

Quantitative Methods with RStudio: Application for Management and Business Research

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Welcome

This is the code version of *Quantitative Methods with RStudio: Application for Management and Business Research*, a book released in 2024 by IPB Press. The book was written by Muhammad Firdaus, Farit M Afendi, Deri Siswara, and Nafisa Berliana Indah Pratiwi. You can order the full version here, which includes more detailed explanations.

Management quantitative analysis is widely utilized by students, lecturers, and researchers in Indonesia. This book aims to enhance the reputation of education and research in the country by presenting a variety of alternative analysis tools that are commonly used. Managers must accurately synthesize information during the decision-making process and prioritize various options precisely. Additionally, large volumes of transformed data such as customer identities and characteristics or consumer behavior survey results need to be synthesized properly.

The first chapter introduces RStudio software and the R programming language, while the second chapter focuses on nonparametric statistical analysis including correlation analysis of two nonparametric variables and causality relationships. Chapter three discusses logistic regression analysis for making practical decisions, followed by discriminant analysis in chapter four which models problems involving one dependent variable influenced by multiple independent variables.

Chapter five covers principal component analysis (PCA) and biplots to reduce a large selection of research variables into more compact dimensions. Chapter six delves into cluster analysis useful for mapping multiple entities whereas chapter seven comprehensively discusses factor analysis along with structural equation modeling (SEM), including PLS-SEM widely used for various problems involving latent variables such as prosperity, loyalty, and company performance.

The final chapter explores Analytic Hierarchy Process (AHP) aimed at determining priority choices based on hierarchical decision hierarchy using freely accessible RStudio software across all methods presented in this book. Updates will be made frequently.

This book may contain bugs/errors which readers can report at *deri-siswarads@gmail.com*

Chapter 1

Basics of R

1.1 Introduction

```
A <- 2
```

```
A # Print A
```

```
[1] 2
```

```
A = 2
```

```
A
```

```
[1] 2
```

```
B <- "Halo Semua"
```

```
B
```

```
[1] "Halo Semua"
```

```
a<-10 # Space is not sensitive but lettercase is sensitive.
```

```
A
```

```
[1] 2
```

```
a
```

```
[1] 10
```

```
# Arithmetic operation
```

```
x <- 5
```

```
y <- 3
```

```
x + y
```

```
[1] 8
```

```
x - y
```

```
[1] 2
```

```
x * y
```

```
[1] 15
```

```
x / y
```

```
[1] 1.666667
```

```
# Logic operation
```

```
a <- TRUE
```

```
b <- FALSE
```

```
a & b
```

```
[1] FALSE
```

```
a | b
```

```
[1] TRUE
```

```
!a
```

```
[1] FALSE
```

```
x <- 5
```

```
y <- 3
```

```
x > y
```

```
[1] TRUE
```

```
x < y
```

```
[1] FALSE
```

```
x == y
```

```
[1] FALSE
```

```
x >= y
```

```
[1] TRUE
```

```
x <= y
```

```
[1] FALSE
```

1.2 Types of Objects in R

1.2.1 Vector

```
a1 <- c(2,4,7,3) # Numeric vector
a2 <- c("one","two","three") # Character vector
a3 <- c(TRUE,TRUE,TRUE,FALSE,TRUE,FALSE) # Logical vector
```

```
a1
```

```
[1] 2 4 7 3
```

```
a3[4]
```

```
[1] FALSE
```

```
a2[c(1,3)]
```

```
[1] "one"    "three"
```

```
a1[-1]
```

```
[1] 4 7 3
```

```
a1[2:4]
```

```
[1] 4 7 3
```

```
a <- c(1, 2, 3)
```

```
b <- c(4, 5, 6)
```

```
c <- c(a, b)
```

```
c
```

```
[1] 1 2 3 4 5 6
```

```
c[1:3]
```

```
[1] 1 2 3
```

```
d <- a + b
```

```
d
```

```
[1] 5 7 9
```

```
a4 <- 1:12
```

```
b1 <- matrix(a4,3,4)
```

```
b2 <- matrix(a4,3,4,byrow=TRUE)
```

```
b3 <- matrix(1:14,4,4)
```

```
b1
```

```
      [,1] [,2] [,3] [,4]
[1,]    1    4    7   10
[2,]    2    5    8   11
```

```
[3,]    3    6    9   12
```

```
b2
```

```
      [,1] [,2] [,3] [,4]
[1,]     1     2     3     4
[2,]     5     6     7     8
[3,]     9    10    11    12
```

```
b3
```

```
      [,1] [,2] [,3] [,4]
[1,]     1     5     9    13
[2,]     2     6    10    14
[3,]     3     7    11     1
[4,]     4     8    12     2
```

```
b2[2,3]
```

```
[1] 7
```

```
b2[1:2,]
```

```
      [,1] [,2] [,3] [,4]
[1,]     1     2     3     4
[2,]     5     6     7     8
```

```
b2[c(1,3),-2]
```

```
      [,1] [,2] [,3]
[1,]     1     3     4
[2,]     9    11    12
```

```
dim(b2)
```

```
[1] 3 4
```

```
m1 <- matrix(c(1, 2, 3, 4, 5, 6), nrow = 2, ncol = 3)
m2 <- matrix(c(7, 8, 9, 10, 11, 12), nrow = 2, ncol = 3)
```

```
m3 <- m1 + m2
```

```
m3
```

```
      [,1] [,2] [,3]
[1,]     8    12    16
[2,]    10    14    18
```

```
m4 <- m1 %*% t(m2)
```

```
m4
```

```
      [,1] [,2]
[1,]    89    98
[2,]   116   128
```

1.2.2 Factor

```
a5 <- c("A","B","AB","O")
d1 <- factor(a5)
levels(d1)
```

```
[1] "A" "AB" "B" "O"
```

```
levels(d1) <- c("Darah A","Darah AB","Darah B","Darah O")
d1
```

```
[1] Darah A Darah B Darah AB Darah O
Levels: Darah A Darah AB Darah B Darah O
```

```
a6 <- c("SMA","SD","SMP","SMA","SMA","SMA","SMA","SMA","SMA","SMA","SMA","SMA","SMA")
d5 <- factor(a6, levels=c("SD","SMP","SMA")) # Skala pengukuran ordinal
levels(d5)
```

```
[1] "SD" "SMP" "SMA"
```

```
d5
```

```
[1] SMA SD SMP SMA SMA SMA SMA SMA SMA SMA SMA SMA SMA
Levels: SD SMP SMA
```

1.2.3 List

```
a1; b2; d1
```

```
[1] 2 4 7 3
```

```
      [,1] [,2] [,3] [,4]
[1,]    1    2    3    4
[2,]    5    6    7    8
[3,]    9   10   11   12
```

```
[1] Darah A Darah B Darah AB Darah O
Levels: Darah A Darah AB Darah B Darah O
```

```
e1 <- list(a1,b2,d1)
e2 <- list(vect=a1,mat=b2,fac=d1)
e1
```

```
[[1]]
```

```
[1] 2 4 7 3
```

```
[[2]]
```

```
      [,1] [,2] [,3] [,4]
[1,]    1    2    3    4
[2,]    5    6    7    8
[3,]    9   10   11   12
```

```
[[3]]
[1] Darah A   Darah B   Darah AB Darah O
Levels: Darah A Darah AB Darah B Darah O
```

```
e2
```

```
$vect
[1] 2 4 7 3
```

```
$mat
      [,1] [,2] [,3] [,4]
[1,]     1     2     3     4
[2,]     5     6     7     8
[3,]     9    10    11    12
```

```
$fac
[1] Darah A   Darah B   Darah AB Darah O
Levels: Darah A Darah AB Darah B Darah O
```

```
e1[[1]][2]
```

```
[1] 4
```

```
e2$fac
```

```
[1] Darah A   Darah B   Darah AB Darah O
Levels: Darah A Darah AB Darah B Darah O
```

```
e2[2]
```

```
$mat
      [,1] [,2] [,3] [,4]
[1,]     1     2     3     4
[2,]     5     6     7     8
[3,]     9    10    11    12
```

```
names(e2)
```

```
[1] "vect" "mat"  "fac"
```

1.2.4 Data Frame

```
Angka <- 11:15
Huruf <- factor(LETTERS[6:10])
f1 <- data.frame(Angka,Huruf)
f1
```

```
  Angka Huruf
1     11     F
```

```
2    12    G
3    13    H
4    14    I
5    15    J
```

```
f1[1,2]
```

```
[1] F
Levels: F G H I J
```

```
f1$Angka
```

```
[1] 11 12 13 14 15
```

```
f1[, "Huruf"]
```

```
[1] F G H I J
Levels: F G H I J
```

```
colnames(f1)
```

```
[1] "Angka" "Huruf"
```

```
str(f1)
```

```
'data.frame':  5 obs. of  2 variables:
 $ Angka: int  11 12 13 14 15
 $ Huruf: Factor w/ 5 levels "F","G","H","I",...: 1 2 3 4 5
```

1.3 Data Frame Management

```
data(iris)
```

```
head(iris)
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa
4	4.6	3.1	1.5	0.2	setosa
5	5.0	3.6	1.4	0.2	setosa
6	5.4	3.9	1.7	0.4	setosa

```
tail(iris)
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
145	6.7	3.3	5.7	2.5	virginica
146	6.7	3.0	5.2	2.3	virginica
147	6.3	2.5	5.0	1.9	virginica
148	6.5	3.0	5.2	2.0	virginica

```
149          6.2          3.4          5.4          2.3 virginica
150          5.9          3.0          5.1          1.8 virginica
```

```
str(iris)
```

```
'data.frame':  150 obs. of  5 variables:
 $ Sepal.Length: num  5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
 $ Sepal.Width : num  3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
 $ Petal.Length: num  1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
 $ Petal.Width : num  0.2 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
 $ Species      : Factor w/ 3 levels "setosa","versicolor",...: 1 1 1 1 1 1 1 1 1 1 ...
```

1.3.1 R Package

```
# install.packages("readxl") - code to install R package
library(readxl)
```

```
#install.packages("dplyr")
library(dplyr)
```

1.3.2 Data Management With dplyr

```
head(iris)
```

```
      Sepal.Length Sepal.Width Petal.Length Petal.Width Species
1           5.1         3.5         1.4         0.2   setosa
2           4.9         3.0         1.4         0.2   setosa
3           4.7         3.2         1.3         0.2   setosa
4           4.6         3.1         1.5         0.2   setosa
5           5.0         3.6         1.4         0.2   setosa
6           5.4         3.9         1.7         0.4   setosa
```

```
irisbaru <- mutate(iris, sepal2 = Sepal.Length + Sepal.Width)
```

```
head(irisbaru)
```

```
      Sepal.Length Sepal.Width Petal.Length Petal.Width Species sepal2
1           5.1         3.5         1.4         0.2   setosa    8.6
2           4.9         3.0         1.4         0.2   setosa    7.9
3           4.7         3.2         1.3         0.2   setosa    7.9
4           4.6         3.1         1.5         0.2   setosa    7.7
5           5.0         3.6         1.4         0.2   setosa    8.6
6           5.4         3.9         1.7         0.4   setosa    9.3
```

```
irisetosa <- filter(iris, Species=="setosa")
head(irisetosa)
```

```
      Sepal.Length Sepal.Width Petal.Length Petal.Width Species
```


1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa
4	4.6	3.1	1.5	0.2	setosa
5	5.0	3.6	1.4	0.2	setosa
6	5.4	3.9	1.7	0.4	setosa

```
levels(iris$Species)
```

```
[1] "setosa"      "versicolor" "virginica"
```

```
irisversicolor <- filter(iris, Species=="setosa"& Petal.Length==1.3)
head(irisversicolor)
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	4.7	3.2	1.3	0.2	setosa
2	5.4	3.9	1.3	0.4	setosa
3	5.5	3.5	1.3	0.2	setosa
4	4.4	3.0	1.3	0.2	setosa
5	5.0	3.5	1.3	0.3	setosa
6	4.5	2.3	1.3	0.3	setosa

```
iris3 <- select(iris, Sepal.Length, Species)
head(iris3)
```

	Sepal.Length	Species
1	5.1	setosa
2	4.9	setosa
3	4.7	setosa
4	4.6	setosa
5	5.0	setosa
6	5.4	setosa

```
iris4 <- arrange(iris, Petal.Width)
head(iris4)
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	4.9	3.1	1.5	0.1	setosa
2	4.8	3.0	1.4	0.1	setosa
3	4.3	3.0	1.1	0.1	setosa
4	5.2	4.1	1.5	0.1	setosa
5	4.9	3.6	1.4	0.1	setosa
6	5.1	3.5	1.4	0.2	setosa

```
iris4 <- arrange(iris, Species, desc(Petal.Width))
head(iris4)
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	5.0	3.5	1.6	0.6	setosa
2	5.1	3.3	1.7	0.5	setosa

```

3      5.4      3.9      1.7      0.4 setosa
4      5.7      4.4      1.5      0.4 setosa
5      5.4      3.9      1.3      0.4 setosa
6      5.1      3.7      1.5      0.4 setosa

```

```

names(iris4)[1] <- "length"
head(iris4)

```

```

      length Sepal.Width Petal.Length Petal.Width Species
1      5.0      3.5      1.6      0.6 setosa
2      5.1      3.3      1.7      0.5 setosa
3      5.4      3.9      1.7      0.4 setosa
4      5.7      4.4      1.5      0.4 setosa
5      5.4      3.9      1.3      0.4 setosa
6      5.1      3.7      1.5      0.4 setosa

```

```

head(iris4[,c(-1,-3)])

```

```

      Sepal.Width Petal.Width Species
1      3.5      0.6 setosa
2      3.3      0.5 setosa
3      3.9      0.4 setosa
4      4.4      0.4 setosa
5      3.9      0.4 setosa
6      3.7      0.4 setosa

```

```

iris %>% group_by(Species) %>% summarise(rata2_Sepal.Width = mean(Sepal.Width))

```

```

# A tibble: 3 x 2
  Species rata2_Sepal.Width
  <fct>      <dbl>
1 setosa      3.43
2 versicolor  2.77
3 virginica   2.97

```

1.4 Visualization

1.4.1 Histogram

```

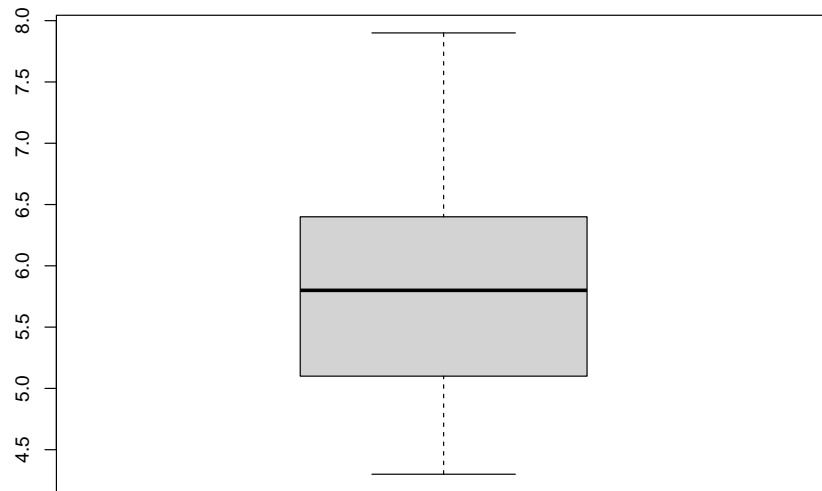
hist(iris$Sepal.Length)

```



```
boxplot(iris$Sepal.Length)
```

1.4.2 Box Plot

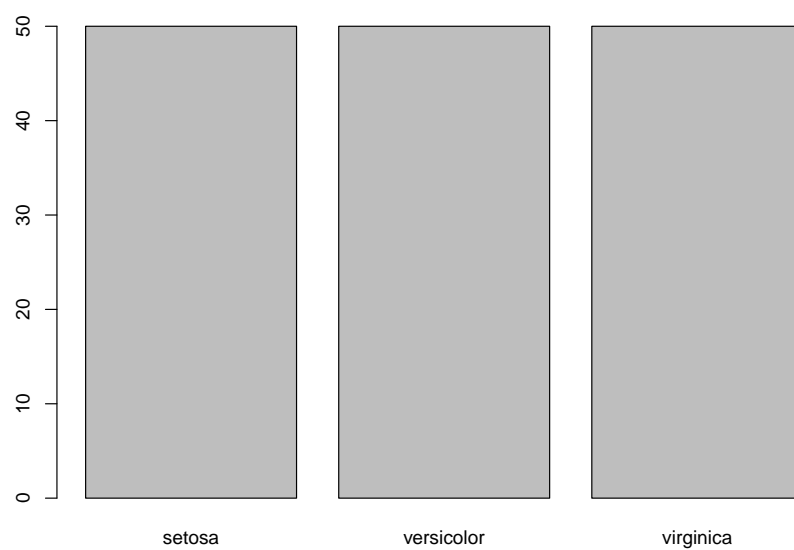


```
table(iris$Species)
```

1.4.3 Barplot

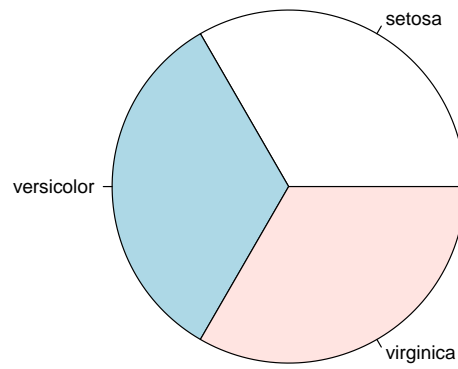
```
setosa versicolor virginica  
50      50      50
```

```
barplot(table(iris$Species))
```



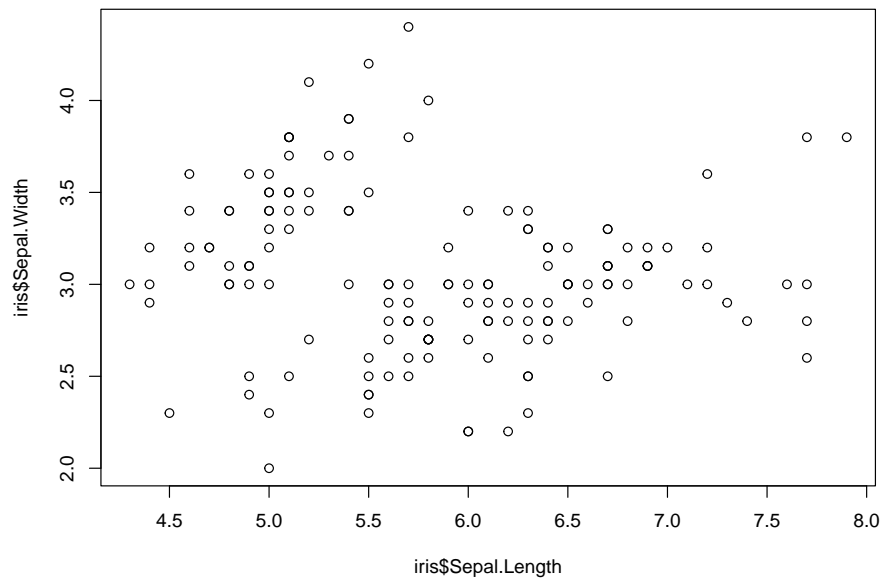
```
pie(table(iris$Species))
```

1.4.4 Pie Chart

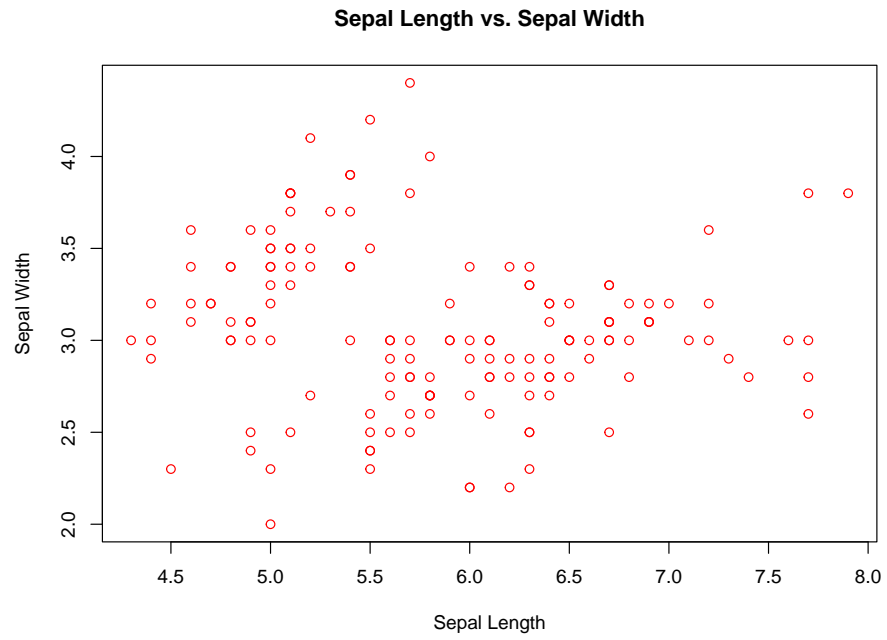


```
plot(iris$Sepal.Length,iris$Sepal.Width)
```

1.4.5 Scatter Plot



```
plot(iris$Sepal.Length, iris$Sepal.Width, main = "Sepal Length vs. Sepal Width",  
     xlab = "Sepal Length", ylab = "Sepal Width", col = "red")
```



Chapter 2

Nonparametric Statistics

2.1 Correlation

```
# Membuat data contoh
# Membuat vektor untuk responden, X, dan Y
X <- c(2, 1, 6, 11, 7, 11, 1, 12, 13, 13, 11)
Y <- c(9, 8, 16, 13, 11, 12, 7, 7, 13, 17, 10)

# Membuat dataframe
dataku <- data.frame(X = X, Y = Y)

# Menampilkan data
dataku
```

	X	Y
1	2	9
2	1	8
3	6	16
4	11	13
5	7	11
6	11	12
7	1	7
8	12	7
9	13	13
10	13	17
11	11	10

```
# Menggunakan fungsi cor.test untuk menghitung Tau-Kendall
cor.test(dataku$X, dataku$Y, method = "kendall")
```



```
# Membuat dataframe
dataku2 <- data.frame(Status_Pegawai,
                      Tingkat_Produktivitas)
# Menampilkan data
head(dataku2)
```

```
      Status_Pegawai Tingkat_Produktivitas
1      Kontrak      Rendah
2      Kontrak      Rendah
3      Kontrak      Rendah
4      Kontrak      Rendah
5      Kontrak      Rendah
6      Kontrak      Rendah
```

```
# Transformasi menjadi factor
dataku2$Status_Pegawai <- as.factor(dataku2$Status_Pegawai)
dataku2$Tingkat_Produktivitas <- as.factor(dataku2$Tingkat_Produktivitas)

summary(dataku2)
```

```
      Status_Pegawai Tingkat_Produktivitas
Kontrak:75      Rendah:51
Tetap  :75      Sedang:49
                Tinggi:50
```

```
# Melakukan tabel kontingensi
dataku2_kt <- table(dataku2$Status_Pegawai, dataku2$Tingkat_Produktivitas)
dataku2_kt
```

```
      Rendah Sedang Tinggi
Kontrak    30    30    15
Tetap     21    19    35
```

```
# Melakukan uji Chi-Square
chisq.test(dataku2_kt)
```

Pearson's Chi-squared test

```
data: dataku2_kt
X-squared = 12.058, df = 2, p-value = 0.002408
```

2.2 Difference Test

2.2.1 Two sample test (Independent)

2.2.1.1 Mann-Whitney Test

```
# Membuat data contoh
# Vektor data untuk efisiensi pada skala besar dan kecil
efisiensi_besar <- c(1.31, 1.25, 1.32, 1.3, 1.33, 1.31, 1.35, 1.34, 0.28, 1.34, 1.28)
efisiensi_kecil <- c(1.21, 1.28, 1.32, 1.25, 1.27, 1.31, 1.26, 1.31, 1.24, 1.22)

wilcox.test(efisiensi_besar, efisiensi_kecil)
```

Wilcoxon rank sum test with continuity correction

```
data: efisiensi_besar and efisiensi_kecil
W = 82.5, p-value = 0.05614
alternative hypothesis: true location shift is not equal to 0
```

2.2.1.2 Chi-Square Test

2.2.2 More than two sample test (Independent)

2.2.2.1 Kruskal-Wallis Test

```
# Membuat data contoh
# Membuat vektor untuk Industri A, B, dan C
industri_A <- c(2.33, 2.79, 3.01, 2.33, 1.22, 2.79, 1.9, 1.65)
industri_B <- c(2.33, 2.33, 2.79, 3.01, 1.99, 2.45)
industri_C <- c(1.06, 1.37, 1.09, 1.65, 1.44, 1.11)

# Membuat vektor industri
industri <- c(rep("Industri A", length(industri_A)),
             rep("Industri B", length(industri_B)),
             rep("Industri C", length(industri_C)))

# Menggabungkan semua vektor value
nilai <- c(industri_A, industri_B, industri_C)

# Membuat data frame
dataku4 <- data.frame(industri, nilai)

# Menampilkan data frame
dataku4$industri <- as.factor(dataku4$industri)
dataku4
```

```
industri nilai
```

```

1 Industri A 2.33
2 Industri A 2.79
3 Industri A 3.01
4 Industri A 2.33
5 Industri A 1.22
6 Industri A 2.79
7 Industri A 1.90
8 Industri A 1.65
9 Industri B 2.33
10 Industri B 2.33
11 Industri B 2.79
12 Industri B 3.01
13 Industri B 1.99
14 Industri B 2.45
15 Industri C 1.06
16 Industri C 1.37
17 Industri C 1.09
18 Industri C 1.65
19 Industri C 1.44
20 Industri C 1.11

```

```

# Uji kruskal wallis
kruskal.test(nilai ~ industri, data = dataku4)

```

Kruskal-Wallis rank sum test

```

data: nilai by industri
Kruskal-Wallis chi-squared = 10.619, df = 2, p-value = 0.004943

```

```

# Post hoc kruskal-wallis - Uji Dun
#installed.packages("FSA")
library(FSA)
dunnTest(nilai ~ industri, data = dataku4)

```

	Comparison	Z	P.unadj	P.adj
1	Industri A - Industri B	-0.6428883	0.520296550	0.52029655
2	Industri A - Industri C	2.6109139	0.009030062	0.01806012
3	Industri B - Industri C	3.0436533	0.002337243	0.00701173

2.2.2.2 Chi-Square Test

2.2.3 Two sample test (Dependent)

2.2.3.1 Sign Test

```

# Membuat data contoh
# Data Skor Kepuasan

```

```

produk_lama <- c(16, 15, 18, 16, 17, 18, 20, 15, 14, 16, 19, 17)
produk_baru <- c(18, 17, 16, 19, 17, 20, 18, 16, 15, 18, 20, 18)
# Data Responden
responden <- c(1:12)
# Membuat data frame
dataku5 <- data.frame(Responden = c(rep(responden, 2)),
                      Produk = factor(c(rep("Produk Lama", length(produk_lama)),
                                         rep("Produk Baru", length(produk_baru)))),
                      Skor_Kepuasan = c(produk_lama, produk_baru))
# Menampilkan data frame
dataku5

```

	Responden	Produk	Skor_Kepuasan
1	1	Produk Lama	16
2	2	Produk Lama	15
3	3	Produk Lama	18
4	4	Produk Lama	16
5	5	Produk Lama	17
6	6	Produk Lama	18
7	7	Produk Lama	20
8	8	Produk Lama	15
9	9	Produk Lama	14
10	10	Produk Lama	16
11	11	Produk Lama	19
12	12	Produk Lama	17
13	1	Produk Baru	18
14	2	Produk Baru	17
15	3	Produk Baru	16
16	4	Produk Baru	19
17	5	Produk Baru	17
18	6	Produk Baru	20
19	7	Produk Baru	18
20	8	Produk Baru	16
21	9	Produk Baru	15
22	10	Produk Baru	18
23	11	Produk Baru	20
24	12	Produk Baru	18

```

# Menghitung perbedaan
diff <- dataku5[dataku5$Produk == 'Produk Baru', ]$Skor_Kepuasan - dataku5[dataku5$Produk == 'Produk Lama', ]$Skor_Kepuasan
# Menghitung jumlah perbedaan yang positif
jumlah_positif <- sum(diff > 0)
# Melakukan uji tanda
binom.test(jumlah_positif, length(diff),

```

```
p = 0.5,
alternative = "two.sided")
```

Exact binomial test

```
data: jumlah_positif and length(diff)
number of successes = 9, number of trials = 12, p-value = 0.146
alternative hypothesis: true probability of success is not equal to 0.5
95 percent confidence interval:
 0.4281415 0.9451394
sample estimates:
probability of success
          0.75
```

Interpretation: <https://www.geeksforgeeks.org/sign-test-in-r/>

2.2.4 More than two sample test (Dependent)

2.2.4.1 Friedman Test

```
# Membuat data contoh
dataku6 <- matrix(c(1.24,1.50,1.62,
                    1.71,1.85,2.05,
                    1.37,2.12,1.68,
                    2.53,1.87,2.62,
                    1.23,1.34,1.51,
                    1.94,2.33,2.86,
                    1.72,1.43,2.86), nrow = 7, byrow = TRUE,
                  dimnames = list(Person= as.character(1:7),
                                   Obat = c("Obat A","Obat B","Obat C")))
dataku6
```

	Obat		
Person	Obat A	Obat B	Obat C
1	1.24	1.50	1.62
2	1.71	1.85	2.05
3	1.37	2.12	1.68
4	2.53	1.87	2.62
5	1.23	1.34	1.51
6	1.94	2.33	2.86
7	1.72	1.43	2.86

```
friedman.test(dataku6)
```

Friedman rank sum test

```
data: dataku6
Friedman chi-squared = 8.8571, df = 2, p-value = 0.01193
```

2.2.4.2 Cochran Test

```
# Membuat data contoh
## Input data
responden <- c(1:8)
produk_A <- c("Tidak","Tidak","Ya","Ya","Ya","Tidak","Tidak","Tidak")
produk_B <- c("Tidak","Ya","Ya","Ya","Tidak","Tidak","Ya","Tidak")
produk_C <- c("Ya","Tidak","Tidak","Ya","Tidak","Ya","Ya","Tidak")
dataku7 <- data.frame(responden, produk_A, produk_B, produk_C)
dataku7$produk_A <- as.factor(dataku7$produk_A)
dataku7$produk_B <- as.factor(dataku7$produk_B)
dataku7$produk_C <- as.factor(dataku7$produk_C)
dataku7
```

	responden	produk_A	produk_B	produk_C
1	1	Tidak	Tidak	Ya
2	2	Tidak	Ya	Tidak
3	3	Ya	Ya	Tidak
4	4	Ya	Ya	Ya
5	5	Ya	Tidak	Tidak
6	6	Tidak	Tidak	Ya
7	7	Tidak	Ya	Ya
8	8	Tidak	Tidak	Tidak

```
dataku7 <- ifelse(dataku7=="Ya", 1,0)
```

```
#install.packages("nonpar")
library(nonpar)
cochrans.q(as.matrix(dataku7[,-1]), alpha = 0.05)
```

Cochran's Q Test

H0: There is no difference in the effectiveness of treatments.

HA: There is a difference in the effectiveness of treatments.

Q = 0.333333333333333

Degrees of Freedom = 2

Significance Level = 0.05

The p-value is 0.846481724890614

Chapter 3

Logistic Regression

3.1 Regresi Logistik Biner

3.1.1 Data

```
credit <- read.csv("Data/credit.csv")
head(credit[,1:5],10)
```

	creditability	account.balance	duration	credit.amount	saving.balance
1	1	1	18	1049	1
2	1	1	9	2799	1
3	1	2	12	841	2
4	1	1	12	2122	1
5	1	1	12	2171	1
6	1	1	10	2241	1
7	1	1	8	3398	1
8	1	1	6	1361	1
9	1	4	18	1098	1
10	1	2	24	3758	3

```
str(credit)
```

```
'data.frame': 1000 obs. of 14 variables:
 $ creditability : int 1 1 1 1 1 1 1 1 1 1 ...
 $ account.balance : int 1 1 2 1 1 1 1 1 4 2 ...
 $ duration : int 18 9 12 12 12 10 8 6 18 24 ...
 $ credit.amount : int 1049 2799 841 2122 2171 2241 3398 1361 1098 3758 ...
 $ saving.balance : int 1 1 2 1 1 1 1 1 1 3 ...
 $ employment.year : int 2 3 4 3 3 2 4 2 1 1 ...
 $ installment.rate: int 4 2 2 3 4 1 1 2 4 1 ...
 $ marital.status : int 2 3 2 3 3 3 3 3 2 2 ...
```

```
$ duration.address: int  4 2 4 2 4 3 4 4 4 4 ...
$ age             : int  21 36 23 39 38 48 39 40 65 23 ...
$ dependents      : int  1 2 1 2 1 2 1 2 1 1 ...
$ number.of.credit: int  1 2 1 2 2 2 2 1 2 1 ...
$ occupation       : int  3 3 2 2 2 2 2 2 1 1 ...
$ previous.credit  : int  4 4 2 4 4 4 4 4 4 2 ...
```

```
library(dplyr)
credit <- credit %>% mutate(across(-c(duration,
                                     credit.amount,
                                     age),as.factor))
str(credit)
```

```
'data.frame':  1000 obs. of  14 variables:
 $ creditability   : Factor w/ 2 levels "0","1": 2 2 2 2 2 2 2 2 2 2 ...
 $ account.balance : Factor w/ 4 levels "1","2","3","4": 1 1 2 1 1 1 1 1 4 2 ...
 $ duration        : int   18 9 12 12 12 10 8 6 18 24 ...
 $ credit.amount   : int  1049 2799 841 2122 2171 2241 3398 1361 1098 3758 ...
 $ saving.balance  : Factor w/ 5 levels "1","2","3","4",...: 1 1 2 1 1 1 1 1 1 3 ...
 $ employment.year : Factor w/ 5 levels "1","2","3","4",...: 2 3 4 3 3 2 4 2 1 1 ...
 $ installment.rate: Factor w/ 4 levels "1","2","3","4": 4 2 2 3 4 1 1 2 4 1 ...
 $ marital.status  : Factor w/ 4 levels "1","2","3","4": 2 3 2 3 3 3 3 3 2 2 ...
 $ duration.address: Factor w/ 4 levels "1","2","3","4": 4 2 4 2 4 3 4 4 4 4 ...
 $ age             : int   21 36 23 39 38 48 39 40 65 23 ...
 $ dependents      : Factor w/ 2 levels "1","2": 1 2 1 2 1 2 1 2 1 1 ...
 $ number.of.credit: Factor w/ 4 levels "1","2","3","4": 1 2 1 2 2 2 2 1 2 1 ...
 $ occupation       : Factor w/ 4 levels "1","2","3","4": 3 3 2 2 2 2 2 2 1 1 ...
 $ previous.credit  : Factor w/ 5 levels "0","1","2","3",...: 5 5 3 5 5 5 5 5 5 3 ...
```

3.1.2 Pemodelan

```
logreg1 <- glm(creditability~.,data=credit,family = "binomial")
summary(logreg1)
```

Call:

```
glm(formula = creditability ~ ., family = "binomial", data = credit)
```

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	2.990e-01	8.942e-01	0.334	0.738097
account.balance2	4.346e-01	2.013e-01	2.159	0.030852 *
account.balance3	9.490e-01	3.602e-01	2.635	0.008421 **
account.balance4	1.804e+00	2.222e-01	8.119	4.69e-16 ***
duration	-2.705e-02	8.818e-03	-3.068	0.002156 **
credit.amount	-1.025e-04	4.161e-05	-2.465	0.013718 *

```

saving.balance2    1.293e-01  2.701e-01    0.479 0.632222
saving.balance3    4.144e-01  3.987e-01    1.039 0.298644
saving.balance4    1.241e+00  5.032e-01    2.467 0.013629 *
saving.balance5    8.811e-01  2.463e-01    3.577 0.000347 ***
employment.year2  -1.432e-01  4.109e-01   -0.348 0.727561
employment.year3    2.530e-01  3.957e-01    0.639 0.522582
employment.year4    7.646e-01  4.258e-01    1.796 0.072572 .
employment.year5    2.386e-01  3.962e-01    0.602 0.547012
installment.rate2  -2.841e-01  2.953e-01   -0.962 0.336089
installment.rate3  -5.122e-01  3.217e-01   -1.592 0.111374
installment.rate4  -9.279e-01  2.872e-01   -3.230 0.001236 **
marital.status2     1.744e-01  3.742e-01    0.466 0.641255
marital.status3     7.482e-01  3.670e-01    2.039 0.041468 *
marital.status4     5.577e-01  4.371e-01    1.276 0.201928
duration.address2  -7.104e-01  2.832e-01   -2.509 0.012122 *
duration.address3  -5.443e-01  3.163e-01   -1.721 0.085314 .
duration.address4  -4.386e-01  2.762e-01   -1.588 0.112244
age                 1.125e-02  8.468e-03    1.329 0.183990
dependents2        -2.607e-01  2.387e-01   -1.092 0.274669
number.of.credit2  -4.177e-01  2.315e-01   -1.805 0.071133 .
number.of.credit3  -4.131e-01  5.951e-01   -0.694 0.487625
number.of.credit4  -4.589e-01  9.908e-01   -0.463 0.643240
occupation2        -8.953e-02  6.276e-01   -0.143 0.886557
occupation3        -1.487e-01  6.048e-01   -0.246 0.805804
occupation4         1.276e-02  6.087e-01    0.021 0.983277
previous.credit1   -3.136e-01  5.178e-01   -0.606 0.544686
previous.credit2    6.063e-01  4.149e-01    1.461 0.143896
previous.credit3    8.090e-01  4.531e-01    1.785 0.074205 .
previous.credit4    1.511e+00  4.169e-01    3.625 0.000288 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

(Dispersion parameter for binomial family taken to be 1)

```

Null deviance: 1221.7  on 999  degrees of freedom
Residual deviance:  956.0  on 965  degrees of freedom
AIC: 1026

```

Number of Fisher Scoring iterations: 5

3.1.3 Odds Ratio

```

beta = round(coef(logreg1),2)
OR = round(exp(beta),2)
cbind(beta, OR)

```

	beta	OR
(Intercept)	0.30	1.35
account.balance2	0.43	1.54
account.balance3	0.95	2.59
account.balance4	1.80	6.05
duration	-0.03	0.97
credit.amount	0.00	1.00
saving.balance2	0.13	1.14
saving.balance3	0.41	1.51
saving.balance4	1.24	3.46
saving.balance5	0.88	2.41
employment.year2	-0.14	0.87
employment.year3	0.25	1.28
employment.year4	0.76	2.14
employment.year5	0.24	1.27
installment.rate2	-0.28	0.76
installment.rate3	-0.51	0.60
installment.rate4	-0.93	0.39
marital.status2	0.17	1.19
marital.status3	0.75	2.12
marital.status4	0.56	1.75
duration.address2	-0.71	0.49
duration.address3	-0.54	0.58
duration.address4	-0.44	0.64
age	0.01	1.01
dependents2	-0.26	0.77
number.of.credit2	-0.42	0.66
number.of.credit3	-0.41	0.66
number.of.credit4	-0.46	0.63
occupation2	-0.09	0.91
occupation3	-0.15	0.86
occupation4	0.01	1.01
previous.credit1	-0.31	0.73
previous.credit2	0.61	1.84
previous.credit3	0.81	2.25
previous.credit4	1.51	4.53

3.1.4 Multikolineratitas

```
library(car)
vif(logreg1)
```

	GVIF	Df	GVIF ^{1/(2*Df)}
account.balance	1.283532	3	1.042480
duration	1.828834	1	1.352344

credit.amount	2.284117	1	1.511330
saving.balance	1.286469	4	1.031989
employment.year	2.406179	4	1.116005
installment.rate	1.443706	3	1.063114
marital.status	1.439516	3	1.062599
duration.address	1.502426	3	1.070201
age	1.365556	1	1.168570
dependents	1.177252	1	1.085012
number.of.credit	2.060162	3	1.128020
occupation	1.893863	3	1.112307
previous.credit	2.136438	4	1.099541

3.1.5 Akurasi

```
pred_clas <- ifelse(logreg1$fitted.values > 0.5, 1, 0)
conf_matrix <- table(credit$creditability, pred_clas)
conf_matrix
```

```
pred_clas
  0  1
0 145 155
1  68 632
```

```
paste0("Akurasi Model:")
```

```
[1] "Akurasi Model:"
```

```
accuracy <- sum(diag(conf_matrix)) / sum(conf_matrix)
accuracy
```

```
[1] 0.777
```

3.1.6 Kebaikan Model

```
#install.packages("performance")
library(performance)
#Outliers
performance::check_outliers(logreg1)
```

```
OK: No outliers detected.
```

- Based on the following method and threshold: cook (0.8).
- For variable: (Whole model)

```
#Metrik
performance(logreg1)
```

```
# Indices of model performance
```

AIC	AICc	BIC	Tjur's R2	RMSE	Sigma	Log_loss
1025.995	1028.609	1197.767	0.254	0.395	1.000	0.478

AIC	Score_log	Score_spherical	PCP
1025.995	-Inf	0.001	0.687

```
#Goodness Of Fit
performance_hosmer(logreg1)
```

```
# Hosmer-Lemeshow Goodness-of-Fit Test
```

```
Chi-squared: 8.472
df: 8
p-value: 0.389
```

3.2 Regresi Logistik Nominal atau Multinomial

3.2.1 Data

```
library(readxl)
students <- read_excel("Data/students.xlsx")
head(students,10)
```

```
# A tibble: 10 x 6
  gender ses   prog   read write  math
  <chr> <chr> <chr>   <dbl> <dbl> <dbl>
1 female low   vocation 34    35    41
2 male   middle general 34    33    41
3 male   high   vocation 39    39    44
4 male   low    vocation 37    37    42
5 male   middle vocation 39    31    40
6 female high   general 42    36    42
7 male   middle vocation 31    36    46
8 male   middle vocation 50    31    40
9 female middle vocation 39    41    33
10 male  middle vocation 34    37    46
```

```
str(students)
```

```
tibble [200 x 6] (S3: tbl_df/tbl/data.frame)
 $ gender: chr [1:200] "female" "male" "male" "male" ...
 $ ses   : chr [1:200] "low" "middle" "high" "low" ...
 $ prog  : chr [1:200] "vocation" "general" "vocation" "vocation" ...
```



```
$ read : num [1:200] 34 34 39 37 39 42 31 50 39 34 ...
$ write : num [1:200] 35 33 39 37 31 36 36 31 41 37 ...
$ math : num [1:200] 41 41 44 42 40 42 46 40 33 46 ...
```

3.2.2 Ubah jadi faktor

```
library(dplyr)
students <- students %>% mutate(across(-c(read,write,math),as.factor))
students$prog2 <- relevel(students$prog, ref = "academic")
str(students)
```

```
tibble [200 x 7] (S3: tbl_df/tbl/data.frame)
 $ gender: Factor w/ 2 levels "female","male": 1 2 2 2 2 1 2 2 1 2 ...
 $ ses   : Factor w/ 3 levels "high","low","middle": 2 3 1 2 3 1 3 3 3 3 ...
 $ prog  : Factor w/ 3 levels "academic","general",...: 3 2 3 3 3 2 3 3 3 3 ...
 $ read  : num [1:200] 34 34 39 37 39 42 31 50 39 34 ...
 $ write : num [1:200] 35 33 39 37 31 36 36 31 41 37 ...
 $ math  : num [1:200] 41 41 44 42 40 42 46 40 33 46 ...
 $ prog2 : Factor w/ 3 levels "academic","general",...: 3 2 3 3 3 2 3 3 3 3 ...
```

```
table(students$ses, students$prog)
```

	academic	general	vocation
high	42	9	7
low	19	16	12
middle	44	20	31

```
table(students$gender, students$prog)
```

	academic	general	vocation
female	58	24	27
male	47	21	23

3.2.3 Pemodelan

```
#install.packages("nnet")
library(nnet)
logmultinom <- multinom(prog2 ~ ses + gender + write + read, data = students)
```

```
# weights: 21 (12 variable)
initial value 219.722458
iter 10 value 176.754587
final value 174.725397
converged
```

```
summary(logmultinom)
```

Call:

```
multinom(formula = prog2 ~ ses + gender + write + read, data = students)
```

Coefficients:

	(Intercept)	seslow	sesmiddle	gendermale	write	read
general	2.621831	1.0038426	0.5651588	0.1273914	-0.02860308	-0.04730781
vocation	6.505182	0.6239396	1.1539447	-0.3105237	-0.08243508	-0.07108839

Std. Errors:

	(Intercept)	seslow	sesmiddle	gendermale	write	read
general	1.434514	0.5323398	0.4713812	0.4137756	0.02686316	0.02480868
vocation	1.524572	0.6200276	0.5231819	0.4414783	0.02793343	0.02752520

Residual Deviance: 349.4508

AIC: 373.4508

```
z <- summary(logmultinom)$coefficients/summary(logmultinom)$standard.errors
# 2-tailed z test
p <- (1 - pnorm(abs(z), 0, 1)) * 2
p
```

	(Intercept)	seslow	sesmiddle	gendermale	write	read
general	6.759775e-02	0.05933302	0.23055043	0.7581770	0.286980200	0.056532815
vocation	1.982164e-05	0.31426675	0.02741006	0.4818237	0.003166173	0.009804037

3.2.4 Odds Ratio

```
exp(coef(logmultinom))
```

	(Intercept)	seslow	sesmiddle	gendermale	write	read
general	13.7609	2.728747	1.759727	1.135862	0.9718021	0.9537938
vocation	668.5973	1.866266	3.170676	0.733063	0.9208712	0.9313796

3.2.5 Multikolineratitas

```
library(car)
vif(logmultinom)
```

	GVIF	Df	GVIF^(1/(2*Df))
ses	6.640420	2	1.605273
gender	2.650955	1	1.628175
write	66.396002	1	8.148374
read	53.940932	1	7.344449

3.2.6 Akurasi

```
df <- students[,c("ses","gender","write","read")]

#install.packages("caret")
library(caret)
prediksi <- predict(logmultinom, df, type = "class")
confusionMatrix(as.factor(prediksi),
                 students$prog2)
```

Confusion Matrix and Statistics

	Reference		
Prediction	academic	general	vocation
academic	90	25	21
general	3	7	4
vocation	12	13	25

Overall Statistics

Accuracy : 0.61
 95% CI : (0.5387, 0.678)
 No Information Rate : 0.525
 P-Value [Acc > NIR] : 0.009485

Kappa : 0.3094

Mcnemar's Test P-Value : 1.959e-05

Statistics by Class:

	Class: academic	Class: general	Class: vocation
Sensitivity	0.8571	0.1556	0.5000
Specificity	0.5158	0.9548	0.8333
Pos Pred Value	0.6618	0.5000	0.5000
Neg Pred Value	0.7656	0.7957	0.8333
Prevalence	0.5250	0.2250	0.2500
Detection Rate	0.4500	0.0350	0.1250
Detection Prevalence	0.6800	0.0700	0.2500
Balanced Accuracy	0.6865	0.5552	0.6667

3.2.7 Kebaikan Model

```
logmultinom0 <- multinom(prog2 ~ 1, data = students)
```

weights: 6 (2 variable)

```
initial value 219.722458
final value 204.096674
converged
```

```
#install.packages("lmtest")
library(lmtest)
lrtest(logmultinom0, logmultinom)
```

Likelihood ratio test

```
Model 1: prog2 ~ 1
Model 2: prog2 ~ ses + gender + write + read
      #Df  LogLik Df  Chisq Pr(>Chisq)
1     2 -204.10
2    12 -174.72 10  58.743  6.263e-09 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

3.3 Regresi Logistik Ordinal

3.3.1 Data

```
crash <- read.csv("Data/crash.csv")
head(crash, 10)
```

	Gender	Location	SeatBelt	Respon
1	Female	Urban	Yes	1
2	Male	Urban	Yes	1
3	Male	Urban	No	1
4	Female	Urban	No	1
5	Male	Rural	Yes	1
6	Female	Rural	Yes	1
7	Male	Rural	No	1
8	Female	Rural	No	1
9	Female	Urban	No	3
10	Female	Rural	No	3

```
library(dplyr)
crash <- crash %>% mutate(across(-c(Respon), as.factor))
str(crash)
```

```
'data.frame':  80 obs. of  4 variables:
 $ Gender  : Factor w/ 2 levels "Female","Male": 1 2 2 1 2 1 2 1 1 1 ...
 $ Location: Factor w/ 2 levels "Rural","Urban": 2 2 2 2 1 1 1 1 2 1 ...
 $ SeatBelt: Factor w/ 2 levels "No","Yes": 2 2 1 1 2 2 1 1 1 1 ...
 $ Respon   : int  1 1 1 1 1 1 1 1 3 3 ...
```

```
crash$Respon <- ordered(crash$Respon, levels=c("1","2","3","4","5"))
str(crash)
```

```
'data.frame': 80 obs. of 4 variables:
 $ Gender : Factor w/ 2 levels "Female","Male": 1 2 2 1 2 1 2 1 1 1 ...
 $ Location: Factor w/ 2 levels "Rural","Urban": 2 2 2 2 1 1 1 1 2 1 ...
 $ SeatBelt: Factor w/ 2 levels "No","Yes": 2 2 1 1 2 2 1 1 1 1 ...
 $ Respon : Ord.factor w/ 5 levels "1"<"2"<"3"<"4"<...: 1 1 1 1 1 1 1 1 3 3 ...
```

3.3.2 Pemodelan

```
#install.packages("MASS")
library(MASS)
orderlog <- polr(Respon~., method='logistic',data=crash)
summary(orderlog)
```

Call:

```
polr(formula = Respon ~ ., data = crash, method = "logistic")
```

Coefficients:

	Value	Std. Error	t value
GenderMale	-0.05369	0.3974	-0.1351
LocationUrban	0.05661	0.3958	0.1430
SeatBeltYes	-0.31102	0.3974	-0.7827

Intercepts:

	Value	Std. Error	t value
1 2	-1.5425	0.4450	-3.4664
2 3	-0.5523	0.4060	-1.3603
3 4	0.2649	0.3966	0.6678
4 5	1.2472	0.4264	2.9249

Residual Deviance: 256.8444

AIC: 270.8444

3.3.3 Odds Ratio

```
koefisien<-coef(summary(orderlog))
exp(koefisien[,1])
```

GenderMale	LocationUrban	SeatBeltYes	1 2	2 3
0.9477303	1.0582414	0.7327004	0.2138542	0.5756362
3 4	4 5			
1.3032362	3.4805710			

```
# menghitung pvalue
p <- pnorm(abs(koefisien[, "t value"]), lower.tail = FALSE)*2
(ctabel<-cbind(round(koefisien,2), "pvalue"=round(p,3)))
```

	Value	Std. Error	t value	pvalue
GenderMale	-0.05	0.40	-0.14	0.893
LocationUrban	0.06	0.40	0.14	0.886
SeatBeltYes	-0.31	0.40	-0.78	0.434
1 2	-1.54	0.44	-3.47	0.001
2 3	-0.55	0.41	-1.36	0.174
3 4	0.26	0.40	0.67	0.504
4 5	1.25	0.43	2.92	0.003

3.3.4 Multikolineratitas

```
library(car)
vif(orderlog)
```

```
Gender Location SeatBelt
1.002035 1.001265 1.001814
```

3.3.5 Akurasi

```
df <- crash[,1:3]
prediksi <- predict(orderlog, df, type = "class")
confusionMatrix(as.factor(prediksi),
                 crash$Respon)
```

Confusion Matrix and Statistics

	Reference				
Prediction	1	2	3	4	5
1	10	8	7	7	8
2	0	0	0	0	0
3	0	0	0	0	0
4	0	0	0	0	0
5	6	8	9	9	8

Overall Statistics

```
Accuracy : 0.225
95% CI : (0.1391, 0.3321)
No Information Rate : 0.2
P-Value [Acc > NIR] : 0.3292
```

Kappa : 0.0312

McNemar's Test P-Value : NA

Statistics by Class:

	Class: 1	Class: 2	Class: 3	Class: 4	Class: 5
Sensitivity	0.6250	0.0	0.0	0.0	0.5
Specificity	0.5312	1.0	1.0	1.0	0.5
Pos Pred Value	0.2500	NaN	NaN	NaN	0.2
Neg Pred Value	0.8500	0.8	0.8	0.8	0.8
Prevalence	0.2000	0.2	0.2	0.2	0.2
Detection Rate	0.1250	0.0	0.0	0.0	0.1
Detection Prevalence	0.5000	0.0	0.0	0.0	0.5
Balanced Accuracy	0.5781	0.5	0.5	0.5	0.5

3.3.6 Kebaikan Model

```
orderlog0 <-polr(Respon~1, method = "logistic", data = crash)
#install.packages("lmtest")
library(lmtest)
lrtest(orderlog0,orderlog)
```

Likelihood ratio test

Model 1: Respon ~ 1

Model 2: Respon ~ Gender + Location + SeatBelt

```
#Df  LogLik Df  Chisq Pr(>Chisq)
1    4 -128.75
2    7 -128.42  3 0.6657    0.8813
```


Chapter 4

Discriminant Analysis

4.1 Analisis Diskriminan Dua Grup

4.1.1 Data

```
library(readxl)
pinjaman <- read_excel("Data/pinjaman.xlsx")
head(pinjaman,10)
```

```
# A tibble: 10 x 6
      X1     X2     X3     X4     X5     Y
  <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
1    98    35    12     4     4     1
2    65    44     5     3     1     1
3    22    50     0     2     7     1
4    78    60    34     5     5     1
5    50    31     4     2     2     1
6    21    30     5     3     7     1
7    42    32    21     4    11     1
8    20    41    10     2     3     1
9    33    25     0     3     6     1
10   57    32     8     2     5     1
```

```
str(pinjaman)
```

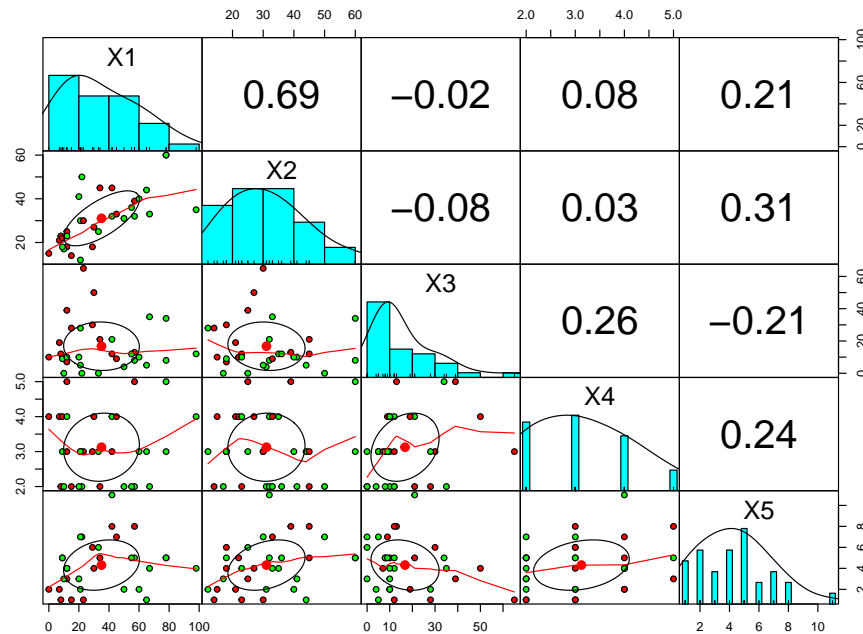
```
tibble [32 x 6] (S3: tbl_df/tbl/data.frame)
 $ X1: num [1:32] 98 65 22 78 50 21 42 20 33 57 ...
 $ X2: num [1:32] 35 44 50 60 31 30 32 41 25 32 ...
 $ X3: num [1:32] 12 5 0 34 4 5 21 10 0 8 ...
 $ X4: num [1:32] 4 3 2 5 2 3 4 2 3 2 ...
 $ X5: num [1:32] 4 1 7 5 2 7 11 3 6 5 ...
```

```
$ Y : num [1:32] 1 1 1 1 1 1 1 1 1 1 ...
```

```
pinjaman$Y <- as.factor(pinjaman$Y)
str(pinjaman)
```

```
tibble [32 x 6] (S3: tbl_df/tbl/data.frame)
 $ X1: num [1:32] 98 65 22 78 50 21 42 20 33 57 ...
 $ X2: num [1:32] 35 44 50 60 31 30 32 41 25 32 ...
 $ X3: num [1:32] 12 5 0 34 4 5 21 10 0 8 ...
 $ X4: num [1:32] 4 3 2 5 2 3 4 2 3 2 ...
 $ X5: num [1:32] 4 1 7 5 2 7 11 3 6 5 ...
 $ Y : Factor w/ 2 levels "0","1": 2 2 2 2 2 2 2 2 2 2 ...
```

```
library(psych)
pairs.panels(pinjaman[1:5],
             gap = 0,
             bg = c("red", "green")[pinjaman$Y],
             pch = 21)
```



4.1.2 Pemodelan Linier

```
library(MASS)
modellda1 <- lda(Y ~ X1 + X2 + X3 + X4 + X5, data=pinjaman)
modellda1
```

Call:

```
lda(Y ~ X1 + X2 + X3 + X4 + X5, data = pinjaman)
```

Prior probabilities of groups:

```
      0      1
0.4375 0.5625
```

Group means:

```
      X1      X2      X3      X4      X5
0 23.07143 26.78571 23.21429 3.428571 4.071429
1 44.33333 34.38889 11.72222 2.888889 4.500000
```

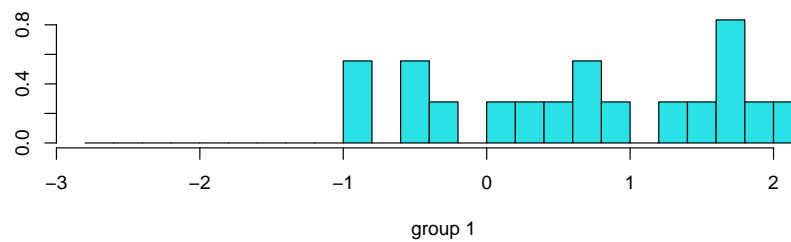
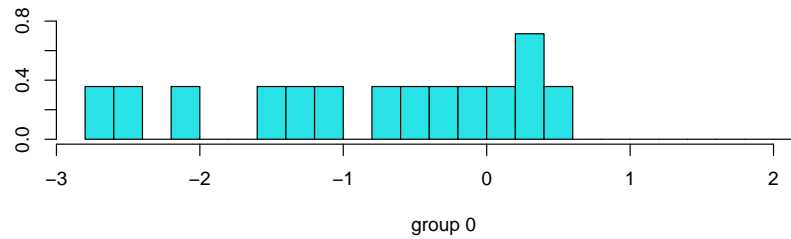
Coefficients of linear discriminants:

```
      LD1
X1 0.037015853
X2 -0.004820049
X3 -0.043555291
X4 -0.477408359
X5 -0.008483836
```

```
m <- manova(cbind(pinjaman$X1,pinjaman$X2,pinjaman$X3,
                  pinjaman$X4,pinjaman$X5) ~ pinjaman$Y)
summary(m, test = 'Wilks')
```

```
      Df  Wilks approx F num Df den Df  Pr(>F)
pinjaman$Y 1 0.62715   3.0915      5    26 0.02544 *
Residuals 30
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
p <- predict(modellda1, pinjaman)
ldahist(data = p$x, g = pinjaman$Y)
```



```
library(caret)
confusionMatrix(p$class, pinjaman$Y)
```

Confusion Matrix and Statistics

	Reference	
Prediction	0	1
0	9	4
1	5	14

Accuracy : 0.7188
 95% CI : (0.5325, 0.8625)
 No Information Rate : 0.5625
 P-Value [Acc > NIR] : 0.0523

Kappa : 0.424

Mcnemar's Test P-Value : 1.0000

Sensitivity : 0.6429
 Specificity : 0.7778
 Pos Pred Value : 0.6923
 Neg Pred Value : 0.7368
 Prevalence : 0.4375

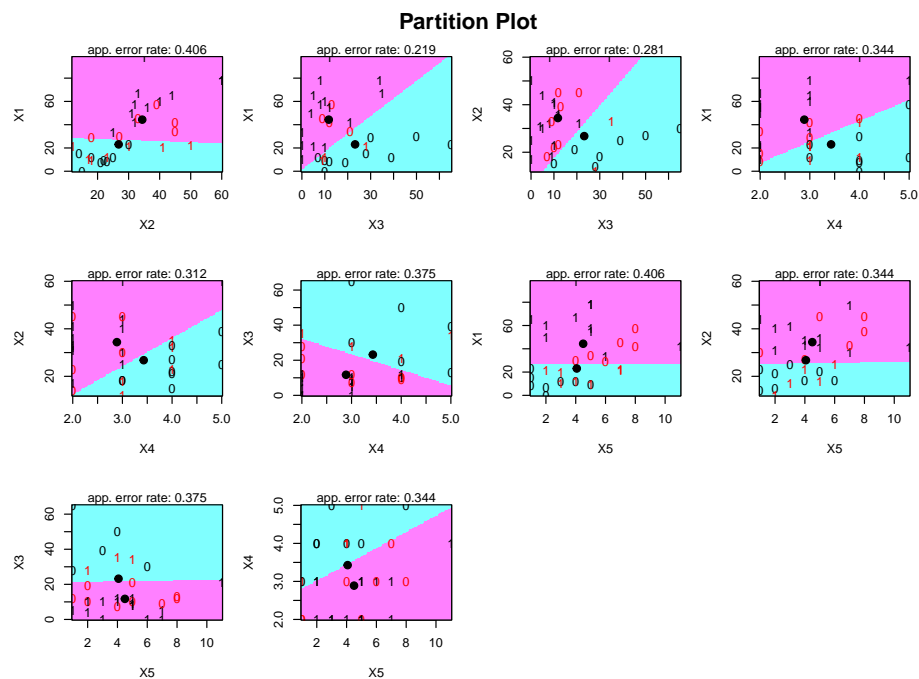
Detection Rate : 0.2812
 Detection Prevalence : 0.4062
 Balanced Accuracy : 0.7103

'Positive' Class : 0

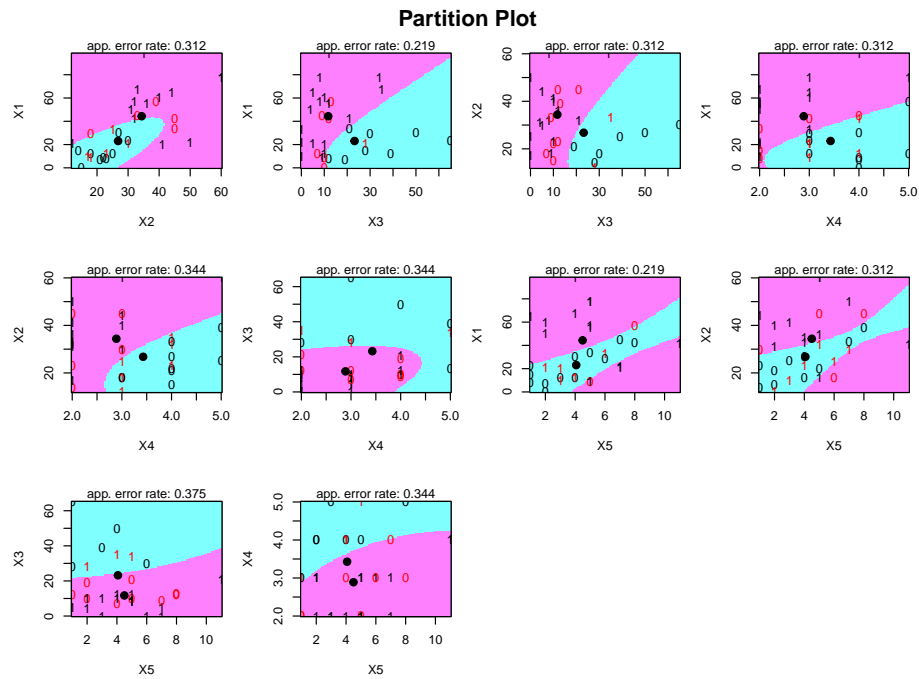
```
mean(p$class==pinjaman$Y)
```

```
[1] 0.71875
```

```
#install.packages("klaR")
library(klaR)
#Partition plot
partimat(Y~., data = pinjaman, method = "lda")
```



```
partimat(Y~., data = pinjaman, method = "qda")
```



4.1.5 Pemodelan Kuadratik

```
modellda2 <- qda(Y ~ X1 + X2 + X3 + X4 + X5, data=pinjaman)
modellda2
```

Call:

```
qda(Y ~ X1 + X2 + X3 + X4 + X5, data = pinjaman)
```

Prior probabilities of groups:

```
0      1
0.4375 0.5625
```

Group means:

```
      X1      X2      X3      X4      X5
0 23.07143 26.78571 23.21429 3.428571 4.071429
1 44.33333 34.38889 11.72222 2.888889 4.500000
```

```
p <- predict(modellda2, pinjaman)
mean(p$class==pinjaman$Y)
```

```
[1] 0.84375
```

4.1.6 Tipe Diskriminan Lainnya

```
# Mixture discriminant analysis - MDA
# install.packages("mda")
library(mda)
modellda3 <- mda(Y ~ X1 + X2 + X3 + X4 + X5, data=pinjaman)
p <- predict(modellda3, pinjaman)
mean(p==pinjaman$Y)
```

```
[1] 0.875
```

```
# Flexible discriminant analysis - FDA
modellda4 <- fda(Y ~ X1 + X2 + X3 + X4 + X5, data=pinjaman)
p <- predict(modellda4, pinjaman)
mean(p==pinjaman$Y)
```

```
[1] 0.71875
```

```
# Regularized discriminant analysis - RDA
modellda5 <- rda(Y ~ X1 + X2 + X3 + X4 + X5, data=pinjaman)
p <- predict(modellda5, pinjaman)
mean(p$class==pinjaman$Y)
```

```
[1] 0.78125
```

4.2 Analisis Diskriminan Tiga Grup

4.2.1 Data

```
data("iris")
head(iris)
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa
4	4.6	3.1	1.5	0.2	setosa
5	5.0	3.6	1.4	0.2	setosa
6	5.4	3.9	1.7	0.4	setosa

```
str(iris)
```

```
'data.frame': 150 obs. of 5 variables:
 $ Sepal.Length: num 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
 $ Sepal.Width : num 3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
 $ Petal.Length: num 1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
 $ Petal.Width : num 0.2 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
 $ Species : Factor w/ 3 levels "setosa","versicolor",...: 1 1 1 1 1 1 1 1 1 1 ...
```

```
library(MASS)
lda.iris <- lda(Species ~ ., iris)
lda.iris
```

Call:

```
lda(Species ~ ., data = iris)
```

Prior probabilities of groups:

```
      setosa versicolor virginica
0.3333333  0.3333333  0.3333333
```

Group means:

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
setosa	5.006	3.428	1.462	0.246
versicolor	5.936	2.770	4.260	1.326
virginica	6.588	2.974	5.552	2.026

Coefficients of linear discriminants:

	LD1	LD2
Sepal.Length	0.8293776	-0.02410215
Sepal.Width	1.5344731	-2.16452123
Petal.Length	-2.2012117	0.93192121
Petal.Width	-2.8104603	-2.83918785

Proportion of trace:

	LD1	LD2
	0.9912	0.0088

4.2.2 Uji Signifikansi Fungsi Diskriminan

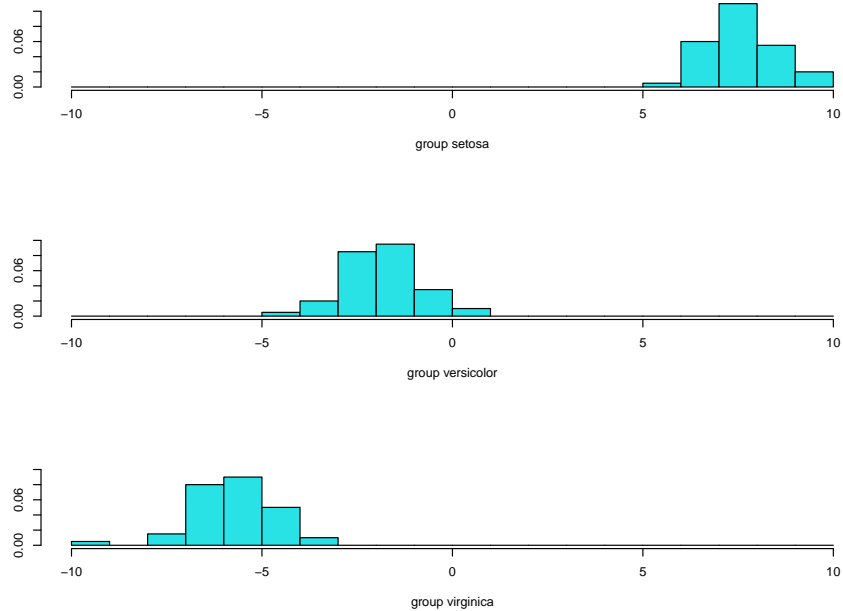
```
m <- manova(cbind(iris$Sepal.Length, iris$Sepal.Width, iris$Petal.Length,
                  iris$Petal.Width) ~ iris$Species)
summary(m, test = 'Wilks')
```

	Df	Wilks	approx F	num Df	den Df	Pr(>F)
iris\$Species	2	0.023439	199.15	8	288	< 2.2e-16 ***
Residuals	147					

 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

4.2.3 Akurasi

```
p <- predict(lda.iris, iris)
ldahist(data = p$x, g = iris$Species)
```

```
table(p$class, iris$Species)
```

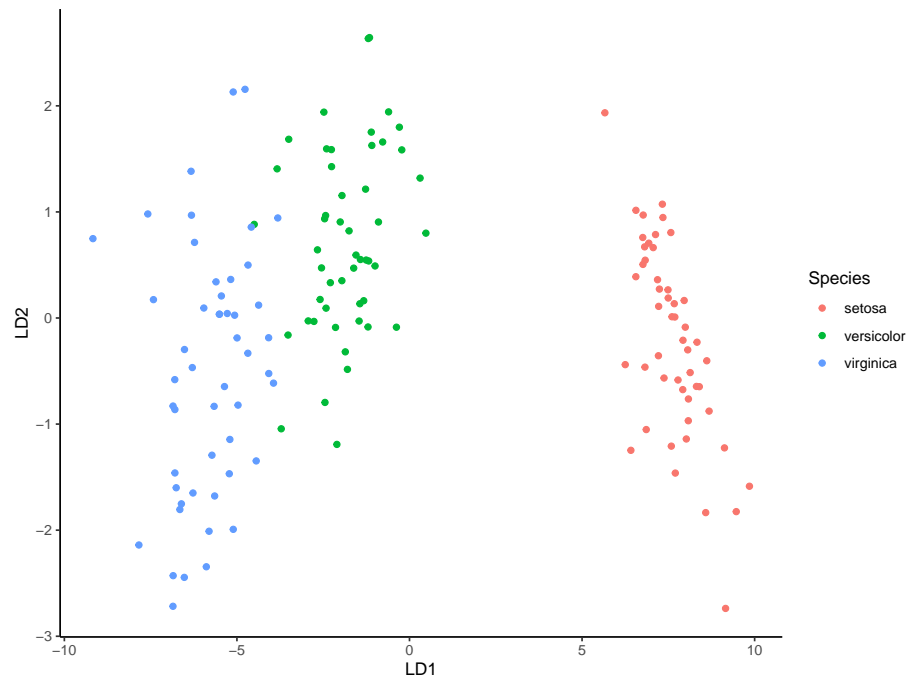
	setosa	versicolor	virginica
setosa	50	0	0
versicolor	0	48	1
virginica	0	2	49

```
mean(p$class==iris$Species)
```

```
[1] 0.98
```

4.2.4. Visualisasi

```
library(ggplot2)
lda.data <- cbind(iris, p$x)
ggplot(lda.data, aes(LD1, LD2)) +
  geom_point(aes(color = Species)) + theme_classic()
```



4.2.5 Pemodelan Kuadratik

```
qda.iris <- qda(Species ~ ., data=iris)
qda.iris
```

Call:
qda(Species ~ ., data = iris)

Prior probabilities of groups:
 setosa versicolor virginica
 0.3333333 0.3333333 0.3333333

Group means:

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
setosa	5.006	3.428	1.462	0.246
versicolor	5.936	2.770	4.260	1.326
virginica	6.588	2.974	5.552	2.026

```
p <- predict(qda.iris, iris)
mean(p$class==iris$Species)
```

```
[1] 0.98
```

4.2.6 Tipe Diskriminan Lainnya

```
# Mixture discriminant analysis - MDA
# install.packages("mda")
library(mda)
mda.iris <- mda(Species ~ ., data=iris)
mda.iris
```

Call:

```
mda(formula = Species ~ ., data = iris)
```

Dimension: 4

Percent Between-Group Variance Explained:

v1	v2	v3	v4
95.06	97.78	99.59	100.00

Degrees of Freedom (per dimension): 5

Training Misclassification Error: 0.01333 (N = 150)

Deviance: 13.302

```
p <- predict(mda.iris, iris)
mean(p==iris$Species)
```

```
[1] 0.9866667
```

```
# Flexible discriminant analysis - FDA
fda.iris <- fda(Species ~ ., data=iris)
fda.iris
```

Call:

```
fda(formula = Species ~ ., data = iris)
```

Dimension: 2

Percent Between-Group Variance Explained:

v1	v2
99.12	100.00

Degrees of Freedom (per dimension): 5

Training Misclassification Error: 0.02 (N = 150)

```
p <- predict(fda.iris, iris)
mean(p==iris$Species)
```

```
[1] 0.98
```

```
# Regularized discriminant analysis - RDA
rda.iris <- rda(Species ~ ., data=iris)
rda.iris
```

Call:

```
rda(formula = Species ~ ., data = iris)
```

Regularization parameters:

```
      gamma      lambda
0.1945631 0.5593066
```

Prior probabilities of groups:

```
      setosa versicolor virginica
0.3333333  0.3333333  0.3333333
```

Misclassification rate:

```
      apparent: 2 %
cross-validated: 2 %
```

```
p <- predict(rda.iris, iris)
mean(p$class==iris$Species)
```

```
[1] 0.98
```

Chapter 5

Cluster Analysis

5.1 Metode berhirarki

Ref: <https://rpubs.com/odenipinedo/cluster-analysis-in-R>

```
library(readxl)
Provinsi <- read_excel("Data/provinsi.xlsx")
Prov.scaled = scale(Provinsi[,c(4:8)])
rownames(Prov.scaled) = Provinsi$Provinsi
head(Prov.scaled)
```

	IPM	UHH	RLS	PPK	Gini
Aceh	0.20822137	0.04044611	0.7444782	-0.62264434	-0.8089350
Sumut	0.20085709	-0.39282591	1.0245728	-0.11277090	-0.6516207
Sumbar	0.36532598	-0.23835502	0.4747574	0.01481560	-1.2546590
Riau	0.50033775	0.59428078	0.5162529	0.19012890	-0.9138112
Jambi	0.05848104	0.50762638	-0.1165536	-0.18648754	-0.6778397
Sumsel	-0.21890679	-0.08765171	-0.2825356	-0.02582306	0.1349510

```
## membuat dissimilarity matrix
dprov = dist(Prov.scaled, method="euclidean")
```

```
c.comp = hclust(dprov, method = "complete")
cor(dprov , cophenetic(c.comp))
```

```
[1] 0.7853523
```

```
c.sing = hclust(dprov, method = "single")
cor(dprov , cophenetic(c.sing))
```

```
[1] 0.7905858
```

```
c.avrg = hclust(dprov, method = "average")
cor(dprov , cophenetic(c.avrg))
```

```
[1] 0.8092689
```

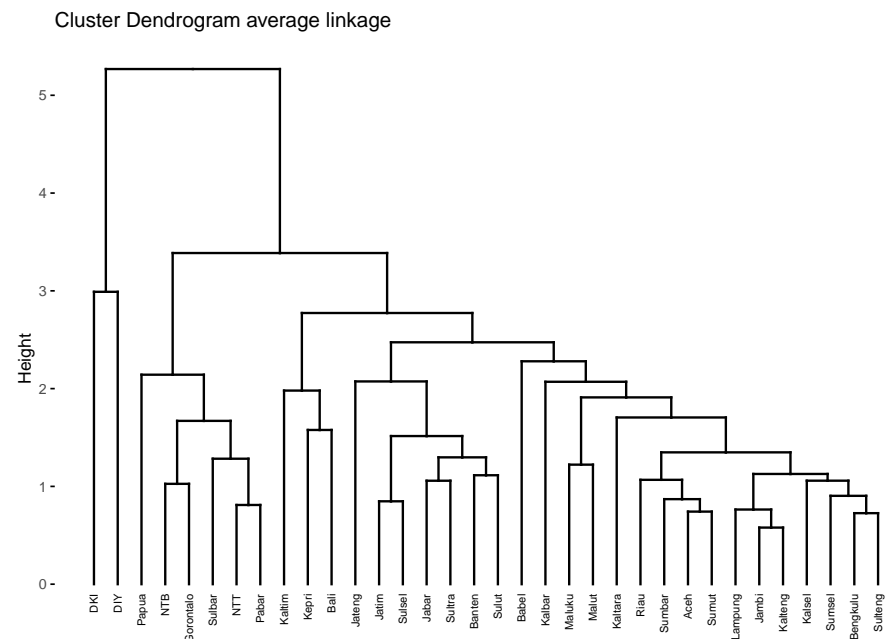
```
c.ward = hclust(dprov, method = "ward.D")
cor(dprov , cophenetic(c.ward))
```

```
[1] 0.5336018
```

```
c.ctrd = hclust(dprov, method = "centroid")
cor(dprov , cophenetic(c.ctrd))
```

```
[1] 0.7700878
```

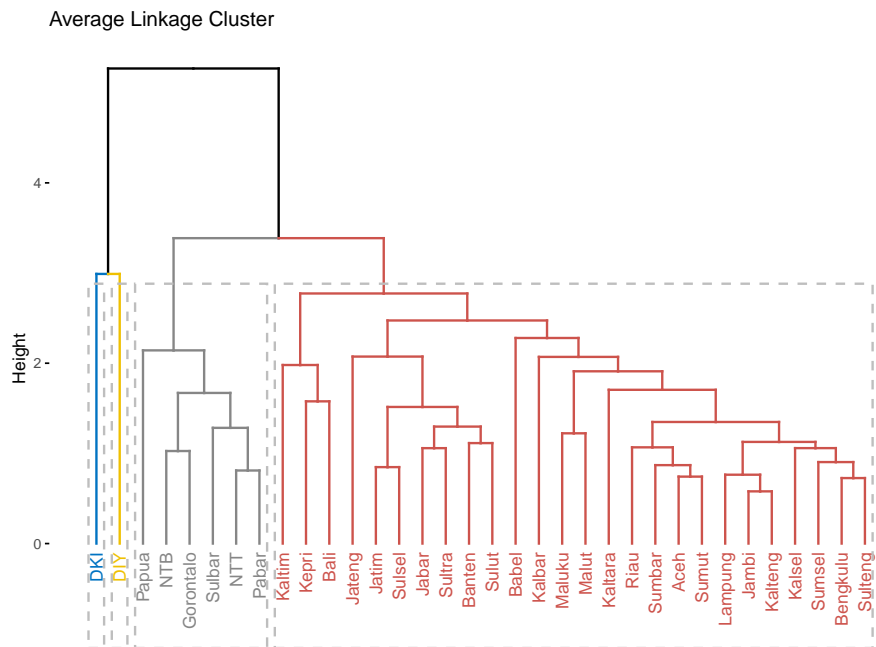
```
library(factoextra)
fviz_dend(c.avrg, cex = 0.5,
          main = "Cluster Dendrogram average linkage")
```



```
avg_coph <- cophenetic(c.avrg)
avg_clust <- cutree(c.avrg, k = 4)
table(avg_clust)
```

```
avg_clust
 1  2  3  4
26  1  1  6
```

```
fviz_dend(c.avrg, k = 4,
          k_colors = "jco",
          rect = T,
          main = "Average Linkage Cluster")
```



```
library(clValid)
library(cluster)
# internal measures
internal <- clValid(Prov.scaled, nClust = 2:6,
                   clMethods = "hierarchical",
                   validation = "internal",
                   metric = "euclidean",
                   method = "average")
summary(internal)
```

Clustering Methods:
hierarchical

Cluster sizes:
2 3 4 5 6

Validation Measures:

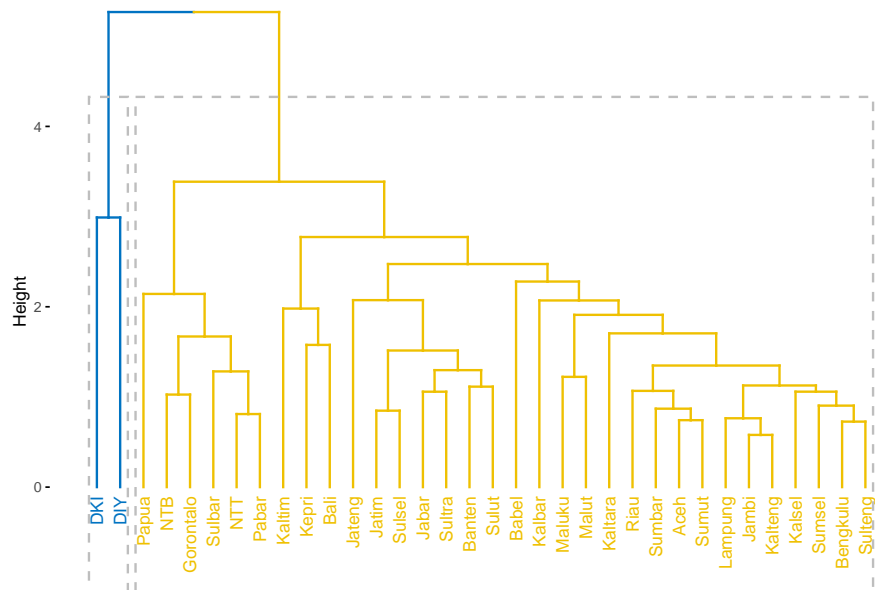
		2	3	4	5	6
hierarchical	Connectivity	4.5246	10.3012	11.6345	18.3198	24.1508
	Dunn	0.3637	0.3703	0.3703	0.3224	0.3592
	Silhouette	0.4915	0.3484	0.3092	0.2567	0.3117

Optimal Scores:

	Score	Method	Clusters
Connectivity	4.5246	hierarchical	2
Dunn	0.3703	hierarchical	3
Silhouette	0.4915	hierarchical	2

```
fviz_dend(c.avrg, k = 2,
          k_colors = "jco",
          rect = T,
          main = "Average Linkage Cluster")
```

Average Linkage Cluster

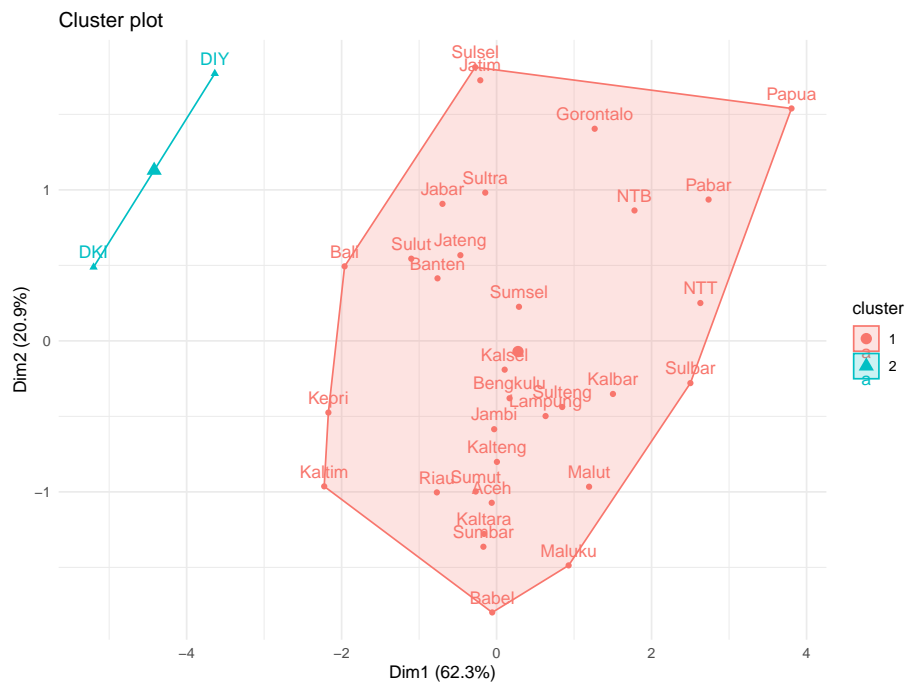


```
group = cutree(c.avrg, k = 2)
group
```

Aceh	Sumut	Sumbar	Riau	Jambi	Sumsel	Bengkulu	Lampung
1	1	1	1	1	1	1	1
Babel	Kepri	DKI	Jabar	Jateng	DIY	Jatim	Banten

1	1	2	1	1	2	1	1
Bali	NTB	NTT	Kalbar	Kalteng	Kalsel	Kaltim	Kaltara
1	1	1	1	1	1	1	1
Sulut	Sulteng	Sulsel	Sultra	Gorontalo	Sulbar	Maluku	Malut
1	1	1	1	1	1	1	1
Pabar	Papua						
1	1						

```
fviz_cluster(list(data = Prov.scaled,
                  cluster = group)) +
  theme_minimal()
```



```
prcomp(Prov.scaled)
```

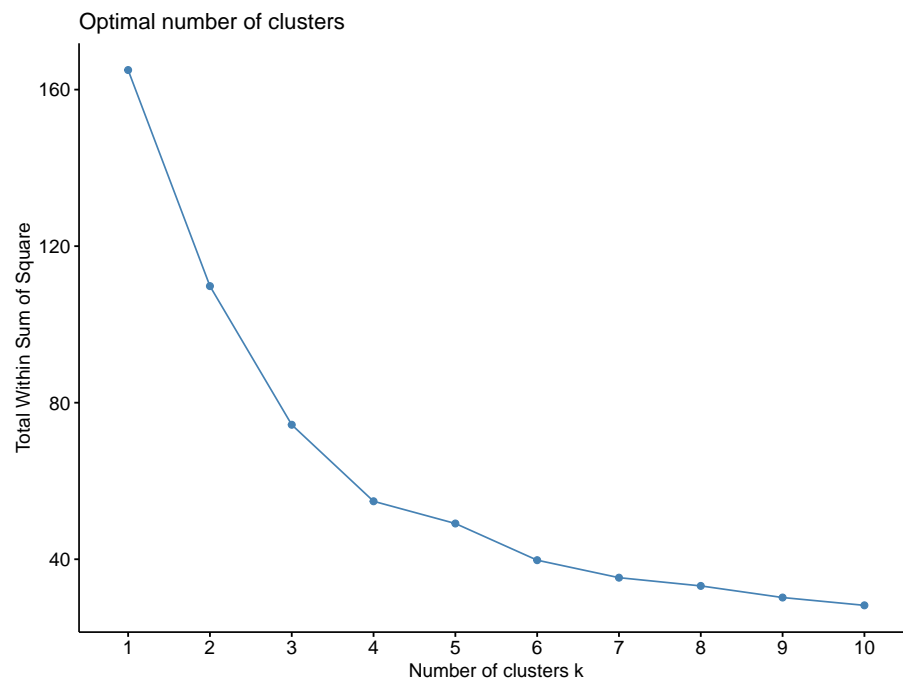
Standard deviations (1, ..., p=5):

```
[1] 1.7653705 1.0227284 0.7270850 0.5299864 0.1671984
```

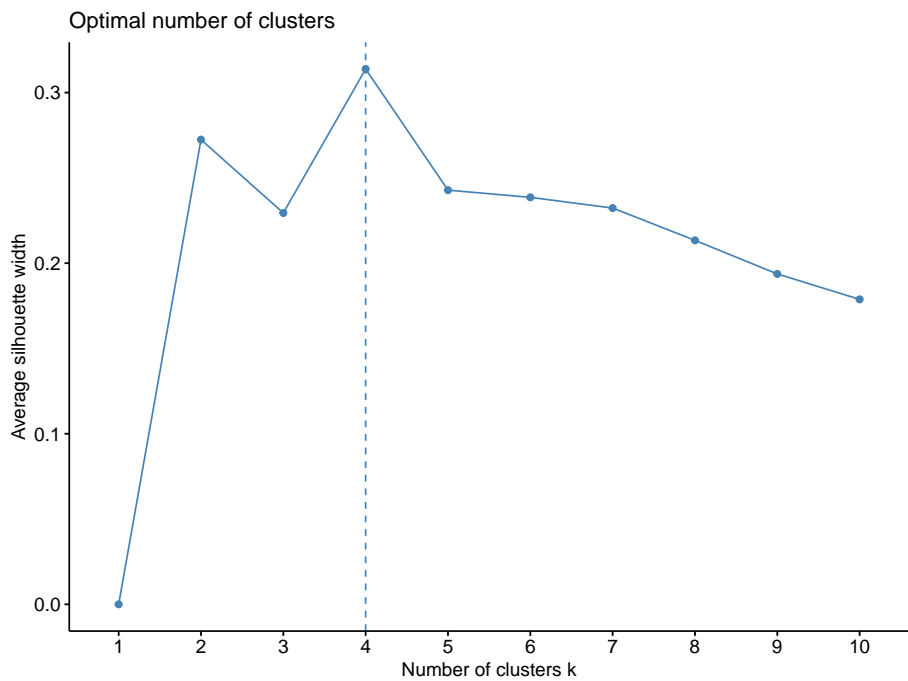
Rotation (n x k) = (5 x 5):

	PC1	PC2	PC3	PC4	PC5
IPM	-0.5601680	-0.05311199	-0.005227509	-0.0006949187	-0.82665781
UHH	-0.4513030	0.05646383	-0.811065327	0.2024129889	0.30714735
RLS	-0.4591728	-0.33781331	0.497619343	0.5648220282	0.32923179
PPK	-0.5069166	0.09086739	0.227624805	-0.7546468667	0.33685862
Gini	-0.1213811	0.93360390	0.206658283	0.2655422416	0.02073819

5.2 Metode tidak berhirarki - kmeans



```
fviz_nbclust(Prov.scaled, kmeans, method = "silhouette")
```



```
set.seed(1)
km = kmeans(Prov.scaled, centers=4)
km
```

K-means clustering with 4 clusters of sizes 5, 7, 16, 6

Cluster means:

	IPM	UHH	RLS	PPK	Gini
1	1.67223995	1.1202353	1.3689855	1.75840321	0.6331131
2	0.22785944	0.6620973	-0.1491572	0.09292014	0.9739608
3	-0.08819085	-0.1001318	0.1246391	-0.24567350	-0.7991029
4	-1.42419372	-1.4389581	-1.2991755	-0.91861351	0.4670591

Clustering vector:

Aceh	Sumut	Sumbar	Riau	Jambi	Sumsel	Bengkulu	Lampung
3	3	3	3	3	3	3	3
Babel	Kepri	DKI	Jabar	Jateng	DIY	Jatim	Banten
3	1	1	2	2	1	2	2
Bali	NTB	NTT	Kalbar	Kalteng	Kalsel	Kaltim	Kaltara
1	4	4	3	3	3	1	3
Sulut	Sulteng	Sulsel	Sultra	Gorontalo	Sulbar	Maluku	Malut
2	3	2	2	4	4	3	3
Pabar	Papua						
4	4						

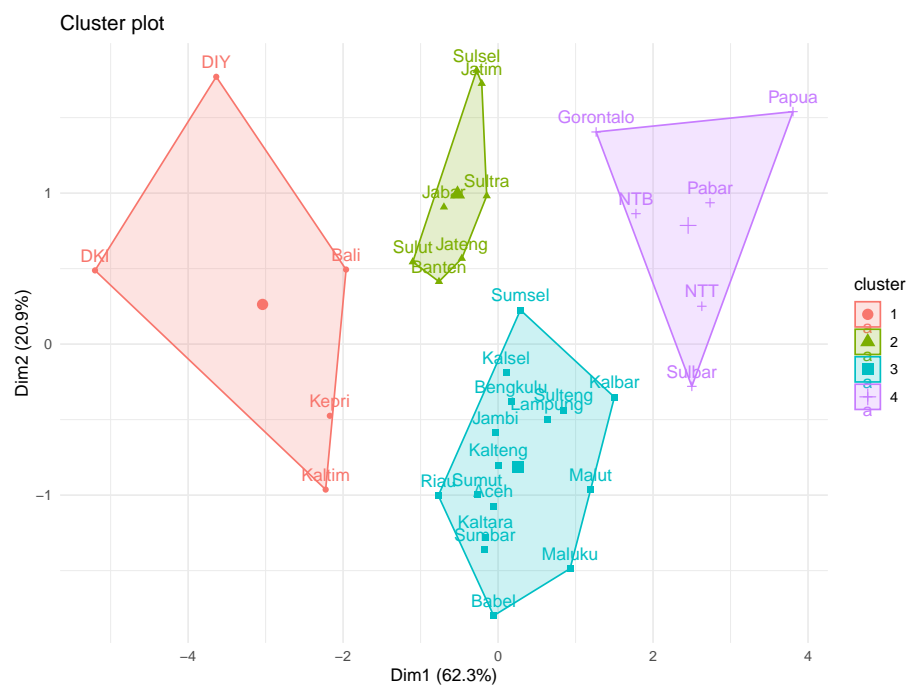
Within cluster sum of squares by cluster:

```
[1] 17.054859 7.933134 22.111511 7.711994
(between_SS / total_SS = 66.8 %)
```

Available components:

```
[1] "cluster"      "centers"      "totss"        "withinss"     "tot.withinss"
[6] "betweenss"    "size"         "iter"         "ifault"
```

```
fviz_cluster(list(data = Prov.scaled, cluster = km$cluster)) + theme_minimal()
```



Chapter 6

PCA Analysis and Biplot

6.1 PCA

```
# impor data dari excel, beri nama: Provinsi
library(readxl)
Provinsi = read_excel("Data/provinsi.xlsx")
Prov.scaled = scale(Provinsi[,c(4:8)])
round(cor(Prov.scaled),3)
```

	IPM	UHH	RLS	PPK	Gini
IPM	1.000	0.780	0.811	0.872	0.159
UHH	0.780	1.000	0.447	0.581	0.153
RLS	0.811	0.447	1.000	0.637	-0.059
PPK	0.872	0.581	0.637	1.000	0.249
Gini	0.159	0.153	-0.059	0.249	1.000

```
# PCA langkah manual
Prov.eigen = eigen(cov(Prov.scaled))
Prov.eigen
```

```
eigen() decomposition
$values
[1] 3.11653307 1.04597347 0.52865259 0.28088555 0.02795532
```

```
$vectors
```

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	-0.5601680	-0.05311199	0.005227509	-0.0006949187	0.82665781
[2,]	-0.4513030	0.05646383	0.811065327	0.2024129889	-0.30714735
[3,]	-0.4591728	-0.33781331	-0.497619343	0.5648220282	-0.32923179
[4,]	-0.5069166	0.09086739	-0.227624805	-0.7546468667	-0.33685862
[5,]	-0.1213811	0.93360390	-0.206658283	0.2655422416	-0.02073819

```
Prov.eigen$values
```

```
[1] 3.11653307 1.04597347 0.52865259 0.28088555 0.02795532
```

```
Prov.eigen$values/5
```

```
[1] 0.623306615 0.209194694 0.105730518 0.056177109 0.005591064
```

```
cumsum(Prov.eigen$values/5)
```

```
[1] 0.6233066 0.8325013 0.9382318 0.9944089 1.0000000
```

```
Prov.pc = as.matrix(Prov.scaled) %*% Prov.eigen$vectors  
round(Prov.pc,3)
```

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	-0.063	-1.072	-0.028	0.684	0.141
[2,]	-0.269	-0.998	-0.667	0.411	0.001
[3,]	-0.170	-1.363	-0.172	-0.125	0.240
[4,]	-0.771	-1.003	0.373	0.025	0.016
[5,]	-0.032	-0.585	0.653	-0.002	0.008
[6,]	0.289	0.226	0.046	-0.122	-0.055
[7,]	0.167	-0.380	-0.246	0.160	0.149
[8,]	0.632	-0.498	0.644	-0.115	-0.054
[9,]	-0.057	-1.798	0.675	-1.464	-0.089
[10,]	-2.171	-0.475	-1.111	-0.280	-0.100
[11,]	-5.201	0.488	-1.517	-0.455	-0.423
[12,]	-0.699	0.908	0.818	0.388	-0.141
[13,]	-0.467	0.567	1.901	-0.226	-0.064
[14,]	-3.637	1.770	0.377	0.349	0.361
[15,]	-0.211	1.726	0.527	-0.300	0.118
[16,]	-0.763	0.414	-0.365	-0.198	0.007
[17,]	-1.962	0.494	0.024	-0.719	0.052
[18,]	1.779	0.864	-0.537	-0.824	0.322
[19,]	2.630	0.251	-0.136	0.131	0.011
[20,]	1.501	-0.351	1.137	-0.243	-0.049
[21,]	0.004	-0.801	0.195	-0.277	-0.039
[22,]	0.104	-0.191	-0.358	-0.828	0.030
[23,]	-2.225	-0.963	0.752	0.305	0.020
[24,]	-0.162	-1.278	1.179	0.698	-0.173
[25,]	-1.101	0.544	-0.154	0.823	-0.143
[26,]	0.847	-0.438	-0.472	0.097	0.061
[27,]	-0.276	1.813	-0.105	0.254	0.105
[28,]	-0.147	0.982	0.109	0.925	-0.004
[29,]	1.266	1.405	-0.356	-0.169	0.136
[30,]	2.501	-0.280	-0.787	-0.540	0.062
[31,]	0.929	-1.487	-1.397	0.735	0.080

```
[32,] 1.193 -0.966 -0.326 0.739 -0.008
[33,] 2.735 0.936 -0.533 0.218 -0.091
[34,] 3.806 1.539 -0.145 -0.057 -0.487
```

```
# dengan fungsi prcomp
pc = prcomp(x = Prov.scaled, center=TRUE, scale=TRUE)
summary(pc)
```

Importance of components:

	PC1	PC2	PC3	PC4	PC5
Standard deviation	1.7654	1.0227	0.7271	0.52999	0.16720
Proportion of Variance	0.6233	0.2092	0.1057	0.05618	0.00559
Cumulative Proportion	0.6233	0.8325	0.9382	0.99441	1.00000

```
round(pc$x,3)#scores
```

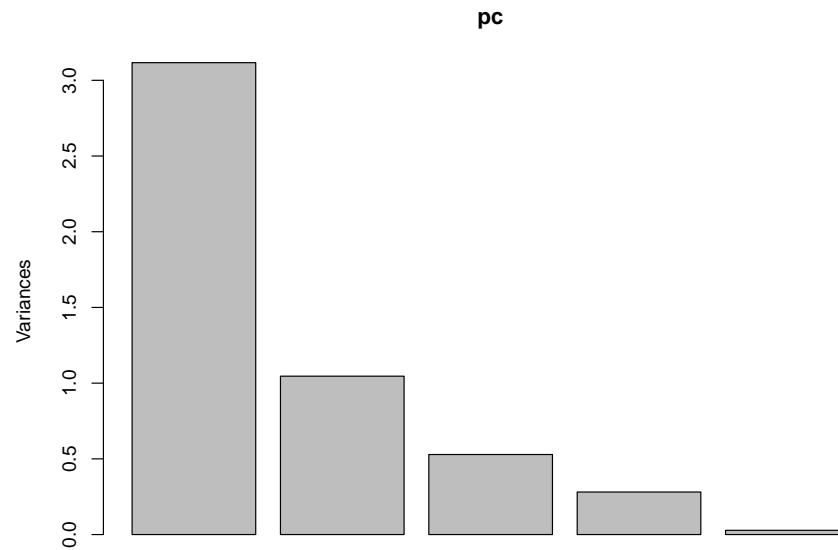
	PC1	PC2	PC3	PC4	PC5
[1,]	-0.063	-1.072	0.028	0.684	-0.141
[2,]	-0.269	-0.998	0.667	0.411	-0.001
[3,]	-0.170	-1.363	0.172	-0.125	-0.240
[4,]	-0.771	-1.003	-0.373	0.025	-0.016
[5,]	-0.032	-0.585	-0.653	-0.002	-0.008
[6,]	0.289	0.226	-0.046	-0.122	0.055
[7,]	0.167	-0.380	0.246	0.160	-0.149
[8,]	0.632	-0.498	-0.644	-0.115	0.054
[9,]	-0.057	-1.798	-0.675	-1.464	0.089
[10,]	-2.171	-0.475	1.111	-0.280	0.100
[11,]	-5.201	0.488	1.517	-0.455	0.423
[12,]	-0.699	0.908	-0.818	0.388	0.141
[13,]	-0.467	0.567	-1.901	-0.226	0.064
[14,]	-3.637	1.770	-0.377	0.349	-0.361
[15,]	-0.211	1.726	-0.527	-0.300	-0.118
[16,]	-0.763	0.414	0.365	-0.198	-0.007
[17,]	-1.962	0.494	-0.024	-0.719	-0.052
[18,]	1.779	0.864	0.537	-0.824	-0.322
[19,]	2.630	0.251	0.136	0.131	-0.011
[20,]	1.501	-0.351	-1.137	-0.243	0.049
[21,]	0.004	-0.801	-0.195	-0.277	0.039
[22,]	0.104	-0.191	0.358	-0.828	-0.030
[23,]	-2.225	-0.963	-0.752	0.305	-0.020
[24,]	-0.162	-1.278	-1.179	0.698	0.173
[25,]	-1.101	0.544	0.154	0.823	0.143
[26,]	0.847	-0.438	0.472	0.097	-0.061
[27,]	-0.276	1.813	0.105	0.254	-0.105
[28,]	-0.147	0.982	-0.109	0.925	0.004
[29,]	1.266	1.405	0.356	-0.169	-0.136
[30,]	2.501	-0.280	0.787	-0.540	-0.062

```
[31,] 0.929 -1.487 1.397 0.735 -0.080
[32,] 1.193 -0.966 0.326 0.739 0.008
[33,] 2.735 0.936 0.533 0.218 0.091
[34,] 3.806 1.539 0.145 -0.057 0.487
```

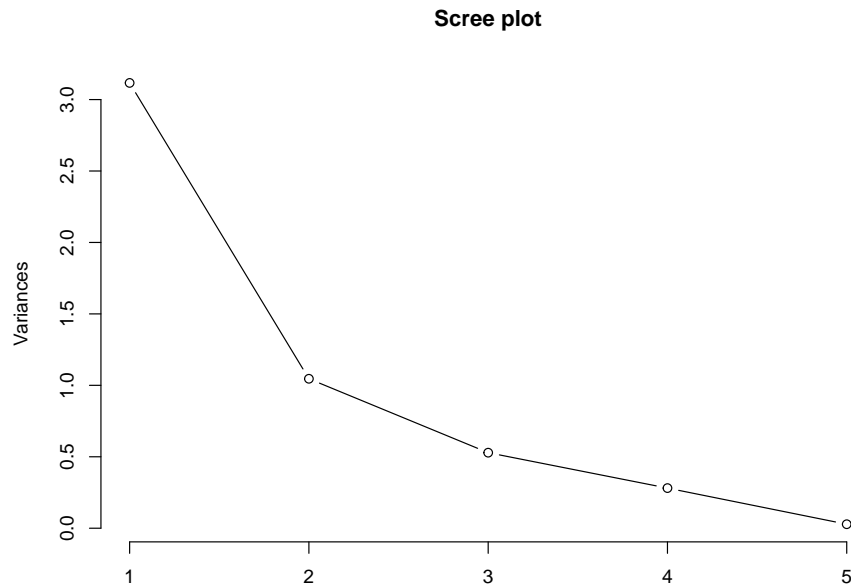
```
round(pc$rotation,3) #loadings
```

	PC1	PC2	PC3	PC4	PC5
IPM	-0.560	-0.053	-0.005	-0.001	-0.827
UHH	-0.451	0.056	-0.811	0.202	0.307
RLS	-0.459	-0.338	0.498	0.565	0.329
PPK	-0.507	0.091	0.228	-0.755	0.337
Gini	-0.121	0.934	0.207	0.266	0.021

```
plot(pc)
```



```
screeplot(x = pc, type="line", main="Scree plot")
```

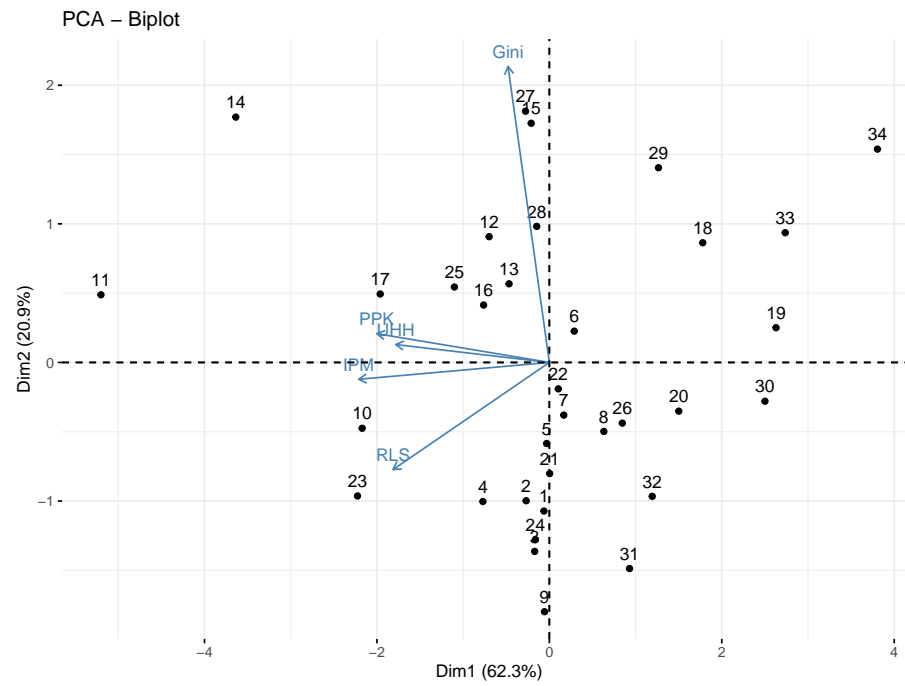



```
# korelasi variabel asli dengan PC
data = cbind(Prov.pc, Prov.scaled)
korelasi = cor(data)
korelasi[6:10,1:2]
```

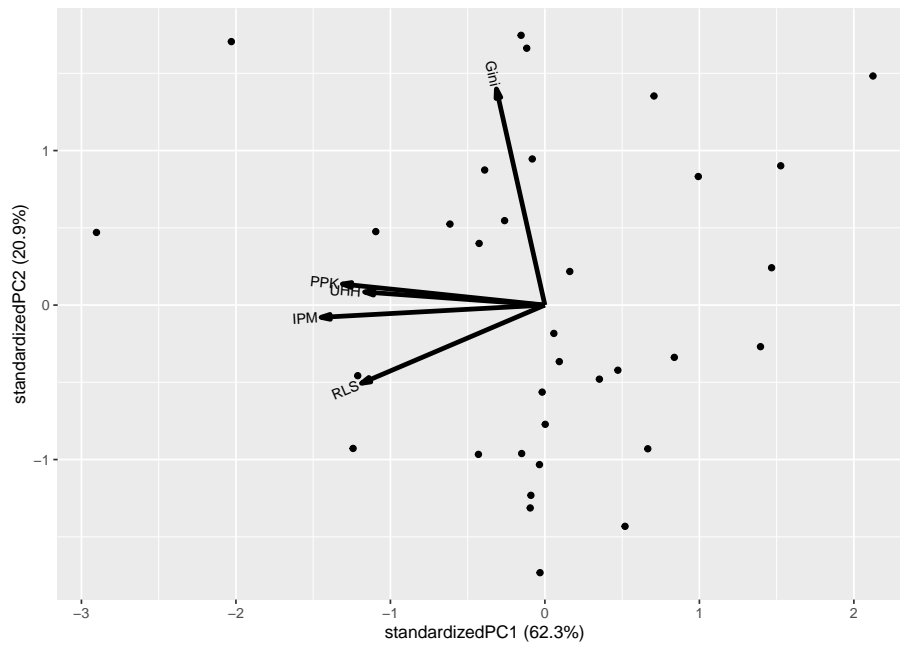
```
IPM  -0.9889040 -0.05431915
UHH  -0.7967169  0.05774717
RLS  -0.8106101 -0.34549128
PPK  -0.8948956  0.09293267
Gini -0.2142826  0.95482326
```

6.3. Biplot

```
# biplot
library(factoextra)
fviz_pca(pc)
```

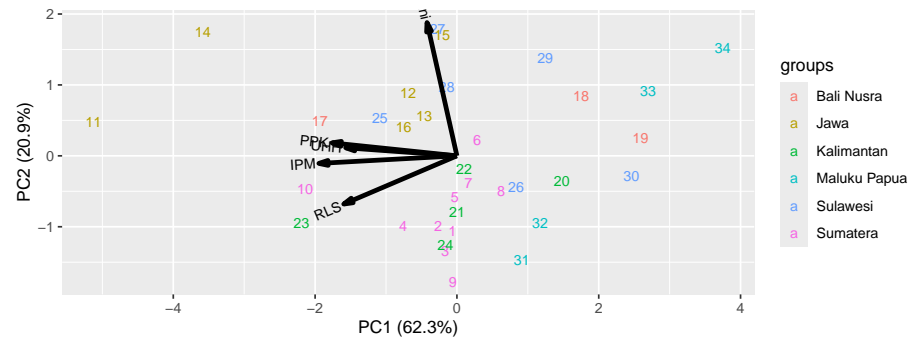


```
# alternatif bentuk biplot
# install.packages("remotes")
# remotes::install_github("vqv/ggbiplot")
library(ggbiplot)
ggbiplot(pc)
```

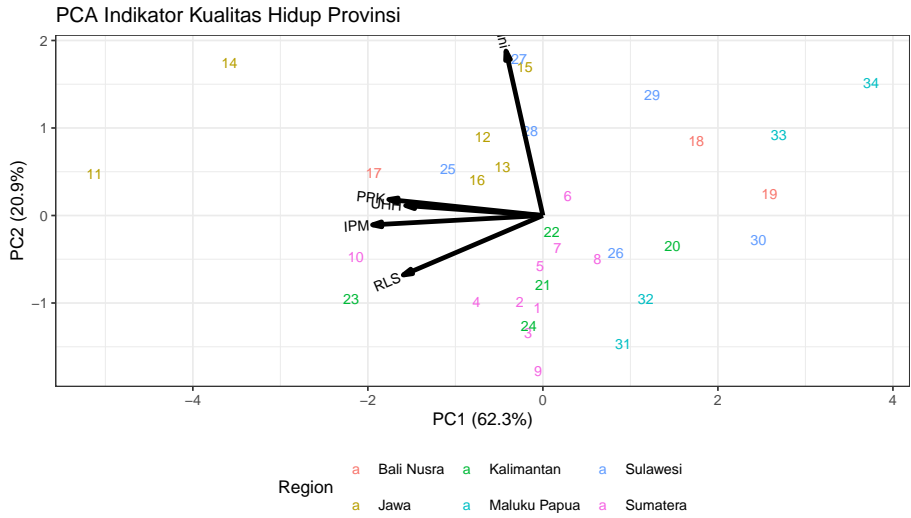


```
biplot = ggbiplot(pcobj = pc,
  choices = c(1,2),
  obs.scale = 1, var.scale = 1,
  labels = row.names(Provinsi),
  varname.size = 3,
  varname.abbrev = FALSE,
  var.axes = TRUE,
  group = Provinsi$Region)

biplot
```



```
biplot2 = biplot + theme_bw() +
  theme(legend.position="bottom") +
  labs(
    title = "PCA Indikator Kualitas Hidup Provinsi",
    color = "Region")
biplot2
```



Chapter 7

Factor Analysis and Structural Equation Modeling (SEM)

7.1 Analisis Faktor

```
harga <- read.csv("Data/harga.csv")
head(harga)
```

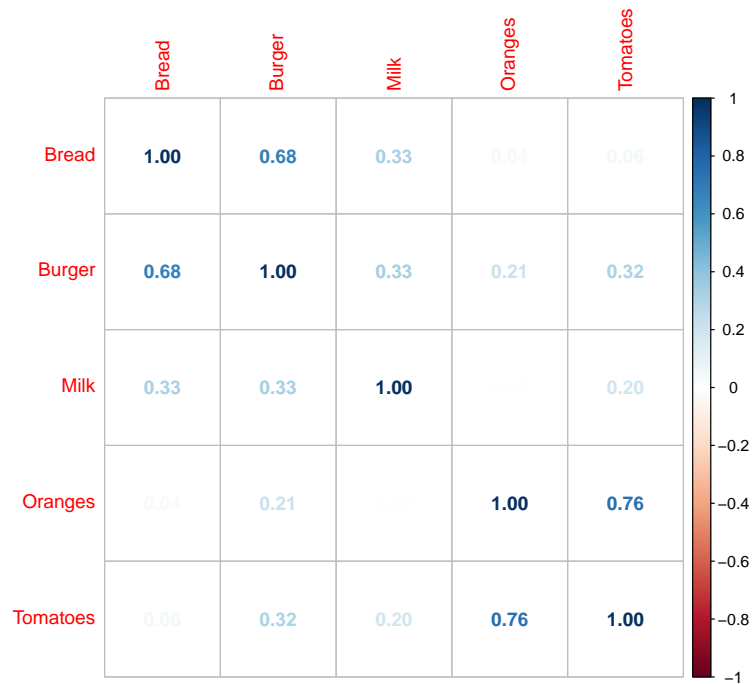
	City	Bread	Burger	Milk	Oranges	Tomatoes
1	Atlanta	24.5	94.5	73.9	80.1	41.6
2	Baltimore	26.5	91.0	67.5	74.6	33.3
3	Boston	29.7	100.8	61.4	104.0	59.6
4	Buffalo	22.8	86.6	65.3	118.4	61.2
5	Chicago	26.7	86.7	62.7	105.9	60.2
6	Cincinnati	25.3	102.5	63.3	99.3	45.6

```
str(harga)
```

```
'data.frame':  23 obs. of  6 variables:
 $ City      : chr  "Atlanta " "Baltimore " "Boston " "Buffalo " ...
 $ Bread     : num  24.5 26.5 29.7 22.8 26.7 25.3 22.8 23.3 24.1 29.3 ...
 $ Burger    : num  94.5 91 100.8 86.6 86.7 ...
 $ Milk      : num  73.9 67.5 61.4 65.3 62.7 63.3 52.4 62.5 51.5 80.2 ...
 $ Oranges   : num  80.1 74.6 104 118.4 105.9 ...
 $ Tomatoes  : num  41.6 33.3 59.6 61.2 60.2 45.6 60.1 60.8 60.5 71.7 ...
```

7.1.1 EFA

```
library(corrplot)
corrplot(cor(harga[,2:6]), method="number")
```



```
library(psych)
KMO(harga[,2:6])
```

Kaiser-Meyer-Olkin factor adequacy

Call: KMO(r = harga[, 2:6])

Overall MSA = 0.52

MSA for each item =

	Bread	Burger	Milk	Oranges	Tomatoes
MSA	0.52	0.58	0.59	0.49	0.48

```
# Bartlett's Test of Sphericity
```

```
cortest.bartlett(harga[,2:6])
```

```
$chisq
```

```
[1] 36.46285
```

```
$p.value
```

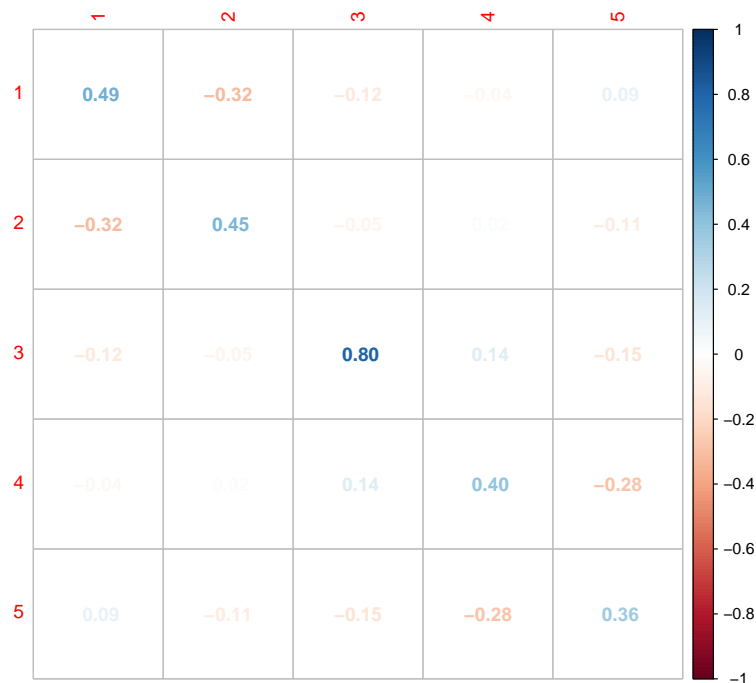
```
[1] 7.006877e-05
```

```
$df
```



```
[1] 10
```

```
# Anti image correlation (AIC)
corrplot(KMO(harga[,2:6])$ImCo, method="number")
```



```
# Determinan positif
det(cor(harga[,2:6]))
```

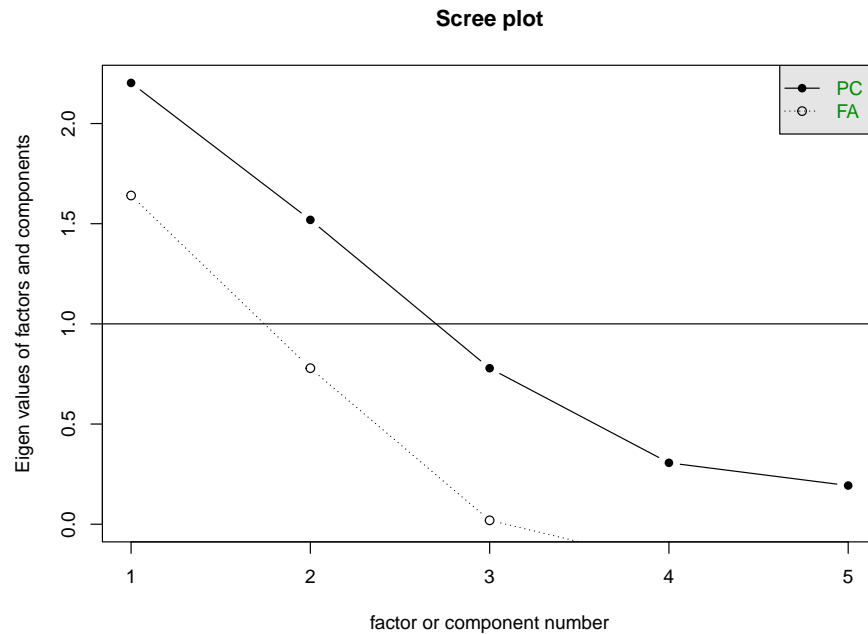
```
[1] 0.1541406
```

```
# Principal component analysis (PCA)
pca1 = princomp(harga[,2:6], scores=TRUE, cor=TRUE)
summary(pca1)
```

Importance of components:

	Comp.1	Comp.2	Comp.3	Comp.4	Comp.5
Standard deviation	1.4841538	1.2325047	0.8824610	0.55357732	0.43935672
Proportion of Variance	0.4405425	0.3038136	0.1557475	0.06128957	0.03860687
Cumulative Proportion	0.4405425	0.7443561	0.9001036	0.96139313	1.00000000

```
scree(harga[,2:6])
```



```
# Menentukan faktor loading Analisis faktor loading
loadings(pca1)
```

Loadings:

	Comp.1	Comp.2	Comp.3	Comp.4	Comp.5
Bread	0.436	0.484	0.354	0.597	0.306
Burger	0.542	0.292	0.307	-0.657	-0.309
Milk	0.346	0.308	-0.866		-0.163
Oranges	0.410	-0.579	0.108	0.399	-0.571
Tomatoes	0.478	-0.500	-0.137	-0.211	0.677

	Comp.1	Comp.2	Comp.3	Comp.4	Comp.5
SS loadings	1.0	1.0	1.0	1.0	1.0
Proportion Var	0.2	0.2	0.2	0.2	0.2
Cumulative Var	0.2	0.4	0.6	0.8	1.0

```
# Rotasi untuk mengkonfirmasi hasil analisis loading
fa1 = factanal(harga[,2:6], factor=2, rotation="varimax")
fa1
```

Call:

```
factanal(x = harga[, 2:6], factors = 2, rotation = "varimax")
```

Uniquenesses:

Bread	Burger	Milk	Oranges	Tomatoes
0.239	0.318	0.830	0.420	0.005

Loadings:

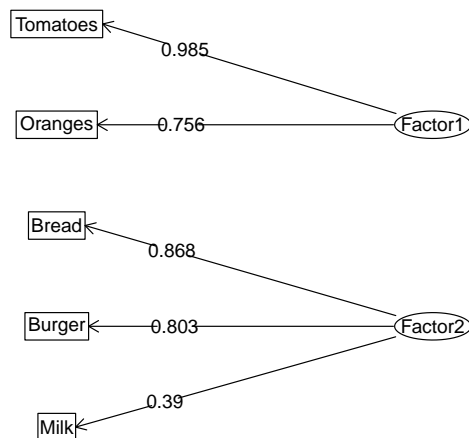
	Factor1	Factor2
Bread		0.868
Burger	0.195	0.803
Milk	0.135	0.390
Oranges	0.756	
Tomatoes	0.985	0.157

	Factor1	Factor2
SS loadings	1.605	1.583
Proportion Var	0.321	0.317
Cumulative Var	0.321	0.638

Test of the hypothesis that 2 factors are sufficient.
 The chi square statistic is 1.16 on 1 degree of freedom.
 The p-value is 0.282

```
# Diagram jalur hasil analisis EFA dan menampilkan faktor loading-nya
fa.diagram(fa1$loadings, digits = 3)
```

Factor Analysis



7.1.2 CFA

```
# Spesifikasi model
attach(harga)
modell1 <- "
F1 =~ Tomatoes + Oranges
F2 =~ Bread + Burger + Milk
F1 ~~ F2 "

library(lavaan)
fitmod = cfa(modell1, data = harga)
summary(fitmod, fit.measures = TRUE, standardized = TRUE)
```

lavaan 0.6-19 ended normally after 85 iterations

Estimator	ML
Optimization method	NLMINB
Number of model parameters	11
Number of observations	23

Model Test User Model:

Test statistic	3.642
Degrees of freedom	4
P-value (Chi-square)	0.457

Model Test Baseline Model:

Test statistic	43.007
Degrees of freedom	10
P-value	0.000

User Model versus Baseline Model:

Comparative Fit Index (CFI)	1.000
Tucker-Lewis Index (TLI)	1.027

Loglikelihood and Information Criteria:

Loglikelihood user model (H0)	-367.812
Loglikelihood unrestricted model (H1)	-365.991
Akaike (AIC)	757.623
Bayesian (BIC)	770.114
Sample-size adjusted Bayesian (SABIC)	736.072

Root Mean Square Error of Approximation:

RMSEA	0.000
90 Percent confidence interval - lower	0.000
90 Percent confidence interval - upper	0.302
P-value H ₀ : RMSEA ≤ 0.050	0.487
P-value H ₀ : RMSEA ≥ 0.080	0.469

Standardized Root Mean Square Residual:

SRMR	0.065
------	-------

Parameter Estimates:

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
F1 =~						
Tomatoes	1.000				10.659	1.062
Oranges	0.934	0.580	1.611	0.107	9.952	0.715
F2 =~						
Bread	1.000				1.622	0.662
Burger	4.700	2.464	1.907	0.056	7.623	1.032
Milk	1.307	0.858	1.523	0.128	2.119	0.312

Covariances:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
F1 ~~						
F2	5.161	4.482	1.151	0.250	0.299	0.299

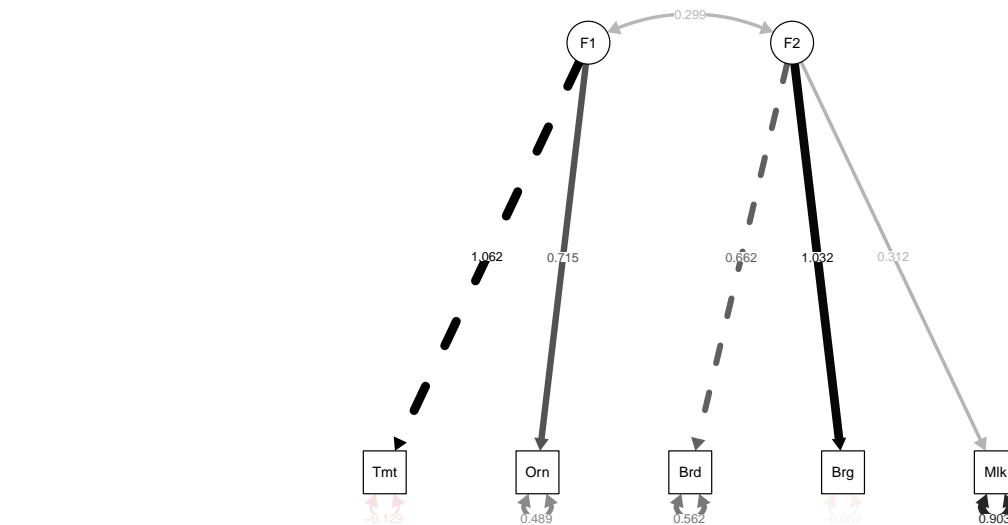
Variances:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
.Tomatoes	-12.966	66.742	-0.194	0.846	-12.966	-0.129
.Oranges	94.906	64.476	1.472	0.141	94.906	0.489
.Bread	3.381	1.581	2.138	0.033	3.381	0.562
.Burger	-3.518	27.199	-0.129	0.897	-3.518	-0.064
.Milk	41.714	12.439	3.354	0.001	41.714	0.903
F1	113.605	72.842	1.560	0.119	1.000	1.000
F2	2.631	1.912	1.376	0.169	1.000	1.000

`fitmeasures(fitmod)`

npar	fmin	chisq
11.000	0.079	3.642
df	pvalue	baseline.chisq
4.000	0.457	43.007
baseline.df	baseline.pvalue	cfi
10.000	0.000	1.000
tli	nnfi	rfi
1.027	1.027	0.788
nfi	pnfi	ifi
0.915	0.366	1.009
rni	logl	unrestricted.logl
1.011	-367.812	-365.991
aic	bic	ntotal
757.623	770.114	23.000
bic2	rmsea	rmsea.ci.lower
736.072	0.000	0.000
rmsea.ci.upper	rmsea.ci.level	rmsea.pvalue
0.302	0.900	0.487
rmsea.close.h0	rmsea.notclose.pvalue	rmsea.notclose.h0
0.050	0.469	0.080
rmr	rmr_nomean	srmr
2.823	2.823	0.065
srmr_bentler	srmr_bentler_nomean	crmr
0.065	0.065	0.080
crmr_nomean	srmr_mplus	srmr_mplus_nomean
0.080	0.065	0.065
cn_05	cn_01	gfi
60.915	84.843	0.947
agfi	pgfi	mfi
0.803	0.253	1.008
ecvi		
1.115		

```
library(semPlot)
semPaths(fitmod, what='std', layout='tree', title = TRUE,
  posCol = 1, nDigits = 3,
  edge.label.cex=0.7,
  exoVar = FALSE,
  sizeMan = 5,
  sizeLat = 5)
```



```
# Estimasi Reliabilitas alpha cronbach
psych::alpha(harga[,2:6])
```

Reliability analysis

Call: psych::alpha(x = harga[, 2:6])

	raw_alpha	std.alpha	G6(smc)	average_r	S/N	ase	mean	sd	median_r
	0.63	0.67	0.77	0.29	2.1	0.1	67	5.8	0.26

95% confidence boundaries

	lower	alpha	upper
Feldt	0.32	0.63	0.82
Duhachek	0.42	0.63	0.83

Reliability if an item is dropped:

	raw_alpha	std.alpha	G6(smc)	average_r	S/N	alpha	se	var.r	med.r
Bread	0.64	0.63	0.68	0.30	1.7	0.110	0.065	0.26	
Burger	0.56	0.54	0.63	0.23	1.2	0.107	0.083	0.13	
Milk	0.64	0.68	0.78	0.34	2.1	0.091	0.096	0.26	
Oranges	0.55	0.65	0.66	0.32	1.9	0.140	0.043	0.32	
Tomatoes	0.37	0.59	0.61	0.26	1.4	0.197	0.062	0.27	

Item statistics

	n	raw.r	std.r	r.cor	r.drop	mean	sd
Bread	23	0.38	0.64	0.56	0.30	25	2.5
Burger	23	0.62	0.77	0.72	0.41	92	7.6
Milk	23	0.42	0.56	0.36	0.20	62	7.0
Oranges	23	0.82	0.61	0.56	0.49	103	14.2
Tomatoes	23	0.86	0.71	0.68	0.71	52	10.3

7.2 Model Persamaan Struktural (SEM)

```
library(lavaan)
library(semPlot)
```

```
library(readxl)
datasem <- read_excel("Data/Datalikert.xlsx")
head(datasem[,1:5])
```

```
# A tibble: 6 x 5
  Perusahaan Provinsi Pulau A1 A2
      <dbl> <chr>      <chr> <dbl> <dbl>
1         1 Jawa Barat Jawa      4      5
2         2 Jawa Timur Jawa      5      5
3         3 Jawa Timur Jawa      4      4
4         4 Jawa Barat Jawa      4      4
5         5 Jawa Timur Jawa      4      4
6         6 Jawa Timur Jawa      4      4
```

```
str(datasem)
```

```
tibble [300 x 45] (S3: tbl_df/tbl/data.frame)
 $ Perusahaan: num [1:300] 1 2 3 4 5 6 7 8 9 10 ...
 $ Provinsi  : chr [1:300] "Jawa Barat" "Jawa Timur" "Jawa Timur" "Jawa Barat" ...
 $ Pulau     : chr [1:300] "Jawa" "Jawa" "Jawa" "Jawa" ...
 $ A1        : num [1:300] 4 5 4 4 4 4 4 4 5 4 5 ...
 $ A2        : num [1:300] 5 5 4 4 4 4 4 4 5 4 5 ...
 $ A3        : num [1:300] 5 5 4 3 4 5 4 5 3 5 ...
 $ A4        : num [1:300] 4 5 4 4 3 4 4 5 3 5 ...
 $ A5        : num [1:300] 4 4 4 4 4 4 4 4 5 3 5 ...
 $ A6        : num [1:300] 4 5 4 4 4 4 4 4 5 3 4 ...
 $ A7        : num [1:300] 5 5 5 4 4 4 4 4 5 3 5 ...
 $ A8        : num [1:300] 5 5 5 4 4 4 4 4 5 3 4 ...
 $ Atotal    : num [1:300] 36 39 34 31 31 33 32 40 26 38 ...
 $ B1        : num [1:300] 4 4 4 4 3 5 3 3 3 4 ...
 $ B2        : num [1:300] 4 4 4 3 4 4 3 3 2 4 ...
 $ Btotal    : num [1:300] 8 8 8 7 7 9 6 6 5 8 ...
 $ C1        : num [1:300] 4 4 4 4 4 4 4 4 5 3 4 ...
 $ C2        : num [1:300] 4 4 4 4 4 4 4 4 4 3 4 ...
```



```

$ Ctotal      : num [1:300] 8 8 8 8 8 8 8 9 6 8 ...
$ D1          : num [1:300] 4 5 4 4 4 4 4 4 3 4 ...
$ D2          : num [1:300] 4 5 4 3 4 5 4 4 2 4 ...
$ D3          : num [1:300] 4 5 4 4 4 4 4 4 3 4 ...
$ D4          : num [1:300] 4 5 4 5 4 4 4 4 3 4 ...
$ Dtotal      : num [1:300] 16 20 16 16 16 17 16 16 11 16 ...
$ E1          : num [1:300] 5 5 4 4 4 4 4 4 3 5 ...
$ E2          : num [1:300] 5 5 4 4 4 5 4 4 3 5 ...
$ E3          : num [1:300] 5 5 4 4 4 5 4 5 4 5 ...
$ E4          : num [1:300] 4 5 4 3 4 5 4 4 3 4 ...
$ E5          : num [1:300] 4 5 4 4 3 5 4 4 3 4 ...
$ E6          : num [1:300] 4 5 4 4 4 4 4 4 3 4 ...
$ E7          : num [1:300] 4 5 4 4 4 5 4 4 3 4 ...
$ E8          : num [1:300] 4 5 4 4 3 5 4 4 3 4 ...
$ E9          : num [1:300] 4 5 4 4 4 4 4 4 3 4 ...
$ E10         : num [1:300] 4 5 4 4 4 5 4 5 3 4 ...
$ E11         : num [1:300] 4 5 4 3 3 5 4 5 3 4 ...
$ E12         : num [1:300] 5 5 4 4 4 5 4 5 3 5 ...
$ Etototal    : num [1:300] 52 60 48 46 45 57 48 52 37 52 ...
$ F1          : num [1:300] 5 5 4 4 4 5 4 4 2 4 ...
$ F2          : num [1:300] 4 5 4 4 4 5 4 4 3 3 ...
$ F3          : num [1:300] 4 5 4 4 4 4 4 4 2 3 ...
$ F4          : num [1:300] 4 5 4 4 4 5 4 5 3 4 ...
$ F5          : num [1:300] 4 5 4 4 3 5 4 4 3 3 ...
$ F6          : num [1:300] 4 5 4 4 3 4 4 5 3 4 ...
$ F7          : num [1:300] 4 5 4 4 3 4 4 4 3 4 ...
$ F8          : num [1:300] 4 5 4 4 4 5 4 4 3 4 ...
$ Fttotal     : num [1:300] 33 40 32 32 29 37 32 34 22 29 ...

```

```

attach(datasem)
table(A1)

```

```

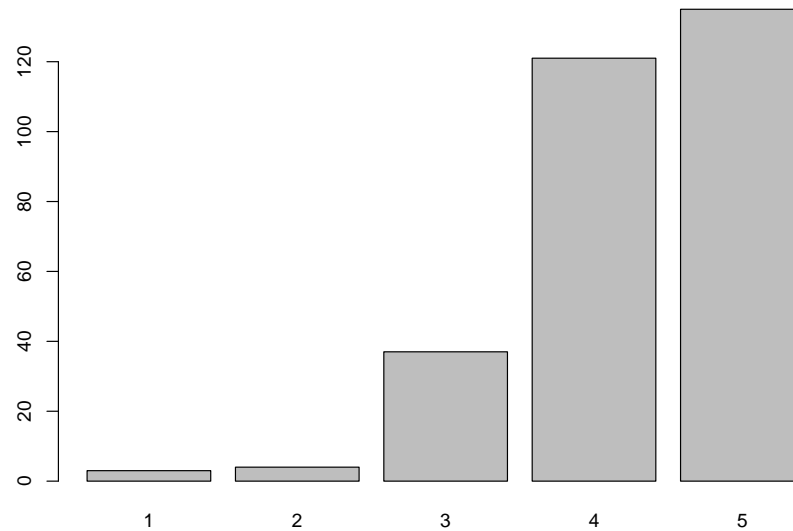
A1
  1  2  3  4  5
  3  4 37 121 135

```

```

barplot(table(A1))

```



```
# Spesifikasi Model
sem.model = "
faktor =~ A1 + A2 + A3 + A4
permintaan =~ B1 + B2
industri =~ C1 + C2
strategi =~ D1 + D2 + D3 + D4
regulasi =~ E1 + E2 + E3 + E4 + E5 + E6
kesempatan =~ F1 + F2 + F3 + F4
kesempatan ~ faktor + permintaan + industri + strategi + regulasi"

sem.fit = sem(sem.model, data = datasem)
summary(sem.fit, fit.measures=TRUE)
```

lavaan 0.6-19 ended normally after 90 iterations

Estimator	ML
Optimization method	NLMINB
Number of model parameters	59
Number of observations	300

Model Test User Model:

Test statistic	555.757
----------------	---------

Degrees of freedom	194
P-value (Chi-square)	0.000

Model Test Baseline Model:

Test statistic	7355.210
Degrees of freedom	231
P-value	0.000

User Model versus Baseline Model:

Comparative Fit Index (CFI)	0.949
Tucker-Lewis Index (TLI)	0.940

Loglikelihood and Information Criteria:

Loglikelihood user model (H0)	-4608.159
Loglikelihood unrestricted model (H1)	-4330.280
Akaike (AIC)	9334.318
Bayesian (BIC)	9552.841
Sample-size adjusted Bayesian (SABIC)	9365.728

Root Mean Square Error of Approximation:

RMSEA	0.079
90 Percent confidence interval - lower	0.071
90 Percent confidence interval - upper	0.087
P-value H ₀ : RMSEA ≤ 0.050	0.000
P-value H ₀ : RMSEA ≥ 0.080	0.410

Standardized Root Mean Square Residual:

SRMR	0.035
------	-------

Parameter Estimates:

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)
faktor =~				
A1	1.000			
A2	1.266	0.089	14.271	0.000

A3	1.312	0.094	13.991	0.000
A4	1.261	0.091	13.913	0.000
permintaan =~				
B1	1.000			
B2	1.020	0.063	16.072	0.000
industri =~				
C1	1.000			
C2	1.035	0.044	23.446	0.000
strategi =~				
D1	1.000			
D2	0.973	0.033	29.472	0.000
D3	0.972	0.043	22.590	0.000
D4	0.817	0.042	19.325	0.000
regulasi =~				
E1	1.000			
E2	0.929	0.039	23.666	0.000
E3	0.950	0.043	22.088	0.000
E4	1.015	0.039	25.697	0.000
E5	0.985	0.042	23.464	0.000
E6	0.913	0.045	20.186	0.000
kesempatan =~				
F1	1.000			
F2	1.006	0.038	26.712	0.000
F3	1.033	0.042	24.672	0.000
F4	0.943	0.046	20.414	0.000

Regressions:

	Estimate	Std.Err	z-value	P(> z)
kesempatan ~				
faktor	0.016	0.111	0.146	0.884
permintaan	0.042	0.059	0.705	0.481
industri	0.129	0.133	0.976	0.329
strategi	0.131	0.091	1.449	0.147
regulasi	0.685	0.077	8.860	0.000

Covariances:

	Estimate	Std.Err	z-value	P(> z)
faktor ~~				
permintaan	0.233	0.034	6.785	0.000
industri	0.327	0.037	8.729	0.000
strategi	0.292	0.035	8.242	0.000
regulasi	0.343	0.039	8.730	0.000
permintaan ~~				
industri	0.366	0.043	8.447	0.000
strategi	0.391	0.045	8.713	0.000
regulasi	0.332	0.043	7.797	0.000

industri ~~				
strategi	0.437	0.043	10.274	0.000
regulasi	0.416	0.043	9.764	0.000
strategi ~~				
regulasi	0.405	0.042	9.580	0.000

Variances:

	Estimate	Std.Err	z-value	P(> z)
.A1	0.323	0.029	11.229	0.000
.A2	0.161	0.018	8.902	0.000
.A3	0.205	0.022	9.430	0.000
.A4	0.198	0.021	9.552	0.000
.B1	0.269	0.032	8.457	0.000
.B2	0.078	0.025	3.161	0.002
.C1	0.122	0.014	8.515	0.000
.C2	0.106	0.014	7.549	0.000
.D1	0.093	0.011	8.749	0.000
.D2	0.063	0.008	7.476	0.000
.D3	0.182	0.017	10.625	0.000
.D4	0.200	0.018	11.219	0.000
.E1	0.145	0.014	10.563	0.000
.E2	0.114	0.011	10.395	0.000
.E3	0.156	0.014	10.845	0.000
.E4	0.091	0.010	9.488	0.000
.E5	0.133	0.013	10.462	0.000
.E6	0.198	0.018	11.224	0.000
.F1	0.139	0.014	9.697	0.000
.F2	0.090	0.011	8.221	0.000
.F3	0.140	0.015	9.540	0.000
.F4	0.233	0.021	10.912	0.000
faktor	0.321	0.047	6.841	0.000
permintaan	0.525	0.065	8.048	0.000
industri	0.480	0.049	9.751	0.000
strategi	0.522	0.050	10.406	0.000
regulasi	0.542	0.055	9.811	0.000
.kesempatan	0.122	0.015	8.068	0.000

```
sem.fit = sem(sem.model, data = datasem, std.lv=TRUE)
summary(sem.fit, fit.measures=TRUE, standardized=TRUE)
```

lavaan 0.6-19 ended normally after 90 iterations

Estimator	ML
Optimization method	NLMINB
Number of model parameters	59

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Number of observations	300
Model Test User Model:	
Test statistic	555.757
Degrees of freedom	194
P-value (Chi-square)	0.000
Model Test Baseline Model:	
Test statistic	7355.210
Degrees of freedom	231
P-value	0.000
User Model versus Baseline Model:	
Comparative Fit Index (CFI)	0.949
Tucker-Lewis Index (TLI)	0.940
Loglikelihood and Information Criteria:	
Loglikelihood user model (H0)	-4608.159
Loglikelihood unrestricted model (H1)	-4330.280
Akaike (AIC)	9334.318
Bayesian (BIC)	9552.841
Sample-size adjusted Bayesian (SABIC)	9365.728
Root Mean Square Error of Approximation:	
RMSEA	0.079
90 Percent confidence interval - lower	0.071
90 Percent confidence interval - upper	0.087
P-value H ₀ : RMSEA ≤ 0.050	0.000
P-value H ₀ : RMSEA ≥ 0.080	0.410
Standardized Root Mean Square Residual:	
SRMR	0.035
Parameter Estimates:	
Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
faktor =~						
A1	0.566	0.041	13.681	0.000	0.566	0.706
A2	0.717	0.038	18.699	0.000	0.717	0.872
A3	0.743	0.041	18.064	0.000	0.743	0.854
A4	0.714	0.040	17.894	0.000	0.714	0.849
permintaan =~						
B1	0.725	0.045	16.097	0.000	0.725	0.813
B2	0.739	0.038	19.509	0.000	0.739	0.935
industri =~						
C1	0.692	0.036	19.503	0.000	0.692	0.893
C2	0.717	0.036	20.132	0.000	0.717	0.911
strategi =~						
D1	0.723	0.035	20.812	0.000	0.723	0.922
D2	0.703	0.033	21.615	0.000	0.703	0.941
D3	0.702	0.038	18.344	0.000	0.702	0.855
D4	0.590	0.036	16.459	0.000	0.590	0.797
regulasi =~						
E1	0.736	0.038	19.623	0.000	0.736	0.888
E2	0.684	0.034	19.941	0.000	0.684	0.897
E3	0.699	0.037	18.967	0.000	0.699	0.870
E4	0.747	0.035	21.120	0.000	0.747	0.927
E5	0.725	0.037	19.819	0.000	0.725	0.894
E6	0.673	0.038	17.720	0.000	0.673	0.834
kesempatan =~						
F1	0.350	0.022	16.135	0.000	0.771	0.900
F2	0.352	0.021	16.722	0.000	0.776	0.933
F3	0.361	0.022	16.227	0.000	0.796	0.905
F4	0.330	0.022	14.833	0.000	0.727	0.833

Regressions:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
kesempatan ~						
faktor	0.026	0.180	0.146	0.884	0.012	0.012
permintaan	0.086	0.123	0.705	0.481	0.039	0.039
industri	0.256	0.263	0.973	0.331	0.116	0.116
strategi	0.272	0.188	1.447	0.148	0.123	0.123
regulasi	1.443	0.190	7.608	0.000	0.654	0.654

Covariances:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
faktor ~~						
permintaan	0.568	0.046	12.297	0.000	0.568	0.568
industri	0.833	0.025	33.258	0.000	0.833	0.833
strategi	0.715	0.033	21.548	0.000	0.715	0.715

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regulasi	0.822	0.023	35.175	0.000	0.822	0.822
permintaan ~~						
industri	0.729	0.035	20.610	0.000	0.729	0.729
strategi	0.746	0.032	23.194	0.000	0.746	0.746
regulasi	0.623	0.041	15.291	0.000	0.623	0.623
industri ~~						
strategi	0.874	0.020	44.744	0.000	0.874	0.874
regulasi	0.816	0.024	33.446	0.000	0.816	0.816
strategi ~~						
regulasi	0.762	0.027	27.976	0.000	0.762	0.762

Variances:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
.A1	0.323	0.029	11.229	0.000	0.323	0.502
.A2	0.161	0.018	8.902	0.000	0.161	0.239
.A3	0.205	0.022	9.430	0.000	0.205	0.271
.A4	0.198	0.021	9.552	0.000	0.198	0.280
.B1	0.269	0.032	8.457	0.000	0.269	0.339
.B2	0.078	0.025	3.161	0.002	0.078	0.126
.C1	0.122	0.014	8.515	0.000	0.122	0.203
.C2	0.106	0.014	7.549	0.000	0.106	0.171
.D1	0.093	0.011	8.749	0.000	0.093	0.151
.D2	0.063	0.008	7.476	0.000	0.063	0.114
.D3	0.182	0.017	10.625	0.000	0.182	0.270
.D4	0.200	0.018	11.219	0.000	0.200	0.365
.E1	0.145	0.014	10.563	0.000	0.145	0.211
.E2	0.114	0.011	10.395	0.000	0.114	0.195
.E3	0.156	0.014	10.845	0.000	0.156	0.242
.E4	0.091	0.010	9.488	0.000	0.091	0.141
.E5	0.133	0.013	10.462	0.000	0.133	0.201
.E6	0.198	0.018	11.224	0.000	0.198	0.304
.F1	0.139	0.014	9.697	0.000	0.139	0.190
.F2	0.090	0.011	8.221	0.000	0.090	0.130
.F3	0.140	0.015	9.540	0.000	0.140	0.181
.F4	0.233	0.021	10.912	0.000	0.233	0.306
faktor	1.000				1.000	1.000
permintaan	1.000				1.000	1.000
industri	1.000				1.000	1.000
strategi	1.000				1.000	1.000
regulasi	1.000				1.000	1.000
.kesempatan	1.000				0.206	0.206

```
#sem.fit = sem(sem.model, data = datasem, std.lv=TRUE, orthogonal=TRUE)
#summary(sem.fit, fit.measures=TRUE, standardized=TRUE)
```



```
# Modification Indices
modificationIndices(sem.fit, minimum.value = 10)
```

	lhs	op	rhs	mi	epc	sepc.lv	sepc.all	sepc.nox
72	faktor	=~	D3	10.792	0.143	0.143	0.174	0.174
82	faktor	=~	F3	14.022	-0.170	-0.170	-0.193	-0.193
99	permintaan	=~	E6	13.919	0.142	0.142	0.176	0.176
112	industri	=~	D3	19.393	0.315	0.315	0.383	0.383
134	strategi	=~	E3	11.975	-0.144	-0.144	-0.179	-0.179
152	regulasi	=~	D3	18.808	0.197	0.197	0.240	0.240
157	regulasi	=~	F4	13.142	0.272	0.272	0.312	0.312
168	kesempatan	=~	D3	22.896	0.100	0.220	0.268	0.268
175	kesempatan	=~	E6	25.214	0.153	0.337	0.418	0.418
176	A1	~~	A2	15.863	0.068	0.068	0.298	0.298
270	B1	~~	F4	14.265	0.063	0.063	0.253	0.253
317	D1	~~	D3	10.752	-0.035	-0.035	-0.272	-0.272
331	D2	~~	E1	11.098	0.025	0.025	0.257	0.257
347	D3	~~	E6	12.029	0.042	0.042	0.223	0.223
351	D3	~~	F4	10.217	-0.043	-0.043	-0.208	-0.208
352	D4	~~	E1	11.953	-0.038	-0.038	-0.223	-0.223
362	E1	~~	E2	17.329	0.038	0.038	0.294	0.294
363	E1	~~	E3	10.360	0.033	0.033	0.220	0.220
364	E1	~~	E4	12.186	-0.031	-0.031	-0.266	-0.266
371	E2	~~	E3	11.663	0.032	0.032	0.236	0.236
373	E2	~~	E5	10.449	-0.028	-0.028	-0.231	-0.231
381	E3	~~	E6	11.439	-0.039	-0.039	-0.221	-0.221
386	E4	~~	E5	25.380	0.043	0.043	0.388	0.388
398	E6	~~	F2	14.478	-0.037	-0.037	-0.275	-0.275
399	E6	~~	F3	20.998	0.052	0.052	0.310	0.310
405	F2	~~	F4	24.019	-0.058	-0.058	-0.404	-0.404
406	F3	~~	F4	14.294	0.050	0.050	0.279	0.279

```
sem.model2 = "
faktor =~ A1 + A2 + A3 + A4
permintaan =~ B1 + B2
industri =~ C1 + C2
strategi =~ D1 + D2 + D3 + D4
regulasi =~ E1 + E2 + E3 + E4 + E5 + E6
kesempatan =~ F1 + F2 + F3 + F4
kesempatan ~ faktor + permintaan + industri + strategi + regulasi
A1 ~~ A2
"
```

```
sem.fit = sem(sem.model2, data = datasem, std.lv=TRUE)
summary(sem.fit, fit.measures=TRUE, standardized=TRUE)
```

lavaan 0.6-19 ended normally after 94 iterations

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Estimator	ML
Optimization method	NLMINB
Number of model parameters	60
Number of observations	300
Model Test User Model:	
Test statistic	540.535
Degrees of freedom	193
P-value (Chi-square)	0.000
Model Test Baseline Model:	
Test statistic	7355.210
Degrees of freedom	231
P-value	0.000
User Model versus Baseline Model:	
Comparative Fit Index (CFI)	0.951
Tucker-Lewis Index (TLI)	0.942
Loglikelihood and Information Criteria:	
Loglikelihood user model (H0)	-4600.548
Loglikelihood unrestricted model (H1)	-4330.280
Akaike (AIC)	9321.095
Bayesian (BIC)	9543.322
Sample-size adjusted Bayesian (SABIC)	9353.038
Root Mean Square Error of Approximation:	
RMSEA	0.077
90 Percent confidence interval - lower	0.070
90 Percent confidence interval - upper	0.085
P-value H ₀ : RMSEA ≤ 0.050	0.000
P-value H ₀ : RMSEA ≥ 0.080	0.303
Standardized Root Mean Square Residual:	
SRMR	0.035
Parameter Estimates:	

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
faktor =~						
A1	0.539	0.043	12.660	0.000	0.539	0.672
A2	0.702	0.039	18.009	0.000	0.702	0.854
A3	0.752	0.041	18.363	0.000	0.752	0.864
A4	0.720	0.040	18.060	0.000	0.720	0.855
permintaan =~						
B1	0.724	0.045	16.093	0.000	0.724	0.813
B2	0.739	0.038	19.507	0.000	0.739	0.935
industri =~						
C1	0.692	0.036	19.469	0.000	0.692	0.892
C2	0.717	0.036	20.171	0.000	0.717	0.912
strategi =~						
D1	0.723	0.035	20.813	0.000	0.723	0.922
D2	0.703	0.033	21.613	0.000	0.703	0.941
D3	0.702	0.038	18.345	0.000	0.702	0.855
D4	0.590	0.036	16.460	0.000	0.590	0.797
regulasi =~						
E1	0.736	0.038	19.615	0.000	0.736	0.888
E2	0.684	0.034	19.943	0.000	0.684	0.897
E3	0.699	0.037	18.964	0.000	0.699	0.870
E4	0.747	0.035	21.115	0.000	0.747	0.927
E5	0.726	0.037	19.826	0.000	0.726	0.894
E6	0.673	0.038	17.728	0.000	0.673	0.834
kesempatan =~						
F1	0.350	0.022	16.137	0.000	0.771	0.900
F2	0.352	0.021	16.726	0.000	0.776	0.933
F3	0.361	0.022	16.232	0.000	0.796	0.905
F4	0.330	0.022	14.836	0.000	0.727	0.833

Regressions:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
kesempatan ~						
faktor	0.031	0.186	0.167	0.867	0.014	0.014
permintaan	0.087	0.122	0.709	0.478	0.039	0.039
industri	0.253	0.267	0.947	0.344	0.115	0.115
strategi	0.272	0.189	1.442	0.149	0.123	0.123
regulasi	1.441	0.190	7.578	0.000	0.654	0.654

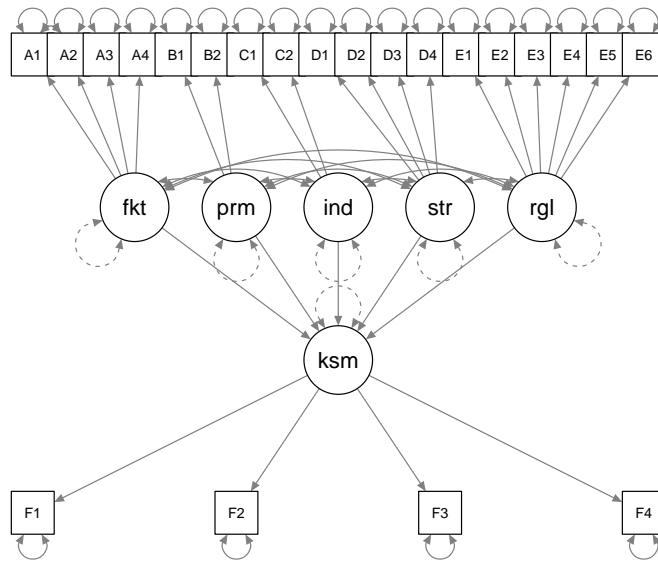
Covariances:

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
.A1 ~~						
.A2	0.068	0.019	3.588	0.000	0.068	0.269
faktor ~~						
permintaan	0.573	0.046	12.417	0.000	0.573	0.573
industri	0.837	0.025	33.458	0.000	0.837	0.837
strategi	0.716	0.033	21.421	0.000	0.716	0.716
regulasi	0.824	0.024	34.919	0.000	0.824	0.824
permintaan ~~						
industri	0.729	0.035	20.581	0.000	0.729	0.729
strategi	0.746	0.032	23.189	0.000	0.746	0.746
regulasi	0.623	0.041	15.292	0.000	0.623	0.623
industri ~~						
strategi	0.874	0.020	44.757	0.000	0.874	0.874
regulasi	0.816	0.024	33.429	0.000	0.816	0.816
strategi ~~						
regulasi	0.762	0.027	27.982	0.000	0.762	0.762
Variances:						
	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
.A1	0.353	0.032	11.133	0.000	0.353	0.549
.A2	0.182	0.020	9.132	0.000	0.182	0.270
.A3	0.192	0.022	8.905	0.000	0.192	0.253
.A4	0.190	0.021	9.171	0.000	0.190	0.268
.B1	0.270	0.032	8.454	0.000	0.270	0.339
.B2	0.078	0.025	3.155	0.002	0.078	0.125
.C1	0.123	0.014	8.573	0.000	0.123	0.205
.C2	0.104	0.014	7.494	0.000	0.104	0.169
.D1	0.093	0.011	8.748	0.000	0.093	0.151
.D2	0.063	0.008	7.481	0.000	0.063	0.114
.D3	0.182	0.017	10.624	0.000	0.182	0.270
.D4	0.200	0.018	11.218	0.000	0.200	0.365
.E1	0.145	0.014	10.565	0.000	0.145	0.211
.E2	0.114	0.011	10.392	0.000	0.114	0.195
.E3	0.157	0.014	10.844	0.000	0.157	0.242
.E4	0.092	0.010	9.490	0.000	0.092	0.141
.E5	0.132	0.013	10.456	0.000	0.132	0.201
.E6	0.197	0.018	11.222	0.000	0.197	0.304
.F1	0.140	0.014	9.700	0.000	0.140	0.190
.F2	0.090	0.011	8.219	0.000	0.090	0.130
.F3	0.140	0.015	9.538	0.000	0.140	0.181
.F4	0.233	0.021	10.912	0.000	0.233	0.306
faktor	1.000				1.000	1.000
permintaan	1.000				1.000	1.000
industri	1.000				1.000	1.000
strategi	1.000				1.000	1.000

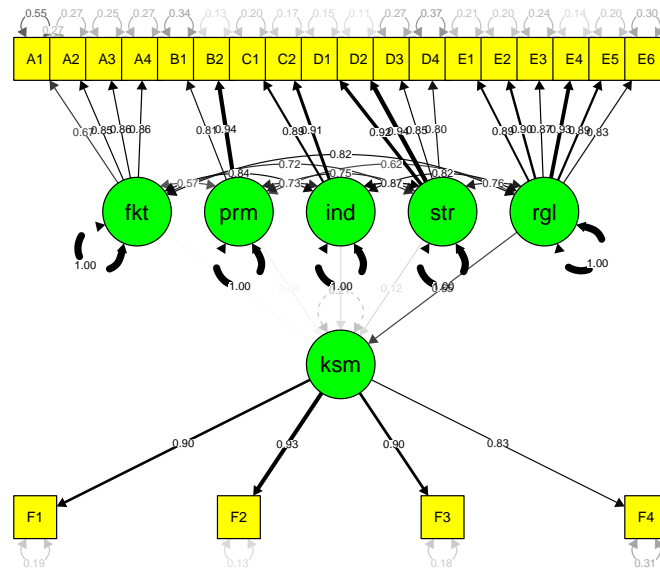
regulasi	1.000	1.000	1.000
.kesempatan	1.000	0.206	0.206

```
semPaths(sem.fit)
```

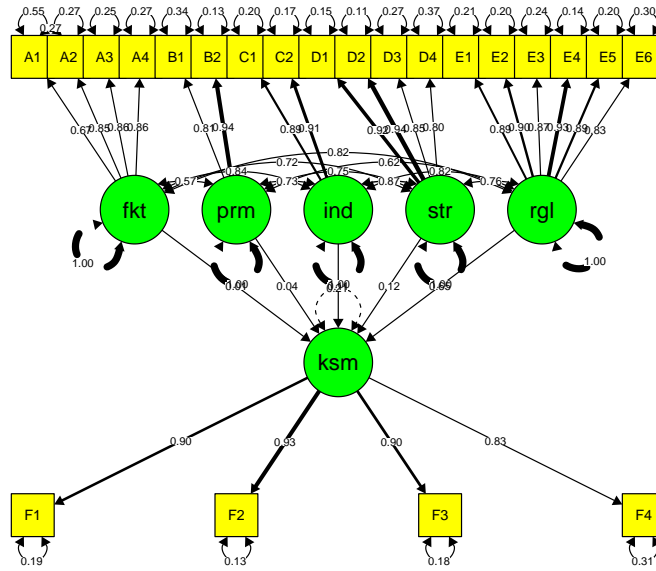
7.2.1 Visualisasi SEM



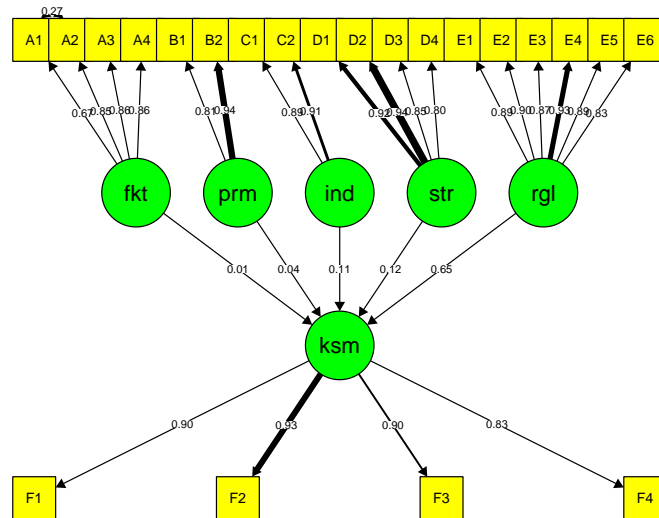
```
semPaths(sem.fit, "std",
  color = list(lat = "green", man = "yellow"),
  edge.color="black")
```



```
semPaths(sem.fit, "std",
  color = list(lat = "green", man = "yellow"),
  edge.color="black", fade=FALSE)
```



```
semPaths(sem.fit, "std",
  color = list(lat = "green", man = "yellow"),
  edge.color="black",
  fade=FALSE, residuals=FALSE, exoCov=FALSE)
```



7.3 PLS SEM

```
# source:https://rpubs.com/ifn1411/PLS
# install plsmp
#install.packages("plsmp")
# load plsmp
library(plsmp)
```

```
# load data spainmodel
data(spainfoot)
# first 5 row of spainmodel data
head(spainfoot)
```

	GSH	GSA	SSH	SSA	GCH	GCA	CSH	CSA	WMH	WMA	LWR	LRWL	YC	RC
Barcelona	61	44	0.95	0.95	14	21	0.47	0.32	14	13	10	22	76	6
RealMadrid	49	34	1.00	0.84	29	23	0.37	0.37	14	11	10	18	115	9
Sevilla	28	26	0.74	0.74	20	19	0.42	0.53	11	10	4	7	100	8
AtleMadrid	47	33	0.95	0.84	23	34	0.37	0.16	13	7	6	9	116	5
Villarreal	33	28	0.84	0.68	25	29	0.26	0.16	12	6	5	11	102	5
Valencia	47	21	1.00	0.68	26	28	0.26	0.26	12	6	5	8	120	6

```
Attack <- c(0, 0, 0)
Defense <- c(1, 0, 0)
```



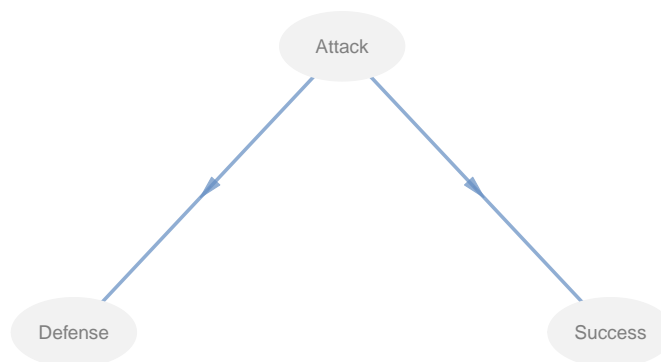
```
Success <- c(1, 0, 0)

model_path <- rbind(Attack, Defense, Success)
colnames(model_path) <- rownames(model_path)

model_path
```

```
      Attack Defense Success
Attack      0      0      0
Defense     1      0      0
Success     1      0      0
```

```
# graph structural model
innerplot(model_path)
```



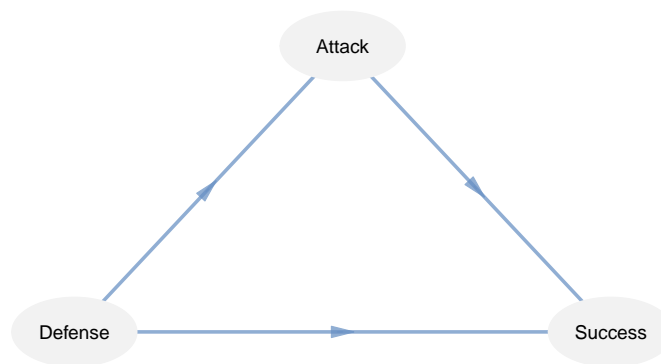
```
Attack <- c(0, 1, 0)
Defense <- c(0, 0, 0)
Success <- c(1, 1, 0)

model_path2 <- rbind(Attack, Defense, Success)
colnames(model_path2) <- rownames(model_path2)

model_path2
```

	Attack	Defense	Success
Attack	0	1	0
Defense	0	0	0
Success	1	1	0

```
# graph structural model
innerplot(model_path2, txt.col = "black")
```



```
# define latent variable associated with
model_blocks <- list(1:4, 5:8, 9:12)

# vector of modes (reflective)
model_modes <- c("A", "A", "A")

# run plspm analysis
model_pls <- plspm(Data = spainfoot, path_matrix = model_path, blocks = model_blocks, r

model_pls
```

Partial Least Squares Path Modeling (PLS-PM)

	NAME	DESCRIPTION
1	\$outer_model	outer model
2	\$inner_model	inner model

```

3 $path_coefs      path coefficients matrix
4 $scores          latent variable scores
5 $crossloadings   cross-loadings
6 $inner_summary   summary inner model
7 $effects         total effects
8 $unidim          unidimensionality
9 $gof             goodness-of-fit
10 $boot           bootstrap results
11 $data           data matrix

```

You can also use the function 'summary'

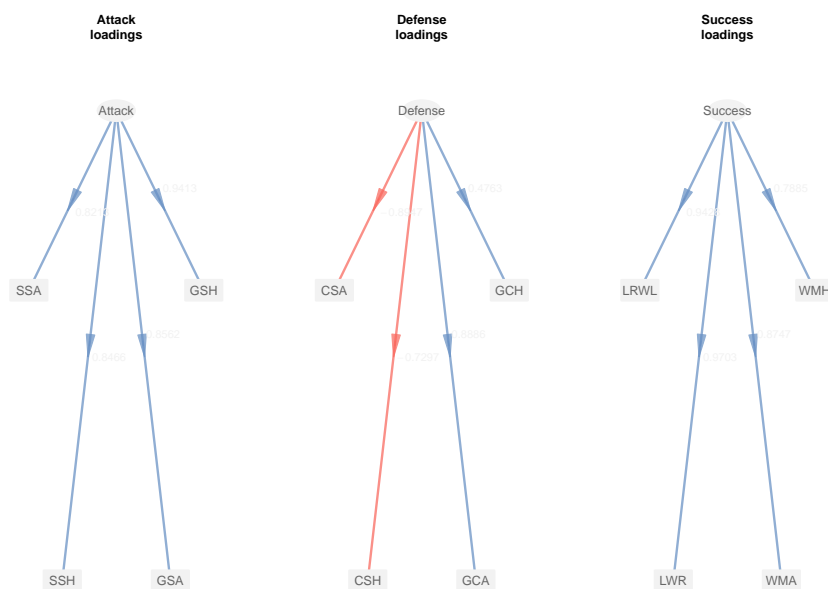
```

# Unidimensionality
model_pls$unidim

```

	Mode	MVs	C.alpha	DG.rho	eig.1st	eig.2nd
Attack	A	4	0.8905919	0.92456079	3.017160	0.7923055
Defense	A	4	0.0000000	0.02601677	2.393442	1.1752781
Success	A	4	0.9165491	0.94232868	3.217294	0.5370492

```
plot(model_pls, what = "loadings")
```



```

# Loadings and Communilaties
model_pls$outer_model

```

	name	block	weight	loading	communality	redundancy
1	GSH	Attack	0.3474771	0.9412506	0.8859527	0.00000000
2	GSA	Attack	0.2671782	0.8562398	0.7331465	0.00000000
3	SSH	Attack	0.2922077	0.8466039	0.7167381	0.00000000
4	SSA	Attack	0.2396012	0.8212987	0.6745316	0.00000000
5	GCH	Defense	-0.1198790	0.4762965	0.2268583	0.05071506
6	GCA	Defense	-0.4264164	0.8885714	0.7895590	0.17650898
7	CSH	Defense	0.2949470	-0.7297095	0.5324759	0.11903706
8	CSA	Defense	0.3898039	-0.8947452	0.8005689	0.17897028
9	WMH	Success	0.2484276	0.7884562	0.6216632	0.49452090
10	WMA	Success	0.2691511	0.8747163	0.7651285	0.60864477
11	LWR	Success	0.2947322	0.9703409	0.9415614	0.74899365
12	LRWL	Success	0.2998524	0.9428112	0.8888929	0.70709694

```
# Crossloadings
model_pls$crossloadings
```

	name	block	Attack	Defense	Success
1	GSH	Attack	0.9412506	-0.5139001	0.9019257
2	GSA	Attack	0.8562398	-0.3403294	0.7483558
3	SSH	Attack	0.8466039	-0.4124617	0.7781795
4	SSA	Attack	0.8212987	-0.3455460	0.6308989
5	GCH	Defense	-0.1302683	0.4762965	-0.1620567
6	GCA	Defense	-0.4633220	0.8885714	-0.5640722
7	CSH	Defense	0.3204993	-0.7297095	0.4850456
8	CSA	Defense	0.4235465	-0.8947452	0.5811253
9	WMH	Success	0.7126127	-0.4120502	0.7884562
10	WMA	Success	0.7720228	-0.7147787	0.8747163
11	LWR	Success	0.8454164	-0.5345709	0.9703409
12	LRWL	Success	0.8600973	-0.5910943	0.9428112

```
# Coefficient of Determination
model_pls$inner_model
```

\$Defense

	Estimate	Std. Error	t value	Pr(> t)
Intercept	5.504973e-17	0.2076918	2.650549e-16	1.00000000
Attack	-4.728148e-01	0.2076918	-2.276521e+00	0.03526176

\$Success

	Estimate	Std. Error	t value	Pr(> t)
Intercept	7.783183e-17	0.1065936	7.301735e-16	1.000000e+00
Attack	8.918971e-01	0.1065936	8.367266e+00	1.285711e-07

```
# Redundancy
model_pls$inner_summary
```

Type	R2	Block_Community	Mean_Redundancy	AVE
------	----	-----------------	-----------------	-----

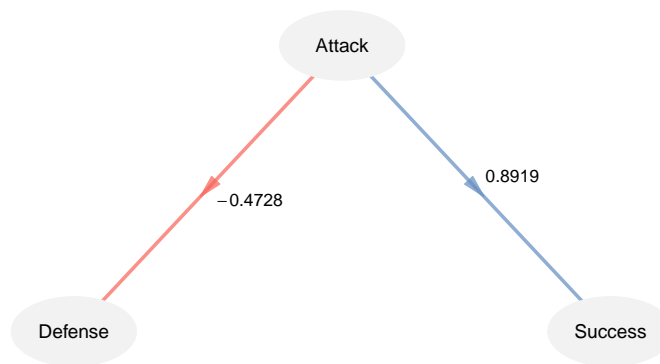
```
Attack    Exogenous 0.0000000      0.7525922      0.0000000 0.7525922
Defense   Endogenous 0.2235539      0.5873656      0.1313078 0.5873656
Success   Endogenous 0.7954804      0.8043115      0.6398141 0.8043115
```

```
# Goodness-of-fit
```

```
model_pls$gof
```

```
[1] 0.6034738
```

```
plot(model_pls, what = "inner", colpos = "#6890c4BB", colneg = "#f9675dBB", txt.col = "black", ar
```



Chapter 8

Analytic Hierarchy Process (AHP)

8.1 Prosedur Pengolahan AHP

8.1.1 Data

```
ahpdata <- read.csv("Data/ahp.csv")
ahpdata
```

	Responden	SAL_QL	SAL_IW	SAL_LC	QL_IW	QL_LC	IW_LC	J1_J2	J1_j3	J2_J3	J1_J2.1
1	1	-5	-2	-4	2	2	-2	-2	-4	-2	2
2	2	-7	-3	-3	3	3	-4	-3	-7	-1	3
	J1_j3.1	J2_J3.1	J1_J2.2	J1_j3.2	J2_J3.2	J1_J2.3	J1_j3.3	J2_J3.3			
1	3	3	7	3	-3	4	7	-2			
2	3	3	4	-1	-3	5	2	-4			

8.1.2 Analisis

8.1.2.1 Faktor

```
# Mendefinisikan faktor
faktor <- c("SAL", "QL", "IW", "LC")
# Menampilkan data frame
faktor_data <- ahpdata[, 2:7]
faktor_data
```

	SAL_QL	SAL_IW	SAL_LC	QL_IW	QL_LC	IW_LC
1	-5	-2	-4	2	2	-2
2	-7	-3	-3	3	3	-4

```
# install.packages("ahpsurvey")
library(ahpsurvey)
faktor_data_mat <- ahp.mat(df = faktor_data, faktor,
                           negconvert = TRUE)
faktor_data_mat

[[1]]
      SAL QL  IW  LC
SAL 1.00  5 2.0 4.0
QL  0.20  1 0.5 0.5
IW  0.50  2 1.0 2.0
LC  0.25  2 0.5 1.0

[[2]]
      SAL QL      IW      LC
SAL 1.0000000  7 3.0000000 3.0000000
QL  0.1428571  1 0.3333333 0.3333333
IW  0.3333333  3 1.0000000 4.0000000
LC  0.3333333  3 0.2500000 1.0000000

# Consistency
ri <- ahp.ri(nsim = 10000, dim = 4, seed = 42)
ahp.cr(faktor_data_mat, faktor, ri)

[1] 0.01780548 0.09677931

#Treatement Consistency (Jika Tidak Konsisten)
#faktor_data_mat <- ahp.harker(faktor_data_mat, faktor, iterations = 10, stopcr = 0.1)
#ahp.cr(faktor_data_mat, faktor)
```

The `ahp.cr` function calculates the consistency ratio of each decision-maker, defined by the following equation:

$$CR = (\lambda_{\max} - n) / ((n - 1)(RI))$$

Where λ_{\max} is the maximum eigenvalue of the pairwise comparison matrix, n is the number of attributes, and RI is the random index. Following Saaty and Tran (2007), the RI is a function of n and is the consistency ratio of randomly generated pairwise comparison matrices.

Saaty showed that when the CR is higher than 0.1, the choice is deemed to be inconsistent

8.1.2.2 Individual Rangking Faktor

```
library(tidyverse)
library(tibble)
faktor_ind <- ahp.indpref(faktor_data_mat,
```



```
faktor,
method = "arithmetic")
round(faktor_ind, 3) %>% rownames_to_column('ID')
```

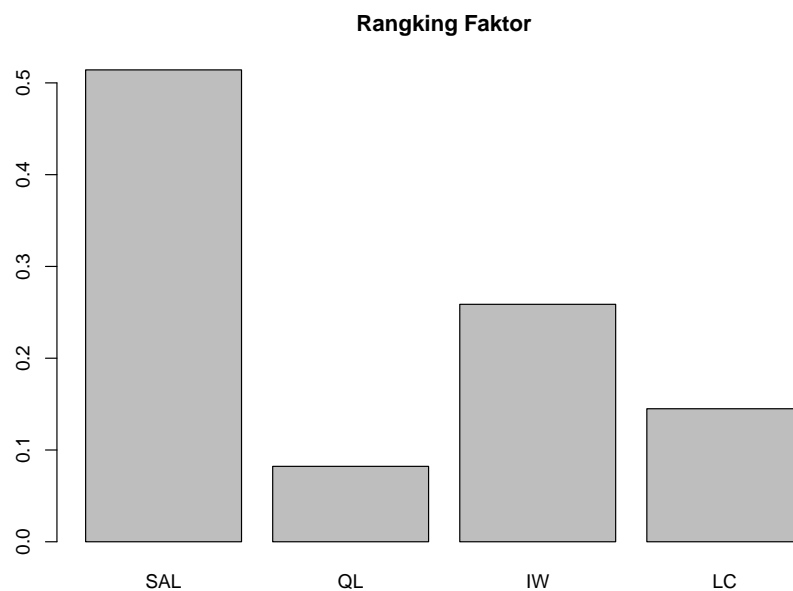
```
  ID  SAL  QL  IW  LC
1  1 0.512 0.099 0.243 0.147
2  2 0.517 0.066 0.274 0.143
```

8.1.2.3 Aggregate Ranging Faktor

```
faktor_agg <- ahp.aggpref(faktor_data_mat,
  faktor,
  method = "arithmetic",
  aggmethod = "arithmetic")
round(faktor_agg, 3) %>% t()
```

```
      SAL  QL  IW  LC
[1,] 0.514 0.082 0.259 0.145
```

```
barplot(faktor_agg, main="Ranging Faktor")
```



```
library(ggplot2)
# Mengubah Cat menjadi factor dengan label yang diinginkan
data = data.frame("Cat"=row.names(data.frame(faktor_agg)),
```

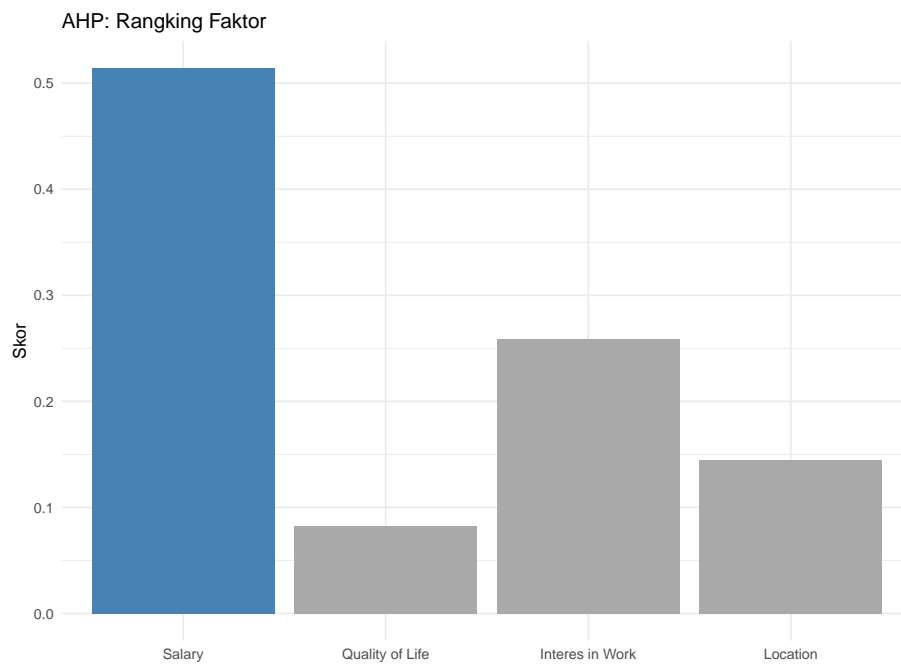
```

        data.frame(faktor_agg))
data$Cat <- factor(data$Cat,
                  levels = c("SAL", "QL", "IW", "LC"),
                  labels = c("Salary", "Quality of Life",
                             "Interes in Work", "Location"))

# Mengurutkan
data$warna <- ifelse(data$faktor_agg ==
                    max(data$faktor_agg),
                    "terbesar", "lainnya")

# Buat grafik batang
ggplot(data, aes(x = Cat,
                 y = faktor_agg,
                 fill = warna)) +
  geom_bar(stat = "identity") +
  scale_fill_manual(values = c("terbesar" = "#4682B4",
                              "lainnya" = "#A9A9A9")) +
  theme_minimal() +
  theme(legend.position = "none") + # Sembunyikan legenda
  labs(
    title = "AHP: Rangking Faktor",
    y = "Skor",
    x = "")

```



8.1.2.4 Alternatif

8.1.2.5 Alternatif untuk Faktor Salary

```
library(dplyr)
alternatif <- c("J1", "J2", "J3")

# Menampilkan data frame
alternatif_data1 <- ahpdata[,8:10]
alternatif1 <- ahp.mat(df = alternatif_data1,
                      atts = alternatif,
                      negconvert = TRUE)
alternatif1_agg <- ahp.aggpref(alternatif1,
                              alternatif,
                              method = "arithmetic",
                              aggmethod = "arithmetic")
round(alternatif1_agg, 3) %>% t()
```

```
      J1    J2    J3
[1,] 0.628 0.232 0.139
```

```
#Consistency
ri <- ahp.ri(nsim = 10000, dim = 3, seed = 42)
ahp.cr(alternatif1, alternatif, ri)
```

```
[1] 0.00000000 0.07669698
```

8.1.2.6 Alternatif untuk Faktor Quality of Life

```
alternatif_data2 <- ahpdata[,11:13]
alternatif2 <- ahp.mat(df = alternatif_data2,
                      atts = alternatif,
                      negconvert = TRUE)
alternatif2_agg <- ahp.aggpref(alternatif2,
                              alternatif,
                              method = "arithmetic",
                              aggmethod = "arithmetic")
round(alternatif2_agg, 3) %>% t()
```

```
      J1    J2    J3
[1,] 0.15 0.269 0.581
```

```
#Consistency
ahp.cr(alternatif2, alternatif, ri)
```

```
[1] 0.05121571 0.12952632
```

8.1.2.7 Alternatif untuk Faktor Interest in Work

```
alternatif_data3 <- ahpdata[,14:16]
alternatif3 <- ahp.mat(df = alternatif_data3,
                      atts = alternatif,
                      negconvert = TRUE)
alternatif3_agg <- ahp.aggpref(alternatif3,
                              alternatif,
                              method = "arithmetic",
                              aggmethod = "arithmetic")
round(alternatif3_agg, 3) %>% t()
```

```
      J1    J2    J3
[1,] 0.132 0.651 0.218
```

```
#Consistency
```

```
ahp.cr(alternatif3, alternatif, ri)
```

```
[1] 0.006706716 0.008789809
```

8.1.2.8 Alternatif untuk Faktor Location

```
alternatif_data4 <- ahpdata[,17:19]
alternatif4 <- ahp.mat(df = alternatif_data4,
                      atts = alternatif,
                      negconvert = TRUE)
alternatif4_agg <- ahp.aggpref(alternatif4,
                              alternatif,
                              method = "arithmetic",
                              aggmethod = "arithmetic")
round(alternatif4_agg, 3) %>% t()
```

```
      J1    J2    J3
[1,] 0.104 0.597 0.299
```

```
#Consistency
```

```
ahp.cr(alternatif4, alternatif, ri)
```

```
[1] 0.16898990 0.02349155
```

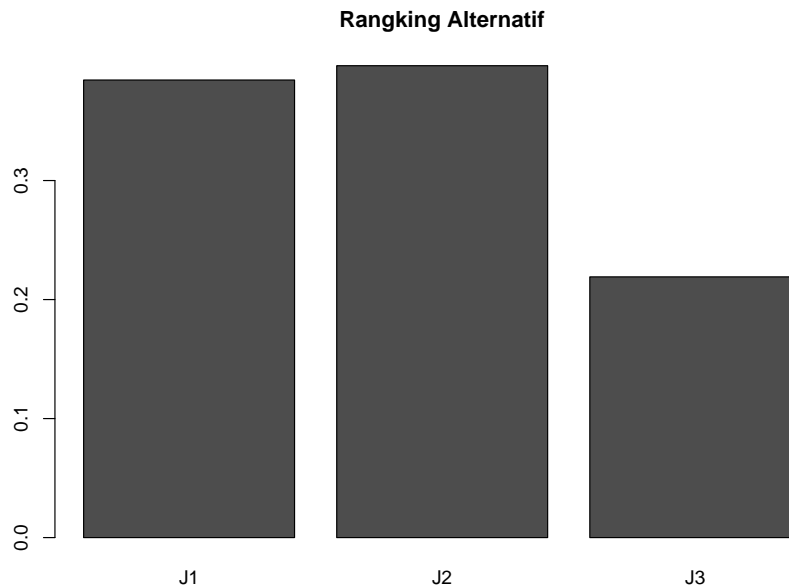
8.1.2.9 Gabungan Alternatif

```
alternatif_agg <- cbind(alternatif1_agg, alternatif2_agg,
                      alternatif3_agg, alternatif4_agg) %*% faktor_agg
alternatif_agg
```

```
[,1]
```

J1 0.3844544
 J2 0.3964920
 J3 0.2190537

```
barplot(t(alternatif_agg) ,main="Rangking Alternatif")
```



```
data = data.frame("Cat"=row.names(data.frame(alternatif_agg)),
                  data.frame(alternatif_agg))
data$Cat <- factor(data$Cat,
                  levels = c( "J1" , "J2" ,"J3"),
                  labels = c("Job1", "Job2","Job3"))
# Buat grafik batang
data$warna <- ifelse(data$alternatif_agg == max(data$alternatif_agg),
                    "terbesar", "lainnya")
# Buat grafik batang
ggplot(data, aes(x = Cat, y = alternatif_agg, fill = warna)) +
  geom_bar(stat = "identity") +
  scale_fill_manual(values = c("terbesar" = "#4682B4",
                              "lainnya" = "#A9A9A9")) +
  theme_minimal() +
  theme(legend.position = "none") +
  labs(
    title = "AHP: Rangking Alternatif",
    y = "Skor",
```

$\Sigma = ""$)