

Computer Graphics (COMP0027) 2022/23

# Texturing

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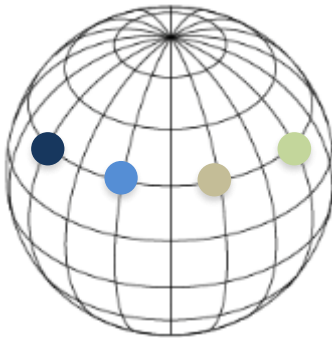
# Texture Mapping

- Have seen: colour can be assigned to vertices
- But: don't want to represent all this detail with geometry



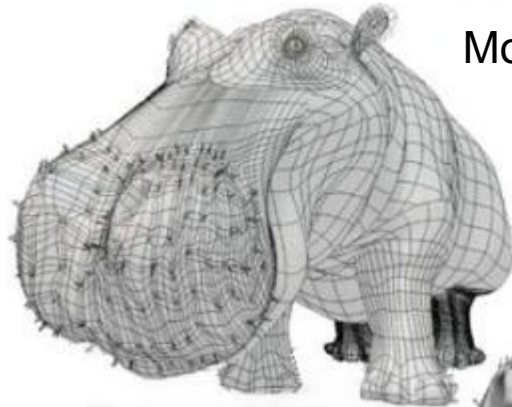
# Texture Mapping

- Considering small details
  - We may not want to add polygons to represent every detail
  - Instead, prefer to keep a large polygon and use an *image* to represent the details



# The Quest for Visual Realism

大河子



Model



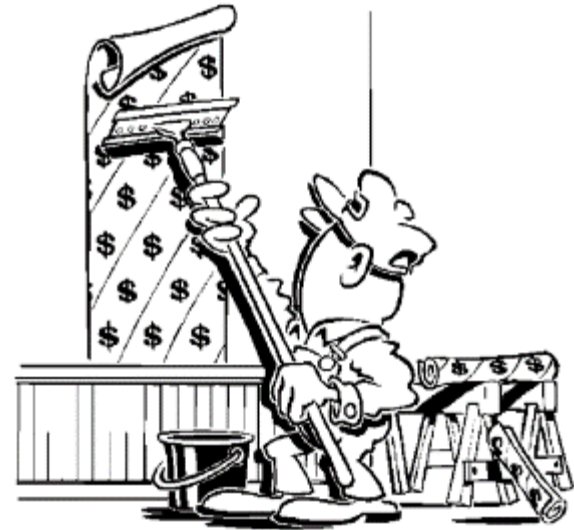
Model + Shading



Model + Shading  
+ Textures

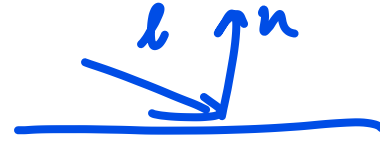
# Texture Mapping

- Increase the apparent complexity of simple geometry
- Efficient packing of flat detail
- Like wallpapering or gift-wrapping with stretchy paper



# Texture Mapping

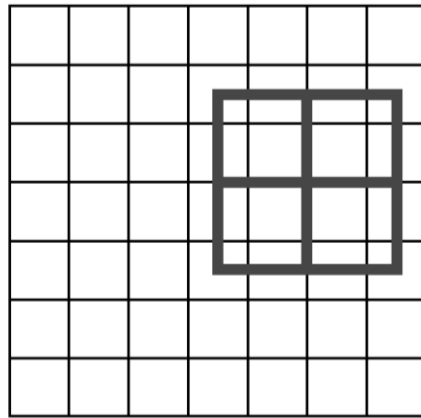
- Standard texture mapping modifies diffuse component  $k_d$ 
  - Pasting a picture onto the polygon
- A texture is a 2D array of texels storing RGB (or RGBA) components



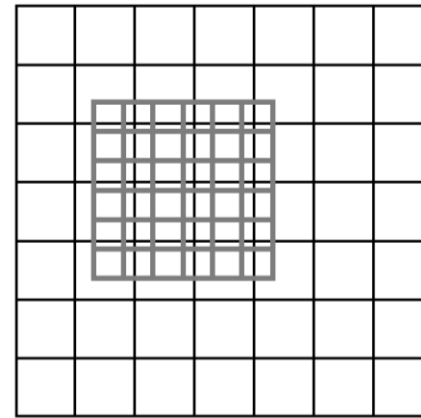
# Difference between pixels and texels

There can be a different match between the pixels of the framebuffer and the texels of the texture

$$N_{\text{texels}} < N_{\text{pixels}}$$



Magnification



Minification

texture 里  
↓ 块  
(+), 知  
pixel ?  
- 样

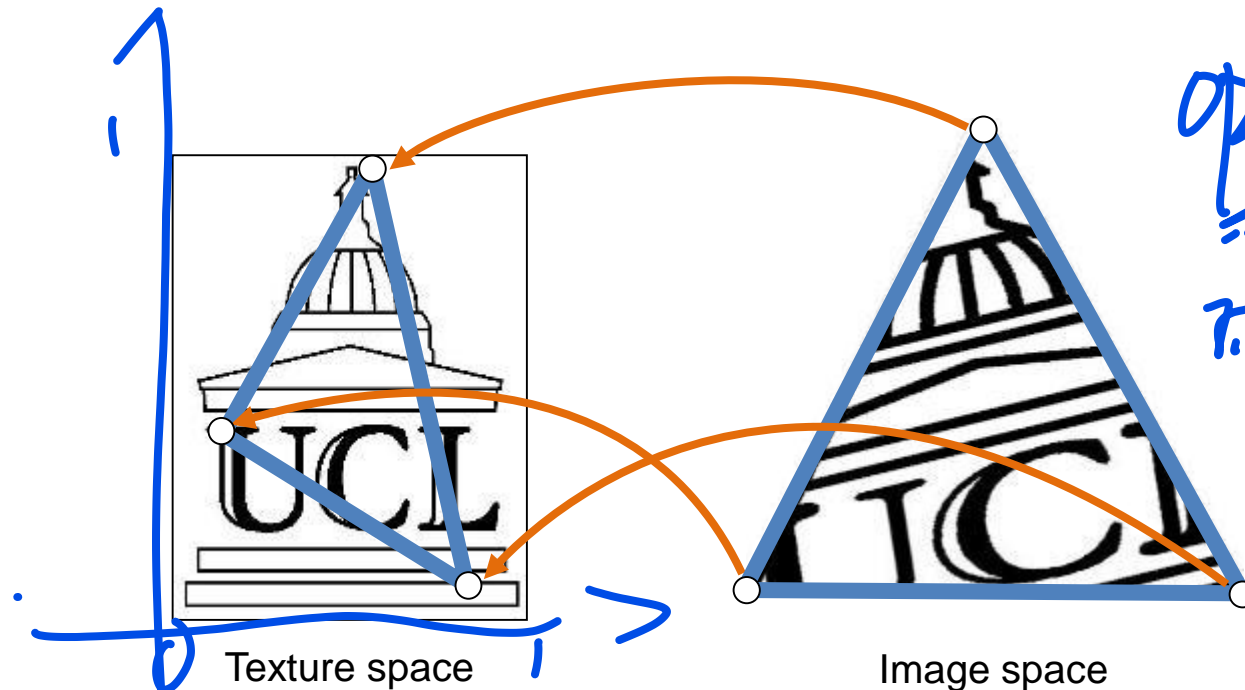
# Overview

- Texture mapping
  - Inverse and Forward Mapping
  - Bilinear interpolation
  - Perspective correction
- Mipmapping 屏幕映射
- Other forms of mapping
  - Environment
  - Bump mapping



# Texture coordinates

Each vertex is associated with a point on an image ( $s, t$ )



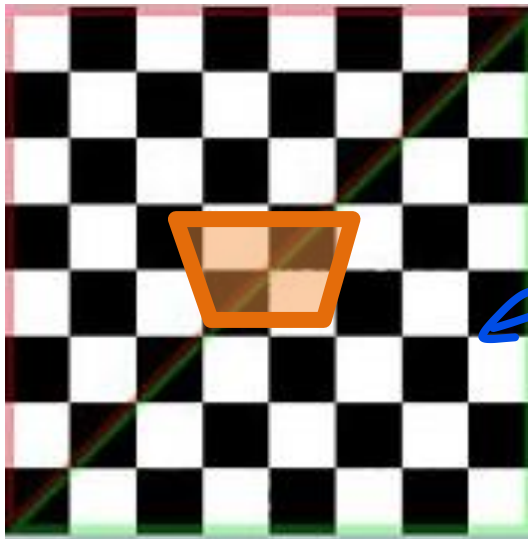
# Forward Mapping

- ✗ For points in the texture, map onto the polygon
  - much harder to implement correctly, and harder to model
- ✓ Inverse mapping is much more commonly used
  - Most 3D modelers output  $u, v$  co-ordinates for texture application

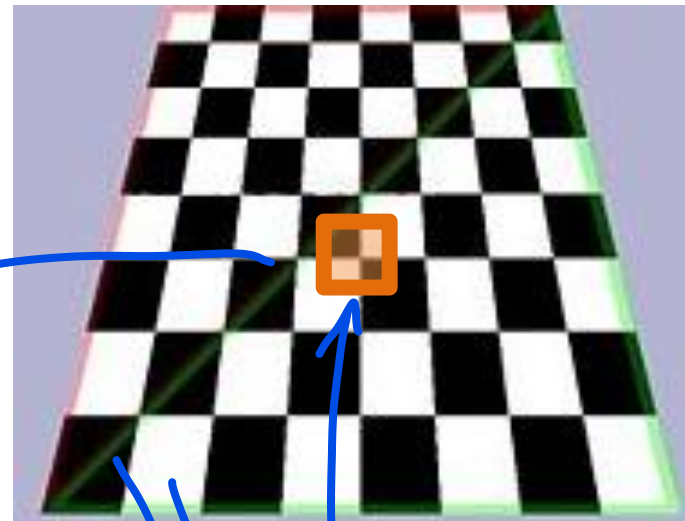
纹理坐标  
放到 model 上

↑  
看 model 放纹理  
(unproject)

# Pixels and texels



Texture



3D view

...perspective.  
- 前面 20 5 know  
have texels  
pixel

# Sampling

- A pixel maps to a non-rectangular region
- Usually only perform map on centre of pixel
- Problem: Under and over-sampling

Oversampling



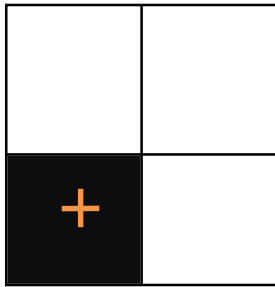
Undersampling



← texel  
pixel

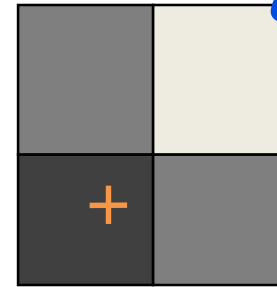
# Undersampling solution: Filtering

Nearest neighbour



Pick texel with closest  
centre

Bilinear



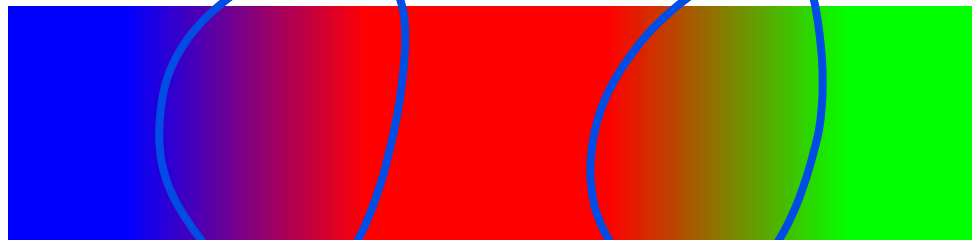
Weighted average  
based on distance to  
texel centre

# Filtering examples

(linear 没有bi)



Nearest Neighbor

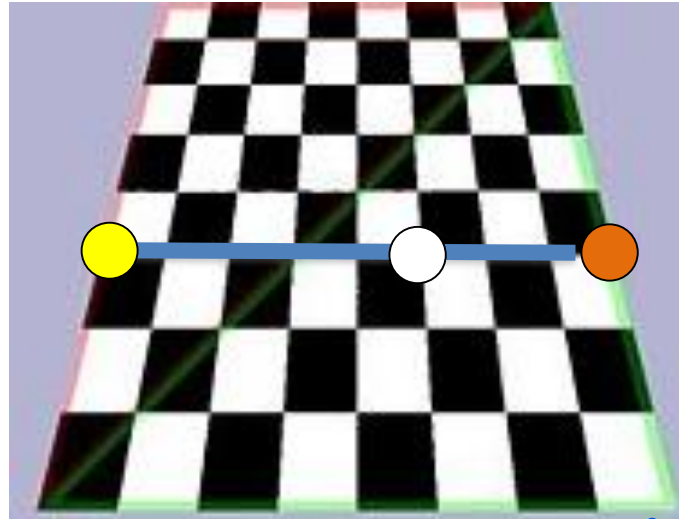


Bilinear Filtering

∴ 有weight了

# Filtering

- Bilinear filtering (partially) solves the undersampling problem since it provides smooth shading between texels



(Minecraft)

# MIP-Mapping

- When oversampling we use **MIP-mapping**
- Resample image at lower resolution
- Create a “pyramid” of textures.
- Interpolate texture between two adjacent layers

mid map 解決  
oversampling  
(1 pixel 对应  
K 3 texels)



# Texture Pyramid



128x128



64x64



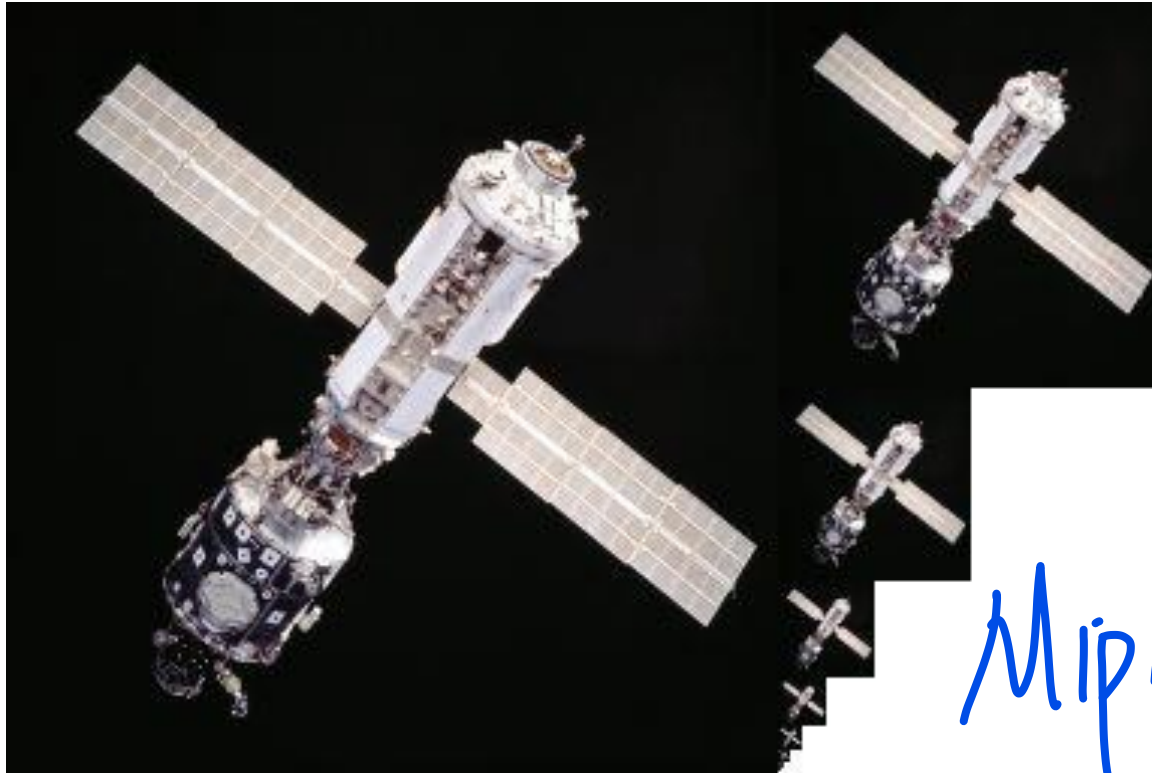
32x32

...

x

1x1

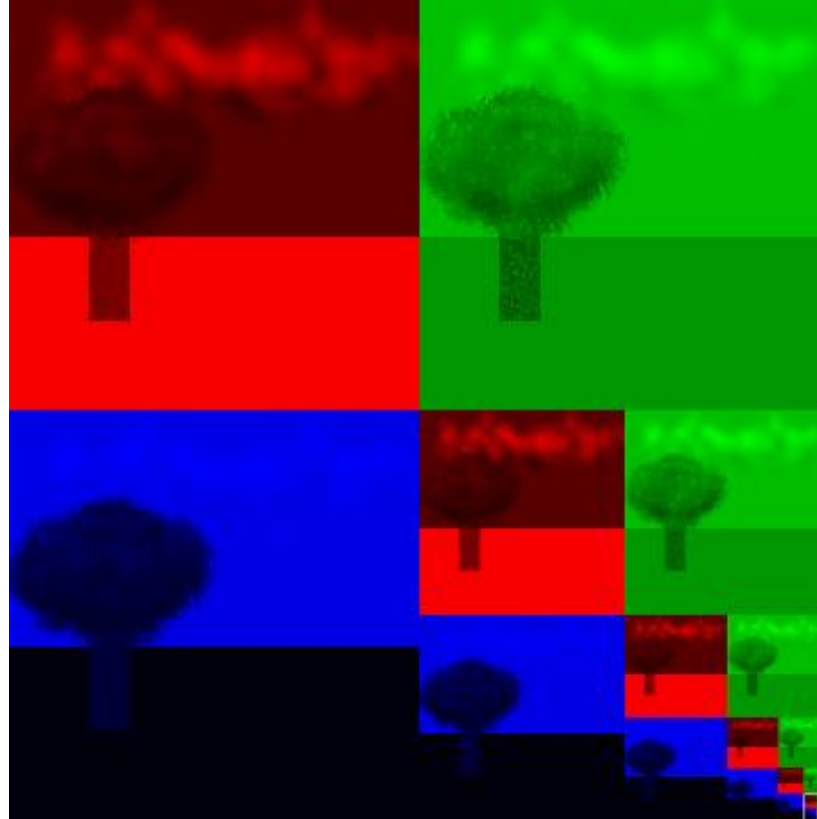
# Efficient spatial layout



Mip Map

# Efficient RGB channel layout

*interesting.*



# Linear MIP Sampling

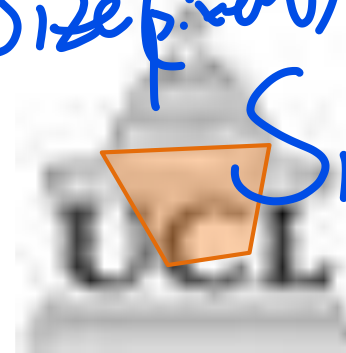
- Choose the level of the MIP-map based on the  $du$  and  $dv$  for  $dx$  and  $dy$  are closest to 1 pixel



— Texel  
— Pixel



— Texel  
— Pixel



— Texel  
— Pixel

$$\text{Size}(\text{pixel}) = \text{Size}(\text{texel})$$

# Tri-linear MIP Sampling

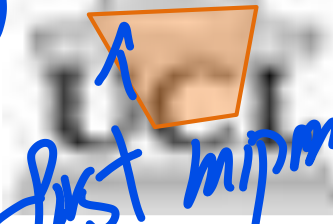
- Choose two level and after interpolating within the levels, interpolate between the outcome



— Texel  
— Pixel



— Texel  
— Pixel

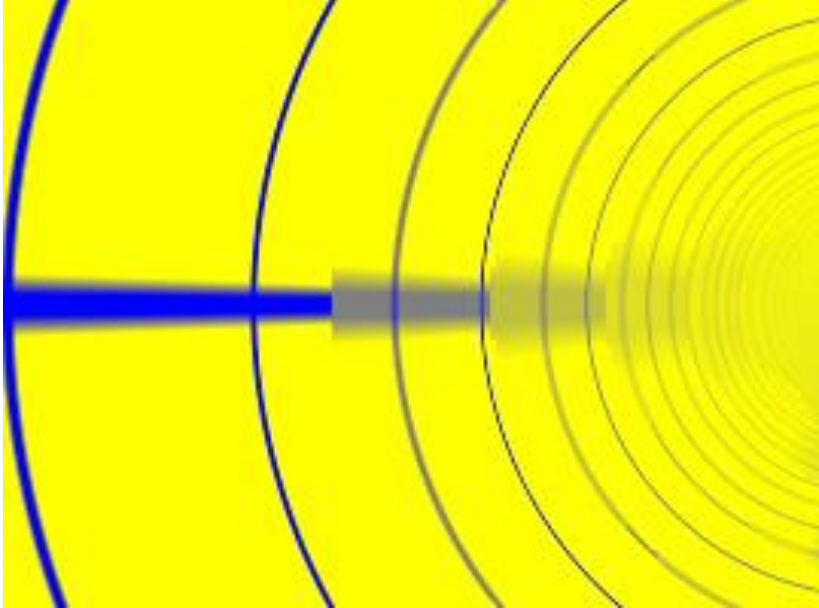


— Texel  
— Pixel

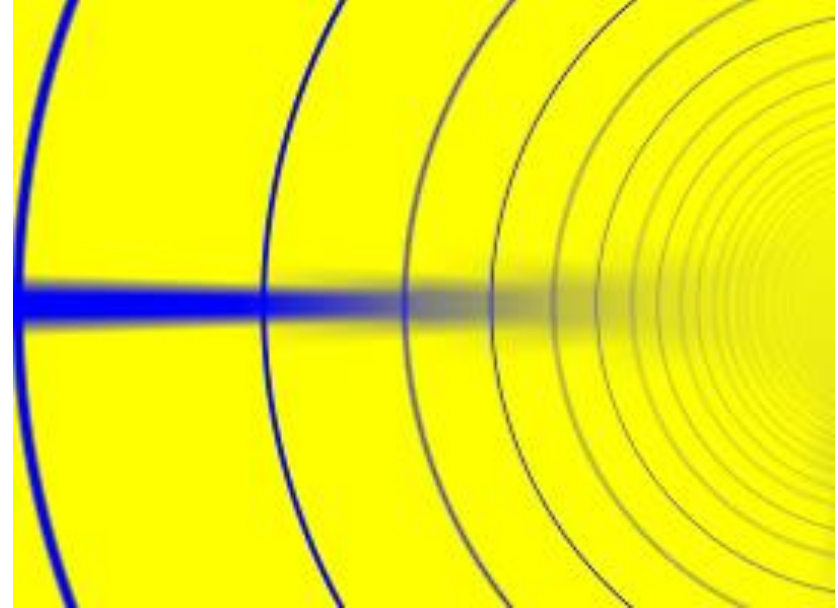
second mip map  
(之前怎么都在想 Tri-linear)

选2个再插值  
(eg. 60% + 40%)  
first mip map

# MIP Mapping Examples

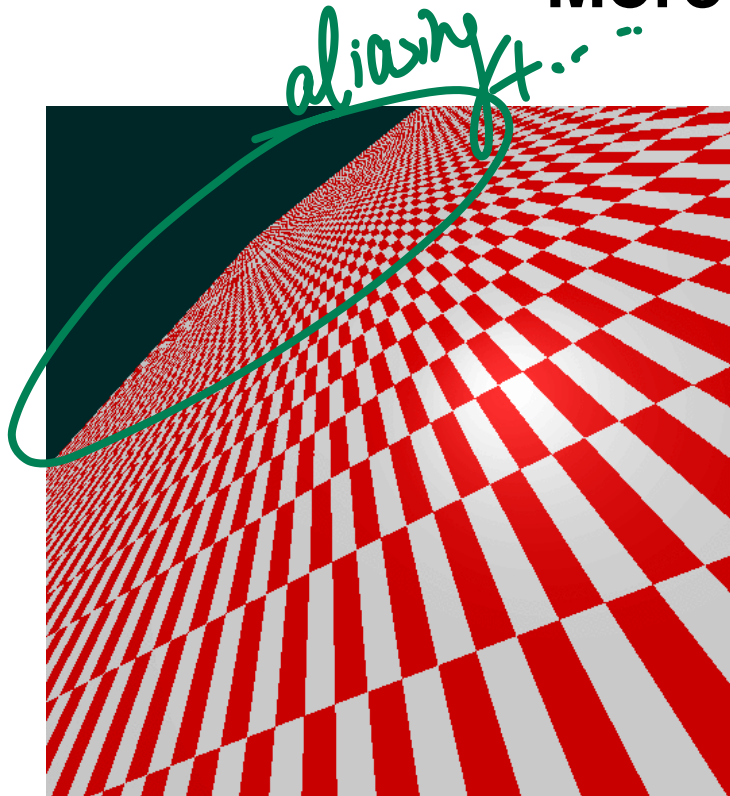


Bilinear Filtering  
(distinct MIP map levels)

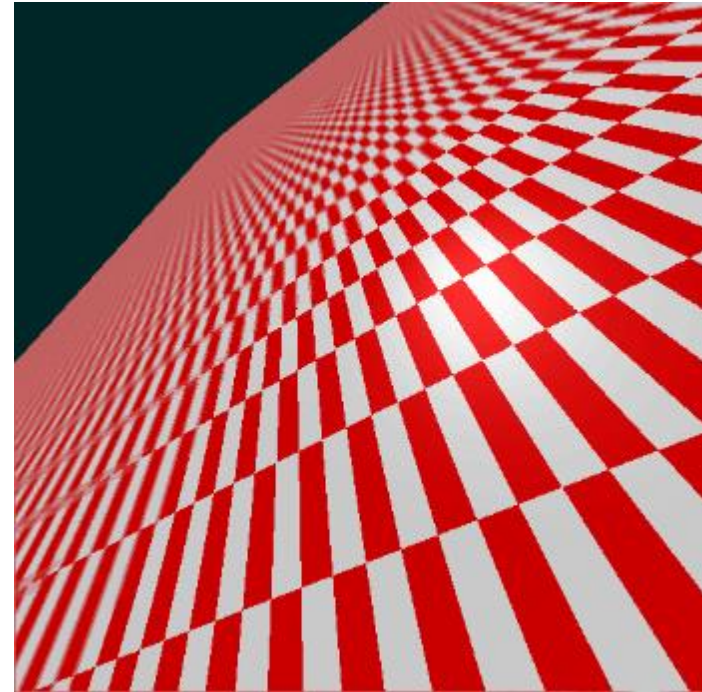


Trilinear Filtering  
(MIP mapping)

## More Examples



Nearest Neighbor

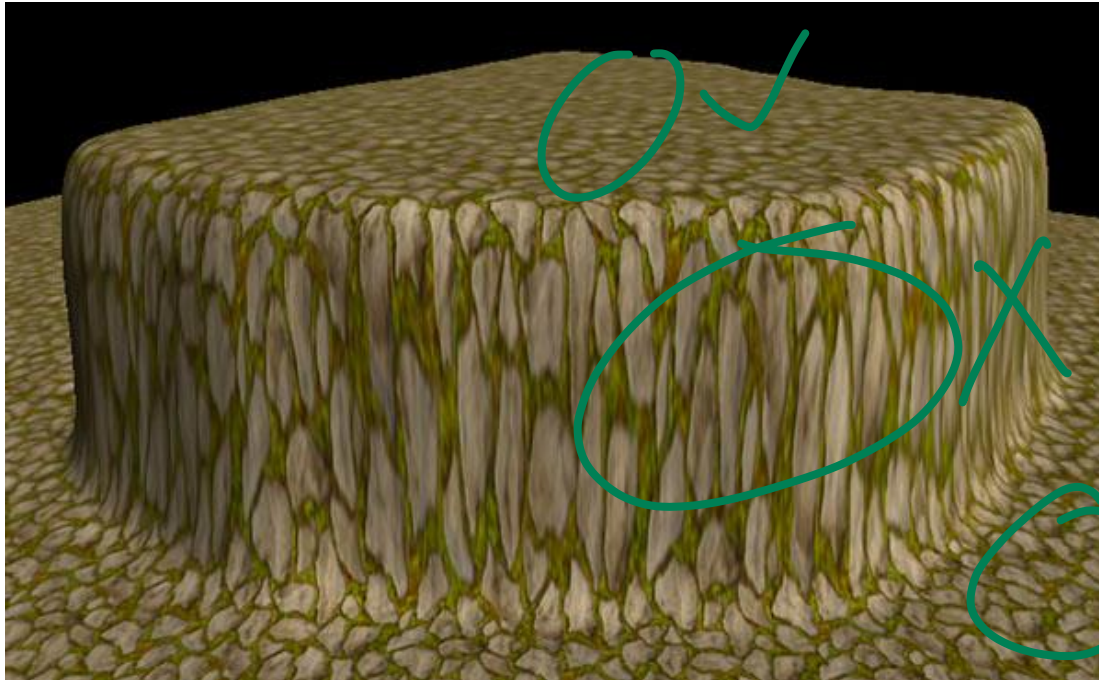


MIP Mapping

# Parametrization *参数化*

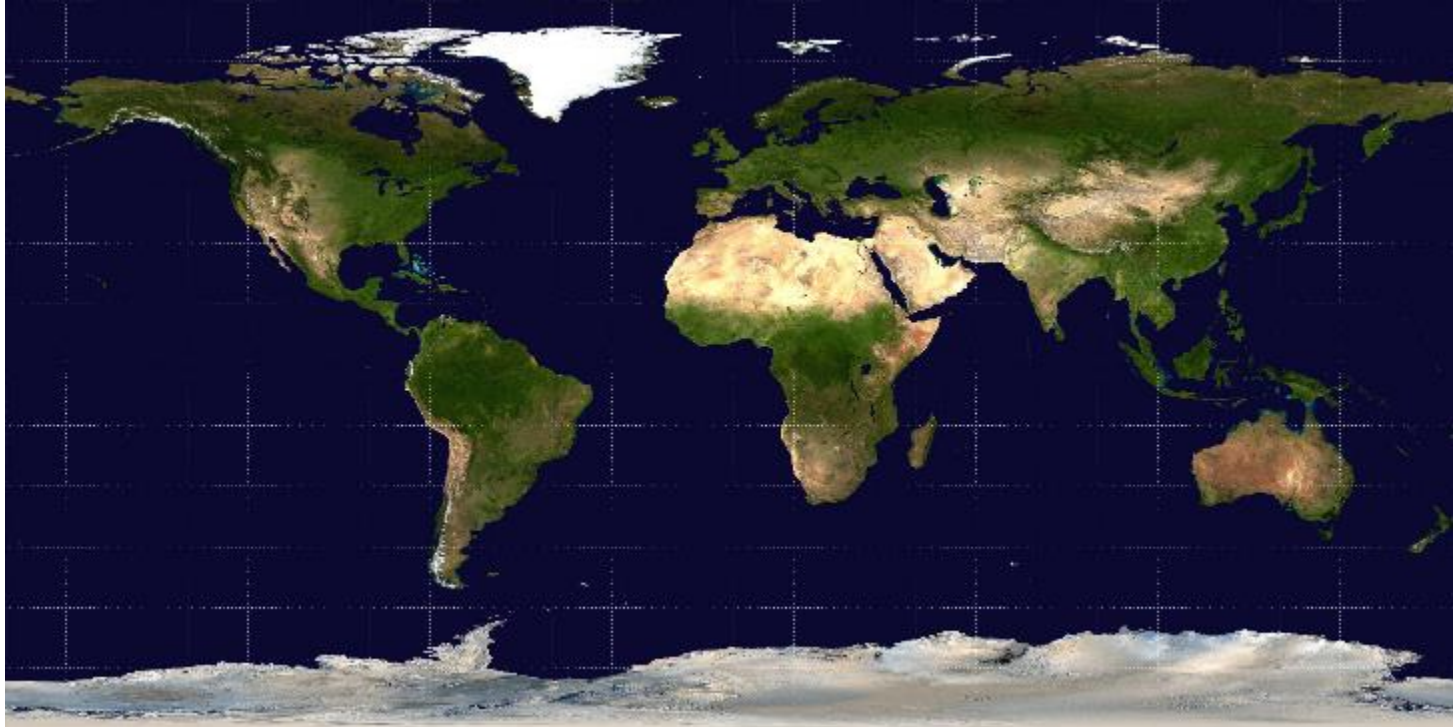


# Where does $u$ , $v$ come from?



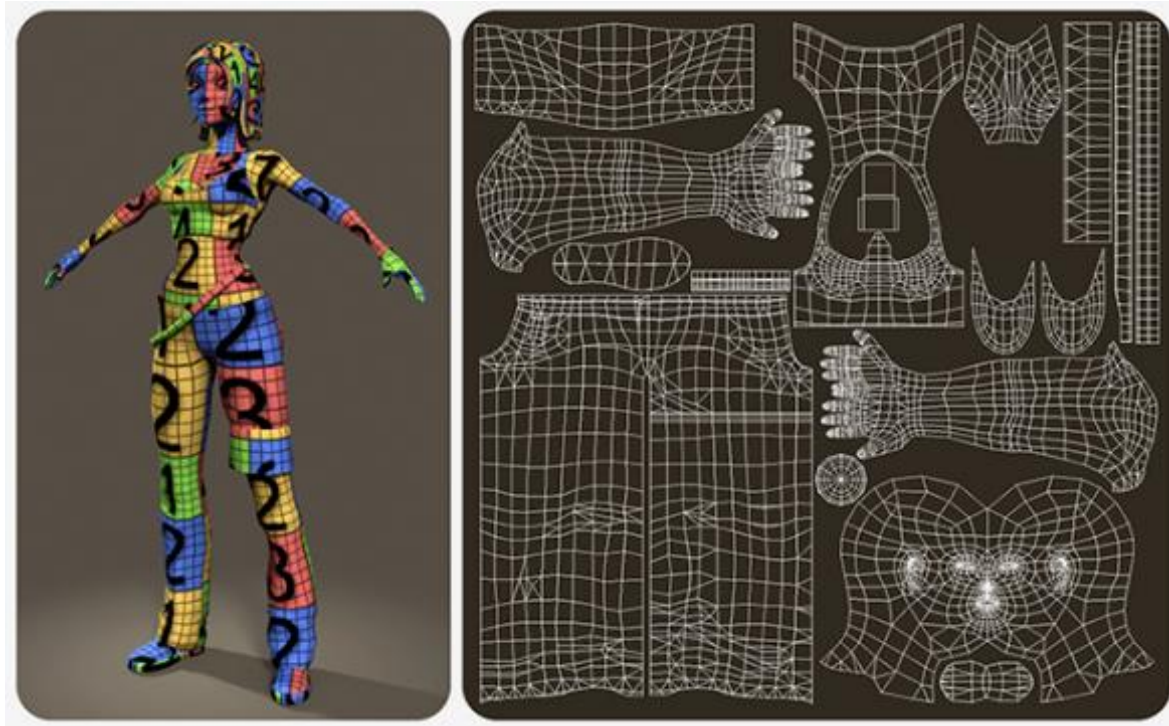
Planar projection

# Where does $u, v$ come from?



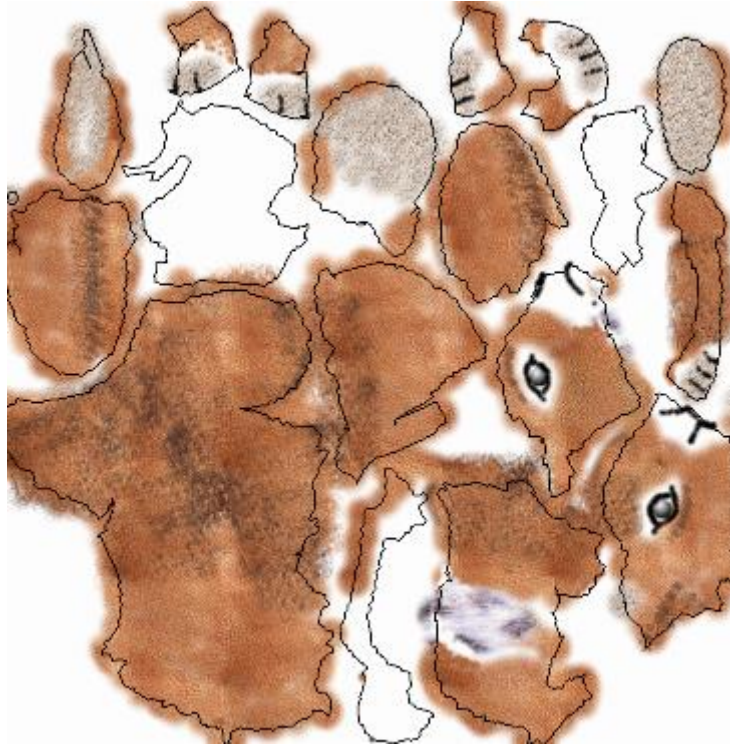
Spherical projection

# Where does $u, v$ come from?



Charts, done manually

# Where does $u$ , $v$ come from?



Charts, done automatically

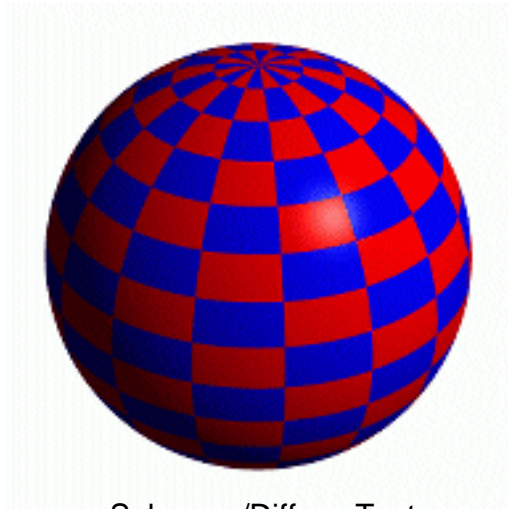
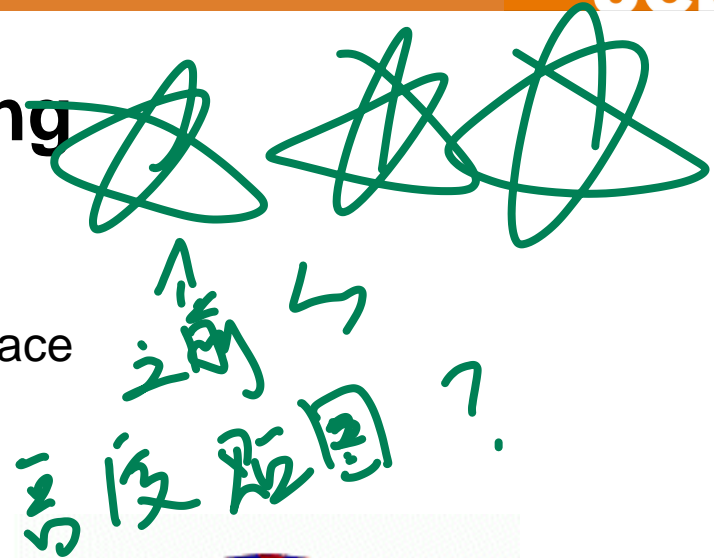
# Other Forms of Texture Mapping

1. Bump Mapping
2. Displacement Mapping
3. Environment Mapping

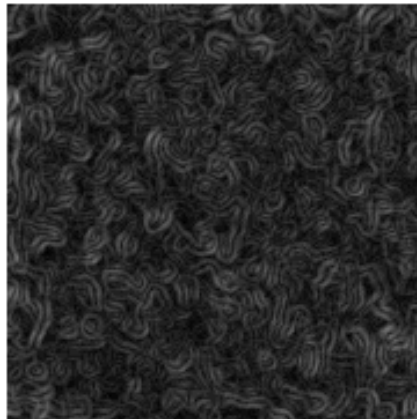


# Bump Mapping

- Use textures to alter the surface normal
  - Does not change the actual shape of the surface
  - Just shaded as if it were a different shape



Sphere w/Diffuse Texture



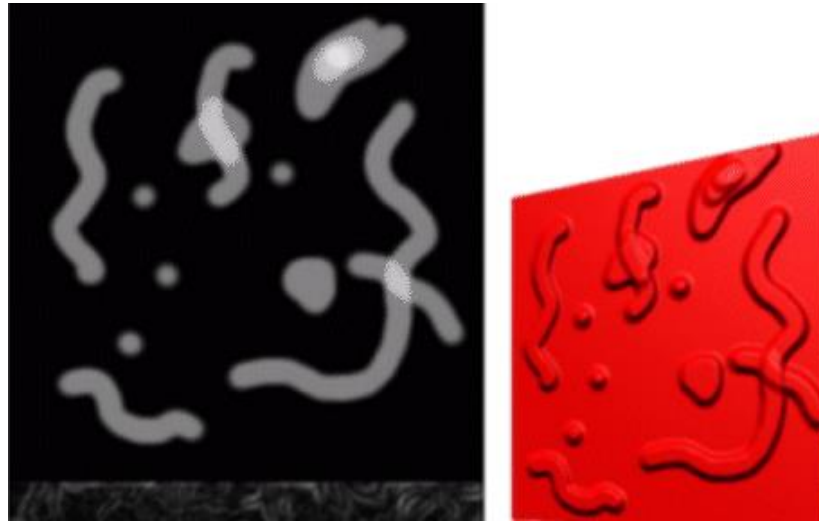
Swirly Bump Map



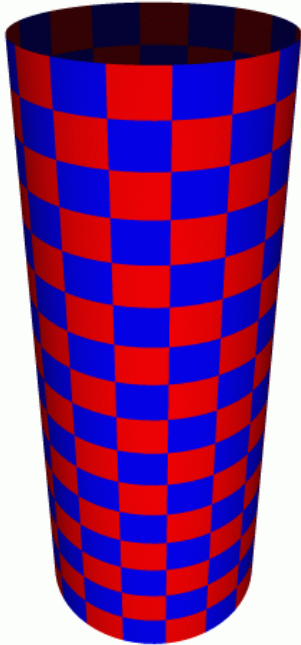
Sphere w/Diffuse Texture & Bump Map

# Bump Mapping

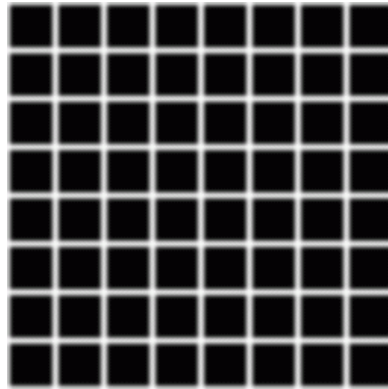
- Treat the texture as a single-valued height function
- Compute the normal from the partial derivatives in the texture



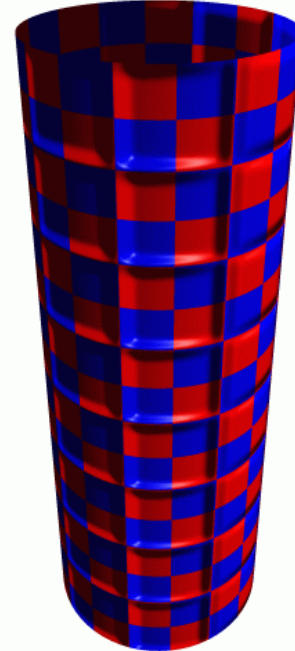
# Another Bump Map Example



Cylinder w/Diffuse Texture Map



Bump Map

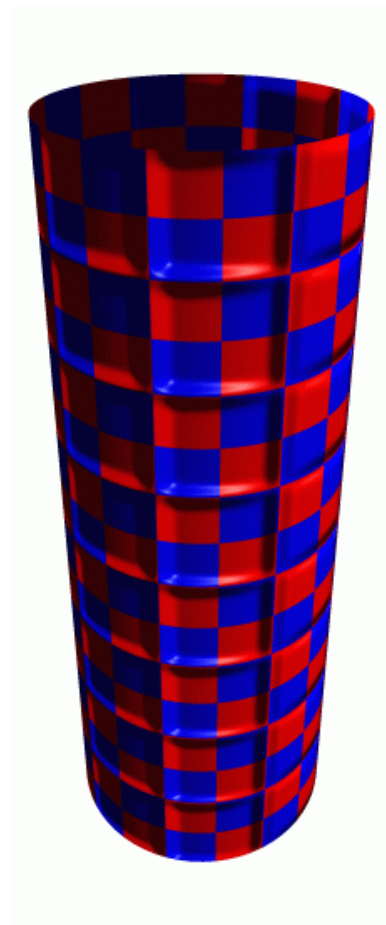
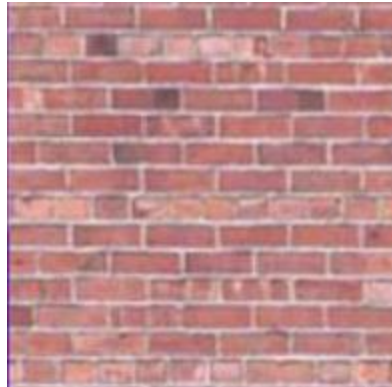


Cylinder w/Texture Map & Bump Map



# What's Missing?

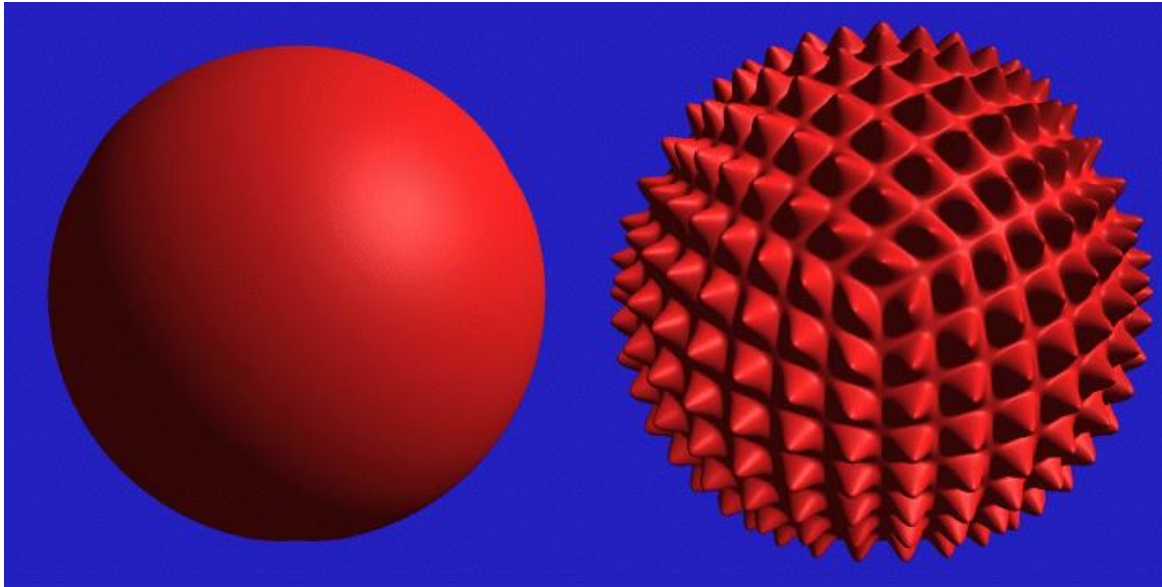
- There are no bumps on the silhouette of a bump-mapped object
- Bump maps don't allow self-occlusion or self-shadowing



# Displacement Mapping

- Use the texture map to actually *move* the surface point
- The geometry must be displaced before visibility is determined

*move Vertices*



# Displacement Mapping



Image from:

Geometry Caching for  
Ray-Tracing Displacement  
Maps

by Matt Pharr and Pat  
Hanrahan.

Note the detailed shadows  
cast by the stones

# Environment Maps

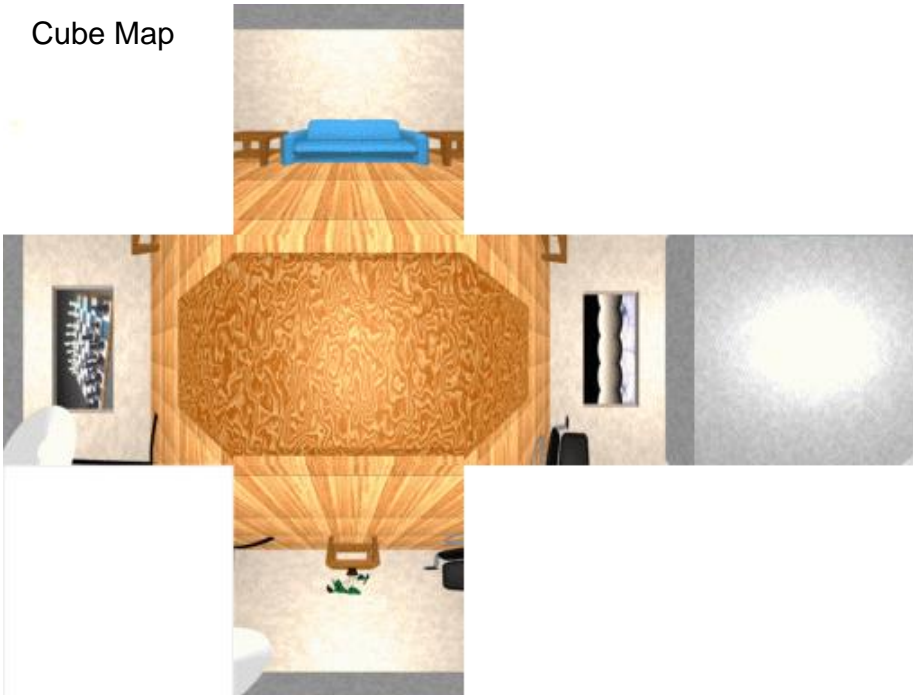


- We can simulate reflections by using the direction of the reflected ray to index a spherical texture map at "infinity".
- Assumes that all reflected rays begin from the same point.



# What's the Best Layout?

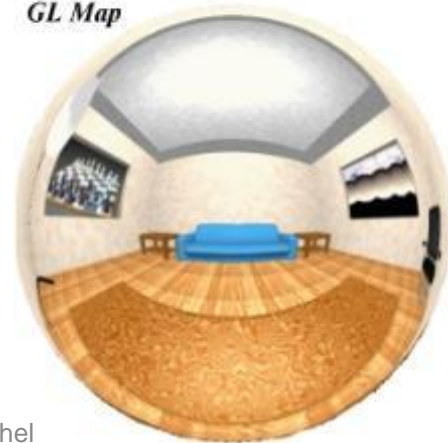
Cube Map



*Latitude Map*



*GL Map*





# Environment Mapping Example

(Render  
Texture  
!)



Terminator II

# Recap

- Texture Mapping adds detail to otherwise simple geometry
- “Texture” can mean different modifications to the calculation of lighting, or can even displace geometry locally
- Sampling issues are very important
- To some extent current graphics cards are built around attempting to do texturing efficiently.