

# Q2.1 PCA of Yale Face Database

## Importing Libraries

```
In [1]: import numpy as np
from matplotlib.image import imread
import matplotlib.pyplot as plt
import scipy.io
import copy

plt.rcParams['figure.figsize'] = [8,4]
```

## Importing Yale Faces Database from .mat file

scipy.io.loadmat() function imports .mat file as dictionary

```
In [2]: data = scipy.io.loadmat('./Yale_64x64.mat')
print(type(data))

<class 'dict'>
```

## Dictionary to Numpy Array

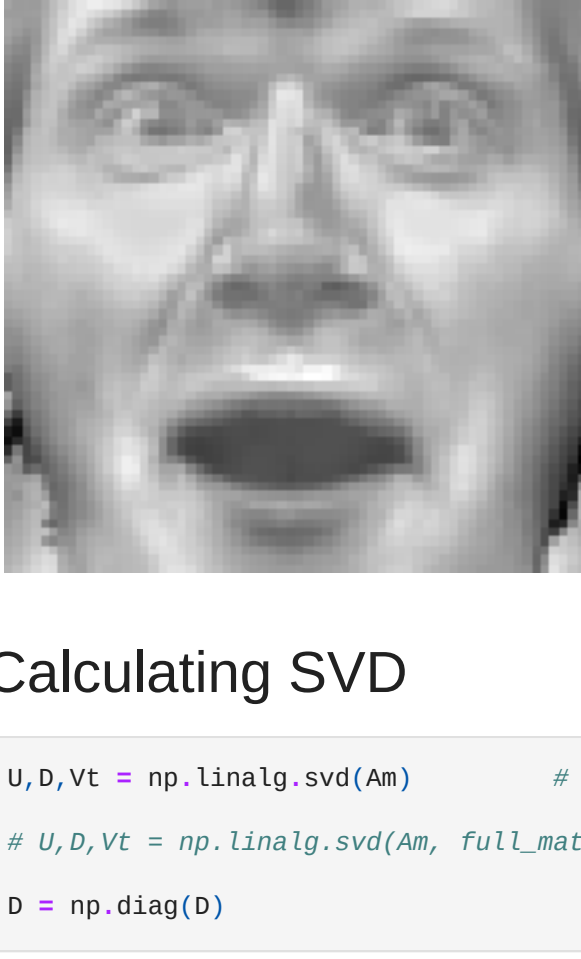
```
In [3]: A = np.array(data['fea']).T
```

```
In [4]: print(A.shape)
```

(4096, 165)

## Sample Image/Face from database

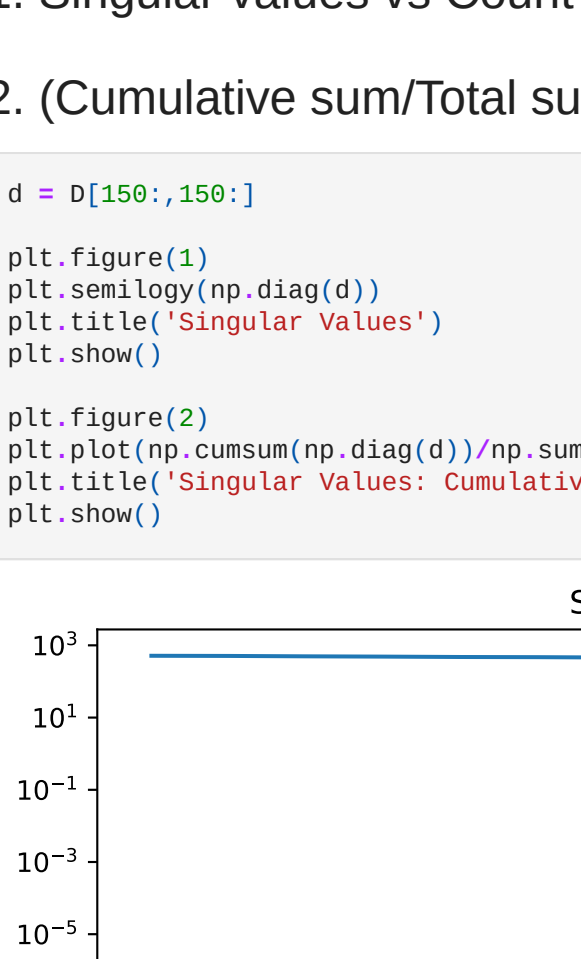
```
In [5]: img = plt.imshow(A[:,1].reshape(64,64).transpose())
img.set_cmap('gray')
plt.axis('off')
plt.show()
```



## Forming Covariance-Matrix

```
In [6]: Amean = A.mean(axis=1, keepdims=True)
Am = A - Amean
```

```
In [7]: img = plt.imshow(Am[:,1].reshape(64,64).transpose())
img.set_cmap('gray')
plt.axis('off')
plt.show()
```



## Calculating SVD

```
In [8]: U,D,Vt = np.linalg.svd(Am) # Complete SVD i.e. calculation corresponding to zero
# U,D,Vt = np.linalg.svd(Am, full_matrices=False) # Economy SVD i.e. Calculations corresponding to non-zero
D = np.diag(D)
```

```
In [9]: print(U.shape, D.shape, Vt.shape)
```

(4096, 4096) (165, 165) (165, 165)

## Finding number of eigen values with least significance

```
In [10]: i = 0
n = len(D)
while(i<n):
    if abs(D[i][1]) < 10:
        break
    i += 1
eig_vals_with_least_significance = n - i
```

```
In [11]: print(eig_vals_with_least_significance)
```

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## Visualizing singular values by plotting graph

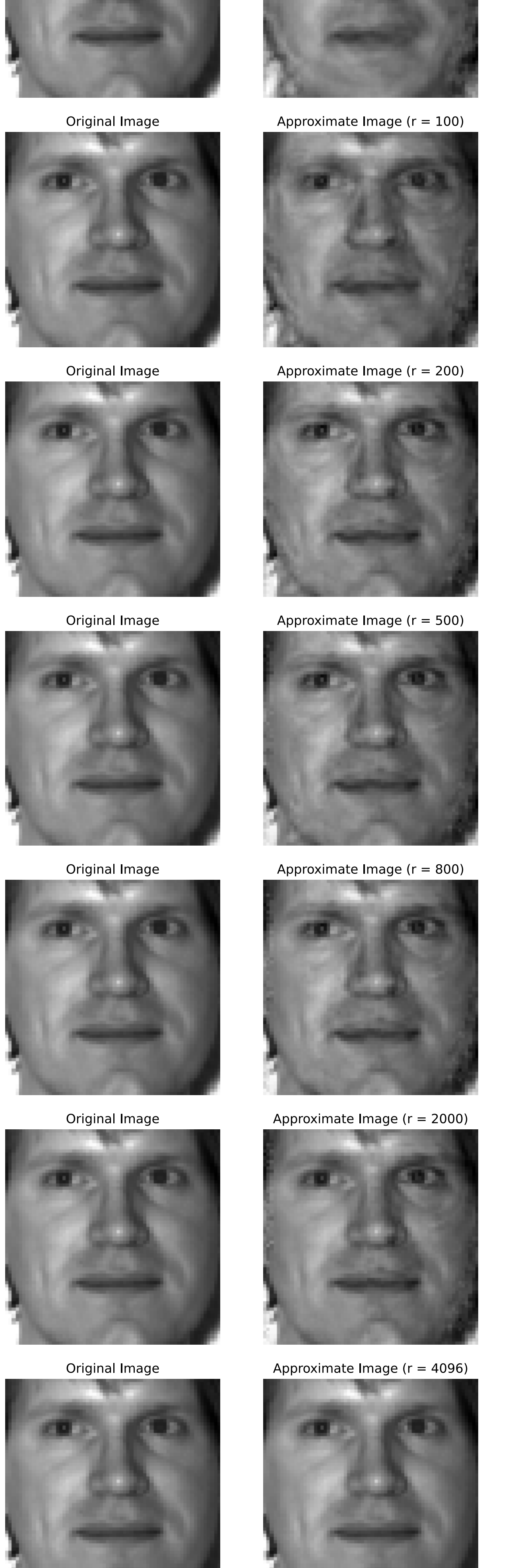
### 1. Singular values vs Count

### 2. (Cumulative sum/Total sum) vs Count

```
In [12]: d = D[150:,150:]

plt.figure(1)
plt.semilogy(np.diag(d))
plt.title('Singular Values')
plt.show()

plt.figure(2)
plt.plot(np.cumsum(np.diag(d))/np.sum(np.diag(d)))
plt.title('Singular Values: Cumulative Sum')
plt.show()
```



## In Sample Projection and Prediction

```
In [13]: sample_size = 150

def InSampleProjectionAndReconstruction(image_number):
    j = 0

    for r in (50, 100, 200, 500, 800, 2000, 4096, 4096-eig_vals_with_least_significance):
        # Construct approximate image
        u = U[:, :r]

        # Projection
        A_train_model = np.matmul(u.T, A[:, :sample_size])

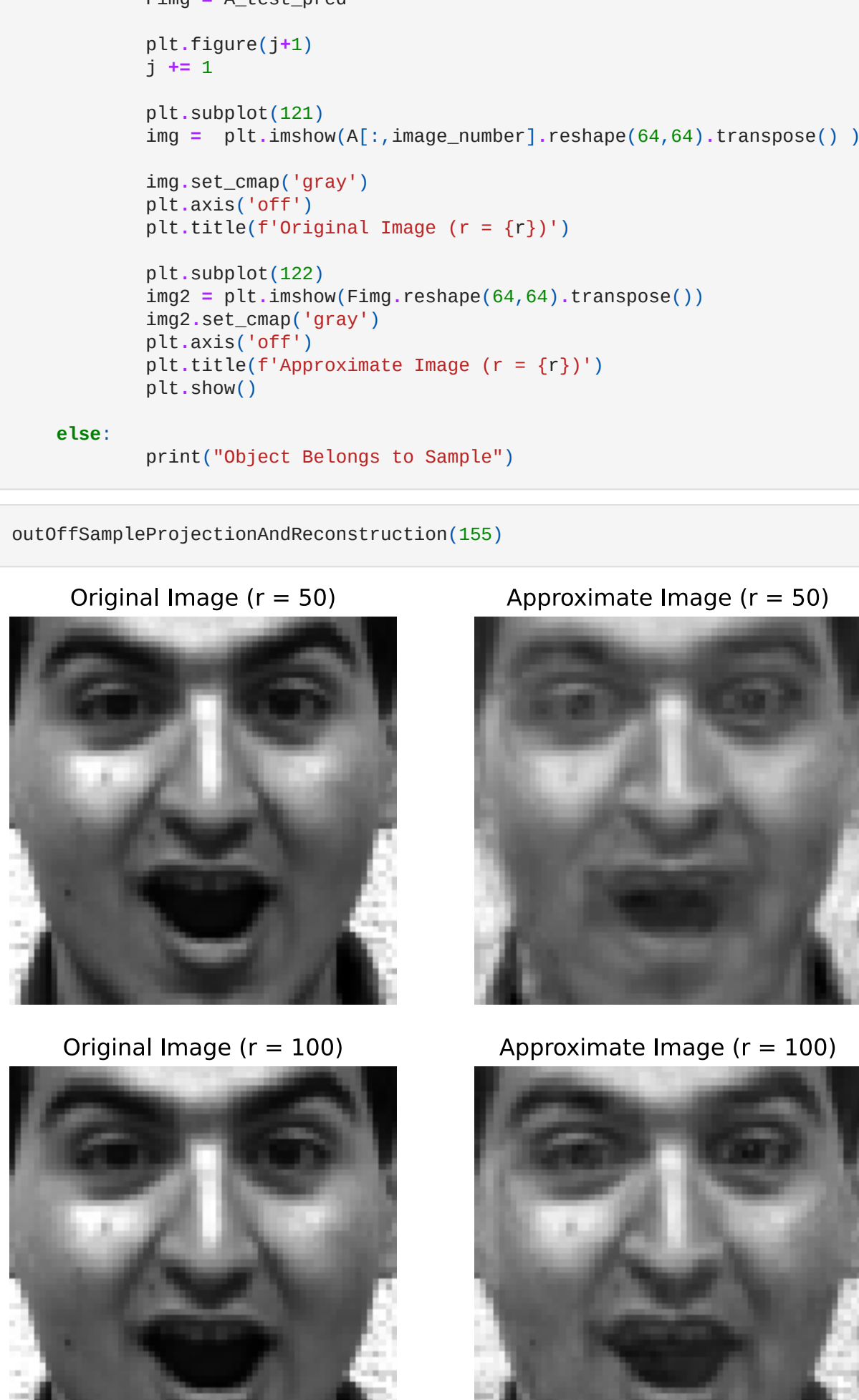
        # Reconstruction
        A_train_pred = np.matmul(u, A_train_model)
        Fimg = A_train_pred

        plt.figure(j+1)
        j += 1

        plot1 = plt.subplot(121)
        img = plt.imshow(A[:, image_number].reshape(64,64).transpose())
        img.set_cmap('gray')
        plt.title(f'Original Image')
        plt.axis('off')

        plot2 = plt.subplot(122)
        img2 = plt.imshow(Fimg[:, image_number].reshape(64,64).transpose())
        img2.set_cmap('gray')
        plt.axis('off')
        plt.title(f'Approximate Image (r = {r})')
        plt.show()
```

```
In [14]: InSampleProjectionAndReconstruction(0)
```



## Out off Sample Projection and Prediction

```
In [15]: def outOffSampleProjectionAndReconstruction(image_number):
    if(image_number>=sample_size):
        j = 0
        for r in (50, 100, 200, 500, 800, 2000, 4096, 4096-eig_vals_with_least_significance):
            # Construct approximate image
            u = U[:, :r]

            # Projection
            A_test_model = np.matmul(u.T, A[:, image_number])

            # Reconstruction
            A_test_pred = np.matmul(u, A_test_model)
            Fimg = A_test_pred

            plt.figure(j+1)
            j += 1

            plt.subplot(121)
            img = plt.imshow(A[:, image_number].reshape(64,64).transpose())
            img.set_cmap('gray')
            plt.axis('off')
            plt.title(f'Original Image (r = {r})')

            plt.subplot(122)
            img2 = plt.imshow(Fimg.reshape(64,64).transpose())
            img2.set_cmap('gray')
            plt.axis('off')
            plt.title(f'Approximate Image (r = {r})')
            plt.show()

        else:
            print("Object Belongs to Sample")
```

```
In [16]: outOffSampleProjectionAndReconstruction(155)
```

