

Empirical means to validate skills models and assess the fit of a student model

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7 avril 2016

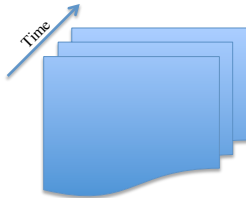
Problem Specification

- Student skills assessment models



Problem Specification

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- Static Vs. Dynamic



Dynamic

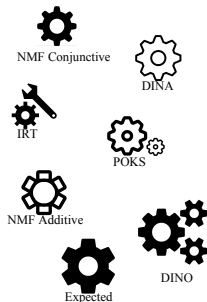


Static



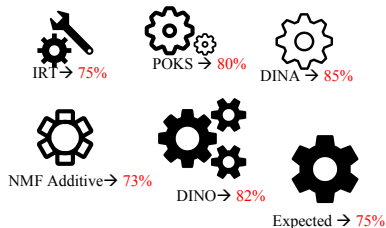
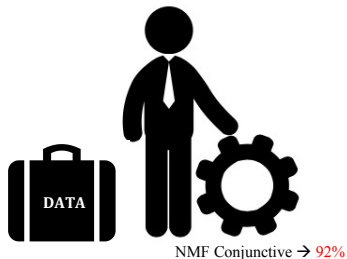
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- Student skills assessment models
- Static Vs. Dynamic
- How to decide which are the most representative of the underlying ground truth?



Problem Specification

- Student skills assessment models
- Static Vs. Dynamic
- How to decide which are the most representative of the underlying ground truth ?
- Model selection and goodness of fit
- A general answer : best performer



Problem Specification

Our contribution

- To make a comprehensive comparison of educational data model performances
- To propose a new approach to assessing model fit

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General hypothesis :

- Recognizing the ground truth based on the uniqueness of this comprehensive comparison

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General hypothesis :

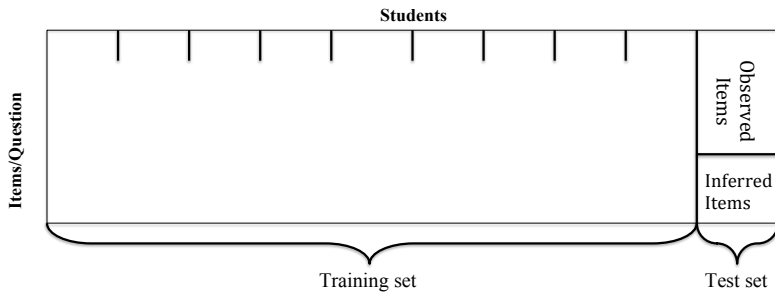
- Recognizing the ground truth based on the uniqueness of this comprehensive comparison

The proposed approach :

- Assessing the fit of the model to the underlying ground truth using a methodology based on **synthetic data**

Presentation terms and concepts

- Performance of a model over a data set



Presentation terms and concepts

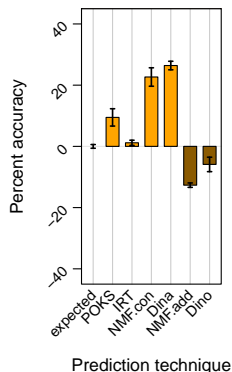
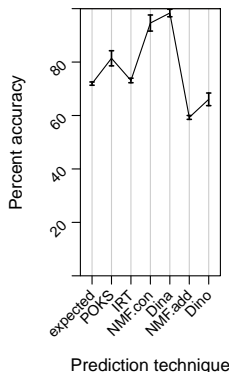
- **Performance of a model** over a data set
- Model parameters

| Skills Model | | Parameters estimated from | | |
|--------------|-----------|---|-------------------|----------------------------------|
| | | Training set | | Observed items |
| Multiple | NMF Conj. | | • Q-matrix | • Students skills mastery matrix |
| | NMF Add. | | | |
| | DINA | • Slip | | |
| | DINO | • Guess | | |
| Single | IRT | • Item difficulty • Item discrimination | • Student Ability | • Student Odds |
| | Expected | • Item Odds | | |
| Zero | POKS | • Initial Odds • Odds ratio • Partial order structure | | |

Contributed skills

Presentation terms and concepts

- **Performance of a model** over a data set
- Model parameters
- Performance vector
- Performance signature



| Model | Performance |
|-----------------|-------------|
| <i>Expected</i> | 0.72% |
| <i>POKS</i> | 0.80% |
| <i>IRT</i> | 0.74% |
| <i>NMF.Conj</i> | 0.94% |
| <i>Dina</i> | 0.99% |
| <i>NMF.Add</i> | 0.60% |
| <i>Dino</i> | 0.65% |

Presentation terms and concepts

- **Performance of a model** over a data set
- Model parameters
- Performance vector
- Performance signature
- Performance prototype

The *performance vector* associated with the synthetic data of a model class.

Presentation terms and concepts

- **Performance of a model** over a data set
- Model parameters
- Performance vector
- Performance signature
- Performance prototype
- Target performance vector

The *performance vector* of the real data set to classify.

Vector space of accuracy performances

- Performance vectors of datasets in columns(Data points in a part of performance space)

| Model | Synthetic data set | | | | | | |
|-----------------|--------------------|------|------|------|------|---------|---------|
| | <i>Random</i> | POKS | IRT | DINA | DINO | L.Conj. | L.Comp. |
| <i>Expected</i> | 0.75 | 0.91 | 0.90 | 0.72 | 0.72 | 0.78 | 0.93 |
| POKS | 0.75 | 0.94 | 0.94 | 0.81 | 0.81 | 0.90 | 0.94 |
| IRT | 0.75 | 0.91 | 0.95 | 0.73 | 0.73 | 0.79 | 0.89 |
| DINA | 0.75 | 0.77 | 0.81 | 1.00 | 0.65 | 0.98 | 0.89 |
| DINO | 0.75 | 0.63 | 0.56 | 0.66 | 1.00 | 0.68 | 0.91 |
| NMF.Conj | 0.75 | 0.59 | 0.53 | 0.95 | 0.65 | 0.97 | 0.58 |
| NMF.Comp | 0.75 | 0.76 | 0.79 | 0.59 | 0.93 | 0.70 | 0.98 |

The diagonal generally displays the best performance

Vector space of accuracy performances

- Given a target vector, we want to define which columns are the closest to the target column

| Model | Synthetic data set | | | | | | | Target |
|-----------------|--------------------|------|------|------|------|---------|---------|--------|
| | <i>Random</i> | POKS | IRT | DINA | DINO | L.Conj. | L.Comp. | |
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| POKS | 0.75 | 0.94 | 0.94 | 0.81 | 0.81 | 0.90 | 0.94 | 0.75 |
| IRT | 0.75 | 0.91 | 0.95 | 0.73 | 0.73 | 0.79 | 0.89 | 0.68 |
| DINA | 0.75 | 0.77 | 0.81 | 1.00 | 0.65 | 0.98 | 0.89 | 0.93 |
| DINO | 0.75 | 0.63 | 0.56 | 0.66 | 1.00 | 0.68 | 0.91 | 0.60 |
| NMF.Conj | 0.75 | 0.59 | 0.53 | 0.95 | 0.65 | 0.97 | 0.58 | 0.80 |
| NMF.Comp | 0.75 | 0.76 | 0.79 | 0.59 | 0.93 | 0.70 | 0.98 | 0.70 |

- Our hypothesis : the similarity of vectors can indicate the nature of data
- The nearest neighbour in this space can be a candidate for the ground truth

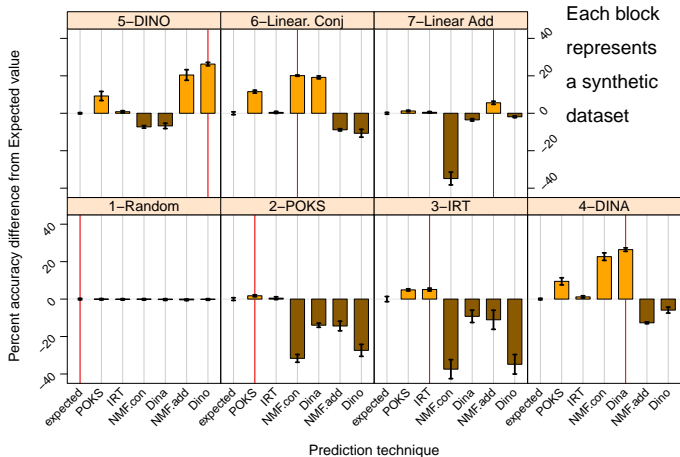
Research questions

- ① ✓ What is the *performance vector* of student skills assessment models over real and over synthetic data created using the same models ?
 - Experiment 1 : Predictive *performance vector* of models over real and synthetic data sets

Datasets

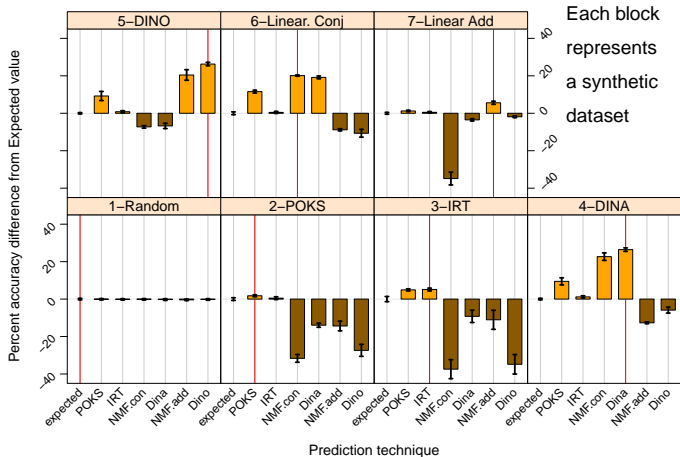
| Data set | Number of | | | Mean Score | Q-matrix |
|---|-----------|-------|----------|------------|-----------------------|
| | Skills | Items | Students | | |
| Synthetic | | | | | |
| 1.Random | 7 | 30 | 700 | 0.75 | Q₀₁ |
| 2.POKS | 7 | 20 | 500 | 0.50 | Q₀₂ |
| 3.IRT-2PL | 5 | 20 | 600 | 0.50 | Q₀₃ |
| 4.DINA | 7 | 28 | 500 | 0.31 | Q₅ |
| 5.DINO | 7 | 28 | 500 | 0.69 | Q₆ |
| Linear (Matrix factorization) | | | | | |
| 6. Conj. | 8 | 20 | 500 | 0.24 | Q₁ |
| 7. Comp. | 8 | 20 | 500 | 0.57 | Q₁ |
| Real | | | | | |
| 8.Fraction | 8 | 20 | 536 | 0.53 | Q₁ |
| 9.Vomlel | 6 | 20 | 149 | 0.61 | Q₄ |
| 10.ECPE | 3 | 28 | 2922 | 0.71 | Q₃ |
| Fraction subsets and variants of Q₁ | | | | | |
| 11. 1 | 5 | 15 | 536 | 0.53 | Q₁₀ |
| 12. 2/1 | 3 | 11 | 536 | 0.51 | Q₁₁ |
| 13. 2/2 | 5 | 11 | 536 | 0.51 | Q₁₂ |
| 14. 2/3 | 3 | 11 | 536 | 0.51 | Q₁₃ |

Predictive performance of models over synthetic datasets



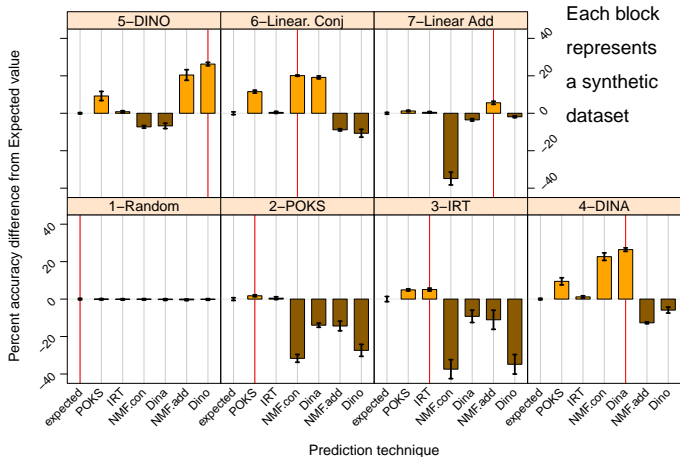
The random data set has a flat performance across techniques

Predictive performance of models over synthetic datasets



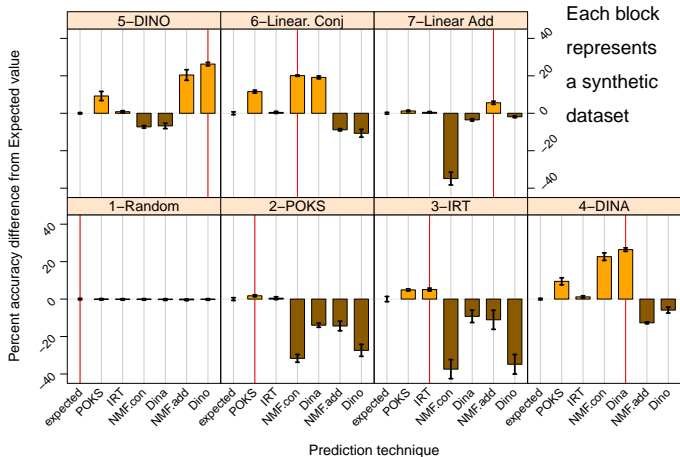
The highest performance is for the generative model behind the dataset

Predictive performance of models over synthetic datasets



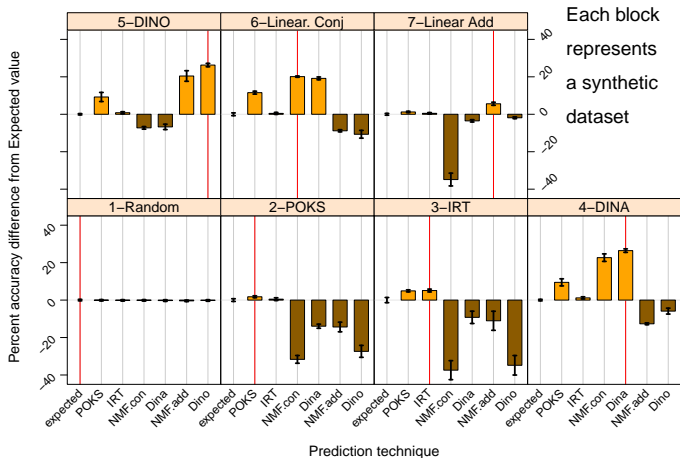
Motivation : Most of the models preform worse than simple expected prediction model

Predictive performance of models over synthetic datasets



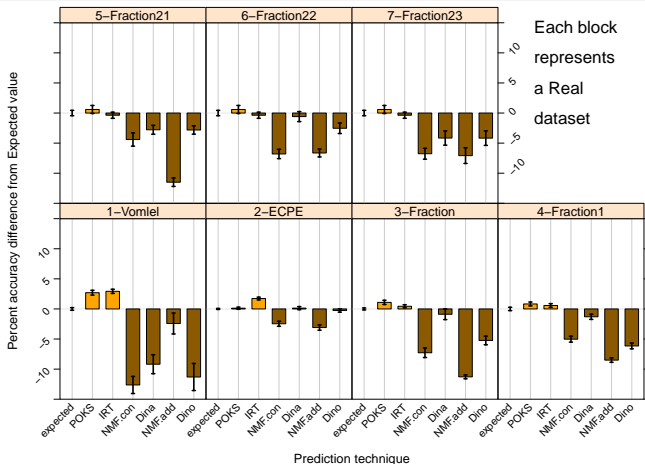
Data sets have discriminant pattern of performance vector across models

Predictive performance of models over synthetic datasets



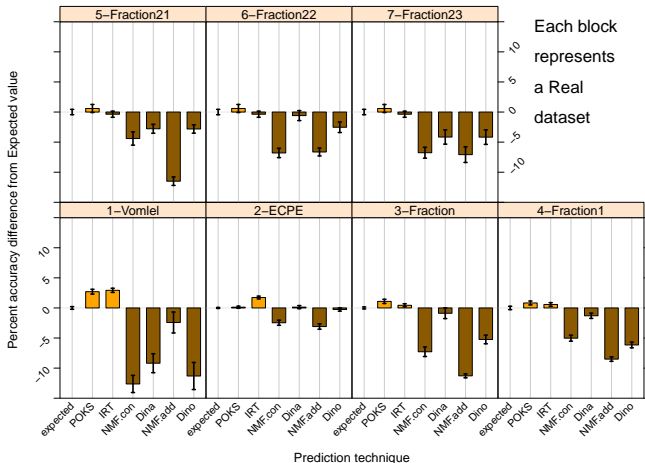
The capacity of recognizing a data set's true model relies on this discriminant characteristic

Predictive performance of models over real datasets



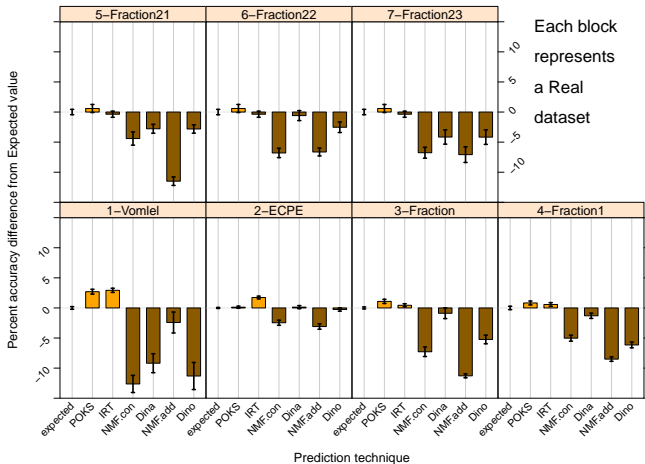
In most cases, the best performer is close to the baseline

Predictive performance of models over real datasets



The pattern of the Fraction performance data set repeats over its subsets

Predictive performance of models over real datasets



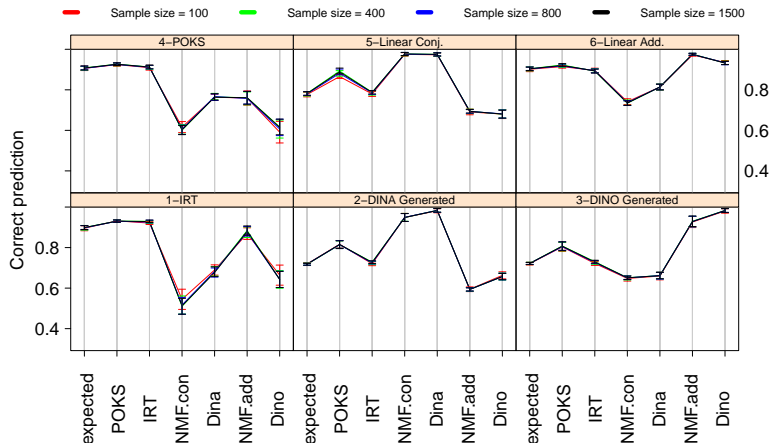
None of the real data sets show the large variance and the differences found in the synthetic data sets models

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 - Experiment 2 : Sensitivity of the Model performance over different data generation parameters

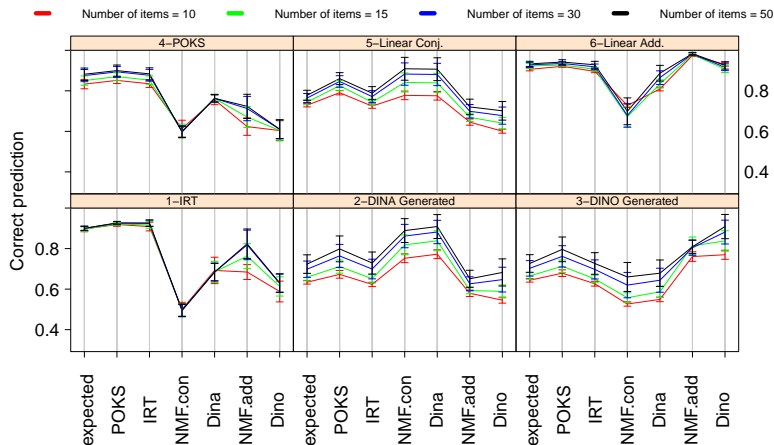
Are they stable in addition to be discriminant ?

Variation of sample size over synthetic data sets



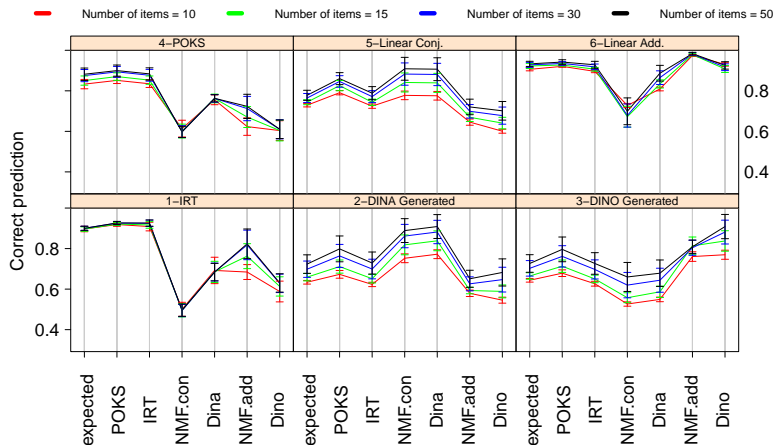
Obviously, the signature pattern did not change significantly for some parameters such as **Sample size**.

Variation of number of items over synthetic data sets



Even for synthetic data the performance of the ground truth model should not necessarily be close to 100%.

Variation of number of items over synthetic data sets



The Performance signature shifts down once the number of items degrades.

Data parameters

- 1 Sample size (Number of students)
- 2 Number of items
- 3 Number of latent skills
- 4 Item score variance
- 5 Student score variance
- 6 Average success rate

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Conclusion :

- Data parameters can potentially influence the performance of a model
- For better comparison of the vectors, we also consider **data characteristic parameters** of the real data in the generation process

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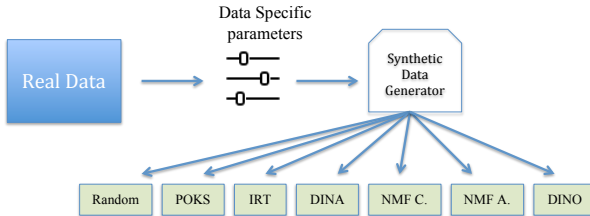
Signature framework

This approach relies on generating synthetic datasets



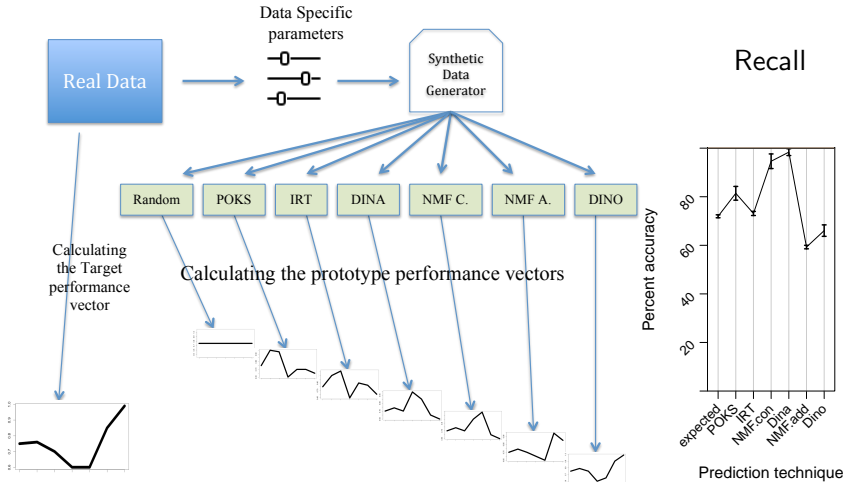
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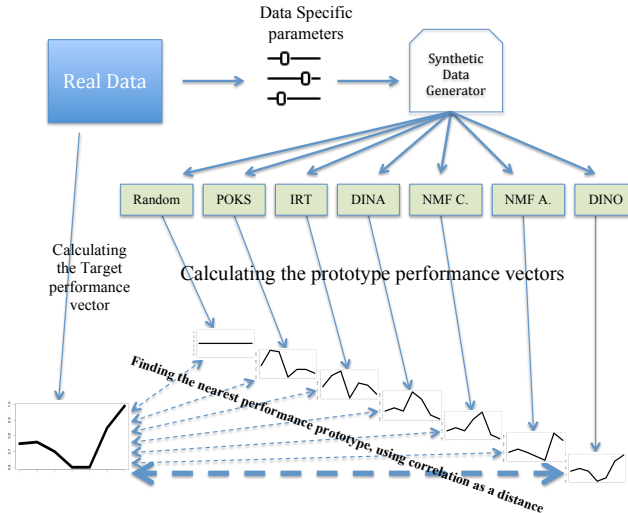
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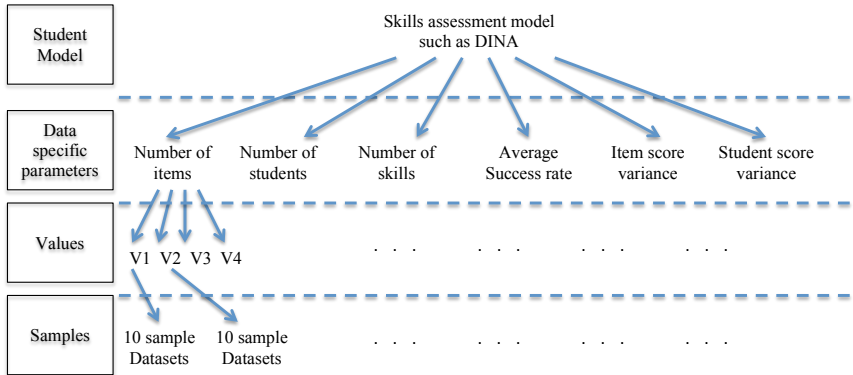


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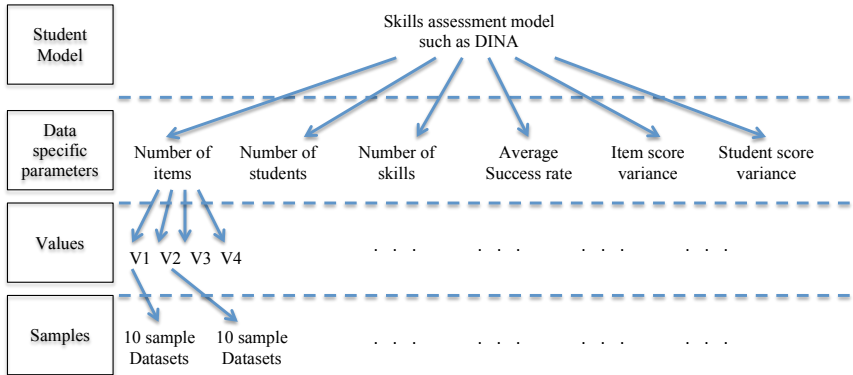


Database of synthetic datasets



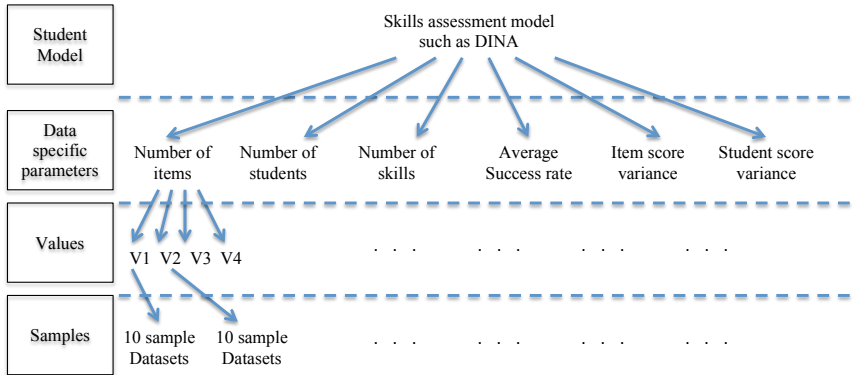
There exists 6 skills assessment models

Database of synthetic datasets



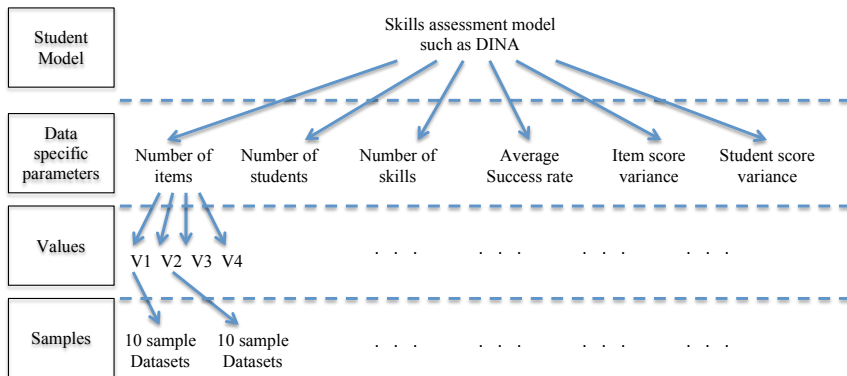
There exists 6 skills assessment models X 6 data characteristic parameters

Database of synthetic datasets



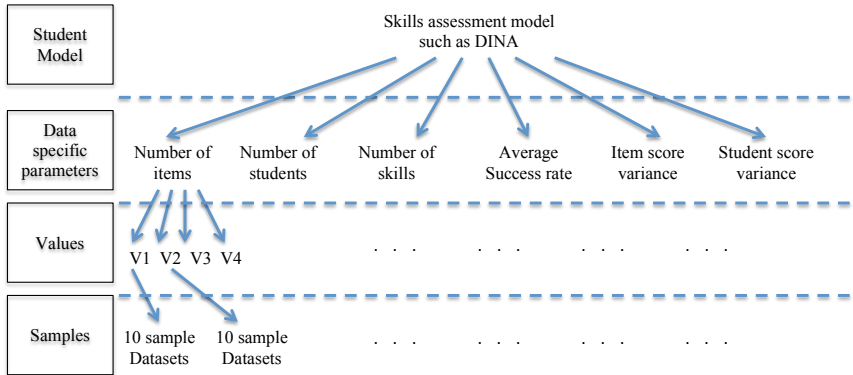
There exists 6 skills assessment models X 6 data characteristic parameters X 4 values

Database of synthetic datasets



There exists 6 skills assessment models X 6 data characteristic parameters X 4 values X 10 samples = 1440 samples in the Database (*DB*)

Database of synthetic datasets



$$|DB| = 1440 \text{ and } |DC| = 24$$

Prototype definition

Target performance vector : $\mathcal{T}^{(tm)} = \text{Performance.vector}(D_c^{(tm)} \in DB)$
where : $D_c^{(tm)}$ is characterized with data parameter condition $c \in DC$ and
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- Pearson correlation coefficient is used as a measure of similarity between $\mathcal{T}^{(tm)}$ and \mathcal{N}^m (for data condition c)
- Next slid shows the average of correlation between $\mathcal{T}^{(tm)}$ and \mathcal{N}^m for all data parameter conditions in DC

Degree of similarity between six synthetic performance vector based on the correlation

Target performance vectors

| | | POKS | IRT | NMF Conj. | DINA | NMF Add. | DINO |
|---|-----------|-------------|-------------|-------------|-------------|-------------|-------------|
| Centroid synthetic performance vectors | POKS | 0.96 | | | | | |
| | IRT | 0.86 | 0.96 | | | | |
| | NMF Conj. | 0.22 | -0.20 | 0.96 | | | |
| | DINA | 0.02 | -0.40 | 0.94 | 0.96 | | |
| | NMF Add. | 0.44 | 0.75 | -0.62 | -0.73 | 0.93 | |
| | DINO | -0.15 | 0.20 | -0.70 | -0.69 | 0.63 | 0.95 |

- The diagonal shows high correlations because it compares performance vectors of the same model generated datasets.
- Performance vectors with similar ground truth also show a high correlation.

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In general, correlation similarity provides a very good measure of model fit.

Degree of similarity between six real datasets and the ground truth based on the correlation

Target performance vectors of Real Datasets

| | | | | | Fraction subsets | | | |
|--|-----------|-------------|-------------|-------------|------------------|-------------|-------------|-------------|
| | | Vomlel | ECPE | Fraction | 1 | 21 | 22 | 23 |
| Performance Prototype of Synthetic Datasets | Random | 0.58 | 0.73 | 0.61 | 0.43 | 0.24 | 0.61 | 0.57 |
| | IRT | 0.90 | 0.42 | 0.72 | 0.88 | 0.60 | 0.77 | 0.61 |
| | DINA | -0.38 | -0.09 | 0.23 | 0.30 | 0.56 | 0.06 | 0.38 |
| | DINO | 0.34 | 0.15 | -0.18 | -0.31 | 0.10 | -0.08 | 0.38 |
| | POKS | 0.75 | 0.40 | 0.83 | 0.95 | 0.70 | 0.83 | 0.80 |
| | NMF Conj. | -0.05 | 0.54 | 0.51 | 0.55 | 0.66 | 0.33 | 0.57 |
| | NMF Add. | 0.39 | 0.06 | -0.04 | -0.19 | -0.03 | 0.13 | 0.28 |

The centroid performance vector of each model is the average of performance vectors of 10 generated datasets

Degree of similarity between six real datasets and the ground truth based on the correlation

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Vomlel dataset shows a high correlation with IRT model

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Fraction with its subset datasets show similarity with POKS model.

Degree of similarity between six real datasets and the ground truth based on the correlation

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As expected, ECPE has the highest correlation with random generated dataset.

Research questions

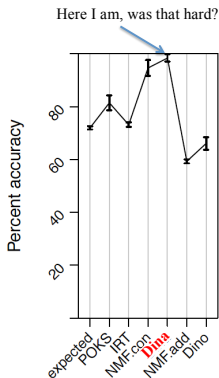
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- ③ ✓ Can the *performance vector* be used to define a method to reliably identify the ground truth behind the synthetic data ?
 - Experiment 3 : Model selection based on performance vector classification
- ④ **How does the method compare with the standard practice of using the model with the best performance ?**
 - Experiment 4 : Signature vs. best performer classification

Problem specification

- What we did ? to evaluate the ability of the Signature approach to identify the ground truth model

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- What we did ? to evaluate the ability of the Signature approach to identify the ground truth model
- What we want to do ? to compare the results of classification based on signature approach with the best performer approach.
- Reporting the accuracy of these classification in terms of F1 and accuracy measures

| | | Prediction outcome | |
|--------------|----------|--------------------|----------|
| | | Positive | Negative |
| Actual value | Positive | TP | FN |
| | Negative | FP | TN |

$$Precision = \frac{TP}{TP + FP}$$

$$Recall = \frac{TP}{TP + FN}$$

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

$$F_1 = \frac{Precision \cdot Recall}{Precision + Recall}$$

Signature classifier

Target performance vector : $\mathcal{T}^{(tm)} = \text{Performance.vector}(D_c^{(tm)} \in DB)$
where : $D_c^{(tm)}$ is characterized with data parameter condition $c \in DC$ and
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- Neighbors of $\mathcal{T}^{(tm)}$ are performance vectors of D
- A majority voting among the ground truth of 10 nearest neighbors to $\mathcal{T}^{(tm)}$ defines the estimated ground truth

Results of signature vs. best performer classification

| | | Performance | | | |
|----------------|-----------|----------------|----------|--------------------|----------|
| | | Best Performer | | Signature approach | |
| | | F-Measure | Accuracy | F-Measure | Accuracy |
| Models | POKS | 0.719 | 0.871 | 0.998 | 99.9 |
| | IRT | 0.625 | 0.908 | 0.998 | 99.9 |
| | NMF Conj. | 0.502 | 0.887 | 0.985 | 99.5 |
| | DINA | 0.734 | 0.891 | 1 | 100 |
| | NMF Add. | 0.905 | 0.969 | 1 | 100 |
| | DINO | 0.963 | 0.988 | 0.970 | 0.990 |
| Total accuracy | | 75% | | 99% | |

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- The F-measure increases when the signature approach is used for classification.
- In terms of individual scores per method, the accuracy increases when signature approach is used.
- The total accuracy considers true positive numbers over number of datasets regardless of individual models

Research questions

- 1 ✓ What is the *performance vector* of student skills assessment models over real and over synthetic data created using the same models ?
 - Experiment 1 : Predictive performance of models over real and synthetic data sets
 - In terms of signature pattern : it is unique for each generative model
 - In terms of data points in the performance vector space : They are data points in this space
 - For real data sets, the performances are not better than the expected performance
 - For synthetic data, datasets with different ground truths that share some concepts, show a high correlation.

Research questions

- ① ✓ Predictive performance of models over real and synthetic data sets
 - ② ✓ Is the *performance vector* unique to each synthetic data type (data from the same ground truth model) ?
- Experiment 2 : Sensitivity of the Model performance over different data generation parameters
 - Different parameters can create different points in the performance vector space
 - There would be a cloud of points for a particular model (Ground truth)
 - The cloud is not too dispersed

Research questions

- ① ✓ Predictive performance of models over real and synthetic data sets
 - ② ✓ Sensitivity of the Model performance over different data parameters
 - ③ ✓ Can the *performance vector* be used to define a method to reliably identify the ground truth behind the synthetic data ?
- Experiment 3 : Model selection based on performance vector classification
 - A comparison between the target and the prototype signature
 - Datasets that share a common source have correlated performance vectors.

Research questions

- ① ✓ Predictive performance of models over real and synthetic data sets
 - ② ✓ Sensitivity of the Model performance over different data parameters
 - ③ ✓ Model selection based on performance vector classification
 - ④ ✓ How does the method compare with the standard practice of using the model with the best performance?
- Experiment 4 : Signature vs. best performer classification
 - The ground truth model does not always correspond to the best performer and our approach provides a more reliable means

Future works

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- to be extend over different models, different domains and more datasets
- generalize to dynamic data and skills assessment models
- Candidate models and their complexity where the data is created with a mixture of models
- Application in other fields of study

Thank you

