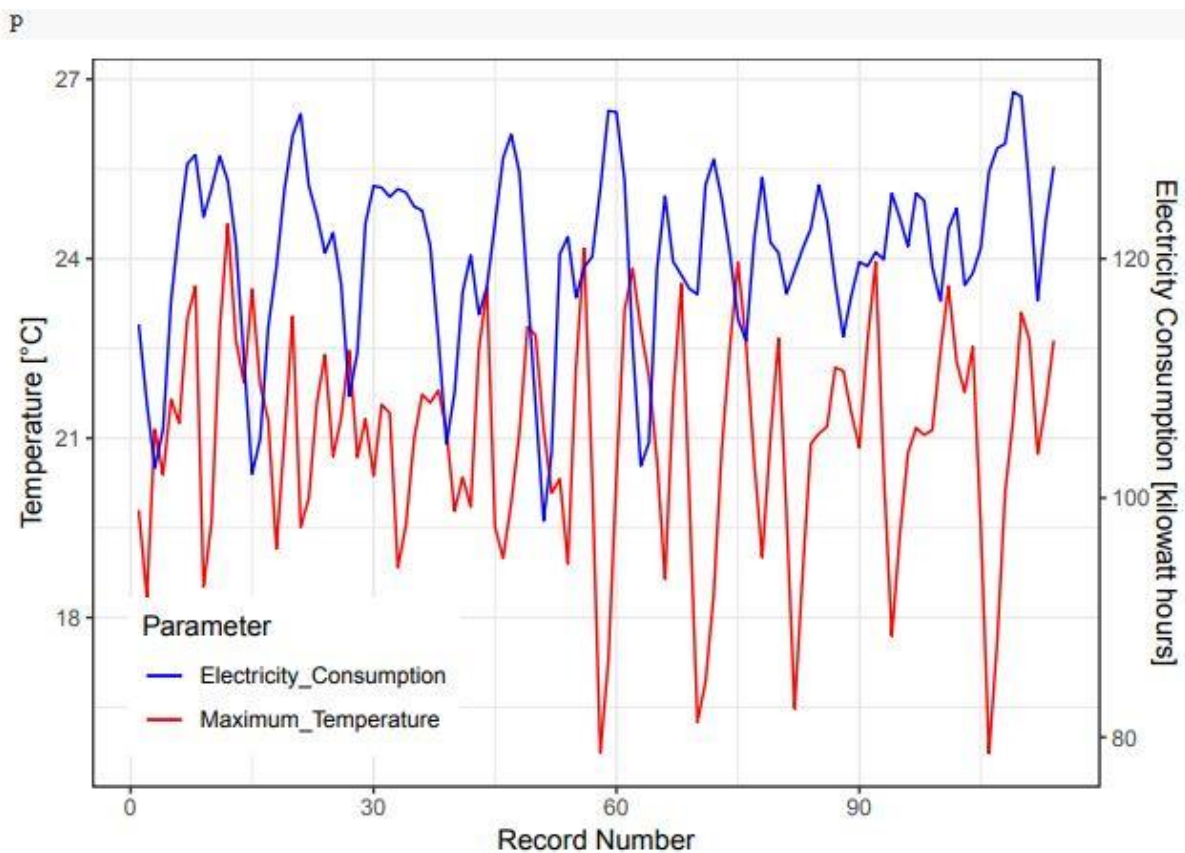


IEE 579

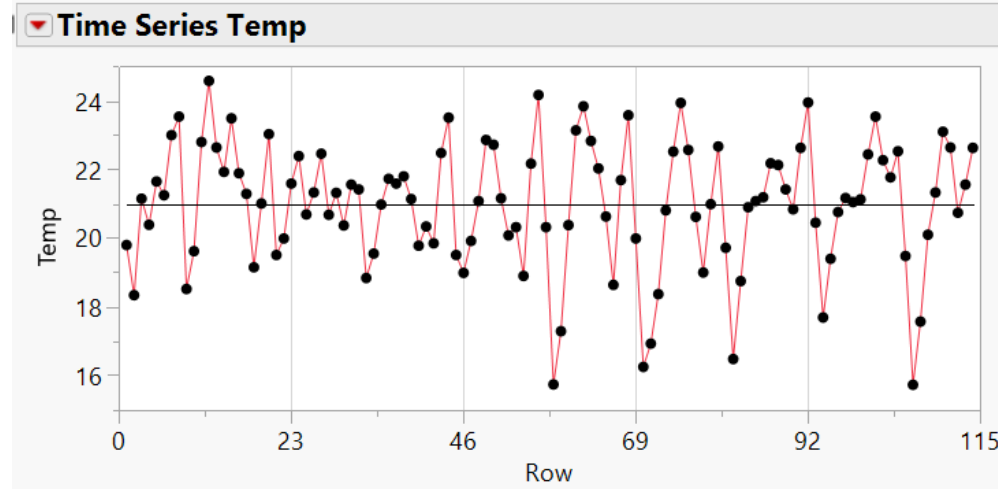
Case Study II

By: Abhishek Deshpande (1213336811)

Problem Description A small city XYZ has been taking record of its monthly electricity consumption (in kilowatt hours) for about 10 years from 1997. Meanwhile, the monthly maximum temperature (in degree C) has also been recorded. The time series plots shown below indicate the varying of electricity consumption as well as temperature from Jan. 1997 to Dec. 2006. The data are included in the csv file (train.csv). A small part of them is shown as below.



Q.1) Use the Holt-Winter forecasting method to build a temperature forecasting model. Choose the best exponential smoothing parameter.

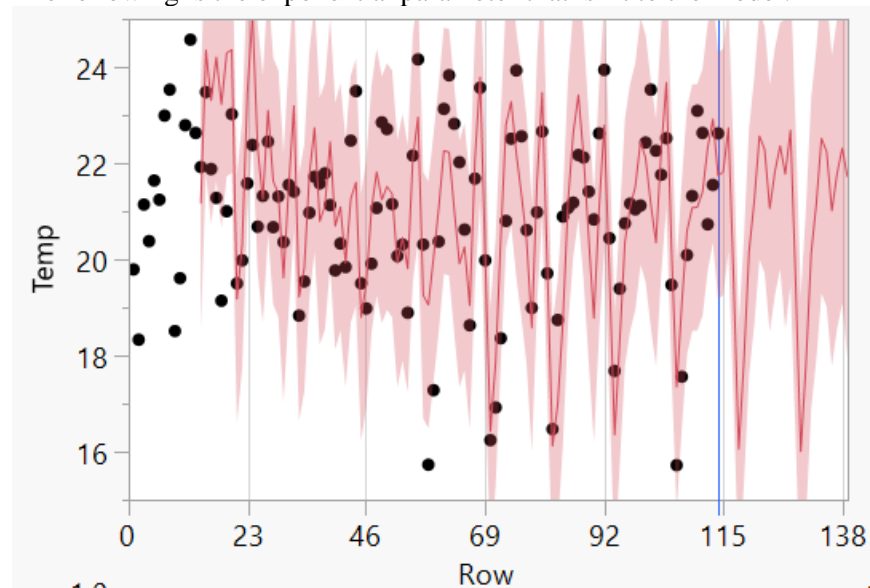


- Model Chosen : Holt-Winters Additive Model
- Reason: Seasonal pattern is approximately constant in time and it is independent of the average.

Holt-Winters Additive Model

$$y_t = L_t + S_t + E_t$$

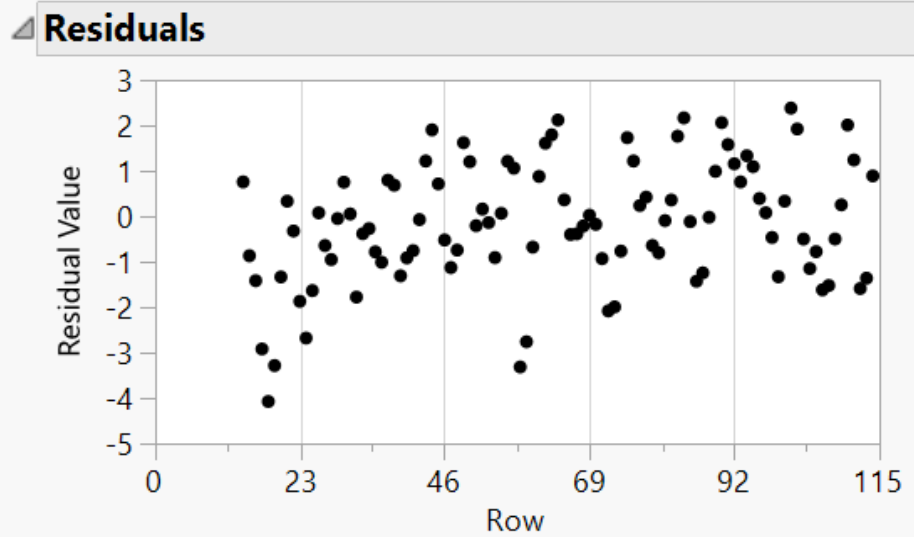
The following is the exponential parameter that is fit to the model.



Parameter Estimates Obtained:

| Parameter Estimates | | | | |
|---------------------------|------------|-----------|---------|---------|
| Term | Estimate | Std Error | t Ratio | Prob> t |
| Level Smoothing Weight | 1.74478e-8 | 1.8354e-7 | 0.10 | 0.9245 |
| Trend Smoothing Weight | 0.00009885 | 0.0012006 | 0.08 | 0.9346 |
| Seasonal Smoothing Weight | 0.76083326 | 0.1390828 | 5.47 | <.0001* |

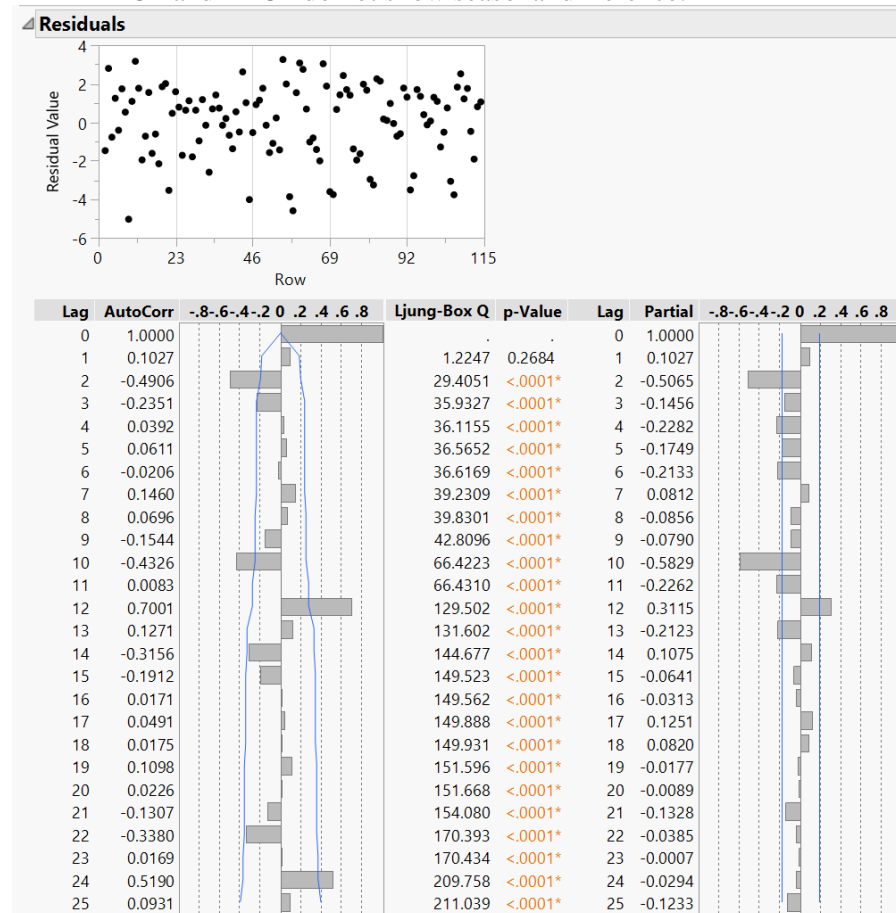
- Seasonal smoothing weight is only the significant estimate here.
- Residual plot supports the statement stated above.



- No unusual pattern observed here. Hence, we can say that the model is adequate.
- We do not need the Level Smoothing and trend smoothing weight. The coefficient for seasonal smoothing is 0.7608 and is the best exponential smoothing parameter.

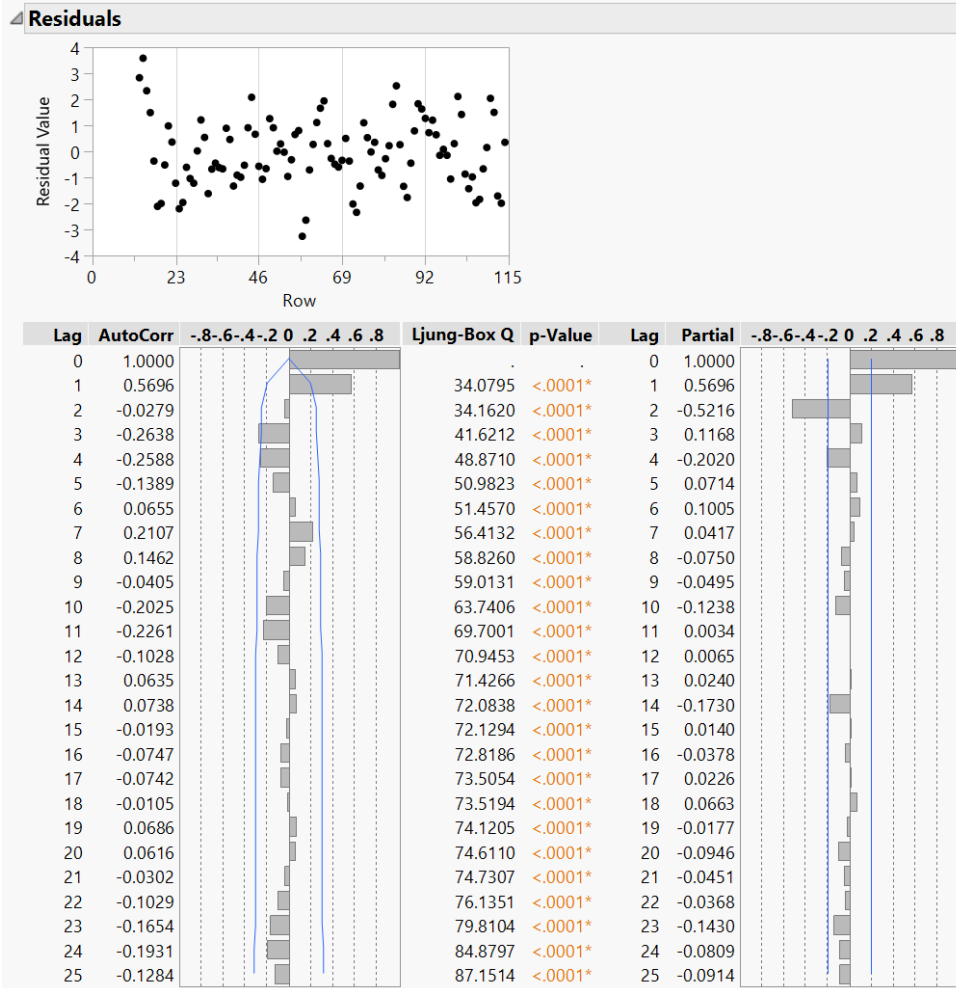
Q.2) Develop a seasonal ARIMA model for temperature. Please clearly describe each step of your model building process. Compare this model with the model you found for Question 1), in terms of some performance statistics including MSE, MAD, and MAPE.

- Fitting ARIMA model to the seasonal data: Take the first difference of the data.
 - I) $d=1$
 - II) $D=1$
 - III) $d=1$ and $D=1$
- Plots And Adequacy Checks
 1. $d=1$
 - Residuals are normal
 - ACF and PACF do not show seasonal difference.



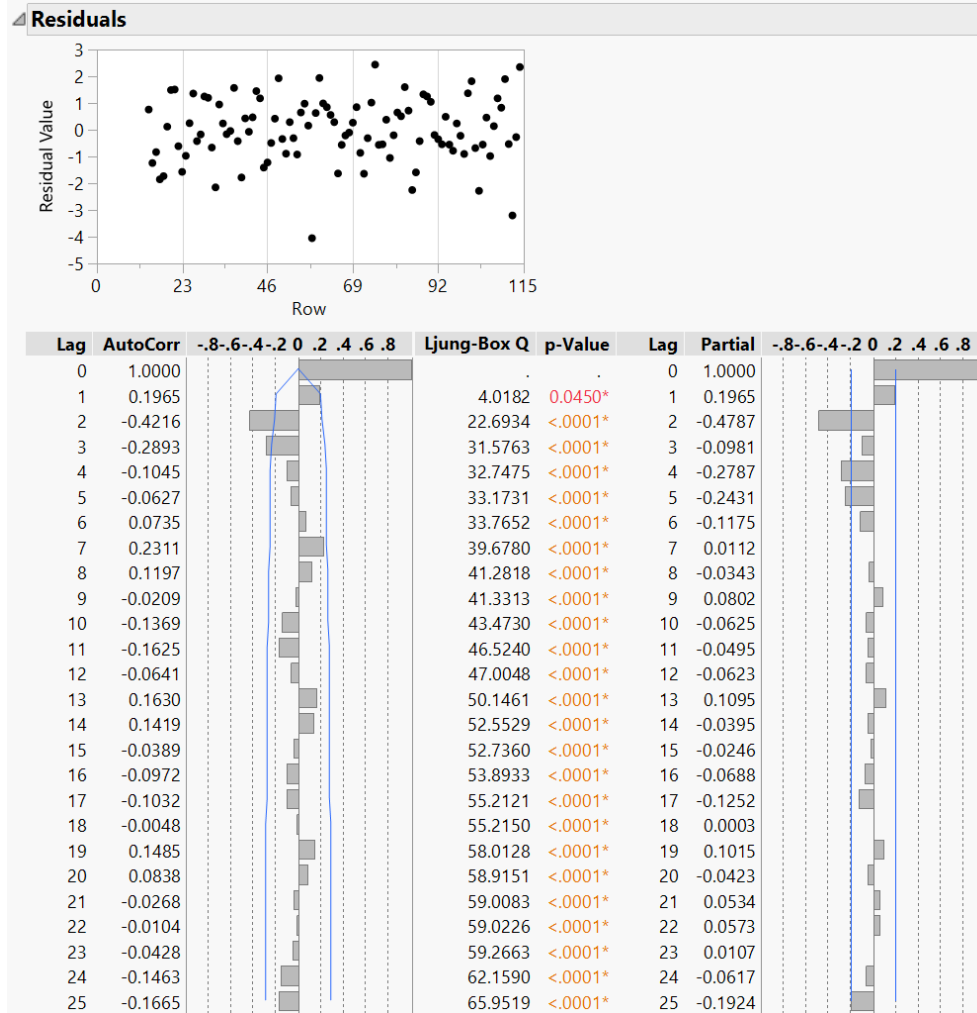
2) D=1

- Residuals do not show any pattern.
- ACF and PACF within limits for the difference term.
- Potential candidate for the ARIMA model.

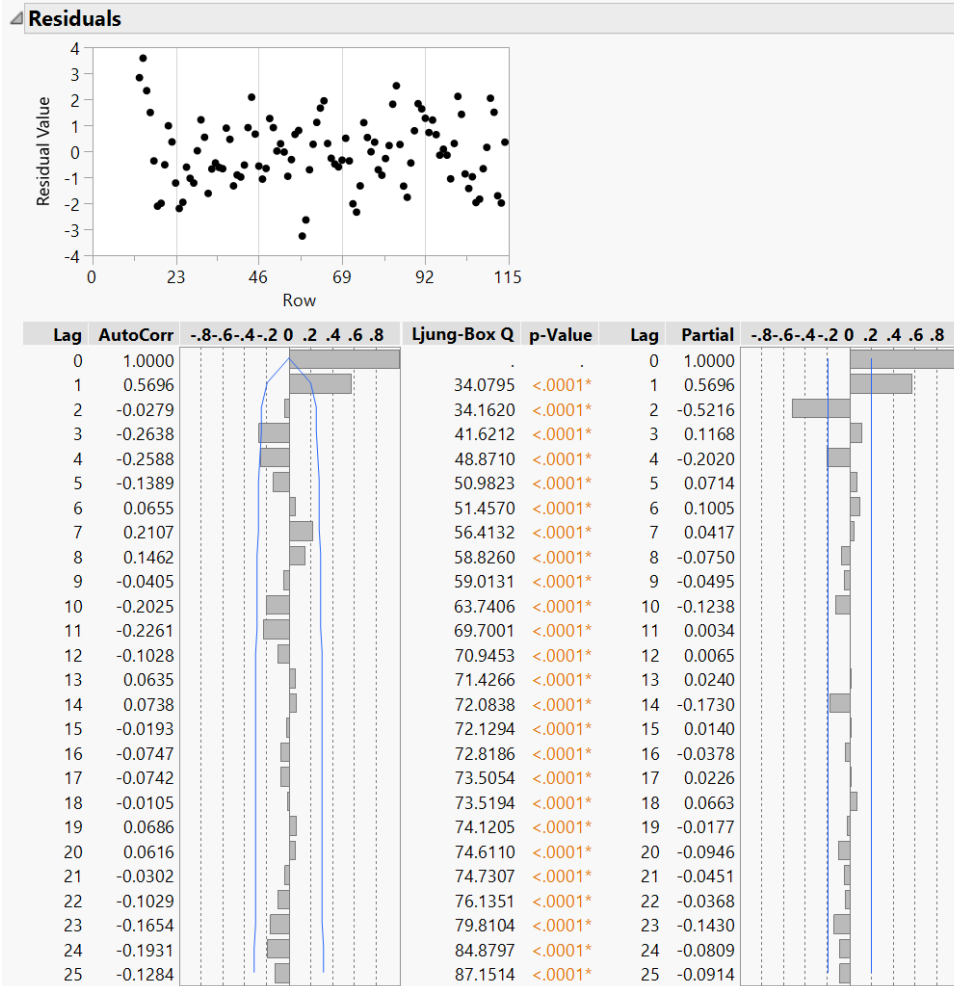


3) $d=1$ and $D=1$

- ACF and PACF within limits.
- But the initial lags have may insignificant values.



- Choose $D=1$
- Why? Because the other models have insignificant values or fail to explain seasonality.



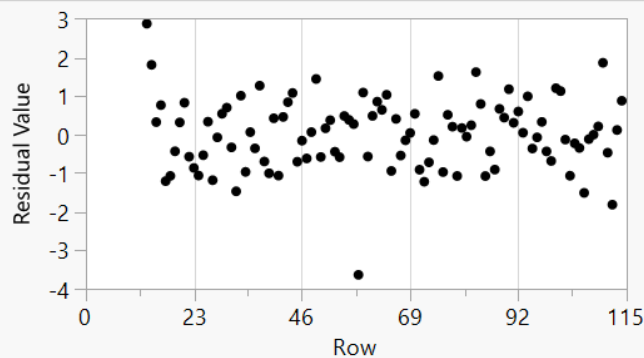
- There are 2 significant lags in PACF
- Hence, we can try AR1 MA2 along with seasonal difference.

Parameter Estimates

| Term | Factor | Lag | Estimate | Std Error | t Ratio | Prob> t | Constant | Mu |
|-----------|--------|-----|-----------|-----------|---------|---------|------------|------------|
| AR1,1 | 1 | 1 | -0.036385 | 0.2159751 | -0.17 | 0.8666 | Estimate | -0.0308922 |
| MA1,1 | 1 | 1 | -1.077503 | 0.1938059 | -5.56 | <.0001* | -0.0320162 | |
| MA1,2 | 1 | 2 | -0.377771 | 0.1766128 | -2.14 | 0.0349* | | |
| Intercept | 1 | 0 | -0.030892 | 0.1993360 | -0.15 | 0.8772 | | |

Forecast

Residuals



| Lag | AutoCorr | -0.8 | -0.6 | -0.4 | -0.2 | 0 | .2 | .4 | .6 | .8 | Ljung-Box Q | p-Value | Lag | Partial | -0.8 | -0.6 | -0.4 | -0.2 | 0 | .2 | .4 | .6 | .8 |
|-----|----------|------|------|------|------|---|----|----|----|----|-------------|---------|-----|---------|------|------|------|------|---|----|----|----|----|
| 0 | 1.0000 | | | | | | | | | | | | 0 | 1.0000 | | | | | | | | | |
| 1 | 0.0186 | | | | | | | | | | 0.0362 | 0.8490 | 1 | 0.0186 | | | | | | | | | |
| 2 | -0.0742 | | | | | | | | | | 0.6210 | 0.7331 | 2 | -0.0746 | | | | | | | | | |
| 3 | -0.1233 | | | | | | | | | | 2.2493 | 0.5223 | 3 | -0.1211 | | | | | | | | | |
| 4 | -0.1312 | | | | | | | | | | 4.1115 | 0.3911 | 4 | -0.1357 | | | | | | | | | |
| 5 | -0.0446 | | | | | | | | | | 4.3295 | 0.5030 | 5 | -0.0643 | | | | | | | | | |
| 6 | -0.0152 | | | | | | | | | | 4.3551 | 0.6287 | 6 | -0.0542 | | | | | | | | | |
| 7 | 0.1993 | | | | | | | | | | 8.7900 | 0.2681 | 7 | 0.1636 | | | | | | | | | |
| 8 | 0.0268 | | | | | | | | | | 8.8712 | 0.3533 | 8 | -0.0066 | | | | | | | | | |
| 9 | -0.0169 | | | | | | | | | | 8.9038 | 0.4462 | 9 | -0.0076 | | | | | | | | | |
| 10 | -0.1327 | | | | | | | | | | 10.9342 | 0.3627 | 10 | -0.1077 | | | | | | | | | |
| 11 | -0.0908 | | | | | | | | | | 11.8958 | 0.3715 | 11 | -0.0548 | | | | | | | | | |
| 12 | -0.1110 | | | | | | | | | | 13.3471 | 0.3443 | 12 | -0.1270 | | | | | | | | | |
| 13 | 0.1127 | | | | | | | | | | 14.8623 | 0.3160 | 13 | 0.0932 | | | | | | | | | |
| 14 | 0.0463 | | | | | | | | | | 15.1202 | 0.3700 | 14 | -0.0513 | | | | | | | | | |
| 15 | -0.0393 | | | | | | | | | | 15.3082 | 0.4295 | 15 | -0.0811 | | | | | | | | | |
| 16 | -0.0124 | | | | | | | | | | 15.3271 | 0.5008 | 16 | -0.0398 | | | | | | | | | |
| 17 | -0.0437 | | | | | | | | | | 15.5650 | 0.5549 | 17 | -0.0085 | | | | | | | | | |
| 18 | -0.0405 | | | | | | | | | | 15.7723 | 0.6084 | 18 | -0.0431 | | | | | | | | | |
| 19 | 0.0613 | | | | | | | | | | 16.2527 | 0.6404 | 19 | 0.0967 | | | | | | | | | |
| 20 | 0.0565 | | | | | | | | | | 16.6662 | 0.6745 | 20 | -0.0158 | | | | | | | | | |
| 21 | -0.0585 | | | | | | | | | | 17.1138 | 0.7042 | 21 | -0.0962 | | | | | | | | | |
| 22 | 0.0065 | | | | | | | | | | 17.1193 | 0.7567 | 22 | -0.0016 | | | | | | | | | |
| 23 | -0.1116 | | | | | | | | | | 18.7915 | 0.7133 | 23 | -0.1099 | | | | | | | | | |
| 24 | 0.0222 | | | | | | | | | | 18.8584 | 0.7595 | 24 | 0.0175 | | | | | | | | | |
| 25 | -0.2282 | | | | | | | | | | 26.0355 | 0.4057 | 25 | -0.2697 | | | | | | | | | |

- As we can see that, there are no significant lags we cannot proceed with this model.
- We try fitting ARIMA model with the help of R software's optimal ARIMA.
- Obtained model was $(2,0,1) \times (0,1,1)_{12}$

| Parameter Estimates | | | | | | |
|---------------------|--------|-----|------------|-----------|---------|---------|
| Term | Factor | Lag | Estimate | Std Error | t Ratio | Prob> t |
| AR1,1 | 1 | 1 | 0.6383751 | 0.1631358 | 3.91 | 0.0002* |
| AR1,2 | 1 | 2 | -0.4142309 | 0.1365723 | -3.03 | 0.0031* |
| MA1,1 | 1 | 1 | -0.3819288 | 0.1769813 | -2.16 | 0.0334* |
| MA2,12 | 2 | 12 | 0.1795443 | 0.1043152 | 1.72 | 0.0884 |

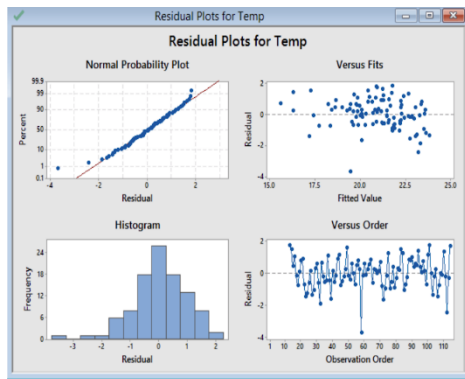
- Parameter estimates show that the MA2,12 term is not significant.
- Thus, this model is discarded.
- Now trying to fit a seasonal ARIMA of order $(2,0,1) \times (0,1,0)_{12}$

| Parameter Estimates | | | | | | |
|---------------------|--------|-----|------------|-----------|---------|---------|
| Term | Factor | Lag | Estimate | Std Error | t Ratio | Prob> t |
| AR1,1 | 1 | 1 | 0.6246971 | 0.1625715 | 3.84 | 0.0002* |
| AR1,2 | 1 | 2 | -0.3922484 | 0.1379396 | -2.84 | 0.0054* |
| MA1,1 | 1 | 1 | -0.4022916 | 0.1713703 | -2.35 | 0.0209* |

- All parameters are significant.

- Residuals**

| Lag | AutoCorr | - .8 -.6 -.4 -.2 0 .2 .4 .6 .8 | Ljung-Box Q | p-Value | Lag | Partial | - .8 -.6 -.4 -.2 0 .2 .4 .6 .8 |
|-----|----------|--------------------------------|-------------|---------|-----|---------|--------------------------------|
| 0 | 1.0000 | [Bar chart] | . | . | 0 | 1.0000 | [Bar chart] |
| 1 | 0.0200 | [Bar chart] | 0.0418 | 0.8379 | 1 | 0.0200 | [Bar chart] |
| 2 | -0.0217 | [Bar chart] | 0.0918 | 0.9552 | 2 | -0.0221 | [Bar chart] |
| 3 | 0.0132 | [Bar chart] | 0.1105 | 0.9905 | 3 | 0.0141 | [Bar chart] |
| 4 | -0.0496 | [Bar chart] | 0.3772 | 0.9843 | 4 | -0.0507 | [Bar chart] |
| 5 | -0.0755 | [Bar chart] | 1.0002 | 0.9625 | 5 | -0.0730 | [Bar chart] |
| 6 | -0.0370 | [Bar chart] | 1.1518 | 0.9792 | 6 | -0.0369 | [Bar chart] |
| 7 | 0.1496 | [Bar chart] | 3.6499 | 0.8191 | 7 | 0.1504 | [Bar chart] |
| 8 | -0.0166 | [Bar chart] | 3.6811 | 0.8847 | 8 | -0.0249 | [Bar chart] |
| 9 | -0.0354 | [Bar chart] | 3.8236 | 0.9226 | 9 | -0.0364 | [Bar chart] |
| 10 | -0.0999 | [Bar chart] | 4.9733 | 0.8930 | 10 | -0.1170 | [Bar chart] |
| 11 | -0.0664 | [Bar chart] | 5.4875 | 0.9053 | 11 | -0.0547 | [Bar chart] |
| 12 | -0.1438 | [Bar chart] | 7.9247 | 0.7910 | 12 | -0.1312 | [Bar chart] |
| 13 | 0.0779 | [Bar chart] | 8.6487 | 0.7989 | 13 | 0.0961 | [Bar chart] |
| 14 | 0.0122 | [Bar chart] | 8.6665 | 0.8518 | 14 | -0.0354 | [Bar chart] |
| 15 | -0.0481 | [Bar chart] | 8.9488 | 0.8802 | 15 | -0.0588 | [Bar chart] |
| 16 | 0.0064 | [Bar chart] | 8.9538 | 0.9153 | 16 | -0.0233 | [Bar chart] |
| 17 | -0.0329 | [Bar chart] | 9.0893 | 0.9374 | 17 | -0.0210 | [Bar chart] |
| 18 | -0.0445 | [Bar chart] | 9.3391 | 0.9514 | 18 | -0.0356 | [Bar chart] |
| 19 | 0.0431 | [Bar chart] | 9.5768 | 0.9626 | 19 | 0.0833 | [Bar chart] |
| 20 | 0.0392 | [Bar chart] | 9.7754 | 0.9721 | 20 | -0.0208 | [Bar chart] |
| 21 | -0.0895 | [Bar chart] | 10.8248 | 0.9661 | 21 | -0.1214 | [Bar chart] |
| 22 | -0.0072 | [Bar chart] | 10.8318 | 0.9771 | 22 | -0.0325 | [Bar chart] |
| 23 | -0.0882 | [Bar chart] | 11.8773 | 0.9723 | 23 | -0.1023 | [Bar chart] |
| 24 | 0.0275 | [Bar chart] | 11.9803 | 0.9801 | 24 | 0.0369 | [Bar chart] |
| 25 | -0.2498 | [Bar chart] | 20.5800 | 0.7158 | 25 | -0.2631 | [Bar chart] |



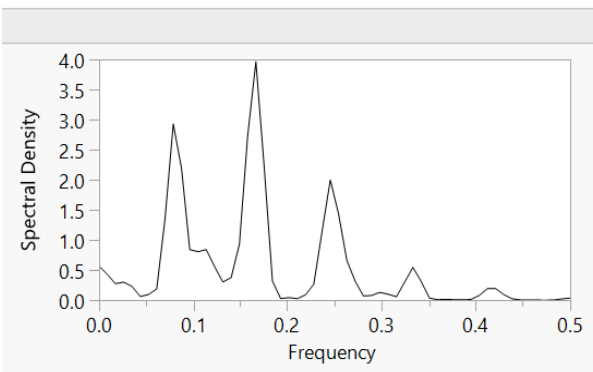
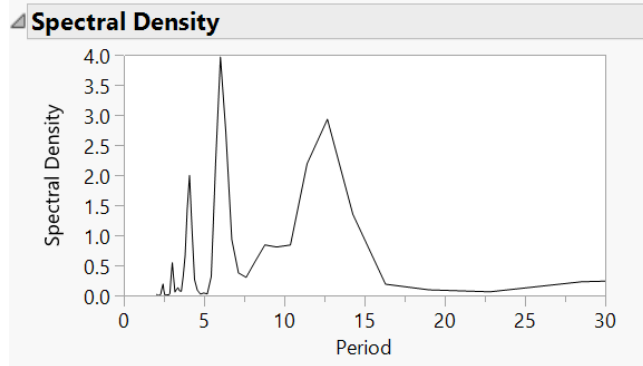
- Residual plots show normal probability plot which looks linear, residual vs. fits is scattered, histogram shows normal curve and residual vs. observation order shows observations around mean almost equidistant.
- Comparison of Winters vs. ARIMA model

| | WINTERS | ARIMA |
|------|---------|-------|
| MAD | 1.056 | 0.70 |
| MAPE | 5.09 | 3.43 |
| MSE | 181.40 | 0.81 |

- As the MAD, MAPE and MSE of ARIMA is lesser than winters method, ARIMA model is the better of the two models.

Q.3) Perform a spectral analysis of the temperature process to identify the significant frequency and make explanation.

- The important frequencies are listed as follows:
- 1st spikes obtained is in the period of 0.08 ~ 12 months
- 2nd spikes is at frequency of 0.16 ~ 24 months



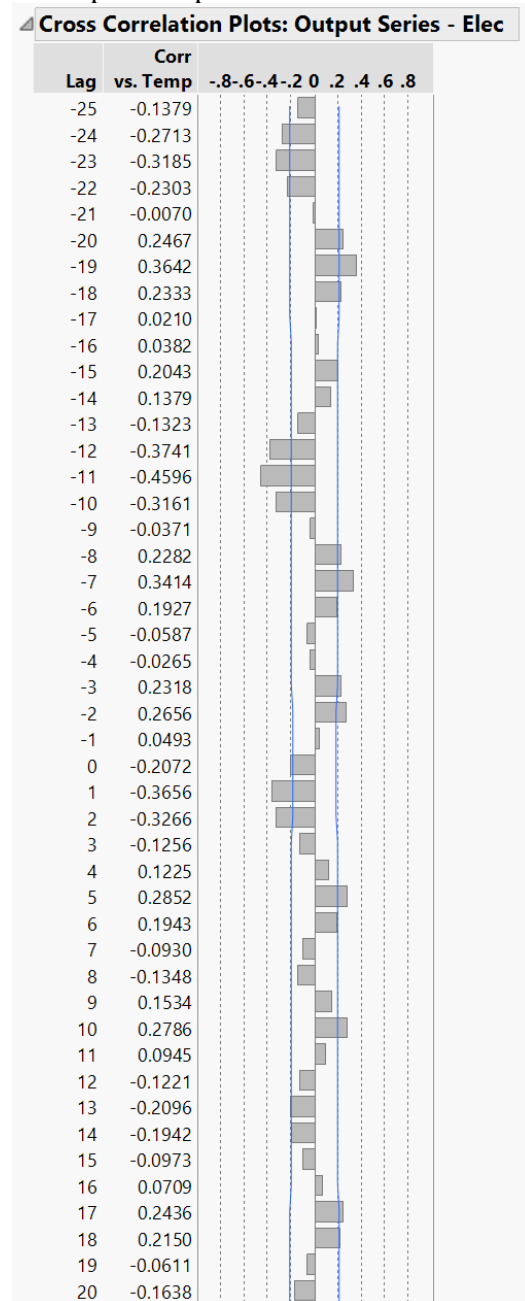
White Noise test

| | |
|-------------------------------|-----------|
| Fisher's Kappa | 11.752839 |
| Prob > Kappa | 0.0001323 |
| Bartlett's Kolmogorov-Smirnov | 0.3899686 |

- Thus, we can say that Periodicity in the data with period = 12 months.

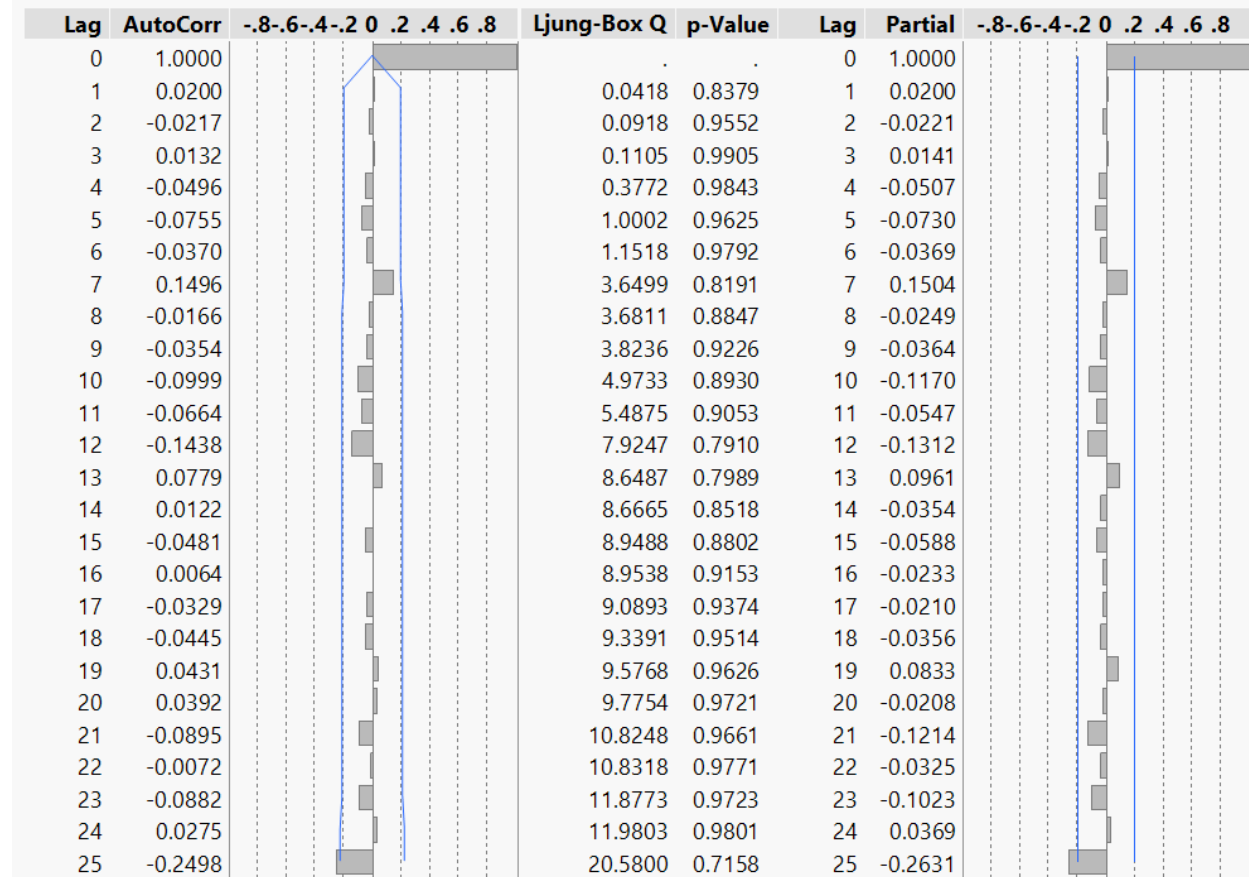
Q.4) Develop a transfer function model to illustrate the change of electricity consumption with its relation to the exogenous variable – temperature. You may choose any temperature model developed for Question 1), 2) or 3). Please clearly describe each step of your model building process. Remember to show your model adequacy checks.

- Check cross correlation of Electricity and temperature.:
It indicates that there is autocorrelation between electricity and temperature.
- Perform Pre-whitening in order to remove the auto correlation; this helps in finding the possible impulse response function.

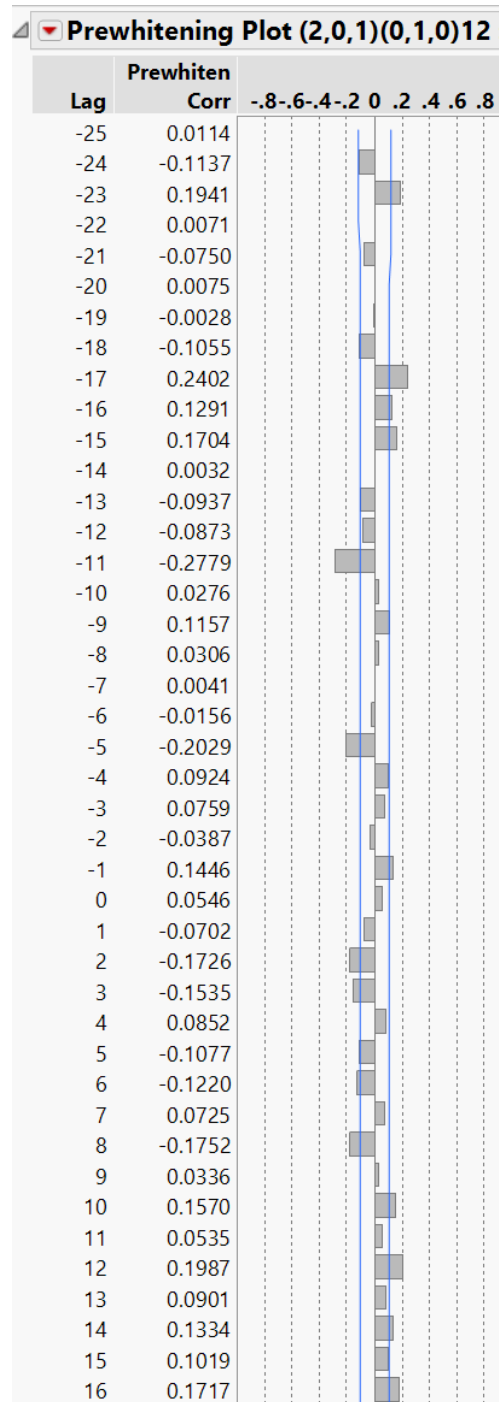


- Selecting ARIMA model of question 2 of order $(2,0,1) \times (0,1,0)_{12}$ for the temperature data to find out the possible impulse response function.

The following is the ACF and PACF of temp using the above ARIMA model.



- As there are no significant lags, we use the above model to pre-white the temp variable.
- Following shows the prewhitening plot for the chosen ARIMA model.



From the above plot, following are the possible impulse response functions:
 $b = 2, r = 1, s = 1$

Comparison of impulse response function:

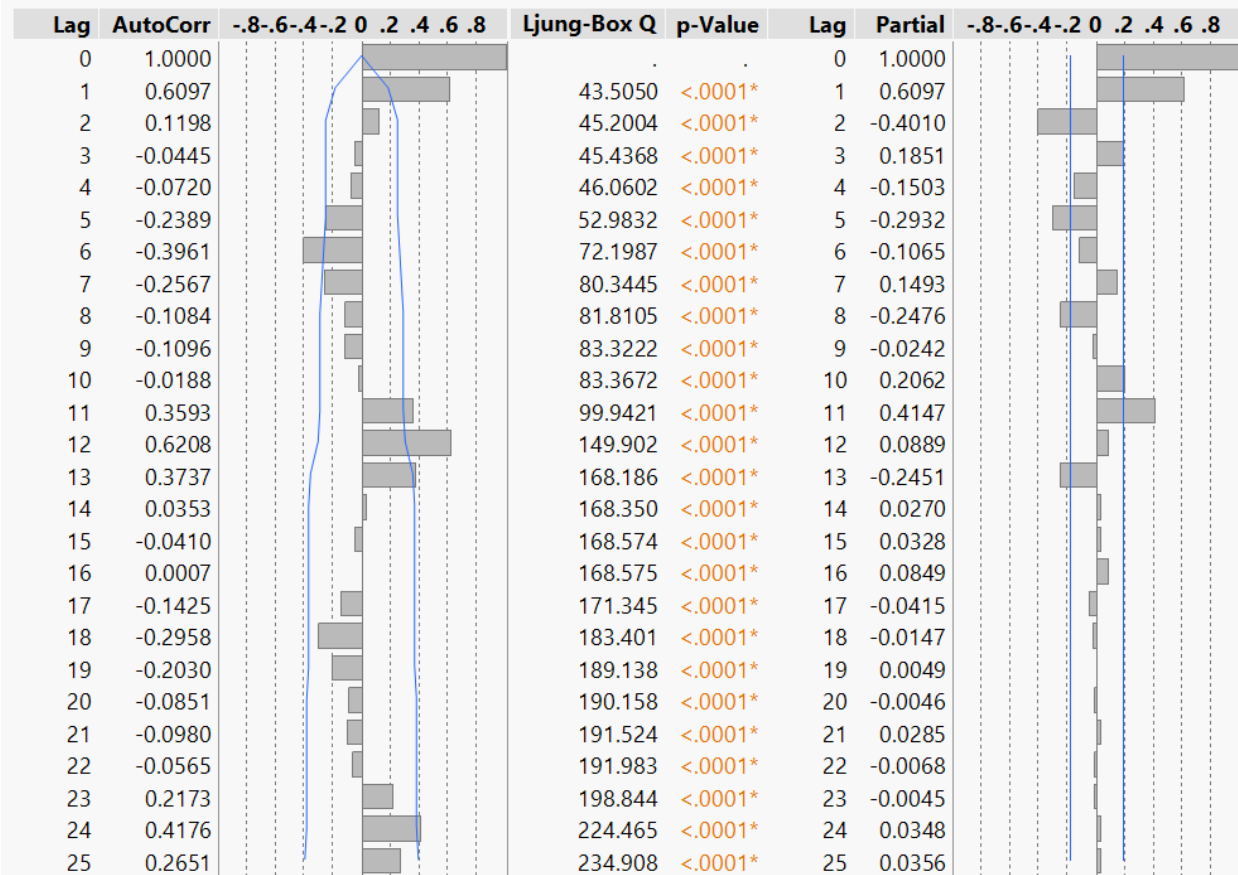
1) $b = 2, r = 1, s = 1$

| Model Summary | | | | | | | |
|------------------------------------|--|--|--|------------|--|--|--|
| DF | | | | 107 | | | |
| Sum of Squared Errors | | | | 4843.74737 | | | |
| Variance Estimate | | | | 45.2686664 | | | |
| Standard Deviation | | | | 6.72819934 | | | |
| Akaike's 'A' Information Criterion | | | | 742.130779 | | | |
| Schwarz's Bayesian Criterion | | | | 752.9689 | | | |
| RSquare | | | | 0.22439723 | | | |
| RSquare Adj | | | | 0.20324443 | | | |
| MAPE | | | | 4.07791606 | | | |
| MAE | | | | 4.79979714 | | | |
| -2LogLikelihood | | | | 734.13078 | | | |

| Parameter Estimates | | | | | | | |
|---------------------|-----------|--------|-----|----------|-----------|---------|---------|
| Variable | Term | Factor | Lag | Estimate | Std Error | t Ratio | Prob> t |
| Temp | Num0,0 | 0 | 0 | -1.3865 | 0.328937 | -4.22 | <.0001* |
| Temp | Num1,1 | 1 | 1 | -1.4306 | 0.318899 | -4.49 | <.0001* |
| Temp | Den1,1 | 1 | 1 | 0.7532 | 0.120491 | 6.25 | <.0001* |
| | Intercept | 0 | 0 | 117.0371 | 6.397970 | 18.29 | <.0001* |

$$\text{Elec}_t = 117.0371 + \left(\frac{(-1.3865 + 1.4306 \cdot B)}{(1 - 0.7532 \cdot B)} \right) \cdot \text{Temp}_{t-2} + e_t$$

- Clearly, the first model $b = 2, r = 1, s = 1$ is the best because of the best parameters obtained.
- We will need to check adequacy for this model or else we will have to consider second model.
- Fitting the noise term for $b = 2, r = 1, s = 1$.
- ACF and PACF of response function:



- Trying Seasonal ARIMA (2,1,1)x(1,1,0)12 here (p=2 q=1 d=1, P=1 Q=0 D=1),
- All the parameters that are obtained are significant.
- Ignoring the insignificant intercept term.

Model Summary

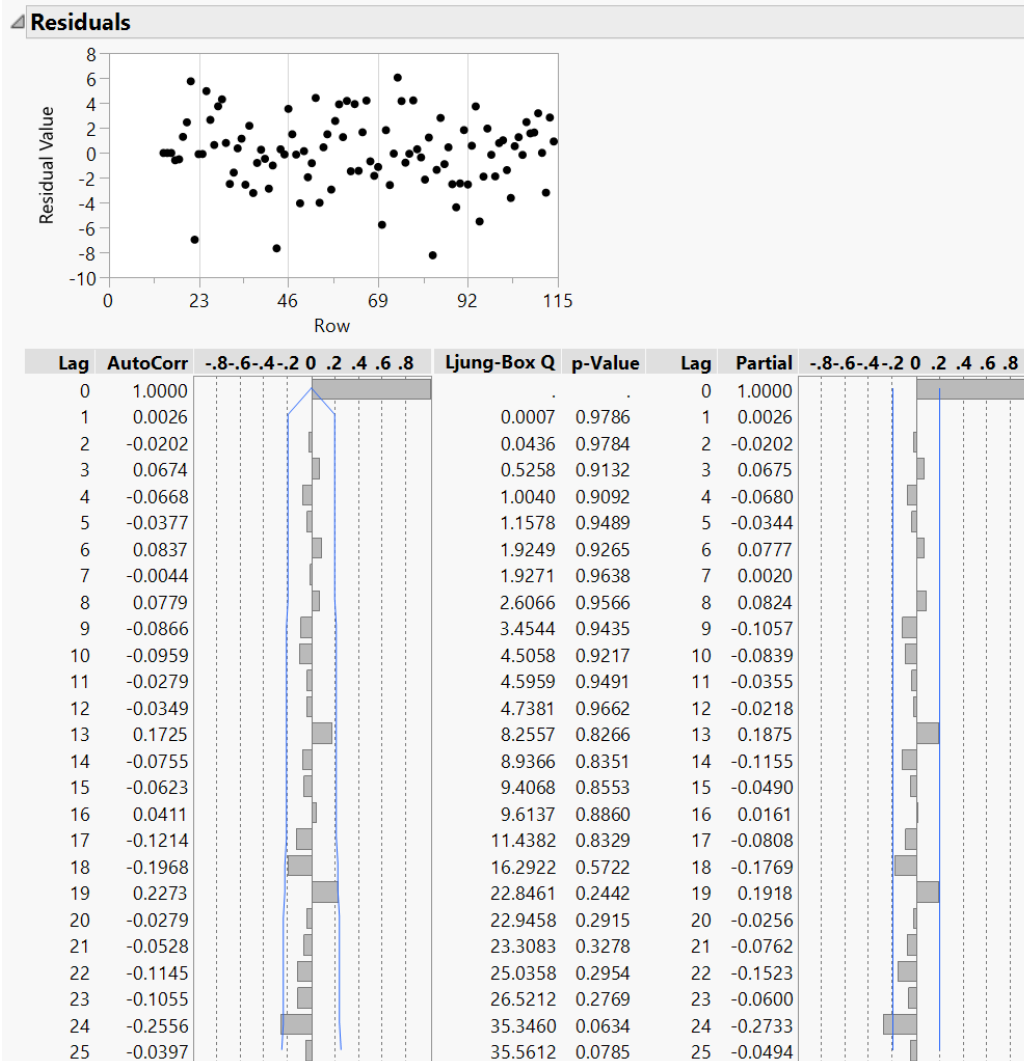
| | |
|------------------------------------|------------|
| DF | 90 |
| Sum of Squared Errors | 780.494935 |
| Variance Estimate | 8.67211342 |
| Standard Deviation | 2.94484523 |
| Akaike's 'A' Information Criterion | 503.120047 |
| Schwarz's Bayesian Criterion | 523.799787 |
| RSquare | 0.43730574 |
| RSquare Adj | 0.39495241 |
| MAPE | 1.61009529 |
| MAE | 1.93621525 |
| -2LogLikelihood | 487.120047 |

Parameter Estimates

| Variable | Term | Factor | Lag | Estimate | Std Error | t Ratio | Prob> t |
|-----------|--------|--------|-----|-----------|-----------|---------|---------|
| Temp | Num0,0 | 0 | 0 | -0.135726 | 0.0134464 | -10.09 | <.0001* |
| Temp | Num1,1 | 1 | 1 | -0.136886 | 0.0135261 | -10.12 | <.0001* |
| Temp | Den1,1 | 1 | 1 | 0.952139 | 0.0995505 | 9.56 | <.0001* |
| Elec | AR1,1 | 1 | 1 | 1.002047 | 0.0848539 | 11.81 | <.0001* |
| Elec | AR1,2 | 1 | 2 | -0.526135 | 0.0855363 | -6.15 | <.0001* |
| Elec | AR2,12 | 2 | 12 | -0.244629 | 0.1078992 | -2.27 | 0.0258* |
| Elec | MA1,1 | 1 | 1 | 1.000000 | 0.0314689 | 31.78 | <.0001* |
| Intercept | | 0 | 0 | -0.424804 | 0.6036267 | -0.70 | 0.4834 |

$$(1-B) \cdot (1-B^{-12}) \cdot \text{Elec}_t = -0.4248 + \left(\frac{(-0.1357 + 0.1369 \cdot B)}{(1 - 0.9521 \cdot B)} \right) \cdot \text{Temp}_{t-2} + \left(\frac{(1-B)}{\left(\left((1 - 1.002 \cdot B) + 0.5261 \cdot B^2 \right) \cdot (1 + 0.2446 \cdot B^{12}) \right)} \right) \cdot e_t$$

- Checking Model Adequacy:
- No specific pattern observed in the residual plot.
- ACF and PACF plots are within the limits. Hence, the model is adequate.



We fit another noise term for the same $b = 2$, $r = 1$ and $s = 1$. That is $(1,0,0)(0,1,0)_{12}$

Model Summary

| | |
|------------------------------------|------------|
| DF | 94 |
| Sum of Squared Errors | 1117.98221 |
| Variance Estimate | 11.8934267 |
| Standard Deviation | 3.44868478 |
| Akaike's 'A' Information Criterion | 531.493429 |
| Schwarz's Bayesian Criterion | 544.469028 |
| RSquare | 0.49334146 |
| RSquare Adj | 0.47244832 |
| MAPE | 2.90178971 |
| MAE | 3.43170048 |
| -2LogLikelihood | 521.493429 |

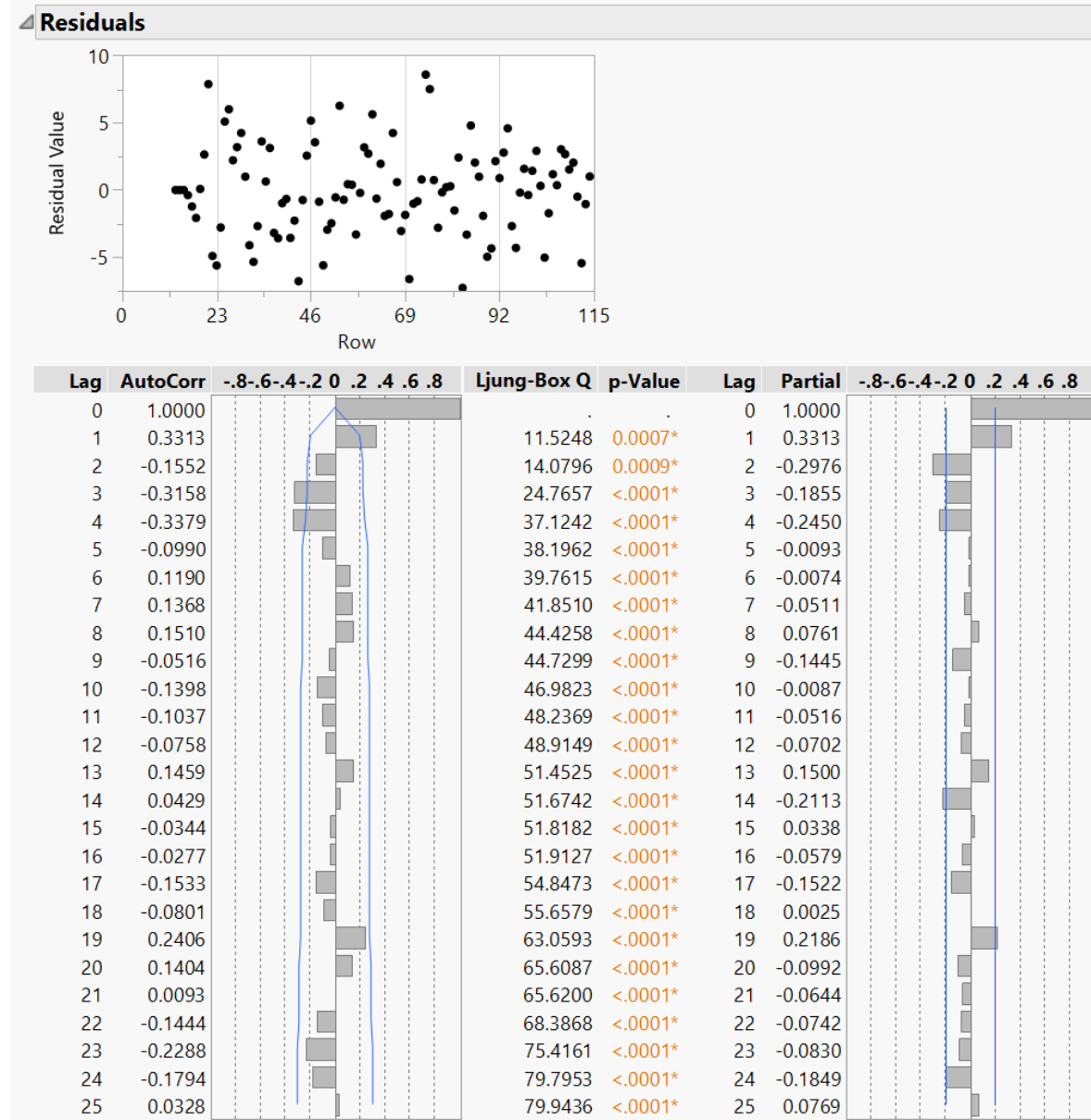
Parameter Estimates

| Variable | Term | Factor | Lag | Estimate | Std Error | t Ratio | Prob> t |
|----------|-----------|--------|-----|-----------|-----------|---------|---------|
| Temp | Num0,0 | 0 | 0 | -0.214952 | 0.001254 | -171.5 | <.0001* |
| Temp | Num1,1 | 1 | 1 | -0.214073 | 0.001247 | -171.6 | <.0001* |
| Temp | Den1,1 | 1 | 1 | 1.066609 | 0.091855 | 11.61 | <.0001* |
| Elec | AR1,1 | 1 | 1 | 0.651167 | 0.074921 | 8.69 | <.0001* |
| | Intercept | 0 | 0 | -0.444996 | 1.422598 | -0.31 | 0.7551 |

$$\left(1 - B^{12}\right) \cdot \text{Elec}_t = -0.445 + \left(\frac{\left(-0.215 + 0.2141 \cdot B \right)}{\left(1 - 1.0666 \cdot B \right)} \right) \cdot \text{Temp}_{t-2} + \left(\frac{1}{\left(1 - 0.6512 \cdot B \right)} \right) \cdot e_t$$

- The estimated parameters are significant as can be seen from above.

- But, the ACF and PACF show that initial lags are not within limits.



So, comparing $b = 2, r = 1$ and $s = 1 (1,0,0)(0,1,0)_{12}$ and $b = 2, r = 1$ and $s = 1 (2,1,1)(1,1,0)_{12}$. We find the later to be a better model because it has a lower AIC, BIC, MAPE and MAE.

Q.5) Forecast the future streamflow of both monthly maximum temperature and electricity consumption for the next 6 months after Jun. 2006.

i) Using R to fit the ARIMA model for the temperature time series we get, Temp (2,0,1)x(0,1,1)₁₂

```
1 library(forecast)
2 electricity <- read.csv("C:/Users/User/Desktop/520 project/elec.csv",header=TRUE)
3 Temperature <- read.csv("C:/Users/User/Desktop/520 project/Temp.csv",header=TRUE)
4 x1<- ts(Temperature,frequency = 12)
5 plot.ts(x1)
6
7 model_fit<-auto.arima(x1, seasonal =TRUE, ic = 'aic')
8 print(model_fit)
9 forecast(model_fit,6)
10
```

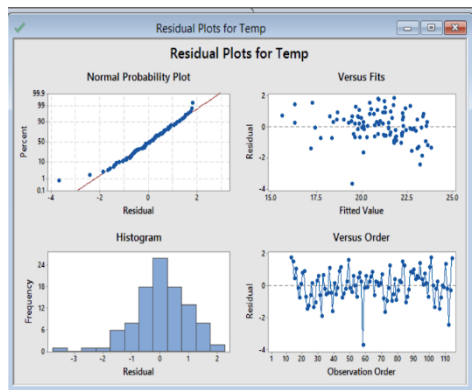
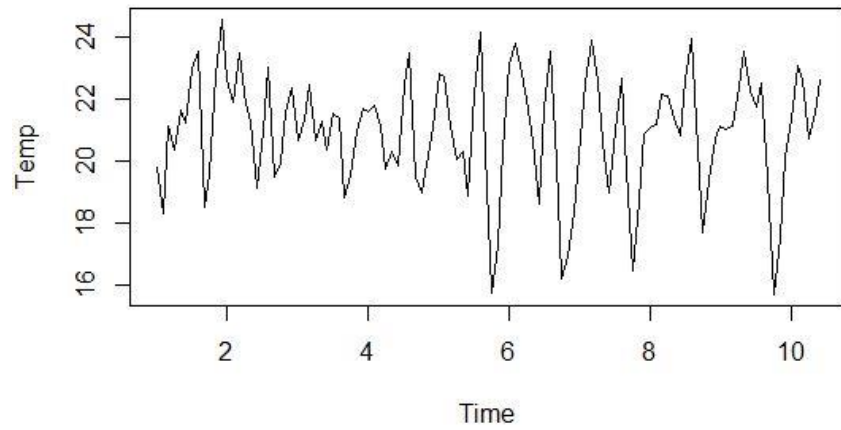
2:12 (Top Level) R Script

Console Terminal

```
> plot.ts(x1)
>
> model_fit<-auto.arima(x1, seasonal =TRUE, ic = 'aic')
> print(model_fit)
Series: x1
ARIMA(2,0,1)(0,1,1)[12]

Coefficients:
      ar1      ar2      ma1      sma1
    0.6384 -0.4142  0.3819 -0.1795
s.e.  0.1631  0.1366  0.1770  0.1043

sigma^2 estimated as 0.7684: log likelihood=-130.1
AIC=270.19 AICC=270.82 BIC=283.32
> forecast(model_fit,6)
      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
Jul 10    23.25970    22.13627    24.38312    21.54157    24.97783
Aug 10    23.35191    21.74694    24.95689    20.89732    25.80651
Sep 10    19.44388    17.81695    21.07080    16.95571    21.93204
Oct 10    15.67176    14.01654    17.32699    13.14032    18.20321
Nov 10    17.70992    16.02685    19.39299    15.13589    20.28395
Dec 10    20.26294    18.57848    21.94740    17.68678    22.83910
> |
```



All the plots in the residual plots look pretty normal, hence, we can say that the model is adequate.

ii) Using R to fit the ARIMA model for the temperature time series we get, Elec (2,0,0)x(1,1,1)₁₂

```
1 library(forecast)
2 electricity <- read.csv("C:/Users/User/Desktop/520 project/elec.csv",header=TRUE)
3 Temperature <- read.csv("C:/Users/User/Desktop/520 project/Temp.csv",header=TRUE)
4 x1<- ts(electricity,frequency = 12)
5 plot.ts(x1)
6
7 model_fit<-auto.arima(x1, seasonal =TRUE, ic = 'aic')
8 print(model_fit)
9 forecast(model_fit,6)
10 |
```

10:1 (Top Level) R Scri

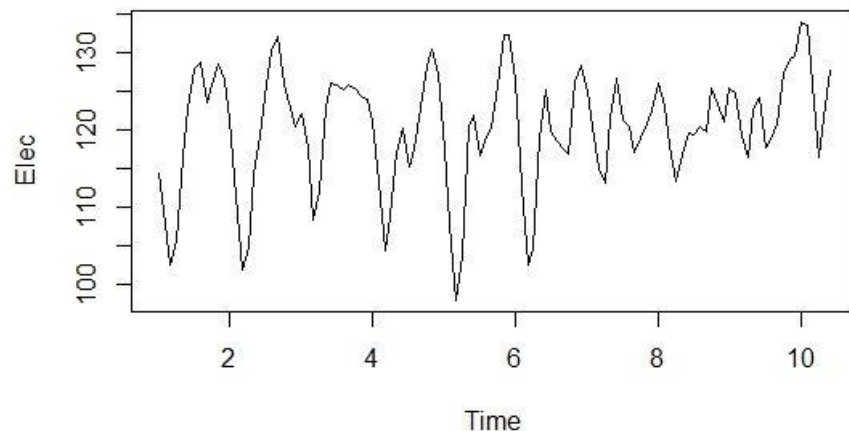
Console Terminal x

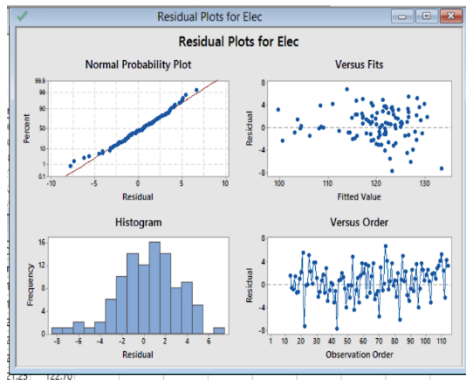
```
> plot.ts(x1)
>
> model_fit<-auto.arima(x1, seasonal =TRUE, ic = 'aic')
> print(model_fit)
Series: x1
ARIMA(2,0,0)(1,1,1)[12] with drift

Coefficients:
      ar1      ar2     sar1     sma1    drift
      1.0542 -0.4997  0.4408  -0.7504  0.0550
s.e.  0.0870  0.0854  0.2461  0.2271  0.0318

sigma^2 estimated as 8.281: log likelihood=-252.04
AIC=516.08 AICC=516.97 BIC=531.83
> forecast(model_fit,6)
```

| | Point | Forecast | Lo 80 | Hi 80 | Lo 95 | Hi 95 |
|--------|-------|----------|----------|----------|----------|----------|
| Jul 10 | | 122.5677 | 118.8781 | 126.2574 | 116.9249 | 128.2106 |
| Aug 10 | | 122.3426 | 116.9813 | 127.7038 | 114.1432 | 130.5419 |
| Sep 10 | | 122.4392 | 116.6223 | 128.2561 | 113.5431 | 131.3353 |
| Oct 10 | | 126.9475 | 121.1144 | 132.7806 | 118.0265 | 135.8685 |
| Nov 10 | | 128.7815 | 122.9103 | 134.6527 | 119.8023 | 137.7607 |
| Dec 10 | | 129.0084 | 123.0657 | 134.9511 | 119.9198 | 138.0970 |





In this model as well, all the residual plots look normal hence, the chosen model is pretty adequate.

Forecasts from Temperature time series:

| Temp | Forecast | Lo 80 | Hi 80 | Lo 95 | Hi 95 |
|---------------|----------|----------|----------|----------|----------|
| Jul 10 | 23.2597 | 22.13627 | 24.38312 | 21.54157 | 24.97783 |
| Aug 10 | 23.35191 | 21.74694 | 24.95688 | 20.89732 | 25.8065 |
| Sep 10 | 19.44388 | 17.81695 | 21.0708 | 16.95571 | 21.93204 |
| Oct 10 | 15.67176 | 14.01654 | 17.32698 | 13.14032 | 18.20321 |
| Nov 10 | 17.70992 | 16.02685 | 19.39299 | 15.13589 | 20.28396 |
| Dec 10 | 20.26294 | 18.57848 | 21.9474 | 17.68678 | 22.8391 |

Forecasts from Electricity time series:

| Elec | Forecast | Lo 80 | Hi 80 | Lo 95 | Hi 95 |
|---------------|-----------------|--------------|--------------|--------------|--------------|
| Jul 10 | 122.5677 | 118.8781 | 126.2574 | 116.9249 | 128.2106 |
| Aug 10 | 122.3426 | 116.9813 | 127.7038 | 114.1432 | 130.5419 |
| Sep 10 | 122.4392 | 116.6223 | 128.2561 | 113.5431 | 131.3353 |
| Oct 10 | 126.9475 | 121.1144 | 132.7806 | 118.0265 | 135.8685 |
| Nov 10 | 128.7815 | 122.9103 | 134.6527 | 119.8023 | 137.7607 |
| Dec 10 | 129.0084 | 123.0657 | 134.9511 | 119.9198 | 138.097 |