## Name: Gavali Deshabhakt Nagnath

Q1-Answer:

a)

1) For w = 0.9

Solution: Iteration = 31

x1 = 1.299979 x2 = -0.300015 x3 = 4.199998 x4 = 4.200009 x5 = -0.299984 x6 = 1.300015

Roll No.: 202CD005

2) For w = 1.0

Solution: Iteration = 26

x1 = 1.299985 x2 = -0.300011 x3 = 4.199999 x4 = 4.200007 x5 = -0.299989 x6 = 1.300010

3) For w = 1.2

Solution: Iteration = 21

x1 = 1.299997 x2 = -0.300002 x3 = 4.200002 x4 = 4.200001 x5 = -0.300001 x6 = 1.300001

b)

1) Table for w = 0.9

Iteration	×1	×2	x3	×4	x5	x6	Max Error
0	3.0	-0.45	1.3725	2.968875	-0.7728187499999999	0.74564625	3.0
1	2.394556125	-0.8178216187500003	2.9903331121875003	3.5610084209531254	-0.6121122233132812	0.9206279272260935	1.6178331121875003
2	1.5754743294259215	-0.6283957078634135	3.6519525582337766	3.908276743452933	-0.509893446128366	1.1410014031819333	0.8190817955740783
3	1.3426238197998308	-0.4946424679481279	3.9639663457244607	4.0497297187359305	-0.40705276753780156	1.252162418234784	0.3120137874906841
: : : :							
29	1.2999715563278311	-0.3000209872709061	4.199997398227232	4.200012179341543	-0.29997824932567524	1.300020756859582	1.0296520730035397e-05
30	1.2999715563278311	-0.3000209872709061	4.199997398227232	4.200012179341543	-0.29997824932567524	1.300020756859582	1.0296520730035397e-05
31	1.2999791167441952	-0.3000154073417953	4.199998092053442	4.200008943520148	-0.2999840304737136	1.3000152393224271	7.560416364071898e-06

#### 2) Table for w = 1.0

Itera	ation	x1	x2	x3	x4	x5	x6	Max Error
1 1	)	3.333333333333333	-0.33333333333333326	1.5	3.33333333333333	-0.7083333333333333	0.638888888888893	3.333333333333335
	L	2.3981481481481484	-0.8842592592592591	3.3020833333333335	3.8582175925925926	-0.5769675925925926	0.8632330246913581	1.802083333333335
	2	1.3553883744855968	-0.6358185442386832	3.9165943287037033	4.112959747942386	-0.4910521958590537	1.1831824952846366	1.0427597736625516
	: : :							
2	24	1.299977174981797	-0.30001579026567593	4.1999992373789885	4.200010271527113	-0.29998330751026536	1.30001531282352	1.1059001914892619e-05
	25	1.2999846230887133	-0.30001063764792724	4.1999994880449805	4.200006921473459	-0.29998875486275534	1.300010315237439	7.448106916330133e-06
	26	1.2999846230887133	-0.30001063764792724	4.1999994880449805	4.200006921473459	-0.29998875486275534	1.300010315237439	7.448106916330133e-06

## 3) Table for w = 1.2

Iteration	x1	x2	x3	x4	x5	x6	Max Error	
0 1 2	4.0 2.33024000000000003 0.7728357683200004	0.0 -1.1458559999999995 -0.7266123310079997	1.7999999999999998 3.8490144 4.392329371699201	4.08 4.429645440000001 4.3945067469619215	-0.49199999999999999999999999999999999999	0.3744 0.7620641791999997 1.3734654823571453	4.08   2.0490144000000003   1.5574042316799999	
19   20   21	1.3000009044578946 1.2999969678787746 1.2999969678787746	-0.30000435536232173 -0.3000016851830683 -0.3000016851830683	4.200000149399344   4.20000201094376   4.20000201094376	4.200002755408012   4.200000702549945   4.200000702549945	-0.3000016301743165 -0.3000008949482202 -0.3000008949482202	1.2999982679501294 1.3000005622799102 1.3000005622799102	1.1774026023481099e-05     3.936579120011885e-06     3.936579120011885e-06	

# Iteration vs Accuracy 4.0 w = 0.93.5 3.0 2.5 Accuracy 2.0 1.5 1.0 0.5 0.0 10 5 15 20 25 30 0 Iteration

- i) From tables we can see that, for w = 1.0 the number of iterations taken to find solution of given system with desired accuracy are 26 and for w = 1.2 it is just 21.
- ii) As we know that for w = 1.0, the successive iteration method behaves as Gauss Siedel Method.
- iii) Hence in this case, over relaxation gives better accuracy than Gauss Siedel method.

c)

- i) Given Matrix is not diagonally dominant.
- ii) Although the given matrix is not diagonally dominant, the Gauss Siedel and SOR method converge for given matrix.
- ii) As from the output of code it can be seen that, rank(G) is greater than 1. Hence system not being diagonally dominant does not contradict with convergence of Gauss Siedel and SOR method.

#### Matrix G:

G =						
	0.00000000	0.66666667	-0.33333333	0.00000000	0.00000000	-0.33333333
	0.00000000	0.33333333	0.33333333	-0.25000000	0.00000000	-0.16666667
	0.00000000	0.00000000	0.25000000	0.37500000	-0.25000000	0.00000000
	0.00000000	-0.08333333	0.04166667	0.25000000	0.37500000	-0.20833333
	0.00000000	-0.04166667	-0.04166667	0.03125000	0.25000000	0.39583333
	0.00000000	-0.2222222	0.06944444	-0.06250000	0.04166667	0.4444444