Empirical means to validate skills models and assess the fit of a student model

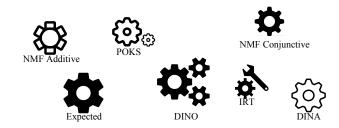
Behzad Beheshti

Supervisor: Michel C. Desmarais

Génie Informatique Et Génie Logiciel École Polytechnique de Montréal

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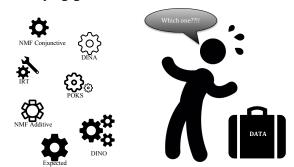
• Student skills assessment models



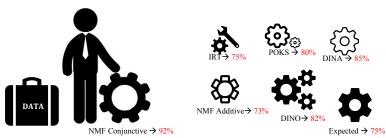
- Student skills assessment models
- Static Vs. Dynamic



- Student skills assessment models
- Static Vs. Dynamic
- How to decide which are the most representative of the underlying ground truth?



- Student skills assessment models
- Static Vs. Dynamic
- How to decide which are the most representative of the underlying ground truth?
- Model selection and goodness of fit
- A general answer : best performer



Our contribution

- To make a comprehensive comparison of educational data model performances
- To propose a new approach to assessing model fit

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General hypothesis:

 Recognizing the ground truth based on the uniqueness of this comprehensive comparison

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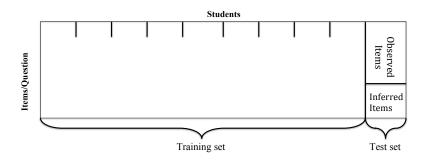
General hypothesis:

 Recognizing the ground truth based on the uniqueness of this comprehensive comparison

The proposed approach:

 Assessing the fit of the model to the underlying ground truth using a methodology based on synthetic data

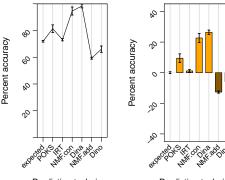
• Performance of a model over a data set



- Performance of a model over a data set
- Model parameters

]	Parameters estin	nated from	
	Ski	lls Model	Tra	ining set	Observed items	
	Multiple	NMF Conj. NMF Add. DINA DINO	• Slip • Guess	• Q-matrix	• Students skills mastery matrix	
Contributed skills	Single	IRT Expected	• Item di • Item di • Item O	scrimination	• Student Ability • Student Odds	
3	Zero	POKS	Initial C Odds ra Partial			

- Performance of a model over a data set
- Model parameters
- Performance vector
- Performance signature



Model	Performace			
Expected	0.72%			
POKS	0.80%			
IRT	0.74%			
NMF.Conj	0.94%			
Dina	0.99%			
NMF.Add	0.60%			
Dino	0.65%			

- Performance of a model over a data set
- Model parameters
- Performance vector
- Performance signature
- Performance prototype

The *performance vector* associated with the synthetic data of a model class.

- Performance of a model over a data set
- Model parameters
- Performance vector
- Performance signature
- Performance prototype
- Target performance vector

The performance vector of the real data set to classify.

Vector space of accuracy performances

 Performance vectors of datasets in columns(Data points in a part of performance space)

Model	Synthetic data set									
iviouei	Random	POKS	IRT	DINA	DINO	L.Conj.	L.Comp.			
Expected	0.75	0.91	0.90	0.72	0.72	0.78	0.93			
POKS	0.75	0.94	0.94	0.81	0.81	0.90	0.94			
IRT	0.75	0.91	0.95	0.73	0.73	0.79	0.89			
DINA	0.75	0.77	0.81	1.00	0.65	0.98	0.89			
DINO	0.75	0.63	0.56	0.66	1.00	0.68	0.91			
NMF.Conj	0.75	0.59	0.53	0.95	0.65	0.97	0.58			
NMF.Comp	0.75	0.76	0.79	0.59	0.93	0.70	0.98			

The diagonal generally displays the best performance

Vector space of accuracy performances

 Given a target vector, we want to define which columns are the closest to the target column

Model	Synthetic data set							Towart
Model	Random	POKS	IRT	DINA	DINO	L.Conj.	L.Comp.	Target
Expected	0.75	0.91	0.90	0.72	0.72	0.78	0.93	0.43
POKS	0.75	0.94	0.94	0.81	0.81	0.90	0.94	0.75
IRT	0.75	0.91	0.95	0.73	0.73	0.79	0.89	0.68
DINA	0.75	0.77	0.81	1.00	0.65	0.98	0.89	0.93
DINO	0.75	0.63	0.56	0.66	1.00	0.68	0.91	0.60
NMF.Conj	0.75	0.59	0.53	0.95	0.65	0.97	0.58	0.80
NMF.Comp	0.75	0.76	0.79	0.59	0.93	0.70	0.98	0.70

- Our hypothesis: the similarity of vectors can indicate the nature of data
- The nearest neighbour in this space can be a candidate for the ground truth

 $\ \ \, \textbf{Experiment} \,\, 1: \,\, \textbf{Predictive performance} \,\,$

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Research questions

- What is the performance vector of student skills assessment models over real and over synthetic data created using the same models?
 - Experiment 1 : Predictive *performance vector* of models over real and synthetic data sets

 $\ \ \, \textbf{Experiment 1: Predictive performance} \\$

Experiment 2 : Sensitivity of the Model performance

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

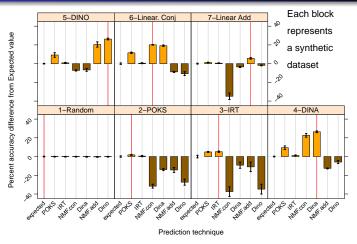
Datasets

Data set	Skills	Number Items	Mean Score	Q-matrix						
Synthetic										
1.Random	7	30	700	0.75	\mathbf{Q}_{01}					
2.POKS	7	20	500	0.50	Q_{02}					
3.IRT-2PL	5	20	600	0.50	Q_{03}					
4.DINA	7	28	500	0.31	\mathbf{Q}_5					
5.DINO	7	28	500	0.69	\mathbf{Q}_6					
Linear (Mate	rix factor	rization)								
6. Conj.	8	20	500	0.24	\mathbf{Q}_1					
7. Comp.	8	20	500	0.57	\mathbf{Q}_1					
	Real									
8.Fraction	8	20	536	0.53	\mathbf{Q}_1					
9.Vomlel	6	20	149	0.61	\mathbf{Q}_4					
10.ECPE 3		28	2922	0.71	Q ₃					
Fraction subsets and variants of \mathbf{Q}_1										
11. 1	5	15	536	0.53	\mathbf{Q}_{10}					
12. 2/1	3	11	536	0.51	Q ₁₁					
13. 2/2	5	11	536	0.51	Q ₁₂					
14. 2/3	3	11	536	0.51	Q ₁₃					

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over synthetic datasets

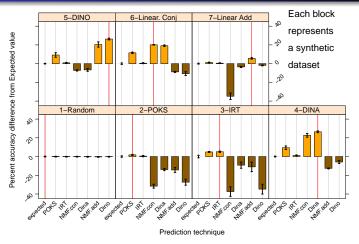


The random data set has a flat performance across techniques

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over synthetic datasets

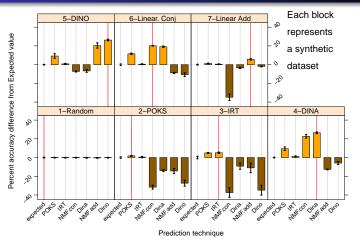


The highest performance is for the generative model behind the dataset

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over synthetic datasets

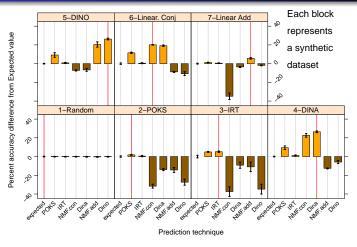


Motivation : Most of the models preform worse than simple expected prediction model

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over synthetic datasets

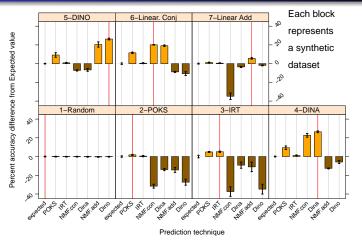


Data sets have discriminant pattern of performance vector across models

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over synthetic datasets

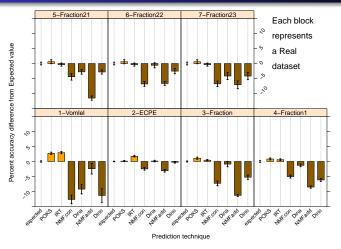


The capacity of recognizing a data set's true model relies on this discriminant characteristic

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over real datasets

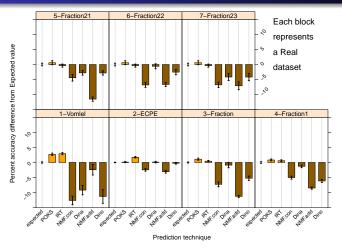


In most cases, the best performer is close to the baseline

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over real datasets

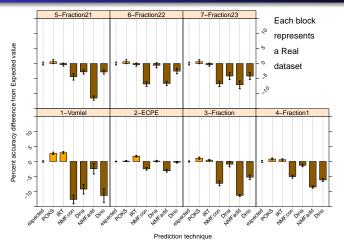


The pattern of the Fraction performance data set repeats over its subsets

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Predictive performance of models over real datasets



None of the real data sets show the large variance and the differences found in the synthetic data sets models

Experiment 1: Predictive performance
Experiment 2: Sensitivity of the Model performance
Experiment 3: Signature Approach

Experiment 4 : Signature vs. best performer

Research questions

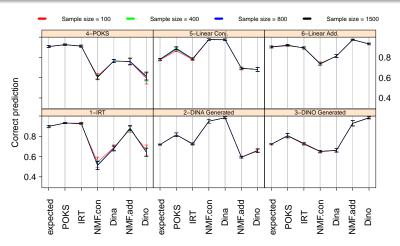
- What is the performance vector of student skills assessment models over real and over synthetic data created using the same models?
 - Experiment 1 : Predictive performance of models over real and synthetic data sets
- ② Is the performance vector unique to each synthetic data type (data from the same ground truth model)?
 - Experiment 2 : Sensitivity of the Model performance over different data generation parameters

Are they stable in addition to be discriminant?

Experiment 1 : Predictive performance
Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Variation of sample size over synthetic data sets

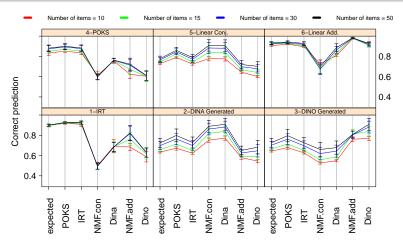


Obviously, the signature pattern did not change significantly for some parameters such as **Sample size**.

Experiment 1: Predictive performance
Experiment 2: Sensitivity of the Model performance
Experiment 3: Signature Approach

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

Variation of number of items over synthetic data sets



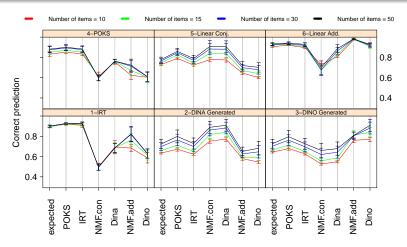
Even for synthetic data the performance of the ground truth model should not necessarily be close to 100%.

Experiment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

Variation of number of items over synthetic data sets



The Performance signature shifts down once the number of items degrades.

Experiment 1: Predictive performance

Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Data parameters

- Sample size (Number of students)
- Number of items
- Number of latent skills
- Item score variance
- Student score variance
- O Average success rate

Experiment 1: Predictive performance
Experiment 2: Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Data parameters

- Sample size (Number of students)
- Number of items
- Number of latent skills
- Item score variance
- Student score variance
- Average success rate

Conclusion:

- Data parameters can potentially influence the performance of a model
- For better comparison of the vectors, we also consider data characteristic parameters of the real data in the generation process

Experiment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 3: Signature Approach
Experiment 4: Signature vs. best performer

Research questions

- What is the performance vector of student skills assessment models over real and over synthetic data created using the same models?
 - Experiment 1 : Predictive performance of models over real and synthetic data sets
- ② ✓ Is the performance vector unique to each synthetic data type (data from the same ground truth model)?
 - Experiment 2 : Sensitivity of the Model performance over different data generation parameters
- Oan the performance vector be used to define a method to reliably identify the ground truth behind the synthetic data?
 - Experiment 3 : Model selection based on performance vector classification

Experiment 2 : Sensitivity of the Model performance

Experiment 3: Signature Approach
Experiment 4: Signature vs. best performer

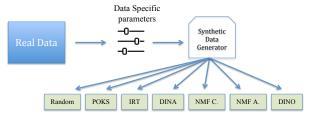
Signature framework



Experiment 2 : Sensitivity of the Model performance

Experiment 3: Signature Approach
Experiment 4: Signature vs. best performer

Signature framework

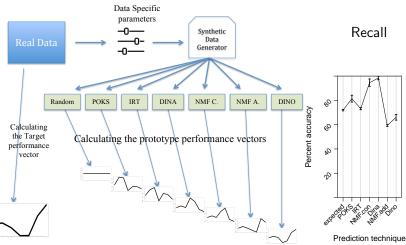


periment $oldsymbol{1}$: Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 3: Signature Approach
Experiment 4: Signature vs. best performer

Signature framework

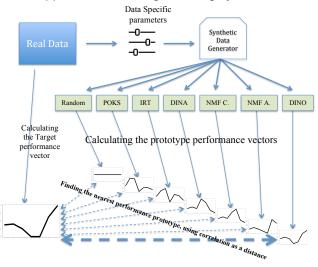


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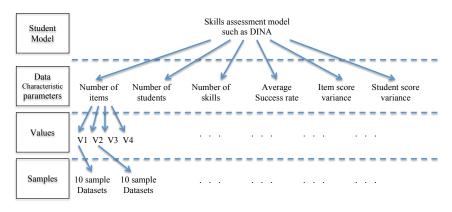


periment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance Experiment 3 : Signature Approach

Experiment 4 : Signature vs. best performer

Database of synthetic datasets

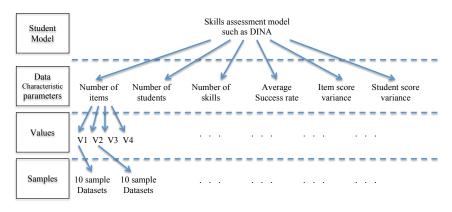


There exists 6 skills assessment models

Experiment 4 : Signature vs. best performer

Experiment 2: Sensitivity of the Model performance **Experiment 3: Signature Approach**

Database of synthetic datasets



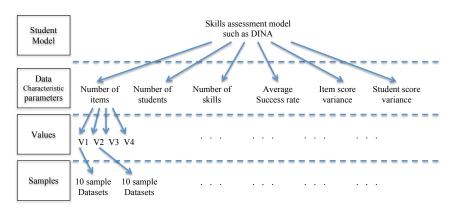
There exists 6 skills assessment models X 6 data characteristic parameters

speriment 1 : Predictive performance

Experiment 4 : Signature vs. best performer

Experiment 2 : Sensitivity of the Model performance Experiment 3 : Signature Approach

Database of synthetic datasets



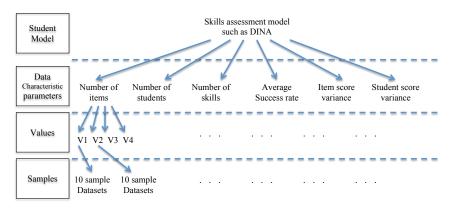
There exists 6 skills assessment models X 6 data characteristic parameters X 4 values

periment 1 : Predictive performance

Experiment 2: Sensitivity of the Model performance Experiment 3: Signature Approach

Experiment 4 : Signature vs. best performer

Database of synthetic datasets



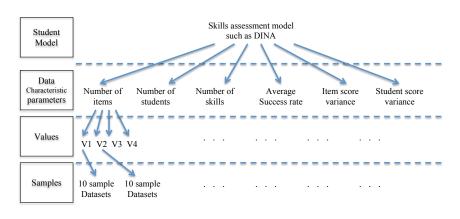
There exists 6 skills assessment models X 6 data characteristic parameters X 4 values X 10 samples = 1440 samples in the Database (DB)

eriment $oldsymbol{1}$: $oldsymbol{\mathsf{Predictive}}$ performance

Experiment 2: Sensitivity of the Model performance Experiment 3: Signature Approach

Experiment 4 : Signature vs. best performer

Database of synthetic datasets



$$|DB| = 1440 \text{ and } |DC| = 24$$

Experiment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

Prototype definition

eriment 1 : Predictive performan

Experiment 2: Sensitivity of the Model performance Experiment 3: Signature Approach

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

Prototype definition

- Given $c \in DC$ and $m \in \mathcal{M} : D = \{ \forall D_i^{(j)} \in DB | i = c, j = m \}$
- ullet \mathcal{N}^m is a centroid performance prototype defined for model m

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- $\mathcal{N}^m = AVG(Performance.vector(D))$

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- Pearson correlation coefficient is used as a measure of similarity between $\mathcal{T}^{(tm)}$ and \mathcal{N}^m (for data condition c)

eriment 1 : Predictive performanc

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Prototype definition

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- $\mathcal{N}^m = AVG(Performance.vector(D))$
- Pearson correlation coefficient is used as a measure of similarity between $\mathcal{T}^{(tm)}$ and \mathcal{N}^m (for data condition c)
- Next slid shows the average of correlation between $\mathcal{T}^{(tm)}$ and \mathcal{N}^m for all data parameter conditions in DC

Experiment 4 : Signature vs. best performer

Degree of similarity between six synthetic performance vector based on the correlation

Target performance vectors

Centroid synthetic

		POKS	IRT	NMF Conj.	DINA	NMF Add.	DINO
performance vectors	POKS	0.96					
	IRT	0.86	0.96				
	NMF Conj.	0.22	-0.20	0.96			
	DINA	0.02	-0.40	0.94	0.96		
	NMF Add.	0.44	0.75	-0.62	-0.73	0.93	
	DINO	-0.15	0.20	-0.70	-0.69	0.63	0.95

- The diagonal shows high correlations because it compares performance vectors of the same model generated datasets.
- Performance vectors with similar ground truth also show a high correlation.

periment 1 : Predictive

Experiment 2: Sensitivity of the Model performance Experiment 3: Signature Approach

Experiment 4 : Signature vs. best performer

Degree of similarity between six synthetic performance vector based on the correlation

Target performance vectors

Centroid synthetic

		POKS	IRT	NMF Conj.	DINA	NMF Add.	DINO
performance vectors	POKS	0.96					
	IRT	0.86	0.96				
	NMF Conj.	0.22	-0.20	0.96			
	DINA	0.02	-0.40	0.94	0.96		
	NMF Add.	0.44	0.75	-0.62	-0.73	0.93	
	DINO	-0.15	0.20	-0.70	-0.69	0.63	0.95

In general, correlation similarity provides a very good measure of model fit.

periment 1 : Predictive

Experiment 2 : Sensitivity of the Model performance Experiment 3 : Signature Approach

Experiment 4 : Signature vs. best performer

Degree of similarity between six real datasets and the ground truth based on the correlation

Target performance vectors of Real Datasets

Fraction subsets Vomlel ECPE Fraction 21 22 23 Performance Prototype Datasets Random 0.58 0.73 0.43 0.24 0.61 0.57 0.61 IRT 0.90 0.42 0.72 0.88 0.60 0.77 0.61 DINA -0.38-0.09 0.23 0.30 0.56 0.06 0.38 Synthetic DINO 0.34 0.15 -0.18-0.310.10 -0.080.38 0.70 0.83 POKS 0.75 0.40 0.83 0.950.80 NMF Coni. -0.05 0.54 0.51 0.55 0.66 0.33 0.57 NMF Add. 0.39 0.06 -0.04-0.19-0.030.13 0.28

The centroid performance vector of each model is the average of performance vectors of 10 generated datasets

Experiment 1 : Predictive performance
Experiment 2 : Sensitivity of the Model performance

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

Degree of similarity between six real datasets and the ground truth based on the correlation

Target performance vectors of Real Datasets

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Vomlel dataset shows a high correlation with IRT model

Degree of similarity between six real datasets and the ground truth based on the correlation

Target performance vectors of Real Datasets

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Fraction with its subset datasets show similarity with POKS model.

Experiment 1 : Predictive performance
Experiment 2 : Sensitivity of the Model performance

Experiment 3 : Signature Approach
Experiment 4 : Signature vs. best performer

Degree of similarity between six real datasets and the ground truth based on the correlation

Target performance vectors of Real Datasets

Fraction subsets ECPE Vomlel Fraction 21 22 23 Performance Prototype Datasets Random 0.58 0.73 0.43 0.24 0.61 0.57 0.61 IRT 0.90 0.42 0.72 0.88 0.60 0.77 0.61 DINA -0.38-0.090.23 0.30 0.56 0.06 0.38 Synthetic DINO 0.34 0.15 -0.18-0.310.10 -0.080.38 0.70 0.83 POKS 0.75 0.40 0.83 0.950.80 NMF Coni. -0.05 0.54 0.51 0.55 0.66 0.33 0.57 NMF Add. 0.39 0.06 -0.04-0.19-0.03 0.13 0.28

As expected, ECPE has the highest correlation with random generated dataset.

periment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 4: Signature vs. best performer

- What is the performance vector of student skills assessment models over real and over synthetic data created using the same models?
 - Experiment 1 : Predictive performance of models over real and synthetic data sets
- ② ✓ Is the performance vector unique to each synthetic data type (data from the same ground truth model)?
 - Experiment 2 : Sensitivity of the Model performance over different data generation parameters
- Solution Series Ser
 - Experiment 3: Model selection based on performance vector classification
- How does the method compare with the standard practice of using the model with the best performance?
 - Experiment 4 : Signature vs. best performer classification

periment 1: Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Problem specification

 What we did? to evaluate the ability of the Signature approach to identify the ground truth model

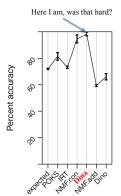
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Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Problem specification

- What we did? to evaluate the ability of the Signature approach to identify the ground truth model
- What we want to do? to compare the results of classification based on signature approach with the best performer approach.



Experiment 4 : Signature vs. best performer

Problem specification

- What we did? to evaluate the ability of the Signature approach to identify the ground truth model
- What we want to do? to compare the results of classification based on signature approach with the best performer approach.
- Reporting the accuracy of these classification in terms of F1 and accuracy measures

		Prediction outcome		
		Positive	Negative	
Actual	Positive	TP	FN	
value	Negative	FP	TN	

$$Precision = rac{TP}{TP + FP}$$
 $Recall = rac{TP}{TP + FN}$

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

$$F_{1} = \frac{Precision.Recall}{Precision + Recall}$$

periment $1: \mathsf{Predictive}$ performance

Experiment 2 : Sensitivity of the Model performance

Experiment 4: Signature vs. best performer

Signature classifier

eriment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 4: Signature vs. best performer

Signature classifier

Target performance vector : $\mathcal{T}^{(tm)} = Performance.vector(D_c^{(tm)} \in DB)$ where : $D_c^{(tm)}$ is characterized with data parameter condition $c \in DC$ and ground truth (tm)

• Given $c \in DC : D = \{ \forall D_i^{(j)} \in DB | i = c, j \in \mathcal{M} \}$

periment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Signature classifier

- Given $c \in DC : D = \{ \forall D_i^{(j)} \in DB | i = c, j \in \mathcal{M} \}$
- ullet Neighbors of $\mathcal{T}^{(tm)}$ are performance vectors of D

eriment 1 : Predictive performance

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Signature classifier

- Given $c \in DC : D = \{ \forall D_i^{(j)} \in DB | i = c, j \in \mathcal{M} \}$
- ullet Neighbors of $\mathcal{T}^{(tm)}$ are performance vectors of D
- A majority voting among the ground truth of 10 nearest neighbors to $\mathcal{T}^{(tm)}$ defines the estimated ground truth

xperiment 1 : Predictive performance

99%

Experiment 2 : Sensitivity of the Model performance

Experiment 4 : Signature vs. best performer

Results of signature vs. best performer classification

		Performance					
		Best Pe	rformer	Signature approach			
		F-Measure	Accuracy	F-Measure	Accuracy		
Models	POKS	0.719	0.871	0.998	99.9		
	IRT	0.625	0.908	0.998	99.9		
	NMF Conj.	0.502	0.887	0.985	99.5		
	DINA	0.734	0.891	1	100		
	NMF Add.	0.905	0.969	1	100		
	DINO	0.963	0.988	0.970	0.990		

75%

Total accuracy

• The F-measure increases when the signature approach is used for classification.

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- The F-measure increases when the signature approach is used for classification.
- In terms of individual scores per method, the accuracy increases when signature approach is used.

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Experiment 2 : Sensitivity of the Model performance

Experiment 3 : Signature Approach

Experiment 4 : Signature vs. best performer

Results of signature vs. best performer classification

Performance Best Performer Signature approach F-Measure Accuracy F-Measure Accuracy **POKS** 0.719 0.871 0.998 99.9 Models IRT 0.625 0.908 0.998 99 9 NMF Conj. 0.502 0.887 0.98599.5 DINA 0.734 0.891 100 NMF Add. 0.905 0.969 100 DINO 0.963 0.988 0.970 0.990 75% Total accuracy 99%

- The F-measure increases when the signature approach is used for classification.
- In terms of individual scores per method, the accuracy increases when signature approach is used.
- The total accuracy considers true positive numbers over number of datasets regardless of individual models

- What is the performance vector of student skills assessment models over real and over synthetic data created using the same models?
 - Experiment 1 : Predictive performance of models over real and synthetic data sets
 - In terms of signature pattern: it is unique for each generative model
 - In terms of data points in the performance vector space :
 They are data points in this space
 - For real data sets, the performances are not better than the expected performance
 - For synthetic data, datasets with different ground truths that share some concepts, show a high correlation.

- Predictive performance of models over real and synthetic data sets
- ② ✓ Is the performance vector unique to each synthetic data type (data from the same ground truth model)?
 - Experiment 2 : Sensitivity of the Model performance over different data generation parameters
 - Different parameters can create different points in the performance vector space
 - There would be a cloud of points for a particular model (Ground truth)
 - The cloud is not too dispersed

- Predictive performance of models over real and synthetic data sets
- Sensitivity of the Model performance over different data parameters
- Can the performance vector be used to define a method to reliably identify the ground truth behind the synthetic data?
 - Experiment 3: Model selection based on performance vector classification
 - A comparison between the target and the prototype signature
 - Datasets that share a common source have correlated performance vectors.

- Predictive performance of models over real and synthetic data sets
- ☑ ✓ Sensitivity of the Model performance over different data parameters
- How does the method compare with the standard practice of using the model with the best performance?
 - Experiment 4 : Signature vs. best performer classification
 - The ground truth model does not always correspond to the best performer and our approach provides a more reliable means

 to be extend over different models, different domains and more datasets

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- generalize to dynamic data and skills assessment models

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- generalize to dynamic data and skills assessment models
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- Application in other fields of study

Thank you

