

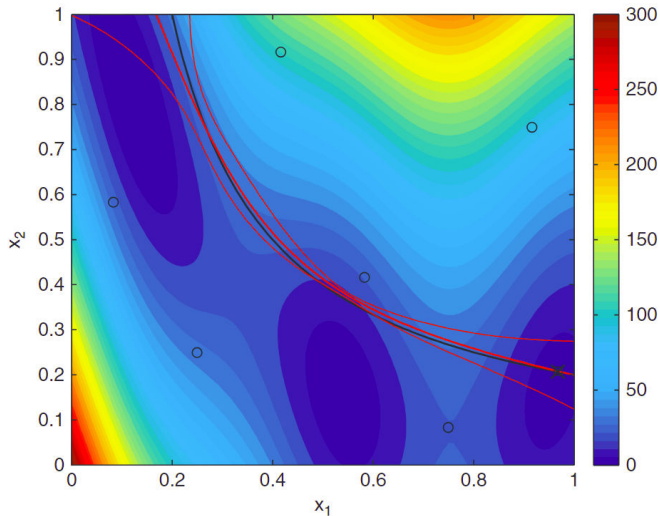
A tutorial on the refined Efficient Global Optimisation algorithm

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This tutorial is the MATLAB code for "A global-local meta-modelling technique for model updating" article [1].

The Test Functions

The first test function is a modified version of the Branin function [4] with an output scaled between 0 and 1 and two input variables. This function has two local minima and its contour plot is shown in Fig. 1.



The second test function is the three storey structure from the EI at LANL [5], the same as in [1]. Fig. 2 shows the system schematic and Fig. 3 the equivalent mass-spring-damper system.

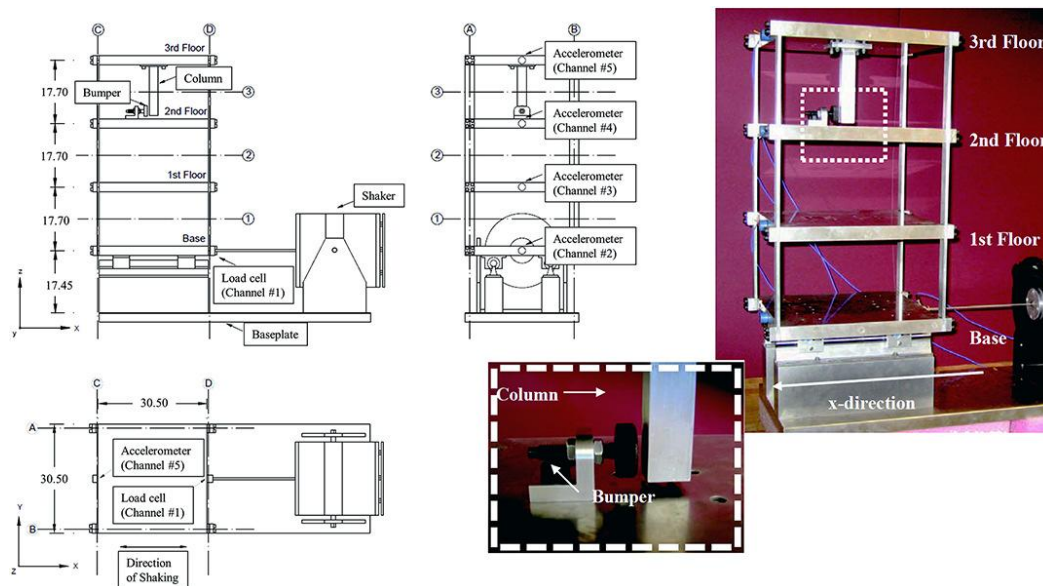


Fig. 2 Three storey structure schematic and photos (Adapted from [5]).

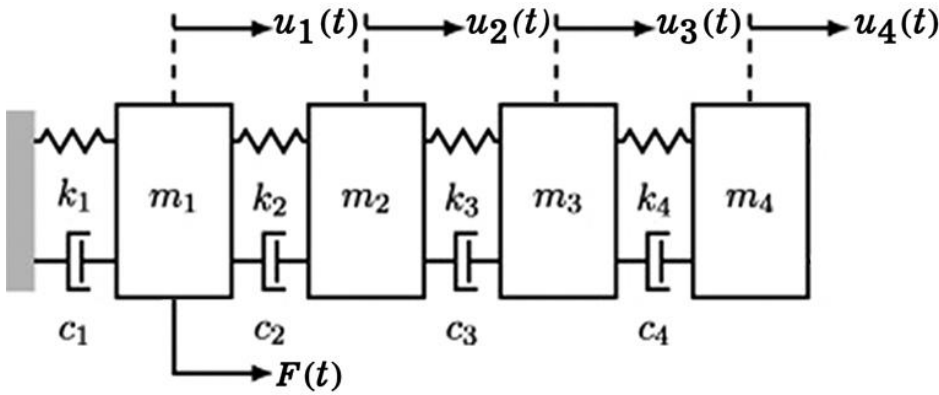


Fig. 3 Equivalent Mass spring damper system.

For the sake of this tutorial, a reduction in stiffness of 25% in the second interstory (k_3) is considered. Please note, only the three stiffness values of the interstories (k_{2-4}) are updated in this tutorial. The difference in the modal parameters between the two systems, quantified as the modified total modal assurance criterion (MTMAC), is to be minimised to characterise the change in stiffness. The numerical model developed in [1] is used for this task.

The Modified Branin Function

In this section the Modified Branin Function is minimised using the rEGO.

```
%% Preamble
close all
clear all
dd = split(fileparts(matlab.desktop.editor.getActiveFilename),'\Tutorial');
cd(dd{1}) %set working directory to main folder
addpath(genpath(dd{1})) % add paths to matlab only for this session
clear dd

%%-----

fun = @(x)braninmodif_n(x); % assign Branin function
num_vari = 2; % call number of variables
lwb = [0 0]; upb = [1 1]; % search bounds
eps1 = 10^(-3); eps2 = 10^(-4); % stopping criterion

[x,fval,results] = rEGO(fun,num_vari,lwb,upb,eps1,eps2)
```

```
iteration: 0, evaluation: 20, current best solution: 0.004209, real optimum: 0.000000
EI: 0.017693
iteration: 1, evaluation: 21, current best solution: 0.004209, real optimum: 0.000000
Stall iterations 1
EI: 0.024865
iteration: 2, evaluation: 22, current best solution: 0.004209, real optimum: 0.000000
Stall iterations 2
EI: 0.035834
iteration: 3, evaluation: 23, current best solution: 0.004209, real optimum: 0.000000
Stall iterations 3
EI: 0.012029
iteration: 4, evaluation: 24, current best solution: 0.004209, real optimum: 0.000000
Stall iterations 4
```

EI: 0.0042808
 iteration: 5, evaluation: 25, current best solution: 0.004209, real optimum: 0.000000
 Stall iterations 5
 EI: 0.0034022
 iteration: 6, evaluation: 26, current best solution: 0.001465, real optimum: 0.000000
 EI: 0.00083229
 iteration: 7, evaluation: 27, current best solution: 0.001465, real optimum: 0.000000
 iteration: 7, evaluation: 28, current best solution: 0.000003, difference: 0.000742
 , samples: 28.000000
 Refinement:0
 Distance is 0.046705
 EI: 0.0054203
 iteration: 8, evaluation: 29, current best solution: 0.000003, real optimum: 0.000000
 Stall iterations 2
 EI: 0.0033849
 iteration: 9, evaluation: 30, current best solution: 0.000003, real optimum: 0.000000
 Stall iterations 3
 EI: 0.0017241
 iteration: 10, evaluation: 31, current best solution: 0.000003, real optimum: 0.000000
 Stall iterations 4
 EI: 0.00016513
 iteration: 11, evaluation: 32, current best solution: 0.000003, real optimum: 0.000000
 iteration: 11, evaluation: 33, current best solution: 0.000003, difference: 0.000025
 , samples: 12.000000
 Refinement:1
 Distance is 0.0074717
 Stall iterations 5
 EI: 4.1224e-09
 iteration: 12, evaluation: 34, current best solution: 0.000003, real optimum: 0.000000
 iteration: 12, evaluation: 35, current best solution: 0.000000, difference: 0.000000
 , samples: 14.000000
 Refinement:1
 Distance is 0.0025392
 EI: 0
 iteration: 13, evaluation: 36, current best solution: 0.000000, real optimum: 0.000000
 iteration: 13, evaluation: 37, current best solution: 0.000000, difference: 0.000000
 , samples: 16.000000
 Refinement:1
 Distance is 0.0002505
 EI: 0


```
clear all
load LANL_3SS_dam_25_3.mat % load damaged modal parameters
load LANL_3SS.mat % load baseline modal parameters
```

Modal properties of the baseline system:

```
baseline(:,2:end)
```

```
ans = 6x3
    30.6968    54.2099    70.7509
     0.0600     0.0200     0.0080
    -1.0000    -1.0000    -0.4826
    -0.4217     0.8100     1.0000
     0.3287     0.8409    -0.9198
     0.8703    -0.8873     0.3989
```

Modal properties of the damaged system:

```
damaged(:,2:end)
```

```
ans = 6x3
    29.3673    50.2963    69.0295
     0.0600     0.0200     0.0080
    -0.9898    -1.0000    -0.5197
    -0.4659     0.5581     1.0000
     0.2406     0.9927    -0.7345
     1.0000    -0.8035     0.2298
```

Difference, in percentage, between damaged and baseline natural frequencies:

```
delta_w = 100.*(damaged(1,2:end)-baseline(1,2:end))./baseline(1,2:end)
```

```
delta_w = 1x3
   -4.3313   -7.2192   -2.4331
```

Diagonal of the MAC matrix of the damaged and baseline mode shapes:

```
mac = diag(compute_mac(damaged(2:end,2:end),baseline(2:end,2:end)))'
```

```
mac = 1x3
    0.9900    0.9707    0.9771
```

$$MTMAC_{residuals} = 1 - \prod_{i=1}^n \frac{MAC(\Phi_i^E, \Phi_i^N)}{\left(1 + \frac{|\omega_i^N - \omega_i^E|}{|\omega_i^N + \omega_i^E|}\right)}$$

```
yt = mac.*((1+abs((damaged(1,2:end)-baseline(1,2:end))./(damaged(1,2:end)+baseline(1,2:end)))));
mtmac=1-prod(yt)
```

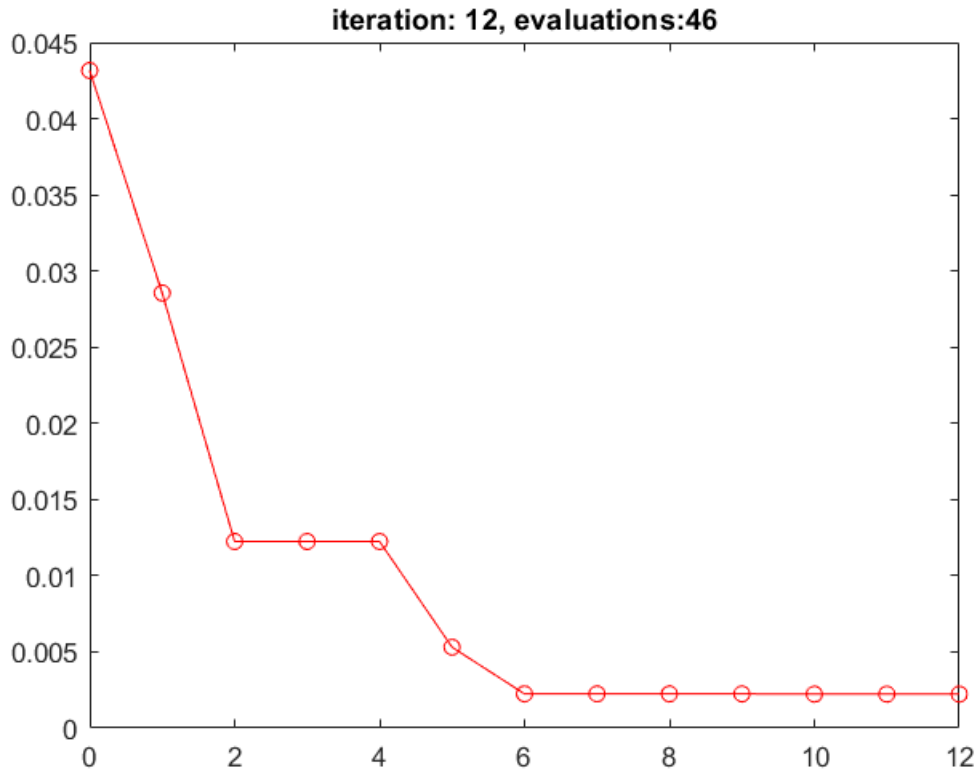
```
mtmac = 0.1253
```

By minimising the MTMAC, the damaged system can be identified starting from the baseline system:

```
fun = @(x)frame_u_opti([ones(1,4) x],damaged(:,2:end),'mtmac'); % assign Branin function
num_vari = 3; % call number of variables
lwb = [.5 .5 .5]; upb = [1.01 1.01 1.01]; % search bounds
eps1 = 10^(-3); eps2 = 10^(-4); % stopping criterion
```

```
[x,fval,results] = rEGO(fun,num_vari,lwb,upb,eps1,eps2)
```

```
iteration: 0, evaluation: 30, current best solution: 0.043161, real optimum: 0.000000
EI: 0.033213
iteration: 1, evaluation: 31, current best solution: 0.028559, real optimum: 0.000000
EI: 0.0056361
iteration: 2, evaluation: 32, current best solution: 0.012247, real optimum: 0.000000
EI: 0.0019854
iteration: 3, evaluation: 33, current best solution: 0.012247, real optimum: 0.000000
Stall iterations 2
EI: 0.026116
iteration: 4, evaluation: 34, current best solution: 0.012247, real optimum: 0.000000
Stall iterations 3
EI: 0.009809
iteration: 5, evaluation: 35, current best solution: 0.005309, real optimum: 0.000000
EI: 5.0411e-07
iteration: 6, evaluation: 36, current best solution: 0.005309, real optimum: 0.000000
iteration: 6, evaluation: 37, current best solution: 0.002244, difference: 0.001983
, samples: 37.000000
Refinement:0
Distance is 0.01406
EI: 0.0024706
iteration: 7, evaluation: 38, current best solution: 0.002244, real optimum: 0.000000
Stall iterations 2
EI: 0.0010568
iteration: 8, evaluation: 39, current best solution: 0.002244, real optimum: 0.000000
Stall iterations 3
EI: 0.00014783
iteration: 9, evaluation: 40, current best solution: 0.002244, real optimum: 0.000000
iteration: 9, evaluation: 41, current best solution: 0.002244, difference: 0.000430
, samples: 12.000000
Refinement:1
Distance is 0.0058791
Stall iterations 4
EI: 5.7887e-05
iteration: 10, evaluation: 42, current best solution: 0.002244, real optimum: 0.000000
iteration: 10, evaluation: 43, current best solution: 0.002228, difference: 0.000024
, samples: 14.000000
Refinement:1
Distance is 0.0024275
EI: 0.00013103
iteration: 11, evaluation: 44, current best solution: 0.002228, real optimum: 0.000000
iteration: 11, evaluation: 45, current best solution: 0.002228, difference: 0.000006
, samples: 16.000000
Refinement:1
Distance is 0.00069398
Stall iterations 2
EI: 0.00014511
```



```

iteration: 12, evaluation: 46, current best solution: 0.002228, real optimum: 0.000000
iteration: 12, evaluation: 47, current best solution: 0.002228, difference: 0.000000
, samples: 18.000000
Refinement:1
Distance is 2.8273e-05
x = 1x3
    0.9924    1.0100    0.7505
fval = 0.0022
results = struct with fields:
    initial: [30x4 double]
    min_x: [13x3 double]
    min_y: [0.0432 0.0286 0.0122 0.0122 0.0122 0.0053 0.0022 0.0022 0.0022 0.0022 0.0022 0.0022 0.0022]
    samples: [30 31 32 33 34 35 8 9 10 12 14 16]
        x: [18x3 double]
        y: [18x1 double]
evaluation: 47
    fval: 0.0022
iteration: 12
    EI: -1.4511e-04
    diff: 2.8273e-05
    flag: 0
refinement: 1
stall: 0

```

References

- [1] G. Dessena, D. I. Ignatyev, J. F. Whidborne, L. Zanutti Fragonara, A global-local meta-modelling technique for model updating, Computer Methods in Applied Mechanics and Engineering, Vol. (2023). (DOI: -)
- [2] G. Dessena, D. I. Ignatyev, J. F. Whidborne, L. Zanutti Fragonara, A Kriging Approach to Model Updating for Damage Detection, in European Workshop of Structural Health Monitoring 2022, LNCE volume 254, EWSHM 2022, pp. 245–255 (2023). (DOI: [10.1007/978-3-031-07258-1_26](https://doi.org/10.1007/978-3-031-07258-1_26))

- [3] G. Dessena, rEGO - A tutorial on the refined Efficient Global Optimisation, GitHub (2023) (DOI: -)
- [4] A. Forrester, A. Sobester, A. Keane, A., Engineering design via surrogate modelling: a practical guide. Wiley. (DOI: [10.1002/9780470770801](https://doi.org/10.1002/9780470770801))
- [5] E. Figueiredo, G. Park, J. Figueiras, C. Farrar, K. Worden, Structural health monitoring algorithm comparisons using standard data sets, Los Alamos National Laboratory (LANL), LA-14393 (DOI: [10.2172/961604](https://doi.org/10.2172/961604))