

Computer Graphics (COMP0027) 2022/23

Photon Mapping

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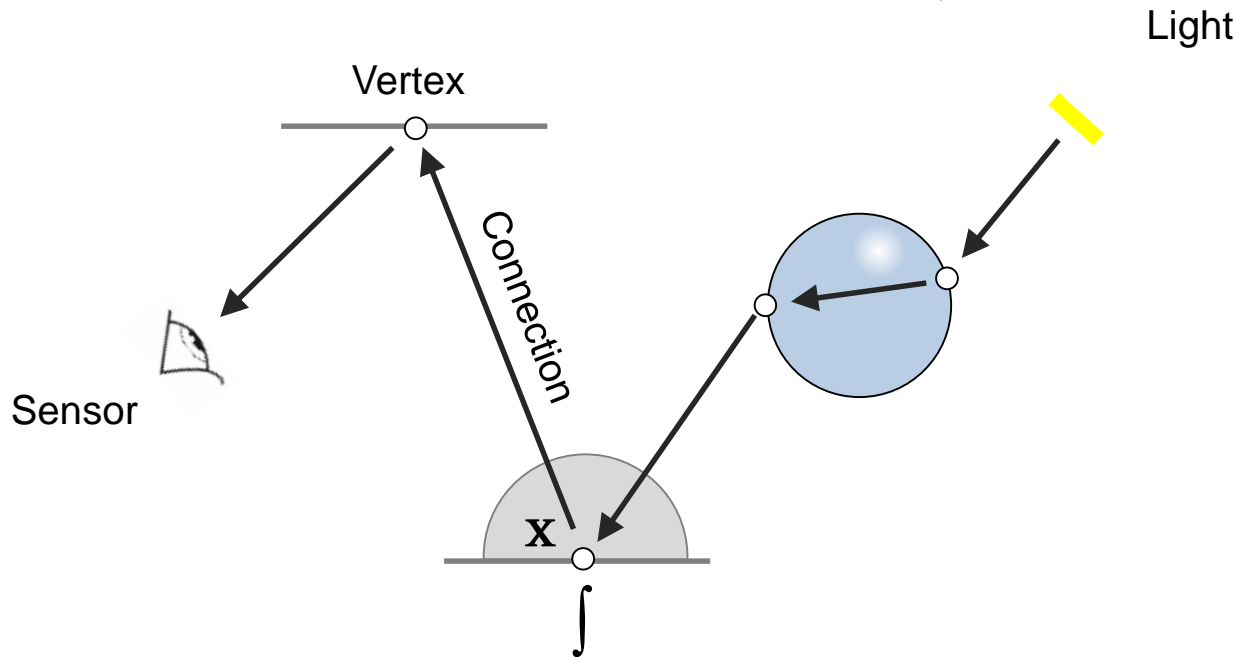
Today

- Motivation
- Idea: Starting light paths at the light
- Methods
 - Light tracing
 - Bi-directional path tracing
 - Photon Mapping
 - Instant Radiosity

光子映射
main idea 居然是这个

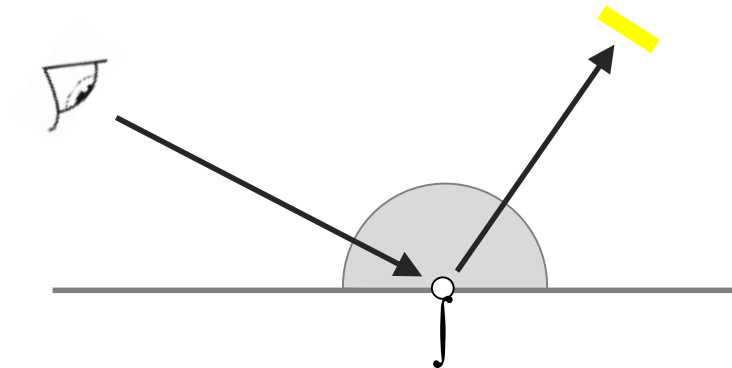
Path space jargon

术语



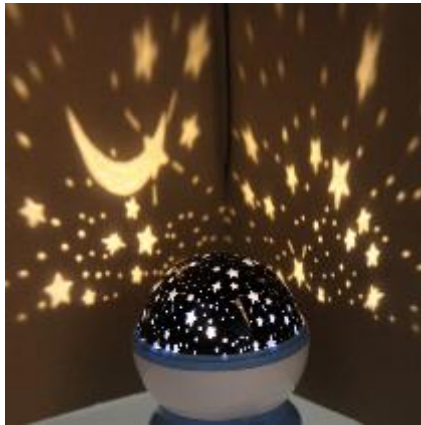
Example 1: Small lights

- Small light sources imply a small hit chance
- Solution: Next-event estimation
- Pre-condition: We know what is a light



What is hard for Path tracing

- Two examples:
 - Occlusion (key hole-like)
 - Specular (caustics)

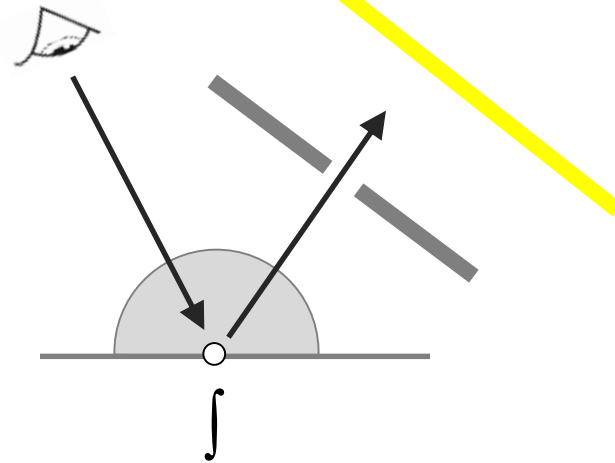
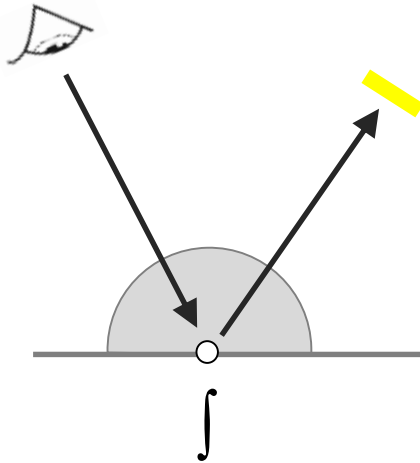


Small lights

Limits of next-event estimation

Small light: Fine!

Large light, small holes, now what?



Roulette in spherical domain

龙显瑞

θ

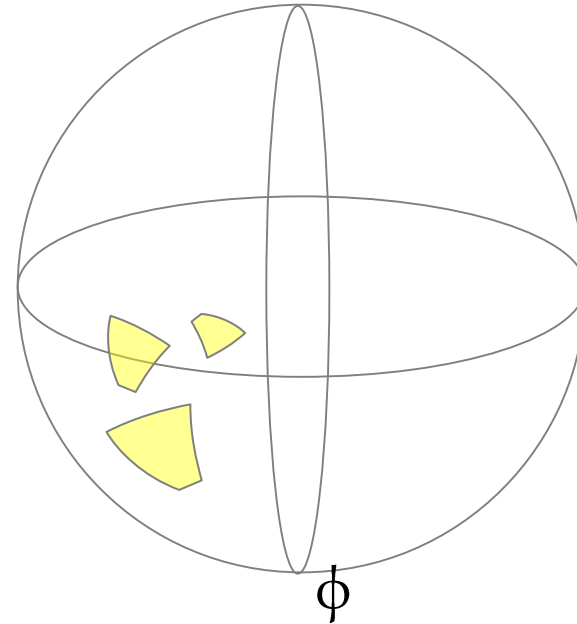
			0	00	
American roulette	1st 12	1-18	1	2	3
		Even	4	5	6
		Red	7	8	9
	2nd 12	Black	10	11	12
		Red	13	14	15
		Black	16	17	18
	3rd 12	Black	19	20	21
		Black	22	23	24
		Black	25	26	27
	19-36	Odd	28	29	30
		Black	31	32	33
		Black	34	35	36
2-1		2-1	2-1		



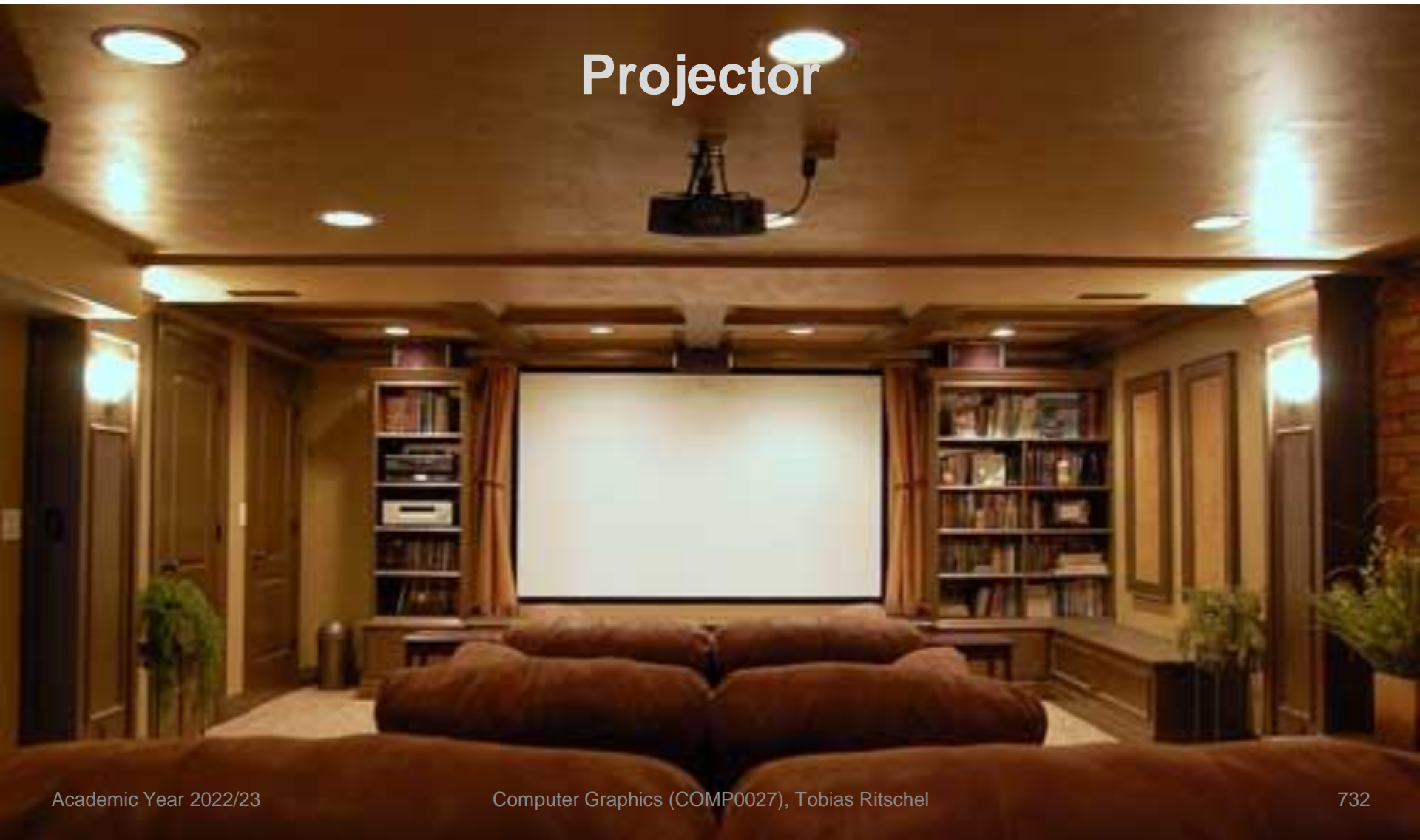
0		00		3	6	9	12	15	18	21	24	27	30	33	36	2-1	2-1	2-1
				1	2	5	8	11	14	17	20	23	26	29	32			
				1st 12				2nd 12				3rd 12						
1-18				Even				Red	Black	Odd	19-36							
American roulette																		

ϕ

θ

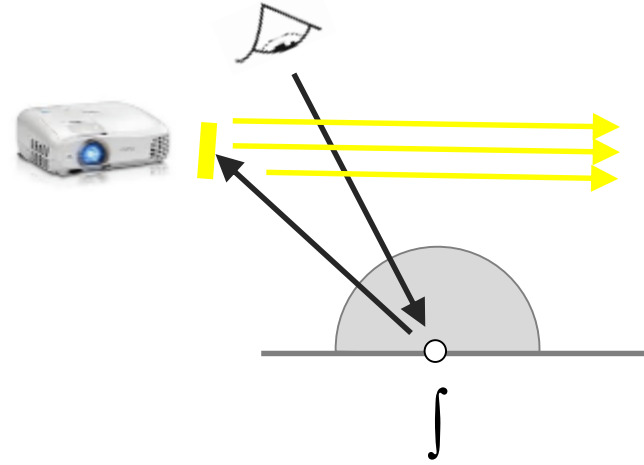
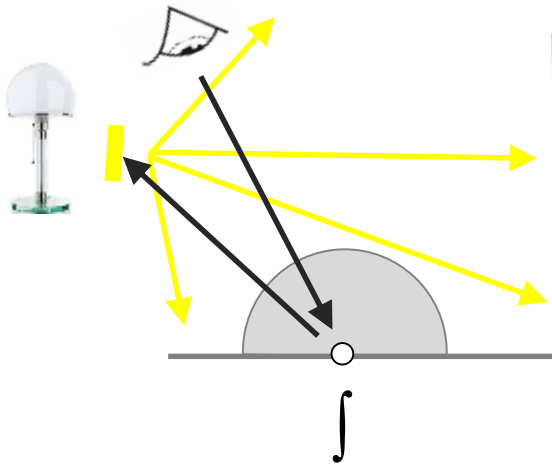


Projector



Next-event can *not* help

- The projector sends light into very few directions only
- Connecting to it is useless most of the time

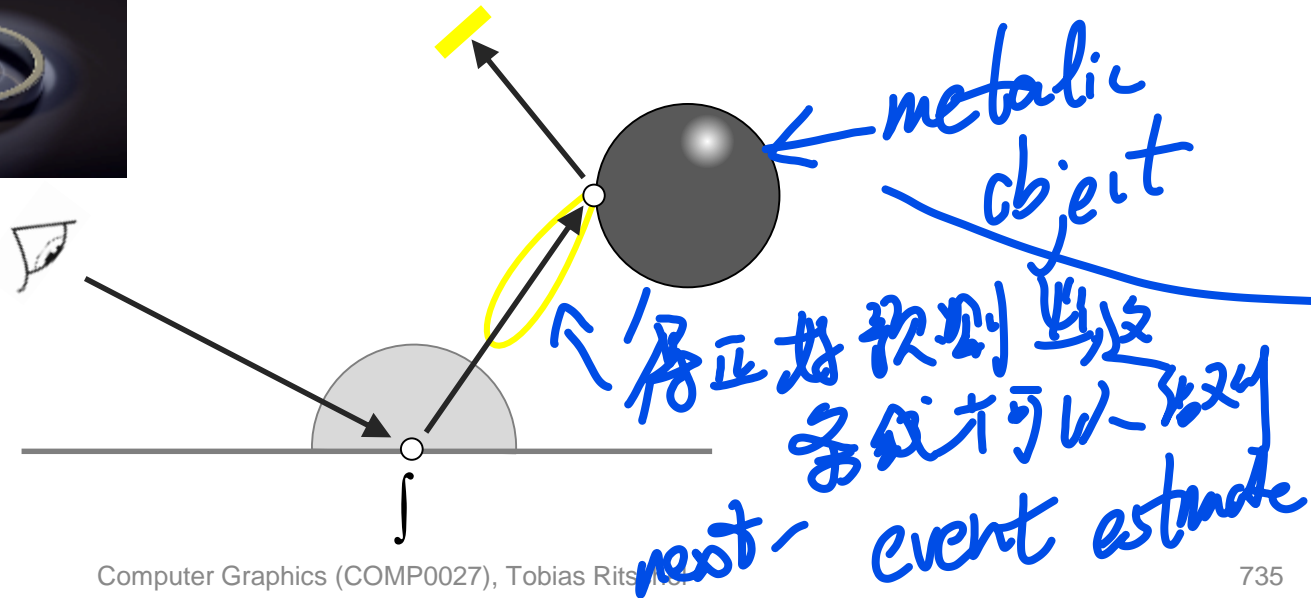


Reflective caustic



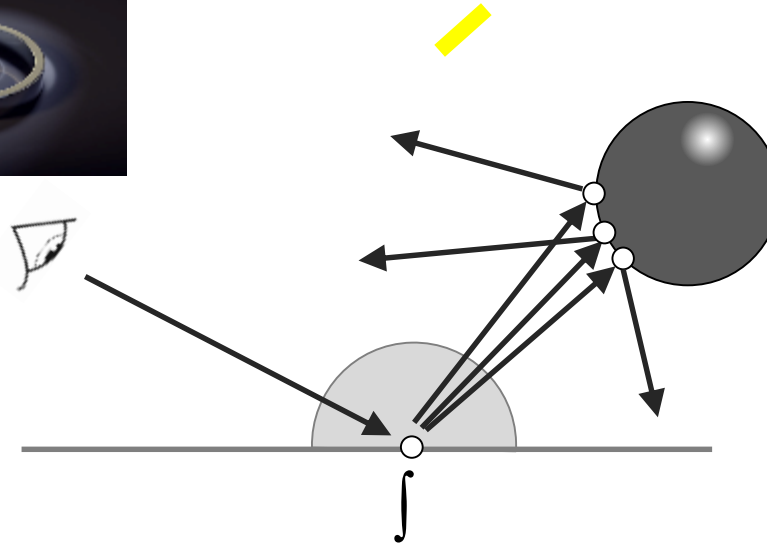
Example 2: Caustics

- A **caustic** is similar to a small light sources
- No obvious way to find it

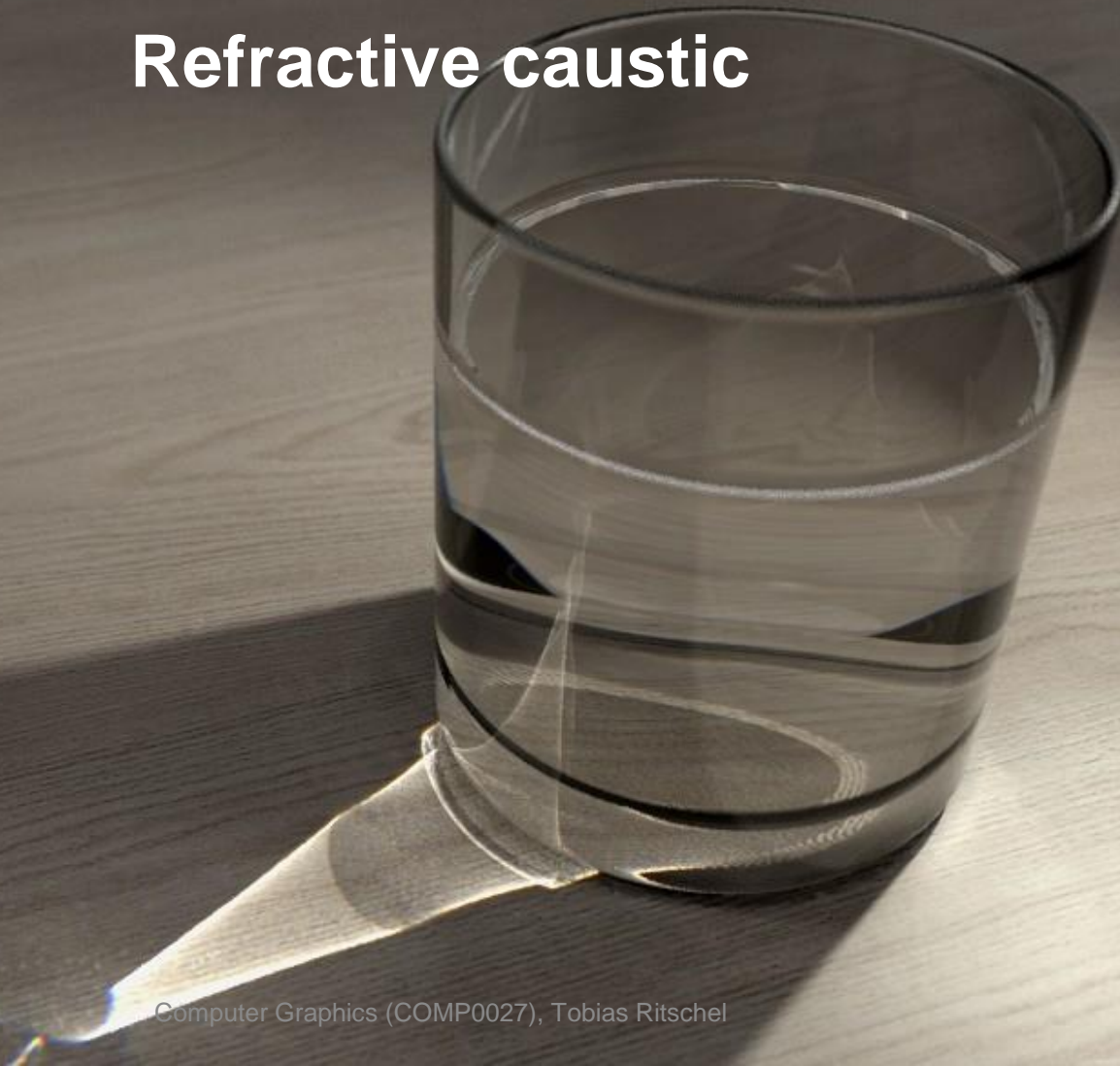


Example 2: Caustics

- This can be wrong in a million of ways
- Needs luck twice
- Three examples

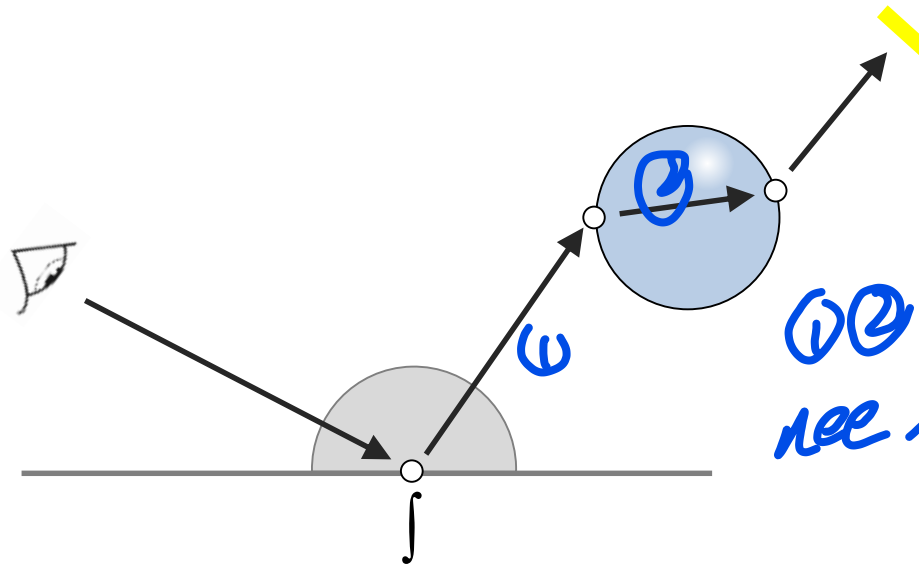


Refractive caustic



Example 2: Caustics

- A **caustic** is similar to a small light sources
- No obvious solution
- Refractive even harder: Two angles!



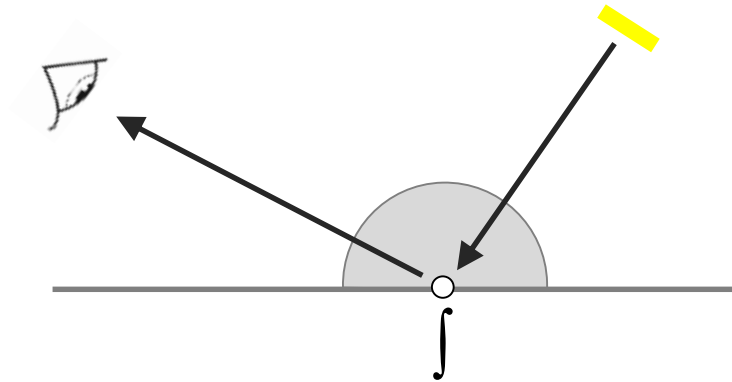
①② 得变正切线
need 检查作用
impossible.

What is hard for path tracing?

- Paths of the form LSDE, LSSDE, etc
- Light that undergoes one or more specular reflections, then a diffuse bounce
- Reflective or refractive caustics

Solution: Light tracing method

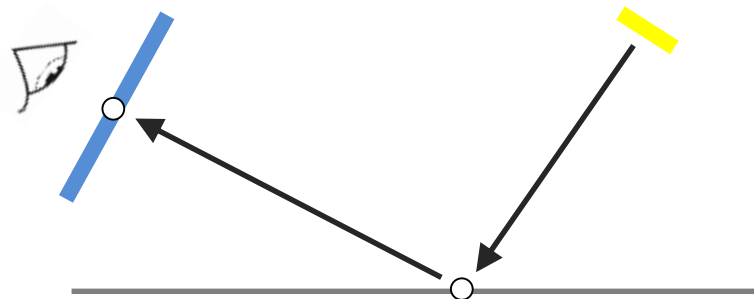
- Start path at the light
- Trace rays through the scene
- In the end **project** onto sensor



Light tracing

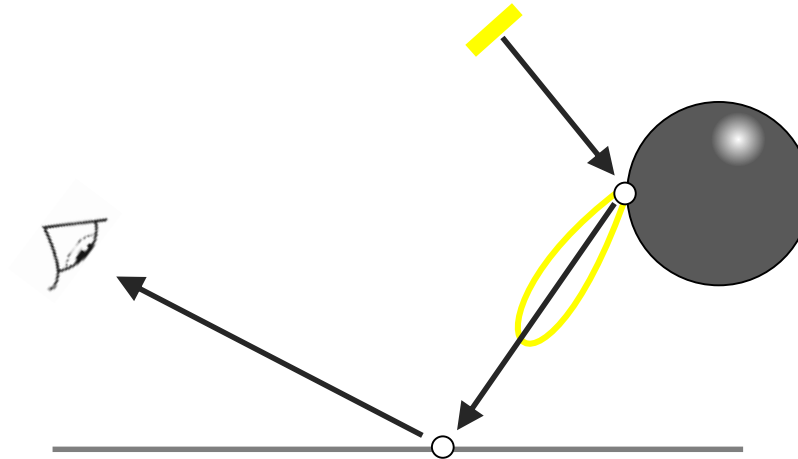
- Need next-event estimation at final vertex
- Sensor is even smaller than light
- Finding it by chance even less likely

↓ 这里 vertex 太小了
第一次 bounce 太难



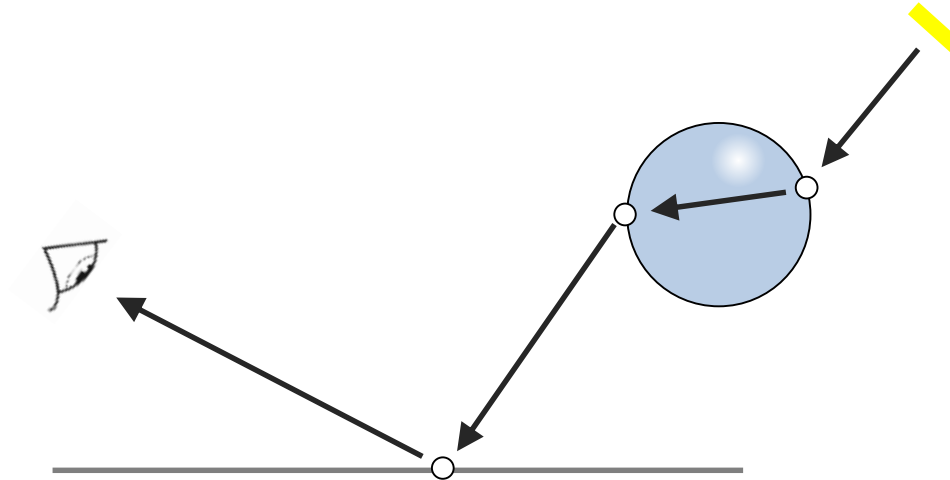
Light tracing for a reflective caustic

- Works quite well



Light tracing for a refractive caustic

- Works quite well

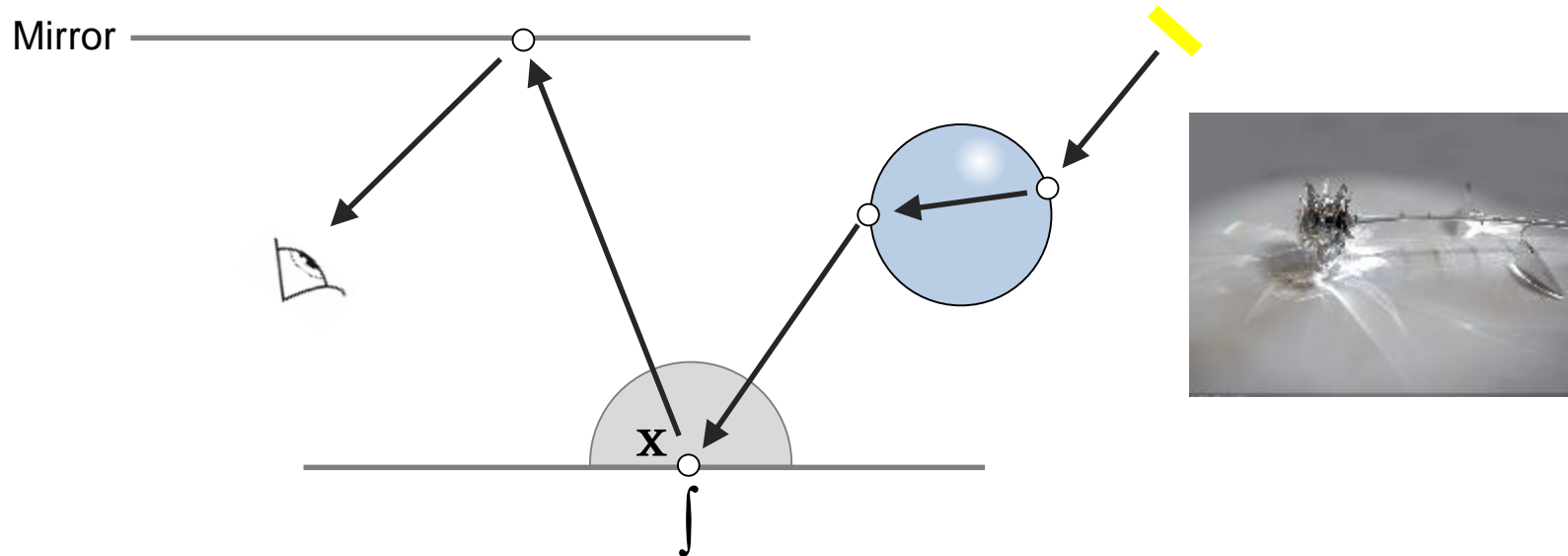


Reflection of a caustic



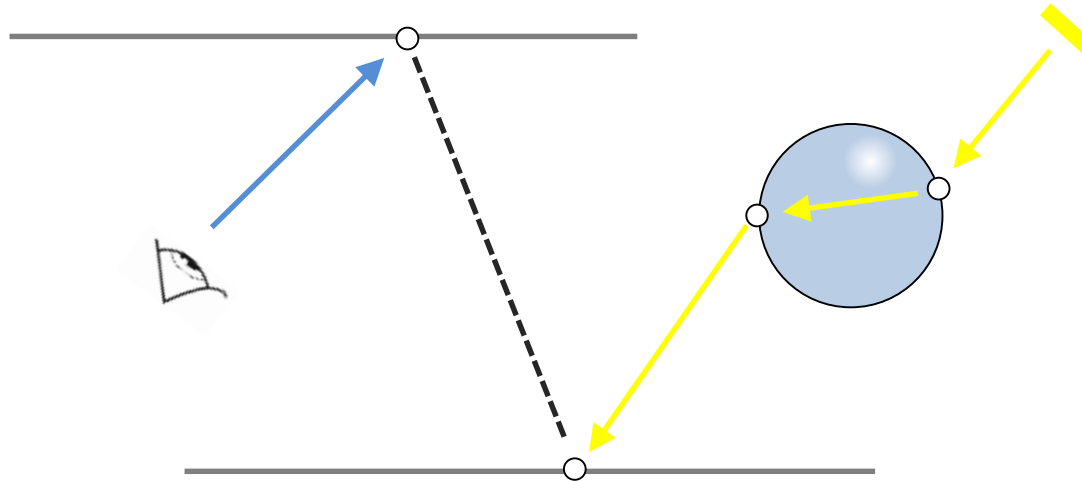
Caustics in a mirror

- Very hard!
- How could we know at x how to go on?



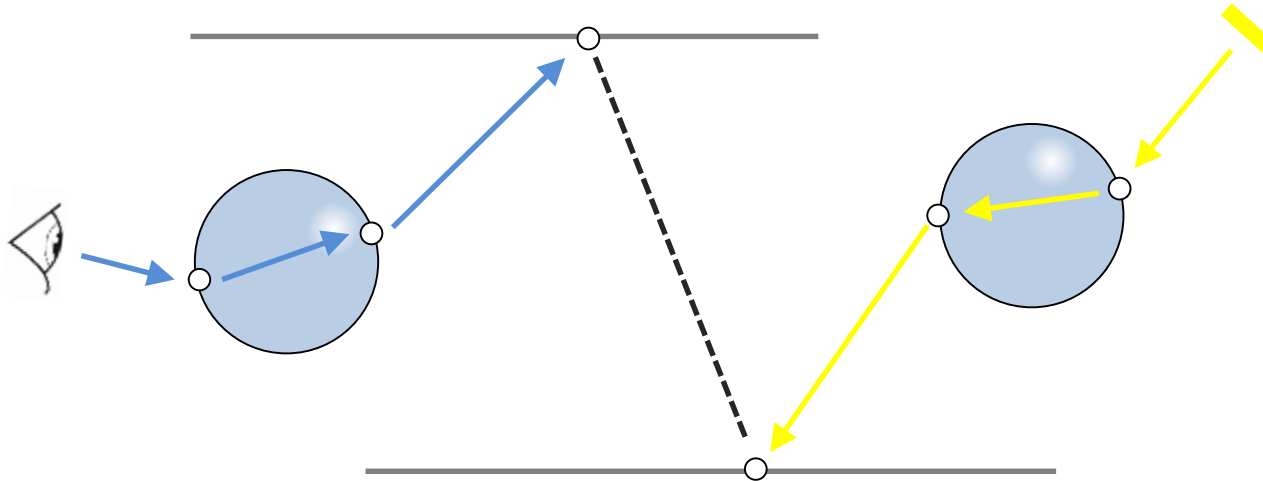
Bi-directional path tracing

- Start a path both at the eye and the light
- Connect the ends



Bi-directional path tracing

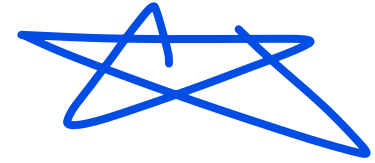
- Start a path both at the eye and the light
- Connect the ends



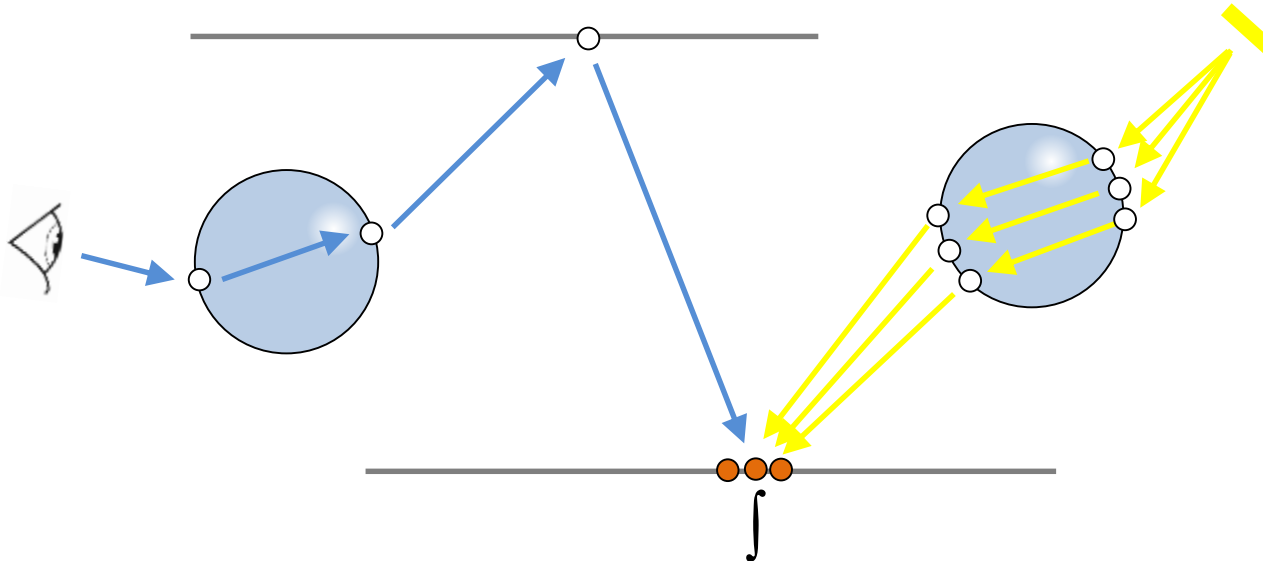
Photon mapping

- When eye paths connect to light paths we don't care about their path, only about the vertex
- Idea:
 - Store end-vertices from the light
 - Re-use from the eye

Photon mapping



- Start many rays at the light, store last vertex ^①
- Re-use from the eye ^②



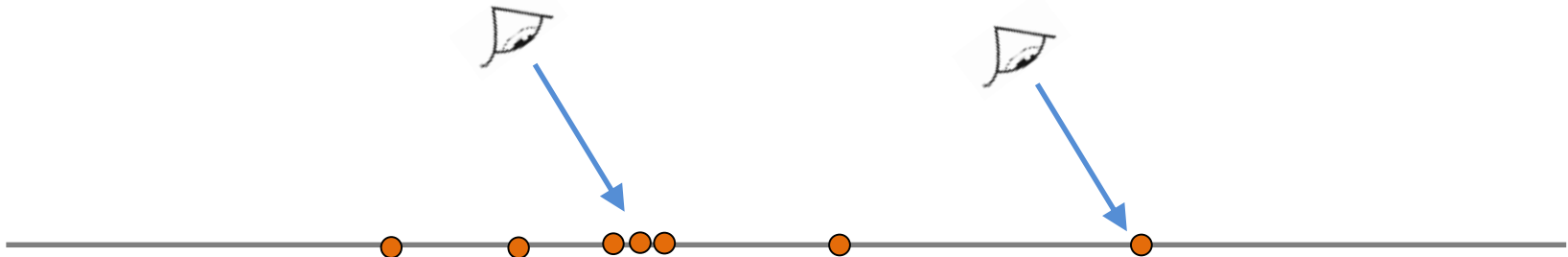
Density estimation

- Photon are just a list of 3D points
- How to convert into $L_i(\mathbf{x}, \omega)$?
- Find how many are nearby!

fix the radius k
 fix the k radius

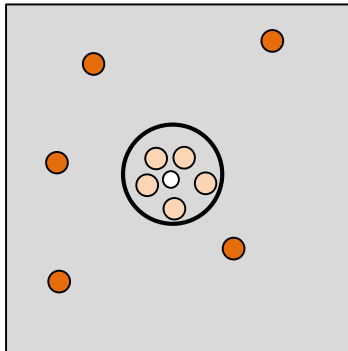
Many photons: bright

Fewer photons: darker



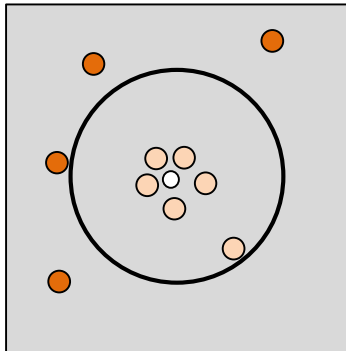
Two options: Option 1

- Find the nearest k
- See how large their radius r is
- Large a is small density and low L



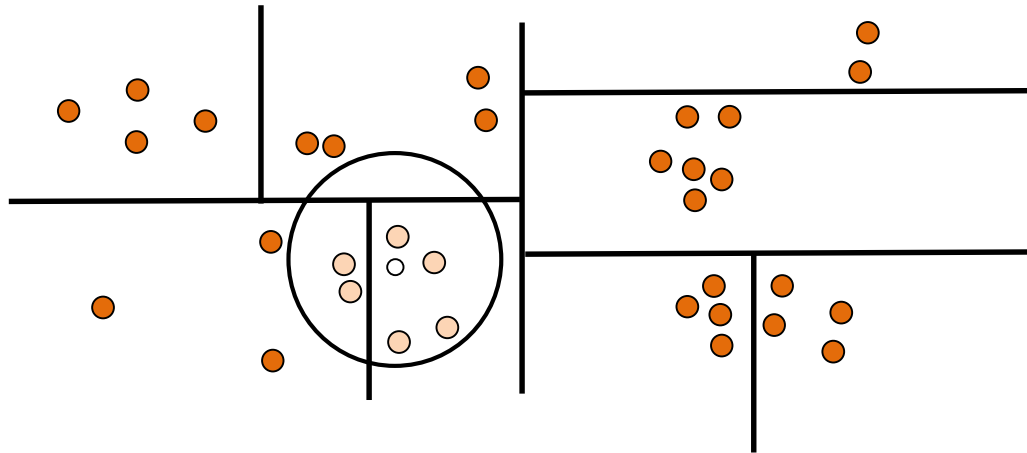
Two options: Option 2

- Fix a radius r
- Count how many k are in this radius
- Large k is high density and high L



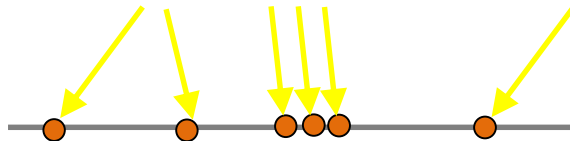
How to find k nearest?

- Spatial bounding structures
- k -d tree
- Can find k NN in $\log(n)+k$ time for n points



BRDF in PM

- The light also depends on the direction
- Photons also store from where they came
- Like this, can take direction into account



Recap

- Can also start from the light
- Sometimes better
- Three ways to to this
 - Light tracing
 - Bi-dir raytracing
 - Photonmapping