

PART 1 Measure of Dispersion

Professional Definition

Measure of Dispersion is a statistical measure used to describe the spread or variability of data values around a central value.

Simple Definition (Classroom Language)

Dispersion batata hai:

Data kitna faila hua hai (spread)

Central tendency → center batata hai

Dispersion → spread batata hai

Why Dispersion is Needed

Suppose 2 companies salary:

Company A:

20k, 25k, 30k, 35k, 40k

Company B:

10k, 20k, 30k, 40k, 100k

Mean same ho sakta hai, but salary variation different hai.

Dispersion helps understand this difference.

Types of Measure of Dispersion

1. Range
 2. Variance
 3. Standard Deviation
-

Range

Professional Definition

Range is the difference between the maximum and minimum value in dataset

Formula

$$\text{Range} = \text{Maximum} - \text{Minimum}$$

Example (Maths Sum)

Data:

10, 15, 20, 25, 30

Solution:

Maximum = 30

Minimum = 10

Range:

$$\text{Range} = 30 - 10 = 20$$

Real Life Use

Used in:

Temperature analysis

Stock price analysis

Python

```
import numpy as np  
  
data=[10,15,20,25,30]  
  
print(max(data)-min(data))
```

Variance

Professional Definition

Variance is the average of squared deviations from mean

Formula

$$Variance = \frac{\sum(X - Mean)^2}{N}$$

Example

Data:

10, 20, 30

Step 1: Mean

$$Mean = (10 + 20 + 30)/3 = 20$$

Step 2: Square difference

Value Difference Square

10	-10	100
20	0	0
30	10	100

Sum = 200

Variance:

$$200/3 = 66.67$$

Real Life Use

Used in:

Stock market risk

3 Standard Deviation

Professional Definition

Standard deviation is square root of variance

Formula

$$SD = \sqrt{Variance}$$

Example

Variance = 66.67

SD:

$$\sqrt{66.67} = 8.16$$

Real Life Use

Used in:

Salary analysis

Risk analysis

Python

```
import numpy as np  
  
data=[10,20,30]  
  
print(np.std(data))
```

PART **2** Percentage

Professional Definition

Percentage is a number expressed as fraction of 100

Formula

$$\text{Percentage} = \frac{\text{Value}}{\text{Total}} \times 100$$

Example

Marks = 45

Total = 50

$$\text{Percentage} = (45/50) \times 100$$

$$= 90$$

Real Life Use

Student marks

Profit calculation

PART 3 Percentile

Professional Definition

Percentile is the value below which certain percentage of observations fall

Simple Explanation

Percentile tells:

Position of value in dataset

Example

Data:

10, 20, 30, 40, 50

50 percentile = Median = 30

Real Life Use

Used in:

Competitive exams

GRE, CAT

Python

```
import numpy as np
```

```
data=[10,20,30,40,50]
```

```
print(np.percentile(data,50))
```

PART 4 Five Number Summary

Professional Definition

Five number summary is set of five values that describe dataset distribution

Five values

- 1 Minimum
 - 2 Q1
 - 3 Median
 - 4 Q3
 - 5 Maximum
-

Formula

$Q1 = 25 \text{ percentile}$

$\text{Median} = 50 \text{ percentile}$

$Q3 = 75 \text{ percentile}$

Example

Data:

10, 20, 30, 40, 50

$\text{Minimum} = 10$

$Q1 = 20$

$\text{Median} = 30$

$Q3 = 40$

$\text{Maximum} = 50$

Python

```
import numpy as np
```

```
data=[10,20,30,40,50]
```

```
print(np.min(data))
```

```
print(np.percentile(data,25))
```

```
print(np.median(data))
```

```
print(np.percentile(data,75))
```

```
print(np.max(data))
```

PART 5 OUTLIERS (VERY IMPORTANT)

Professional Definition

Outlier is an extreme value that differs significantly from other values

Example

Data:

10, 20, 30, 40, 500

Here:

500 is outlier

Why Outlier Important

Because it affects:

Mean

Standard deviation

Outlier Formula (IQR Method)

$$IQR = Q3 - Q1$$

Outlier:

$$Lower = Q1 - 1.5(IQR)$$

$$Upper = Q3 + 1.5(IQR)$$

Example

Q1 = 20

$Q3 = 40$

IQR:

$$40 - 20 = 20$$

Upper:

$$40 + 30 = 70$$

Value above 70 is outlier

Python Outlier Detection

```
import numpy as np  
  
data=[10,20,30,40,500]  
  
Q1=np.percentile(data,25)  
  
Q3=np.percentile(data,75)  
  
IQR=Q3-Q1  
  
upper=Q3+1.5*IQR  
  
print(upper)
```

Data Science Use

Dispersion used in:

EDA

Feature engineering

Machine Learning

Outlier removal

Real Life Example

Fraud detection

Outliers detect fraud transactions

★ Summary Table

Measure Formula

Range Max-Min

Variance $\Sigma(X-\text{mean})^2/N$

SD $\sqrt{\text{Variance}}$

Percentage Value/Total $\times 100$

Percentile Position

IQR Q3-Q1