

CSci370 Computer Architecture: Homework 2 (double-sided)

Due date: On or before Monday, March 30, 2020 in class

Absolutely no copying others' works

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- There are four algorithms discussed for multiplication and division. Make sure you are using the correct ones for the two questions below.
- The purpose of homeworks is for students to practice for the exams without others' help, so the penalty of mistakes will be minor.
- Without practicing for the exams properly, students would not be able to do well on the exams.

1. (Refined multiplication: 50%) Using a table similar to that shown in the Slide 8.6, calculate the product of the octal unsigned 6-bit integers 65_8 (or 110101_2) and 53_8 (or 101011_2) using the hardware and ~~4747~~ algorithm described in the figures of Slide 8.6. You should show the content of each register on each step.

Step	Operation	Multiplicand	Carry	Product = HILO	
0	Initialize	110101	0	000000101011	
1	Add or do nothing	110101	0	110101101011	
	shift			011010110101	
	Add or nothing		1	001111110101	011010
2	shift	110101		100111111010	110101
	Add or not		0	100111111010	001111
3	shift	110101		010011111011	
	Add or not		1	001000111101	011010
4	shift	110101		100100011100	110101
	Add or not		0	100100011100	001000
5	shift	110101		010010001111	
	Add or not		1	000111001111	010010
6	shift	110101		100011100111	110101
					000111

$$100011100111_2 = 4347_8 = 2279_{10}$$

$$\text{Difference} = \text{remainder} - \text{divisor}$$

2. (First-version division: 50%) Using a table similar to that shown in the Slide 8.10, calculate the octal unsigned 6-bit integer 65_8 (or 110101_2) divided by another octal unsigned 6-bit integer 16_8 (or 001110_2) using the hardware and algorithm described in the figures of Slide 8.10. You should show the content of each register on each step.

†Note that you have to actually show the differences in the procedures, not just the signs.

		Remainder	Divisor	Difference	Quotient
0	Initialize	000000110101	001110000000		000000
1	Shift and subtract	000000110101	000111000000	111001110101	000000
	Assign & set or not	000000110101	000111000000	111001110101	000000
2	Shift and subtract	000000110101	000011100000	11101010101	000000
	Assign & set or not	000000110101	000011100000	11101010101	000000
3	Shift and sub	000000110101	000001110000	111001110101	000000
	Assign & set or not	000000110101	000001110000	111001110101	000000
4	Shift and sub	000000110101	000000111000	11111111101	000000
	Assign & set or not	000000110101	000000111000	11111111101	000000
5	Shift and sub	000000110101	000000011100	000000011001	000000
	Assign & set or not	000000011001	000000011100	000000011001	000001
6	Shift and sub	000000011001	000000001110	000000001011	000010
	Assign and set or not	000000001011	000000001110	000000001011	000011

$$53 \div 14$$

$$3_{10} \text{ remainder } 11_{10} = 060011_2 \text{ remainder } 000000001011_2$$

$$\begin{array}{r} 000001119990 \\ 111110001111 \\ 000000000001 \\ 111100100000 \end{array}$$

$$\begin{array}{r} 111000111111 \\ 000000000001 \\ 110010000000 \end{array}$$

$$\begin{array}{r} 600000110101 \\ 111001000000 \\ 111001110101 \end{array}$$

$$\begin{array}{r} 111111000111 \\ 000000000001 \\ 111111001100 \end{array}$$

$$\begin{array}{r} 111110001111 \\ 000000000001 \\ 111110010000 \end{array}$$

$$\begin{array}{r} 00001110 \\ 11101000 \\ 11101011 \\ 11111111 \end{array}$$

$$\begin{array}{r} 00000110101 \\ 11111100100 \\ 000000011001 \end{array}$$

$$\begin{array}{r} 00011000 \\ 11100111 \\ 00000001 \\ 11101000 \end{array}$$

$$\begin{array}{r} 000000011001 \\ 111111100100 \\ 000000001011 \end{array}$$

$$\begin{array}{r} 000011100000 \\ 111100011111 \\ 000000000001 \\ 111100100000 \end{array}$$