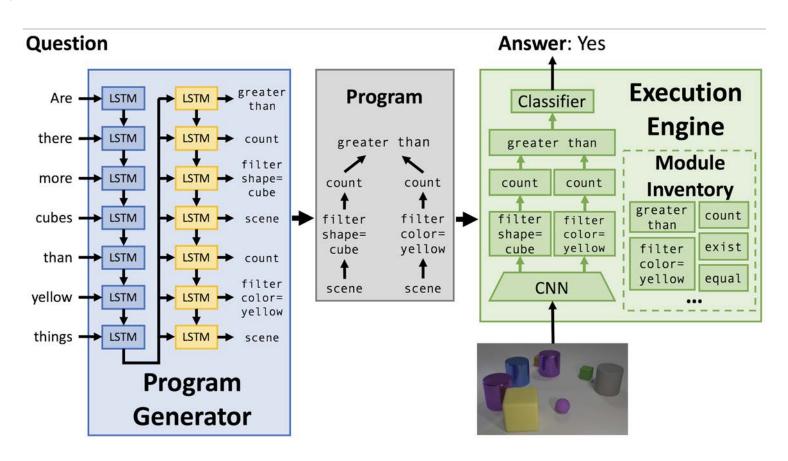


Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks
- Recursive Networks
- Modular Networks



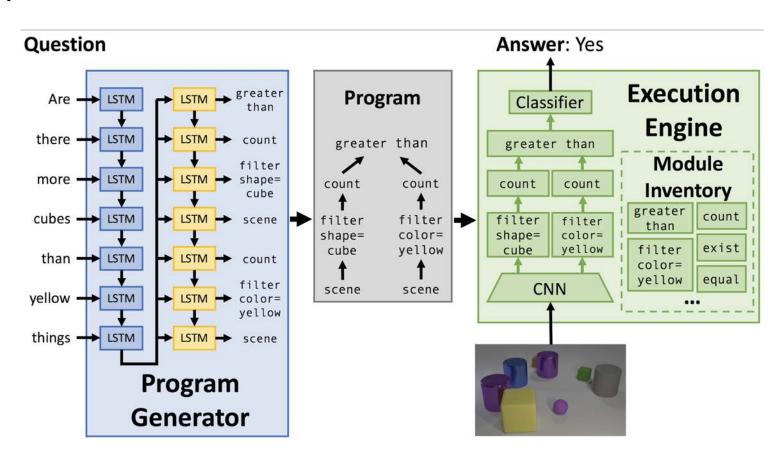
Andreas et al, "Neural Module Networks", CVPR 2016
Andreas et al, "Learning to Compose Neural Networks for Question Answering", NAACL 2016
Johnson et al, "Inferring and Executing Programs for Visual Reasoning", ICCV 2017

Dynamic Graph Applications

Model structure depends on the input:

- Recurrent Networks
- Recursive Networks
- Modular Networks
- (Your idea here!)

Justin Johnson



Andreas et al, "Neural Module Networks", CVPR 2016 Andreas et al, "Learning to Compose Neural Networks for Question Answering", NAACL 2016 Johnson et al, "Inferring and Executing Programs for Visual Reasoning", ICCV 2017

TensorFlow

TensorFlow Versions

TensorFlow 1.0

- Final release: 1.15.3
- Default: static graphs
- Optional: dynamic graphs (eager mode)

TensorFlow 2.0

- Current release: 2.3.1
 - Released 9/24
- Default: dynamic graphs
- Optional: static graphs

TensorFlow 1.0: Static Graphs

import numpy as np
import tensorflow as tf

(Assume imports at the top of each snippet)

```
N, D, H = 64, 1000, 100
x = tf.placeholder(tf.float32, shape=(N, D))
y = tf.placeholder(tf.float32, shape=(N, D))
w1 = tf.placeholder(tf.float32, shape=(D, H))
w2 = tf.placeholder(tf.float32, shape=(H, D))
h = tf.maximum(tf.matmul(x, w1), 0)
y pred = tf.matmul(h, w2)
diff = y pred - y
loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
grad w1, grad w2 = tf.gradients(loss, [w1, w2])
with tf.Session() as sess:
    values = {x: np.random.randn(N, D),
              wl: np.random.randn(D, H),
              w2: np.random.randn(H, D),
              y: np.random.randn(N, D),}
    out = sess.run([loss, grad w1, grad w2],
                   feed dict=values)
    loss_val, grad_wl_val, grad_w2_val = out
```

TensorFlow 1.0: Static Graphs

First **define** computational graph

Then **run** the graph many times

```
N, D, H = 64, 1000, 100
x = tf.placeholder(tf.float32, shape=(N, D))
y = tf.placeholder(tf.float32, shape=(N, D))
w1 = tf.placeholder(tf.float32, shape=(D, H))
w2 = tf.placeholder(tf.float32, shape=(H, D))
h = tf.maximum(tf.matmul(x, w1), 0)
y pred = tf.matmul(h, w2)
diff = y pred - y
loss = tf.reduce_mean(tf.reduce_sum(diff ** 2, axis=1))
grad_w1, grad_w2 = tf.gradients(loss, [w1, w2])
with tf.Session() as sess:
    values = {x: np.random.randn(N, D),
              wl: np.random.randn(D, H),
              w2: np.random.randn(H, D),
              y: np.random.randn(N, D),}
    out = sess.run([loss, grad w1, grad w2],
                   feed dict=values)
    loss_val, grad_w1_val, grad_w2_val = out
```

Create TensorFlow Tensors for data and weights

Weights need to be wrapped in tf.Variable so we can mutate them

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
```

Scope forward pass under a GradientTape to tell TensorFlow to start building a graph

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
```

Ask the tape to compute gradients

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
```

Gradient descent step, update weights

```
import tensorflow as tf
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
```

TensorFlow 2.0: **Static Graphs**

Define a function that implements forward, backward, and update

Annotating with tf.function will compile the function into a graph! (similar to torch.jit.script)

```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
  return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  loss = step(x, y, w1, w2)
```

TensorFlow 2.0: **Static Graphs**

Define a function that implements forward, backward, and update

Annotating with tf.function will compile the function into a graph! (similar to torch.jit.script)

(note TF graph can include gradient computation and update, unlike PyTorch)

```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
  return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  loss = step(x, y, w1, w2)
```

TensorFlow 2.0: **Static Graphs**

Call the compiled step function in the training loop

```
@tf.function
def step(x, y, w1, w2):
  with tf.GradientTape() as tape:
    h = tf.maximum(tf.matmul(x, w1), 0)
    y pred = tf.matmul(h, w2)
    diff = y pred - y
    loss = tf.reduce mean(tf.reduce sum(diff ** 2, axis=1))
  grad w1, grad w2 = tape.gradient(loss, [w1, w2])
  w1.assign(w1 - learning rate * grad w1)
  w2.assign(w2 - learning rate * grad w2)
  return loss
N, Din, H, Dout = 16, 1000, 100, 10
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
w1 = tf.Variable(tf.random.normal((Din, H)))
w2 = tf.Variable(tf.random.normal((H, Dout)))
learning rate = 1e-6
for t in range(1000):
  loss = step(x, y, w1, w2)
```

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
 with tf.GradientTape() as tape:
   y pred = model(x)
   loss = loss fn(y pred, y)
 grads = tape.gradient(loss, params)
 opt.apply gradients(zip(grads, params))
```

Object-oriented API: build the model as a stack of layers

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y pred = model(x)
    loss = loss_fn(y_pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

Keras gives you common loss functions and optimization algorithms

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y pred = model(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

Forward pass:

Compute loss, build graph

Backward pass: compute gradients

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
  with tf.GradientTape() as tape:
    y pred = model(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

Optimizer object updates parameters

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
for t in range(1000):
 with tf.GradientTape() as tape:
   y pred = model(x)
    loss = loss fn(y pred, y)
  grads = tape.gradient(loss, params)
  opt.apply gradients(zip(grads, params))
```

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
def step():
 y pred = model(x)
  loss = loss fn(y pred, y)
  return loss
```

Define a function — that returns the loss

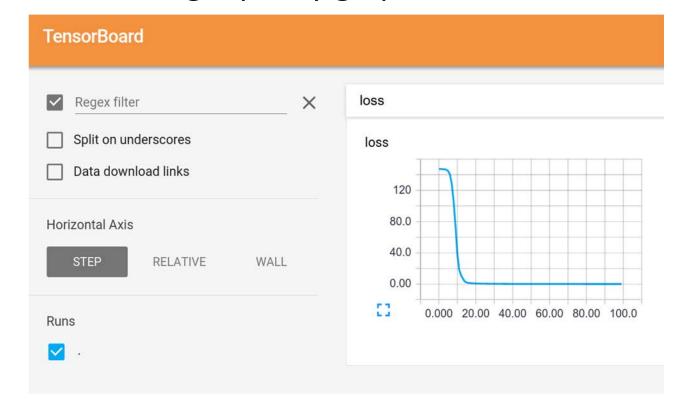
```
for t in range(1000):
   opt.minimize(step, params)
```

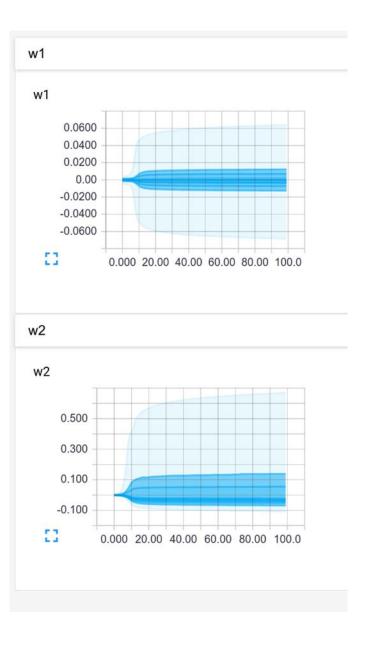
Optimizer computes gradients and updates parameters

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import InputLayer, Dense
N, Din, H, Dout = 16, 1000, 100, 10
model = Sequential()
model.add(InputLayer(input shape=(Din,)))
model.add(Dense(units=H, activation='relu'))
model.add(Dense(units=Dout))
params = model.trainable variables
loss fn = tf.keras.losses.MeanSquaredError()
opt = tf.keras.optimizers.SGD(learning rate=1e-6)
x = tf.random.normal((N, Din))
y = tf.random.normal((N, Dout))
def step():
 y pred = model(x)
  loss = loss fn(y pred, y)
  return loss
for t in range(1000):
  opt.minimize(step, params)
```

TensorBoard

Add logging to code to record loss, stats, etc Run server and get pretty graphs!

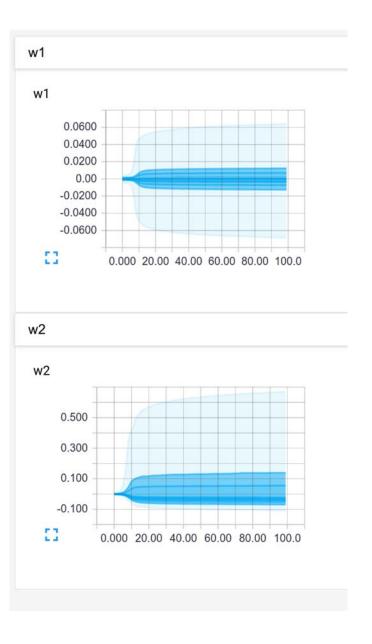




TensorBoard

Also works with PyTorch: torch.utils.tensorboard





PyTorch vs TensorFlow

PyTorch

- My personal favorite
- Clean, imperative API
- Easy dynamic graphs for debugging
- JIT allows static graphs for production
- Cannot use TPUs
- Not easy to deploy on mobile

TensorFlow 1.0

- Static graphs by default
- Can be confusing to debug
- API a bit messy

TensorFlow 2.0

- Dynamic by default
- Standardized on Keras API
- API still confusing

Summary: Hardware

CPU



GPU



TPU



Summary: Software

Static Graphs vs **Dynamic Graphs**

PyTorch vs TensorFlow

Next time: Training Neural Networks