

EDS241: Assignment 3

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This exercise asks you to implement some of the techniques presented in Lectures 6-7. The goal is to estimate the causal effect of maternal smoking during pregnancy on infant birth weight using the treatment ignorability assumptions. The data are taken from the National Natality Detail Files, and the extract “SMOKING_EDS241.csv” is a random sample of all births in Pennsylvania during 1989-1991. Each observation is a mother-infant pair. The key variables are: The outcome and treatment variables are: birthwgt=birth weight of infant in grams tobacco=indicator for maternal smoking The control variables are: mage (mother’s age), meduc (mother’s education), mblack (=1 if mother black), alcohol (=1 if consumed alcohol during pregnancy), first (=1 if first child), diabete (=1 if mother diabetic), anemia (=1 if mother anemic)

1 Clean data

The following code loads and cleans the data.

```
# Load data
smokingdata <- read_csv("SMOKING_EDS241.csv")
# Clean data
smokingdata <- janitor::clean_names(smokingdata)
```

2 Unadjusted mean difference

(a) What is the unadjusted mean difference in birth weight of infants with smoking and nonsmoking mothers? Under what assumption does this correspond to the average treatment effect of maternal smoking during pregnancy on infant birth weight? Provide some simple empirical evidence for or against this assumption.

```
# smoking mothers mean
mu_nonsmoker = smokingdata %>%
  filter(tobacco == 0) %>%
  summarize(mean(birthwgt))

# non-smoking mothers mean
mu_smoker = smokingdata %>%
  filter(tobacco == 1) %>%
  summarize(mean(birthwgt))

# calculate mean diff
mean_diff = as.numeric(mu_nonsmoker - mu_smoker)

# linear regression of choice covariate to show omitted variable bias
```

```
model_1 <- lm_robust(meduc ~ tobacco, data = smokingdata)
huxreg(model_1)
```

	(1)
(Intercept)	13.239 ***
	(0.008)
tobacco	-1.318 ***
	(0.014)
N	94173
R2	0.061
*** p < 0.001; ** p < 0.01; * p < 0.05.	

The unadjusted mean difference in birth weight of infants 244.539 grams. Under the “treatment ignorability assumption”, this corresponds with the average treatment effect (ATE) of maternal smoking during pregnancy on infant birth weight. Assumption of “treatment ignorability” conditional on pre-treatment characteristics that allow us to assume that smoking mothers and nonsmoking mothers are good counterfactuals. The assumption of common support ensures that there is sufficient overlap in the characteristics of smoking mothers and nonsmoking mothers to find adequate matches so this aspect would need further analysis of the data. It’s important to note that the treatment of smoking is not randomly assigned either. The treatment ignorability assumption says that conditional on observable covariates, the assignment to the treatment is independent of the outcome of infant birth weight. Observational regression bias can arise if the smoking mother and nonsmoking mothers are inherently different in a way which would affect their infant birth weight. For example, smoking mothers could be less health conscious which has a negative impact on their infant birth weights aside from the effect of smoking itself. The regression of tobacco on mother’s education yields a statistically significant relationship which questions the validity of the assumption. There is omitted variable bias as shown by the model_1 regression which prevents us from being able to interpret the unadjusted mean difference as a causal effect.

3 Introducing covariates

Assume that maternal smoking is randomly assigned conditional on the observable covariates listed above. Estimate the effect of maternal smoking on birth weight using a linear regression. Report the estimated coefficient on tobacco and its standard error.

```
model_2 <- lm_robust(formula = birthwgt ~ tobacco + mage + meduc + as.factor(anemia)
                     + as.factor(diabete) + as.factor(alcokol) +
                     as.factor(mblack) + as.factor(first), data=smokingdata)

huxreg(model_2)
```

	(1)
(Intercept)	3362.258 *** (12.076)
tobacco	-228.073 *** (4.277)
mage	-0.694 (0.368)
meduc	11.688 *** (0.862)
as.factor(anemia)1	-4.796 (17.874)
as.factor(diabete)1	73.228 *** (13.235)
as.factor(alcokol)1	-77.350 *** (14.039)
as.factor(mblack)1	-240.030 *** (5.348)
as.factor(first)1	-96.944 *** (3.488)
N	94173
R2	0.072
*** p < 0.001; ** p < 0.01; * p < 0.05.	

Table 1 shows the **estimated coefficients from the linear regression of effect of maternal smoking**

on birth weight. -228.073 is the estimated coefficient on tobacco with 4.277 being the standard error.

4 Exact matching

Use the exact matching estimator to estimate the effect of maternal smoking on birth weight. For simplicity, consider the following covariates in your matching estimator: create a 0-1 indicator for mother's age (=1 if $\text{mage} \geq 34$), and a 0-1 indicator for mother's education (1 if $\text{meduc} \geq 16$), mother's race (mblack), and alcohol consumption indicator (alcohol). These 4 covariates will create $2^2 \times 2^2 = 16$ cells. Report the estimated average treatment effect of smoking on birthweight using the exact matching estimator and its linear regression analogue.

```
# create indicator based on mother's age (=1 if mage>=34)
smokingdata<- smokingdata %>%
  mutate(age_indicator = case_when(
    mage < 34 ~ 0,
    mage >= 34 ~ 1))

# create indicator based on mother's education (1 if meduc>=16)
smokingdata<- smokingdata %>%
  mutate(educ_indicator = case_when(
    meduc < 16 ~ 0,
    meduc >= 16 ~ 1))

# create group variable to capture all interactions
smokingdata<- smokingdata %>%
  mutate(g = paste0(age_indicator,educ_indicator,mblack,alcohol))

# regression on including tobacco and the 4 grouped indicators (mother age, mother education, mother race, mother alcohol)
model_3 <- lm_robust(birthwgt ~ tobacco + as.factor(g), data= smokingdata)

# exact matching table
TIA_table <- smokingdata %>%
  group_by(g,tobacco)%>%
  summarise(n_obs = n(),
    birthwgt_mean= mean(birthwgt, na.rm = T))%>% #Calculate number of observations and Y mean by treatment and covariates
  gather(variables, values, n_obs:birthwgt_mean)%>% #Reshape data
  mutate(variables = paste0(variables,"_",tobacco, sep=""))%>% #Combine the treatment and variables for matching
  pivot_wider(id_cols = g, names_from = variables, values_from = values)%>% #Reshape data by treatment and covariates
  ungroup()%>% #Ungroup from X values
  mutate(birthwgt_mean_diff = birthwgt_mean_1 - birthwgt_mean_0, #calculate Y_diff
    w_ATE = (n_obs_0+n_obs_1)/(sum(n_obs_0)+sum(n_obs_1)),
    w_ATT = n_obs_1/sum(n_obs_1))%>% #calculate weights
  mutate_if(is.numeric, round, 3) #Round data

stargazer(TIA_table, type= "text", summary = FALSE, digits = 2)

##
## =====
##      g      n_obs_0 n_obs_1 birthwgt_mean_0 birthwgt_mean_1 birthwgt_mean_diff w_ATE w_ATT
## -----
```

```
## 1 0000 44274 13443 3445.685 3220.247 -225.438 0.613 0.741
## 2 0001 214 448 3450.276 3124.248 -326.028 0.007 0.025
## 3 0010 7007 1980 3195.973 3006.315 -189.659 0.095 0.109
## 4 0011 71 226 3120.07 2817.336 -302.734 0.003 0.012
## 5 0100 13425 535 3483.025 3273.94 -209.084 0.148 0.029
## 6 0101 130 29 3510.946 3413.207 -97.739 0.002 0.002
## 7 0110 625 61 3319.222 3159.049 -160.173 0.007 0.003
## 8 0111 4 10 2983.5 3097.7 114.2 0 0.001
## 9 1000 5115 976 3467.407 3171.424 -295.982 0.065 0.054
## 10 1001 56 45 3358.321 3097.733 -260.588 0.001 0.002
## 11 1010 396 135 3185.076 2994.667 -190.409 0.006 0.007
## 12 1011 7 26 2739.714 2846.385 106.67 0 0.001
## 13 1100 4492 201 3487.19 3249.448 -237.743 0.05 0.011
## 14 1101 57 17 3534.912 3037.471 -497.442 0.001 0.001
## 15 1110 147 19 3328.286 2852.158 -476.128 0.002 0.001
## 16 1111 1 1 3459 2835 -624 0 0
## -----
```

```
# Multivariate matching estimates of ATE
ATE=sum((TIA_table$w_ATE)*(TIA_table$birthwgt_mean_diff))
ATE
```

```
## [1] -225.6413
```

```
ATT=sum((TIA_table$w_ATT)*(TIA_table$birthwgt_mean_diff))
ATT
```

```
## [1] -227.4503
```

Table 2 shows the exact matching table used to estimate ATE.

The exact matching estimator estimates the average treatment effect (ATE) of smoking on birthweight as -225.641. The linear analogue estimates the average treatment effect (ATE) of smoking on birthweight as -226.245.

5 Propensity Score

Estimate the propensity score for maternal smoking using a logit estimator and based on the following specification: mother's age, mother's age squared, mother's education, and indicators for mother's race, and alcohol consumption.

```
# add mother's age variable squared
smokingdata <- smokingdata %>%
  mutate(mage_squared = mage * mage)

model_4 <- glm(tobacco ~ mage + mage_squared + meduc + as.factor(mblack) + as.factor(alcohol), family =
EPS <- predict(model_4, type = "response") # estimated propensity score (EPS)
PS_weighted <- (smokingdata$tobacco / EPS) + ((1 - smokingdata$tobacco)/(1 - EPS)) # weight EPS
```

Use the propensity score weighted regression (WLS) to estimate the effect of maternal smoking on birth weight (Lecture 7, slide 12).

```
# add propensity scores and weighted propensity scores to data as columns
smokingdata <- smokingdata %>%
  mutate("EPS" = EPS, "PS_weighted" = PS_weighted)

model_5 <- lm_robust(birthwgt ~ tobacco + mage + mage_squared + meduc +
  as.factor(mblack) + as.factor(alcohol), data=smokingdata, weights=PS_weighted)

wls_ATE <- model_5$coefficients[2]
```

The weighted OLS regression estimates the average treatment effect(ATE) of smoking on birthweight as -220.233

5.1 Appendix

```
huxreg(model_3)
```

Table A1 shows the estimated coefficients from the linear regression of effect of maternal smoking on birth weight with the inclusion of the following covariates: mother age, mother education, mother race and alcohol.

```
huxreg(model_5)
```

Table A2 shows the estimated coefficients from weighted OLS estimating the effect of maternal smoking on birth weight with the inclusion of the following covariates: mother age, mother age squared, mother education, mother race and alcohol.

	(1)
(Intercept)	3445.873 *** (2.232)
tobacco	-226.245 *** (4.220)
as.factor(g)0001	-63.124 ** (20.431)
as.factor(g)0010	-241.839 *** (5.742)
as.factor(g)0011	-384.006 *** (29.870)
as.factor(g)0100	37.809 *** (4.535)
as.factor(g)0101	88.511 * (38.413)
as.factor(g)0110	-120.775 *** (18.977)
as.factor(g)0111	-219.198 (127.345)
as.factor(g)1000	10.359 (6.819)
as.factor(g)1001	-102.853 * (45.144)
as.factor(g)1010	-251.686 *** (24.106)
as.factor(g)1011	-443.862 *** (79.415)
as.factor(g)1100	40.825 *** (7.404)
as.factor(g)1101	26.737 (55.254)
as.factor(g)1110	-146.188 *** (38.555)
as.factor(g)1111	185.751

	(1)
(Intercept)	2971.444 *** (57.060)
tobacco	-220.233 *** (5.029)
mage	27.627 *** (4.587)
mage_squared	-0.478 *** (0.087)
meduc	7.472 *** (1.584)
as.factor(mblack)1	-220.990 *** (8.245)
as.factor(alcohol)1	-71.914 *** (16.734)
N	94173
R2	0.074
*** p < 0.001; ** p < 0.01; * p < 0.05.	