A Theory-Based Evaluation of Nearest Neighbor Models Put Into Practice HENDRIK FICHTENBERGER AND DENNIS ROHDE

PART OF DATA PROCESSING PIPELINE

fixed here

kissing number

number of

points

d-dimensional

given: point-set in euclidean space

build

nearest neighbor model

- our solution

edccess.

 $\boldsymbol{\omega}$

<u>S</u>

What is the quality of the output?

query: give k nearest points to



measure of efficiency

2. test if given graph is k-nearest neighbor graph

- directed edges
- eregular (out-degree = k)

no need to compute full graph

1. implicit conversion of k-nn

model to geometric graph

edges point to k-nearest neighbors of vertex

Testing k-nearest Neighborhood

- O(k² ½√n ψ²) queries sufficient in bounded average-degree graphs
- $\Omega(\sqrt[n]{\epsilon k} + k\psi^2)$ queries required in general graphs

all models were built ten times for each parameterization, then tested once

EXPERIMENTS

recall of algorithm

constants of O-notation

by ε-distance of model all ANN algorithms, all datasets 1.00 parameters 0.001, 0.05 0.75 -0.001, 0.5 0.001, 5 0.01, 0.05 recall - 0.50 -0.01, 0.5 0.01, 5 0.1, 0.05 0.25 -0.1, 0.5 0.1, 5 0.2 0.001 0.005 0.05 0.01 0.02 0.1

datasets: MNIST, Fashion-MNIST, Sift models: KGraph(Ann Arbor Algorithms), hnsw and SWGraph(NMSLib)

EXAMPLE GRAPHS

bucketed distance

PROPERTY TESTING ALGORITHM

- accepts every k-nearest neighborhood graph with high probability
- rejects every graph that is ε-far from being a k-nearest neighborhood graph with high probability
- at least an ε-fraction of edges are faulty
- can freely answer otherwise

- sample $O(k_{\epsilon}^{\perp} \sqrt{n})$ vertices uniformly at random
- throw away vertices with high degree
- sample O(kψ¬Π) vertices uniformly at random
- for every vertex in first sample check if any vertex from second sample lies nearer than any neighbor

Reject

Accept

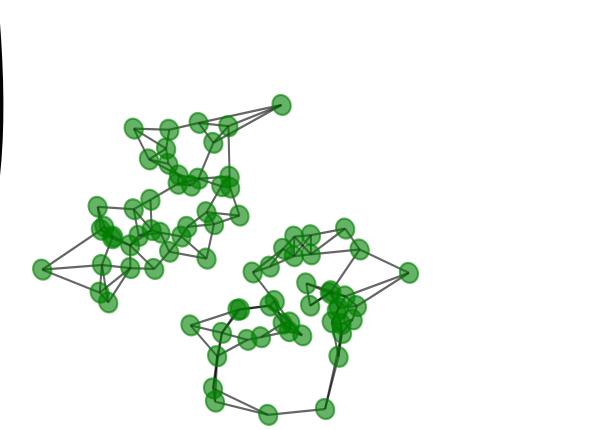
full paper on arXiv

140 random points 420 edges

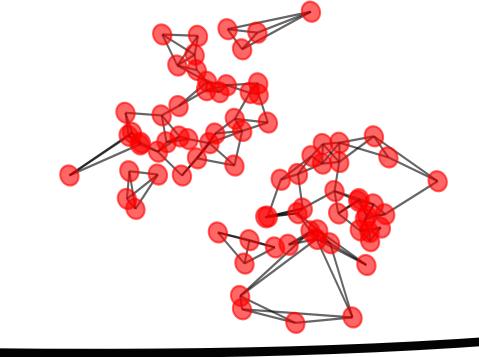
4 clusters



brute force 3-nn graph



graph from Annoy (Spotify) model



60 vertices are incident with faulty edges

OUR CODE:

The algorithm: github.com/deroh_de/knn test Extension of ann-benchmarks: github.com/hfichtenberger/ann-benchmarks

AAALgo: github.com/aaalgo/kgraph NMSLIB: github.com/nmslib/nmslib Annoy: github.com/spotify/annoy



