

The *absolute value of  $x$* , denoted by  $|x|$ , is  $x$  if  $x \geq 0$  and  $-x$  otherwise. The *floor of  $x$* , denoted by  $\lfloor x \rfloor$ , is the greatest integer less than or equal to  $x$ . The *ceiling of  $x$* , denoted by  $\lceil x \rceil$ , is the least integer greater than or equal to  $x$ .

**Example 3.9.** It is the case that  $|-3| = 3 = |3|$ ,  $\lfloor 2.3 \rfloor = 2$ , and  $\lceil \pi \rceil = 4$ .