# The Network of Foreign Direct Investment Flows: Theory and Empirical Analysis<sup>1</sup>

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### Introduction

- Motivation
  - Explain FDI networks
  - Violation of Independence Assumptions
  - Theoretical Importance of Dependence Terms
- FDI as a Network
  - Reciprocity
  - Transitivity
- Demonstrate how to integrate dependence and covariates

### Variables

#### Bilateral FDI:

- Modeled on the rounded logarithmic scale (i.e., count).
- Data from UNCTAD, covering the time-period of 2001 to 2012
- Dyad-level Covariates
  - Gravity +
  - Contiguity +
  - Common Language +
  - Four Types of Defense Treaties +
  - Colonial Relationships +
  - PTA depth +

- Country-level Covariates (s/r)
  - GDP per capita +/-
  - GDP Growth Rate +/+
  - Polity IV +/+
  - Political Violence -/-
  - Trade Openness +/+

## Reciprocity

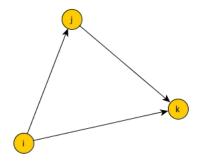
Reciprocity



• Standard practice to resolve political opposition from competing firms

## Transitivity

Transitivity



• MNC expansion and supply-chain fragmentation

# The Count Exponential Random Graph Model (ERGM)

The probability (likelihood function) of observing the network is:

$$\mathrm{Pr}_{\boldsymbol{\theta};h;\boldsymbol{g}}(\boldsymbol{Y}=\boldsymbol{y}) = \frac{h(\boldsymbol{y})\mathrm{exp}(\boldsymbol{\theta}\cdot\boldsymbol{g}(\boldsymbol{y}))}{\kappa_{h,\boldsymbol{g}}(\boldsymbol{\theta})}$$

Decomposition:

$$\underbrace{h\left(y\right)}_{Distribution} \qquad \underbrace{oldsymbol{ heta}}_{Effects} \qquad \underbrace{oldsymbol{g}\left(y\right)}_{Net\ Stats} \qquad \underbrace{\kappa_{h,g}( heta)}_{Normalizer}$$

### Constants:

• Sum, Sum<sup>(1/2)</sup>, and Nonzero

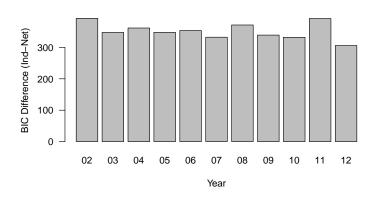
# **ERGM** Dependence Terms

$$\text{Reciprocity}: g\left(\boldsymbol{y}\right) = \sum_{(i,j) \in \mathbb{Y}} \min(\boldsymbol{y}_{i,j}, \boldsymbol{y}_{j,i})$$

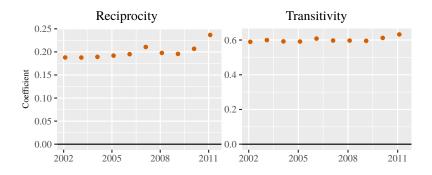
$$\text{Transitive Weights}: \boldsymbol{g}\left(\boldsymbol{y}\right) = \sum_{(i,j) \in \mathbb{Y}} \min \left(\boldsymbol{y}_{i,j}, \max_{k \in N} \left(\min(\boldsymbol{y}_{i,k}, \boldsymbol{y}_{k,j})\right)\right),$$

### Model Fit and Bias

### BIC Difference between Models

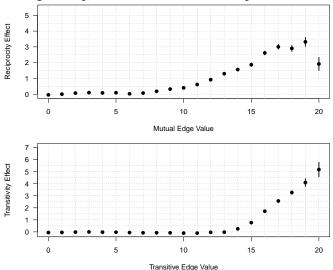


## Count Model and Network Dependencies

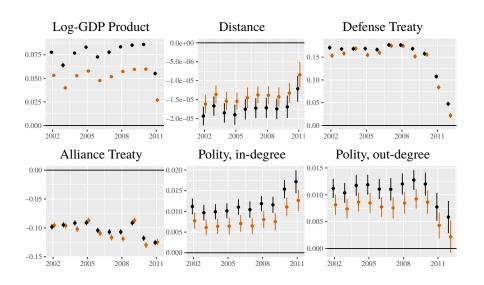


## Network Effects Interpretation

### Change in expected value relative to independence model:

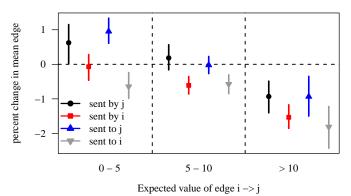


### Covariate Results



## Implications: FDI Ripple Effects

How does the network equilibrate in response to an edge elimination?



## Conclusion and Future Research

- Dyadic FDI characterized by network interdependence
- Network terms need to be modeled instead of being assumed away
- Raises additional complications related to missing data

## **ERGM Constants**

$$\operatorname{Sum}: g\left(\boldsymbol{y}\right) = \sum_{(i,j) \in \mathbb{Y}} \boldsymbol{y}_{i,j}$$

Sum, Fractional Moment :  $g\left(\boldsymbol{y}\right) = \sum_{(i,j)\in\mathbb{Y}} \boldsymbol{y}_{i,j}^{1/2}$ 

Non-Zero : 
$$g(y) = \sum_{(i,j) \in \mathbb{Y}} \mathbb{I}(y_{i,j} \neq 0)$$

## **ERGM Covariates**

Dyadic Covariate : 
$$g(y, x) = \sum_{(i,j)} y_{i,j} x_{i,j}$$

Sender Covariate : 
$$g(y, x) = \sum_{i} x_i \sum_{j} y_{i,j}$$

Receiver Covariate : 
$$g(y, x) = \sum_{j} x_{j} \sum_{i} y_{i,j}$$