

316 9.22.09

## Extended BNF (EBNF)

- "syntactic sugars" for BNF, providing concise notations
- provide no additional power compared to original BNF
- any grammar defined by EBNF can always be defined by equivalent, original BNF

- mandatory multiple choice  $(\alpha_1 \mid \dots \mid \alpha_n)$  denotes a mandatory choice of exactly one  $\alpha_i$

- optional multiple choice  $[\alpha_1 \mid \dots \mid \alpha_n]$  denotes an optional choice of at most one  $\alpha_i$

- zero or more iterations  $\{\alpha_i\}$  denotes zero or more iterations of  $\alpha_i$ ,  
i.e.  $\epsilon, \alpha, \alpha\alpha, \alpha\alpha\alpha, \dots, \alpha^i, \dots$

- one or more iterations  $\{\alpha\}^+$  denotes one or more iterations of  $\alpha$ ,  
i.e.  $\alpha, \alpha\alpha, \alpha\alpha\alpha, \dots, \alpha^i, \dots$

$\{(\alpha_1 \mid \dots \mid \alpha_n)\}$  and  $\{(\alpha_1 \mid \dots \mid \alpha_n)\}^+$  may be abbreviated to, respectively,  
 $\{\alpha_1 \mid \dots \mid \alpha_n\}$  and  $\{\alpha_1 \mid \dots \mid \alpha_n\}^+$

$\langle \text{int} \rangle \rightarrow \{\langle \text{digit} \rangle\}^+$

$\langle \text{id} \rangle \rightarrow \langle \text{letter} \rangle \{\langle \text{digit} \rangle \mid \langle \text{digit} \rangle\}$

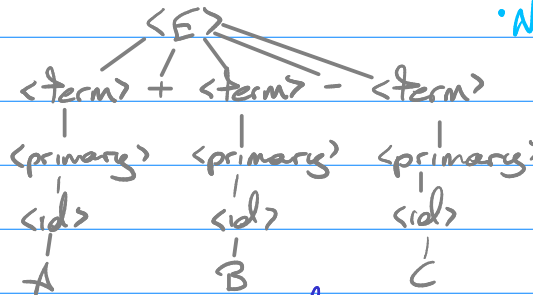
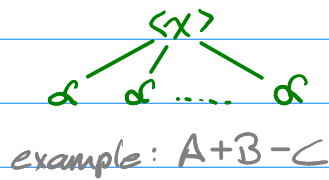
$\langle \text{float} \rangle \rightarrow \{\langle \text{digit} \rangle\}^+ "." \{\langle \text{digit} \rangle\}^+ [(\text{E}|\text{e})[+|-]\{\langle \text{digit} \rangle\}^+]$

$\langle \text{E} \rangle \rightarrow \langle \text{term} \rangle \{(+|-)\langle \text{term} \rangle\}$

$\langle \text{term} \rangle \rightarrow \langle \text{primary} \rangle \{ * | / \} \langle \text{primary} \rangle \}$

$\langle \text{primary} \rangle \rightarrow \langle \text{id} \rangle \mid \langle \text{int} \rangle \mid \langle \text{float} \rangle \mid "(" \langle \text{E} \rangle ")"$

Parse trees for  $\langle x \rangle \rightarrow \{\alpha\}, \langle x \rangle \rightarrow \{\alpha\}^+$



• Associativity information is not specified

• Need a comment about the internal associativity of operators

• In general, EBNF may introduce ambiguity, which must be resolved by concise comments

statements  
categories

$\langle S \rangle \Rightarrow \langle id \rangle = \langle E \rangle;$

if "("  $\langle B \rangle$  ")"  $\langle S \rangle$  [else  $\langle S \rangle$ ]

while "("  $\langle B \rangle$  ")"  $\langle S \rangle$  |

do  $\langle S \rangle$  while "("  $\langle B \rangle$  ")" |  
"{"  $\langle S List \rangle$  "}"

terminal  
symbols

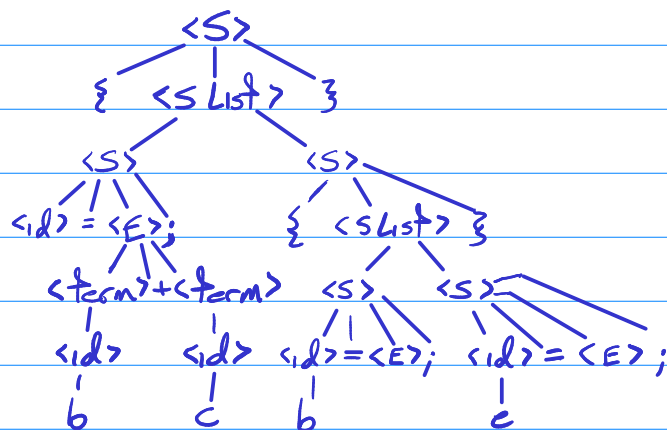
$\langle S List \rangle \Rightarrow \{\langle S \rangle\}^+$

← ambiguity!

comment: Each occurrence of  
else matches the closest preceding  
unmatched if.

Construct a parse tree for:

{  
   $a = b + c;$   
   $b = c / d;$   
   $e = b;$   
}



Metasymbols of BNF/EBNF

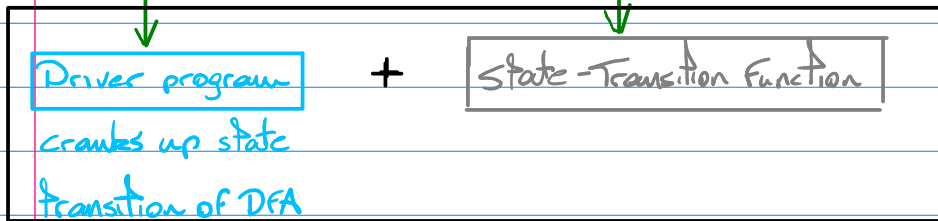
|, <, >, (, ), [, ], {, }

If any of these needs to be used as a terminal symbol, enclose it  
by "..." (example: "<", "|", "{", etc..)

## Methods of Lexical Analysis

- BNF/EBNF for tokens can be done by a small subset of BNF/EBNF corresponding to regular expressions (no need for any recursive production rules, but you need  $\{\alpha\}$  and  $\{\alpha\}^+$ )

Construct a Deterministic Finite Automaton (DFA)



Lexical Analyzer

## Review of DFA's

- A DFA consists of:

- a finite set  $I$  of symbols
- a finite set  $S$  of states
- a special state  $s \in S$ , called the initial (start) state
- a subset  $F \subseteq S$ , called the final state
- a state-transition function  $\delta: S \times I \rightarrow S$

Let  $\delta(s, i) = s'$  In diagram:  $\textcircled{s} \xrightarrow{i} \textcircled{s'}$  Use  $\textcircled{\phantom{x}}$  for final states

- $\langle \text{plus} \rangle \rightarrow +$        $\langle \text{RParen} \rangle \rightarrow ")"$
- $\langle \text{minus} \rangle \rightarrow -$        $\langle \text{int} \rangle \rightarrow \{\langle \text{digit} \rangle\}^+$
- $\langle \text{times} \rangle \rightarrow *$        $\langle \text{id} \rangle \rightarrow \langle \text{letter} \rangle \{\langle \text{letter} \rangle \mid \langle \text{digit} \rangle\}^*$
- $\langle \text{div} \rangle \rightarrow /$        $\langle \text{float} \rangle \rightarrow \{\langle \text{digit} \rangle\}^+ "." \{\langle \text{digit} \rangle\}^+$
- $\langle \text{LParen} \rangle \rightarrow "("$        $\langle \text{float E} \rangle \rightarrow \langle \text{float} \rangle (E \mid e) [+ \mid -] \{\langle \text{digit} \rangle\}^+$
- $\langle \text{digit} \rangle \rightarrow 0 \mid 1 \mid \dots \mid 9$        $\langle \text{letter} \rangle \rightarrow a \mid b \mid \dots \mid z \mid A \mid B \mid \dots \mid Z$

