

**UTN.BA**

UNIVERSIDAD TECNOLÓGICA NACIONAL  
FACULTAD REGIONAL BUENOS AIRES

# Trabajo practico N°2

## APROXIMACION DE FUNCIONES TRANSFERENCIA

Grupo 3 – 08/06

Teoría de los circuitos II

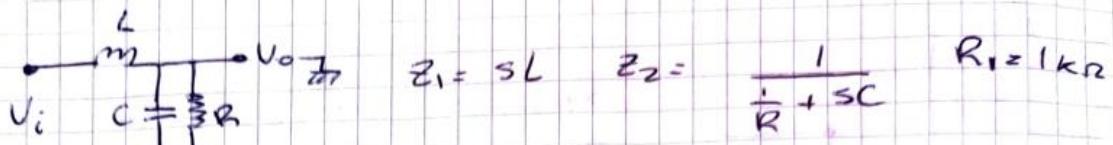
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Ejercicio 1)



$$\frac{V_o}{V_i} = \frac{Z_2}{Z_1 + Z_2} = \frac{\frac{1}{\frac{1}{R} + sC}}{sL + \frac{1}{\frac{1}{R} + sC}} = \frac{\frac{1}{\frac{1}{R} + sC}}{\frac{1}{R} + sC + s^2CL + s^2\frac{L}{R} + 1}$$

$$\frac{V_o}{V_i} = \frac{1}{s^2CL + s\frac{L}{R} + 1} - \frac{1/LC}{s^2 + \frac{1}{RC}s + 1/LC} = \frac{\omega_0^2}{s^2 + s\frac{\omega_0}{Q} + \omega_0^2}$$

Butterworth:  $\frac{V_o}{V_i} = \frac{1}{s^2 + s\sqrt{2} + 1}$

$$\frac{1}{RC} = \sqrt{2}, \text{ si } R = 1 \Rightarrow C = 0,707$$

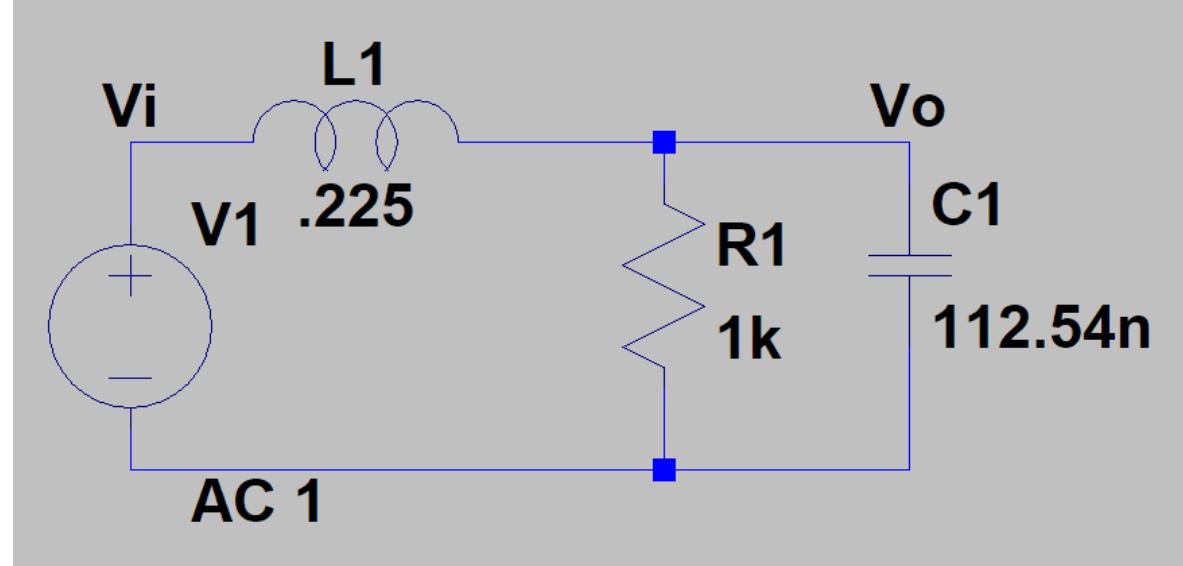
$$\omega_0^2 = 1 = \frac{1}{LC} \Rightarrow C = \frac{1}{L} \Rightarrow L = 1,414$$

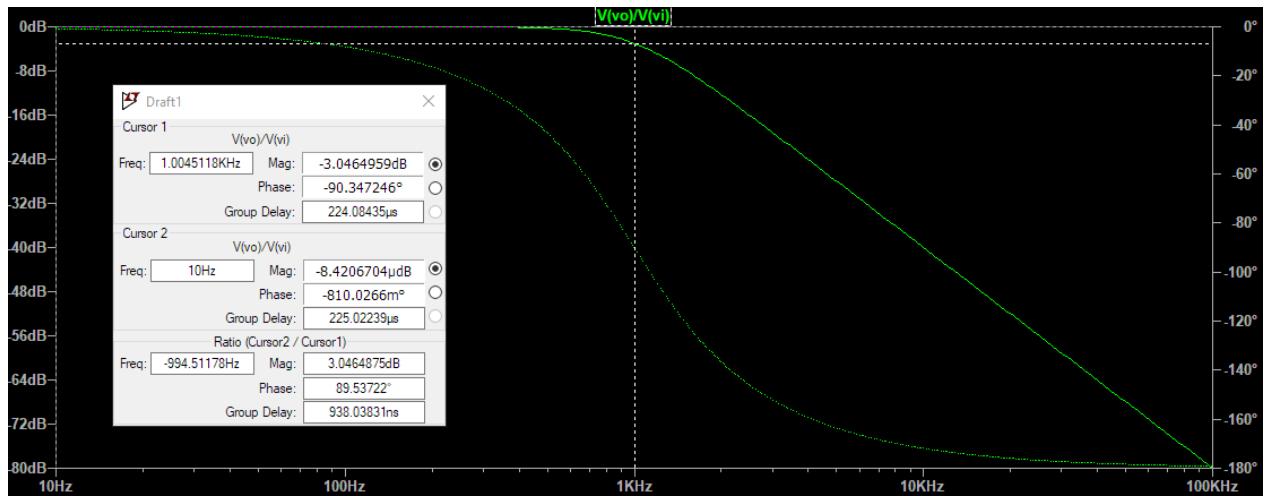
Desnormalizar:  $\Omega z = 1 \text{ k}\Omega$     $\Omega \omega = 2\pi / 1000 \text{ rad/s}$

$$R = 1 \cdot \Omega z = 1 \text{ k}\Omega$$

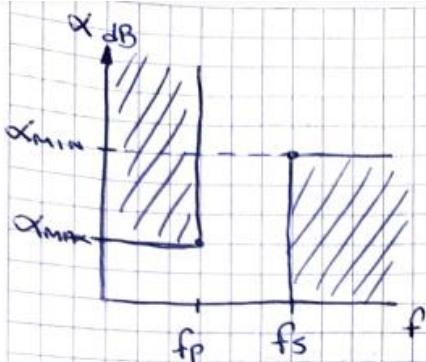
$$L = 1,414 \cdot \Omega z \frac{1}{\Omega \omega} = 0,225 \text{ H}$$

$$C = 0,707 \cdot \frac{1}{\Omega z} \cdot \frac{1}{\Omega \omega} = 112,54 \text{ nF}$$





Ejercicio 2)



$$\alpha_{\min} = 20 \text{ dB} \quad \alpha_{\max} = 0,5 \text{ dB}$$

$$f_p = 1000 \text{ Hz} \quad f_s = 2000 \text{ Hz}$$

Normalizo con  $\Omega_w = \omega_p$ :

$$\omega_p = 1, \quad \omega_s = 2$$

Cálculo  $\xi^2$ :

$$|T(\omega)|^2 = \frac{1}{1 + \xi^2 \omega^{2N}}$$

En  $\omega_p$ :

$$\alpha_{\max} = 10 \log (1 + \xi^2)$$

$$\xi^2 = 10 \frac{\alpha_{\max}}{10} - 1 = 0,122$$

En  $\omega_s$ :

$$\alpha_{\min} = 10 \log (1 + \xi^2 \omega_s^{2N})$$

Itero N

$N=2:$	$\alpha = 4,7 \text{ dB} < \alpha_{\min}$
$N=3:$	$\alpha = 9,45 \text{ dB} < \alpha_{\min}$
$N=4:$	$\alpha = 15,08 \text{ dB} < \alpha_{\min}$
$N=5:$	$\alpha = 21 \text{ dB} > \alpha_{\min} \quad \checkmark \quad [N=5]$

Poles cada  $\frac{\pi}{N} =$

- 1 polo sobre el eje j
- 2 pares de polos complejos conjugados

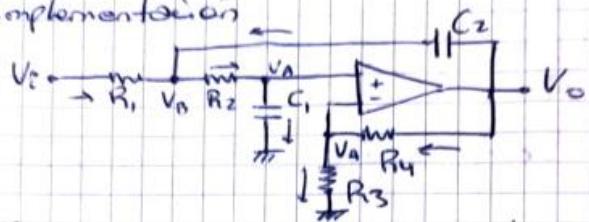
$$P \left\{ \begin{array}{l} P_1 = \cos(\pi) + j \sin(\pi) = -1 \\ P_{2-3} = \cos\left(\frac{4}{5}\pi\right) \pm j \sin\left(\frac{4}{5}\pi\right) = -0,81 \pm j 0,58 \\ P_{4-5} = \cos\left(\frac{3}{5}\pi\right) \pm j \sin\left(\frac{3}{5}\pi\right) = -0,31 \pm j 0,95 \end{array} \right.$$

$$Q \left\{ Q_1 = \frac{1}{2 \cos(\pi)} = 0,5 \right.$$

$$Q_{2-3} = \frac{1}{2 \cos\left(\frac{4}{5}\pi\right)} = 0,617$$

$$(Q_{4-5} = \frac{1}{2 \cos\left(\frac{3}{5}\pi\right)} = 1,613)$$

Implementación



$$V_A = \frac{V_o}{R_3 + R_4} \quad (1) \quad V_A = \frac{V_o}{A}, \quad A = \frac{R_3 + R_4}{R_4}$$

$$I_{C_1} = I_{R_2}: \quad V_A s C_1 = \frac{V_B - V_A}{R_2} \Rightarrow V_B = V_A (s C_1 R_2 + 1)$$

$$V_B = V_o \cdot \frac{s C_1 R_2 + 1}{A} \quad (2)$$

$$\frac{V_B - V_i}{R_1} + \frac{V_B - V_A}{R_2} + \frac{V_B - V_o}{s C_1} = 0$$

$$\frac{(s C_1 R_2 + 1) V_o}{R_1 A} - \frac{V_i}{R_1} + \frac{(s C_1 R_2 + 1) V_o}{R_2 A} - \frac{V_o}{A R_2} + \frac{(s C_1 R_2 + 1) V_o}{A} - \frac{V_o}{s C_1} = 0$$

$$\frac{V_i}{R_1} = V_o \left[ \frac{s C_1 R_2 + 1}{R_1 A} + \frac{s C_1 R_2 + 1}{R_2 A} - \frac{1}{R_2 A} + \frac{s C_1 R_2 + 1 - s C_2}{s C_1} \right]$$

$$\frac{V_i}{R_1} = V_o \left[ \frac{s C_1 R_2}{R_1} + \frac{1}{R_1} + \frac{s C_1 R_2}{R_2} + \frac{1}{R_2} - \frac{1}{R_2} + \frac{s C_1 R_2 R_2 + s C_2 - s C_2 A}{s C_1 R_2 R_2 + s C_2 A} \right]$$

$$\frac{V_i}{R_1} = V_o \left[ \frac{s^2 C_1 C_2 R_2 + s C_1 R_2 + s C_1 R_1 + s C_2 R_1 (1 + A)}{R_1} + 1 \right]$$

$$\frac{V_o}{V_i} = \frac{A}{s^2 C_1 C_2 R_2 + s(C_1 R_1 + C_1 R_2 + C_2 R_1(1 + A)) + 1}$$

$$\frac{V_o}{V_i} = A \frac{\frac{1}{R_1 R_2 C_1 C_2}}{s^2 + s \left( \frac{1}{R_1 C_2} + \frac{1}{R_2 C_1} + \frac{1 - A}{R_2 C_1} \right) + \frac{1}{R_1 R_2 C_1 C_2}} = \frac{A \frac{\omega_0^2}{Q}}{s^2 + s \frac{\omega_0}{Q} + \omega_0^2}$$

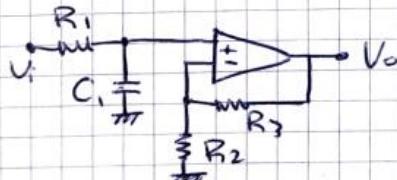
$$\omega_0^2 = \frac{1}{R_1 R_2 C_1 C_2}$$

$$\frac{\omega_0}{Q} = \frac{1}{R_1 C_2} + \frac{1}{R_2 C_1} + \frac{1-A}{R_2 C_1} = \frac{R_1 + R_2 + 1-A}{R_1 R_2 C_1 C_2}$$

$$\frac{\omega_0}{Q} = \frac{C_1(R_1 + R_2) + R_1 C_2(1-A)}{R_1 R_2 C_1 C_2} = [C_1(R_1 + R_2) + R_1 C_2(1-A)] \frac{\omega_0^2}{Q}$$

$$(C_1 R_1 + C_1 R_2 + R_1 C_2 - A R_1 C_2) \cdot \omega_0 = \frac{1}{Q}$$

Primer etapa:  $\omega_{01} = 1$ ,  $Q = 0,5$ ,  $A = 10 \text{ dB}$  (20dB)



$$T(s) = A \cdot \frac{\omega_{01}}{s + \omega_{01}}, \quad \omega_{01} = \frac{1}{R_1 C_1}$$

$$A = 1 + \frac{R_3}{R_2}$$

\* Adoptamos  $R_1 = 1$ ,  $C_1 = 1$ ,  $R_2 = 1$ ,  $R_3 = 9$

Segundo etapa:  $, Q_2 = 0,617$ ,  $A = 1$ ,  $\omega_{02} = 1$

$$\text{Sallen-Ker: } \omega_{02}^2 = \frac{1}{R_5 R_6 C_2 C_3} = 1$$

$$\frac{\omega_{02}}{Q_2} = 1,614 = \frac{1}{R_5 C_3} + \frac{1}{R_6 C_3} + \frac{1-A}{R_6 C_2} = \frac{R_5 + R_6}{R_5 R_6 C_3} = (R_5 + R_6) \omega_{02}^2 Q_2$$

$$\Rightarrow \frac{1}{\omega_{02} Q_2} = (R_5 + R_6) C_2 = 1,627,$$

$$\text{Adopto } [R_5 = 1], [R_6 = 1] \Rightarrow [C_2 = 0,8136]$$

$$\Rightarrow [C_3 = 1,2209] \text{ samblea}$$

Tercera etapa:

$$\omega_{03}^2 = \frac{1}{R_7 R_8 C_4 C_5} = 1$$

$$Q_3 = 1,613, A = 1$$

$$\frac{\omega_{03}}{Q_3} = 0,6195 = \frac{1}{R_7 C_5} + \frac{1}{R_8 C_5} = \frac{R_8 + R_7}{R_8 R_7 C_5} = \frac{(R_8 + R_7) \omega_{03}^2 C_4}{R_8 R_7 C_5}$$

$$\frac{1}{\omega_{03} Q_3} = 1,612 = (R_8 + R_7) C_4$$

$$\text{Adopto: } [R_8 = 1], [R_7 = 1] \Rightarrow [C_4 = 0,806]$$

$$\Rightarrow [C_5 = 1,240]$$

$$\text{Desnormalización } \underline{\Omega}_Z = 1k; \quad \underline{\Omega}\omega = \frac{1}{2\pi 1000} \cdot \underline{\xi}^{1/2} = \frac{1}{7754}$$

$$R_1 = R_2 = R_4 = R_5 = R_6 = R_7 = R_8 = 1k\Omega$$

$$R_3 = 9k\Omega$$

El cálculo de Q  
fue para radio unitario

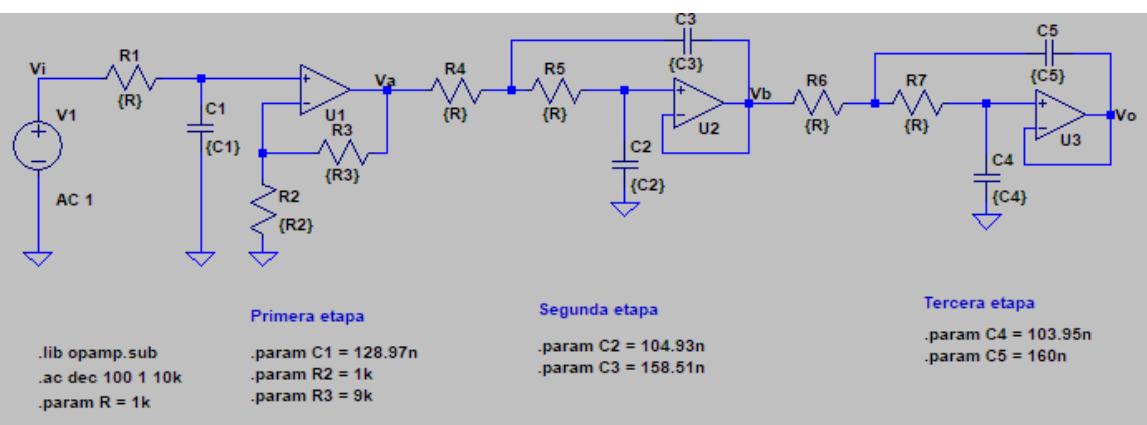
$$C_1 = \frac{1}{\underline{\Omega}_Z} \cdot \underline{\Omega}\omega = 128,97\text{nF}$$

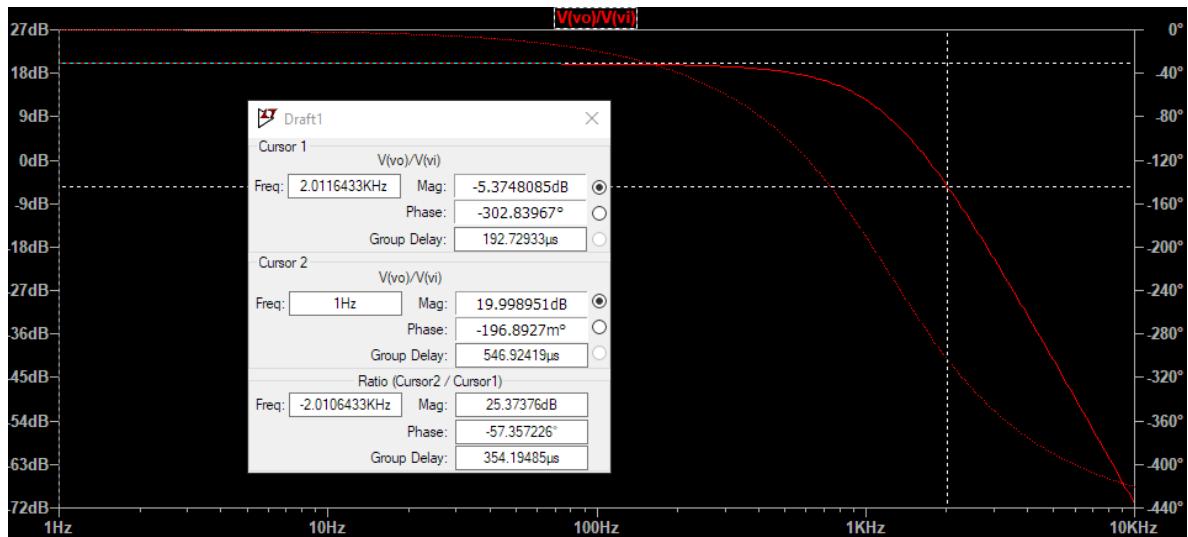
$$C_2 = \frac{0,806}{\underline{\Omega}_Z} \cdot \underline{\Omega}\omega = 104,93\text{nF}$$

$$C_3 = \frac{1,2291}{\underline{\Omega}_Z} \cdot \underline{\Omega}\omega = 158,51\text{nF}$$

$$C_4 = \frac{0,806}{\underline{\Omega}_Z} \cdot \underline{\Omega}\omega = 103,95\text{nF}$$

$$C_5 = \frac{1,2405}{\underline{\Omega}_Z} \cdot \underline{\Omega}\omega = 160\text{nF}$$





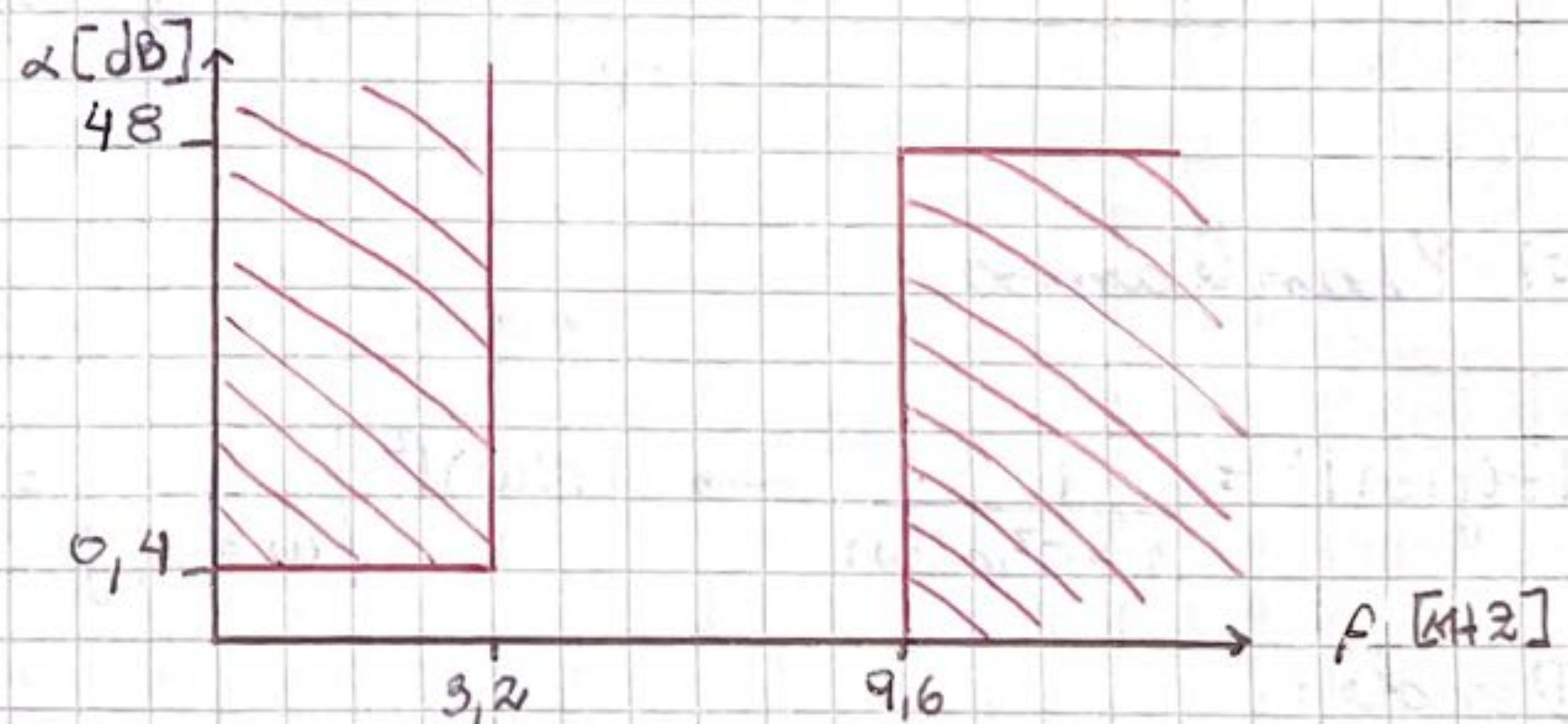
Ganancia de 20 dB sobre la banda de paso y 25 dB en la frecuencia de corte.

- ③ Un filtro pasa-bajos Butterworth se diseña para obtener una atenuación de 48 dB para frecuencias mayores a 9,6 kHz, con una atenuación máxima de 0,4 dB desde continua hasta 3,2 kHz.
- Determinar el orden del filtro y el parámetro  $\epsilon$ .
  - Graficar la respuesta en módulo del filtro.
  - Determinar la ubicación de polos y ceros.
  - Sintetizar el circuito utilizando estructuras Kerwin-Huelsman-Newcomb (KHN, también conocido como Variable de estado) y simular verificando las condiciones de diseño.

Resolución:

- Armamos la plantilla de nuestro pasa-bajos.

$$\left\{ \begin{array}{l} \alpha_{MAX} = 0,4 \text{ dB} \\ \alpha_{MIN} = 48 \text{ dB} \\ w_p = 2\pi \cdot 3,2 \text{ kHz} \\ w_s = 2\pi \cdot 9,6 \text{ kHz} \end{array} \right.$$



Luego, calculamos:

$$\epsilon^2 = 10^{\frac{\alpha_{MAX}/10}{0,4/10}} - 1 = 10^{48/10} - 1 = 0,0965$$

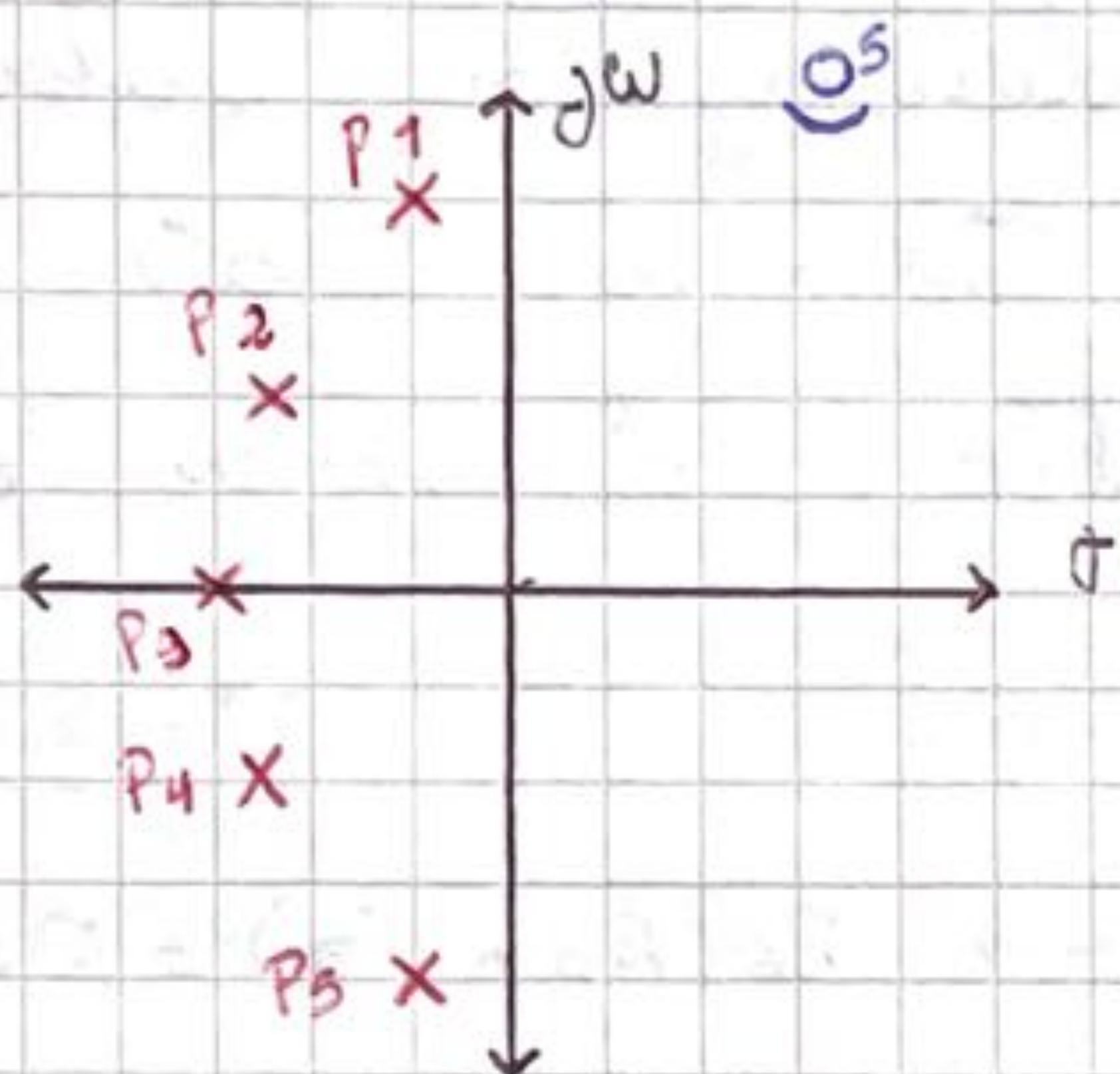
$$\epsilon = 0,3106$$

→

\* Despejamos  $P_1, P_2$  y  $P_3$ , ya que  $P_4 = P_2^*$  y  $P_5 = P_1^*$ .

$$\begin{aligned} \bullet P_1 &= T_1 + W_1 = -0,119 - j 1,02 = 1,027 e^{j 1,45} \\ \bullet P_2 &= T_2 + W_2 = -0,3124 - j 0,63 = 0,703 e^{j 1,11} \\ \bullet P_3 &= T_3 + W_3 = -0,386 = 0,386 e^{j \pi} \end{aligned}$$

Como es un filtro pasa-bajos, los 5 ceros se ubican en el infinito. Entonces:



d) Armamos nuestra transferencia a partir de los polos indicados y lo planteamos como una cascada de un pasa-bajos de orden 1 con dos pasa-bajos de orden 2.

$$T(s) = \frac{0,386}{s + 0,386} + \frac{1,053}{s^2 + 50,238s + 1,053} + \frac{0,494}{s^2 + 50,625s + 0,494}.$$

Sabemos que:

$$\textcircled{i} \quad \left\{ \omega_n^2 = 0,386 \right.$$

$$\textcircled{ii} \quad \left\{ \omega_n^2 = 1,053 \right. \\ Q_2 = 4,312$$

$$\textcircled{iii} \quad \left\{ \omega_n^2 = 0,494 \right. \\ Q_3 = 1,125$$

Hugo, normalizamos con:  $\omega_p = \sqrt{\omega} = 2\pi \cdot 3, 2 \text{ kHz}$ . Así:

$$\begin{cases} \omega_p' = 1 \\ \omega_s' = 3 \end{cases}$$

y finalmente, iteramos para encontrar  $m$ :

$$\alpha_{MIN} = 10 \log \left\{ 1 + \varepsilon^2 \cos^2 h \left[ m \omega_p^{-1} h / \omega_s' \right] \right\}$$

Para  $m = 5$ ,  $\alpha_{MIN} = 54,3 \text{ dB} > 48 \text{ dB} \rightarrow \boxed{m = 5}$

b) Graficamos la respuesta en módulo de un filtro pasa-bajos Butterworth de orden 5:



c) Planteamos:

$$|T(j\omega)|^2 = \frac{1}{1 + c^2 m(\omega)} \rightarrow |T(j\omega)|^2 \Big|_{\omega = s/j} = \frac{1}{1 + c^2 m(s/j)}$$

Donde:

$$\begin{cases} t_k = -\operatorname{senh} \alpha \cdot \operatorname{sen} (\pi (2k-1/2n)) \\ \omega_k = \cosh \alpha \cdot \cos (\pi (2k-1/2n)) \end{cases}$$

$$\text{Siendo } \alpha = \frac{1}{m} \operatorname{sech}^{-1} \left( \frac{1}{\varepsilon} \right) = 0,3771$$

Además, la transferencia de segundo orden de la estructura KHN es:

$$\frac{V_2}{V_1} = \frac{\frac{R_6(R_2+R_3)}{R_3(R_1+R_6)}}{K} \cdot \frac{\frac{R_3}{R_4 R_5 C_2 C_1 R_2}}{s^2 + s \frac{R_6(R_2+R_3)}{R_4 R_2 (R_1+R_6) \cdot C_1} + \frac{R_3}{R_4 R_5 C_2 C_1 R_2}}$$

Donde:

$$\omega_0 = \sqrt{\frac{R_3}{R_4 R_5 C_2 C_1 R_2}} \quad \text{y} \quad \varphi = \frac{\omega_0}{\sqrt{R_4 R_2 (R_1+R_6) C_1}}$$

Entonces, comenzamos a desarrollar sabiendo que  $K=1$  y que como tenemos más grados de libertad que parámetros, debemos adoptar ciertos valores.

$$K=1 \rightarrow \frac{R_6(R_2+R_3)}{R_3(R_1+R_6)} = 1 \rightarrow R_6(R_2+R_3) = R_3(R_1+R_6)$$

Como tenemos 2 variables y 8 grados de libertad, adoptamos:

$$\left\{ \begin{array}{l} C_1 = C_2 = 1 \text{ mF} \\ R_6 = R_4 = 1 \text{ kN} \\ R_2 = R_3 = 1 \text{ kN} \\ R_1 \rightarrow \text{controlo } \omega_0 \\ R_5 \rightarrow \text{controlo } \varphi. \end{array} \right.$$

Entonces:

$$\omega_0 = \sqrt{\frac{10^3}{2 R_5}} \quad \text{y} \quad \varphi = \sqrt{\frac{10^3}{R_5 K}} \cdot \frac{R_1 + 1 \text{ kN}}{2 \text{ kN}}$$

calculamos:

$$\textcircled{II} \quad \left\{ \begin{array}{l} \omega_0^2 = 1,053 \rightarrow \omega_0 = 1,0262 \\ Q = 4,312 \end{array} \right.$$

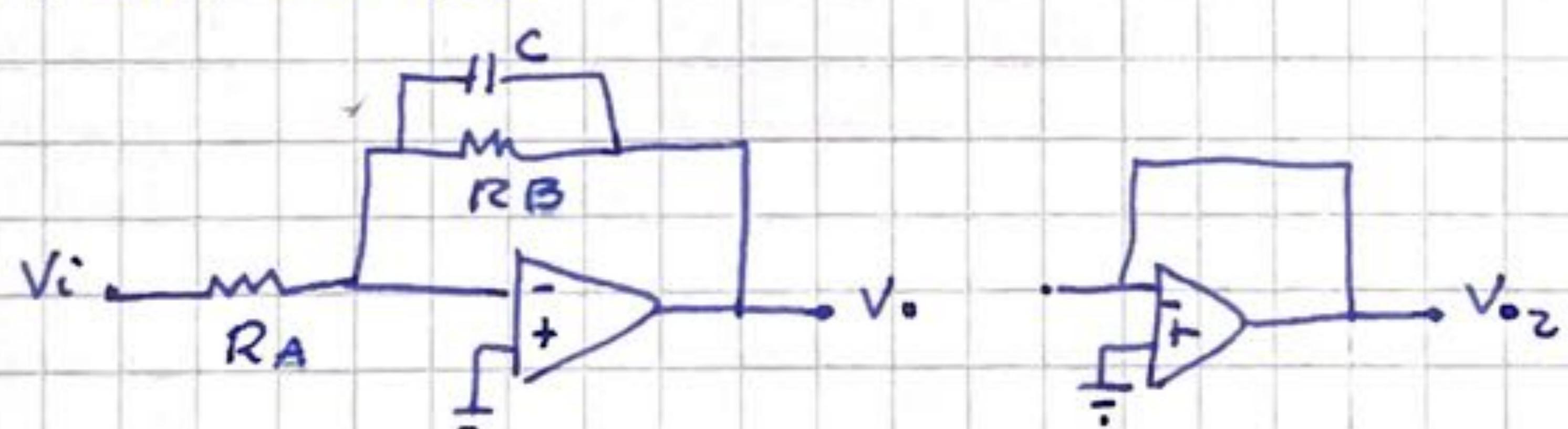
$$\left\{ \begin{array}{l} R_5 = 949,59 \approx 950 \Omega \\ R_1 = 7403,82 \Omega \end{array} \right.$$

$$\textcircled{III} \quad \left\{ \begin{array}{l} \omega_0^2 = 0,494 \rightarrow \omega_0 = 0,703 \\ Q = 1,125 \end{array} \right.$$

$$\left\{ \begin{array}{l} R_S = 2023,44 \Omega \\ R_1 = 2200,57 \Omega \rightarrow R_1 \approx 2200 \Omega \end{array} \right.$$

$$\textcircled{I} \quad \text{Si toda la estructura: } T(s) = \frac{A}{s+A}$$

Planteamos:



$$\frac{V_{02}}{V_i} = \frac{R_B}{R_A} \cdot \frac{1/R_B C}{s + 1/R_B C}$$

Adoptamos  $R_B = R_A$  y luego:

$$\cdot 1/R_B C = \omega_0 = \sqrt{0,386}$$

Adoptamos  $R_B = 1k\Omega$  y despejamos  $C$ :

$$C = 1,61 \times 10^{-3} F.$$

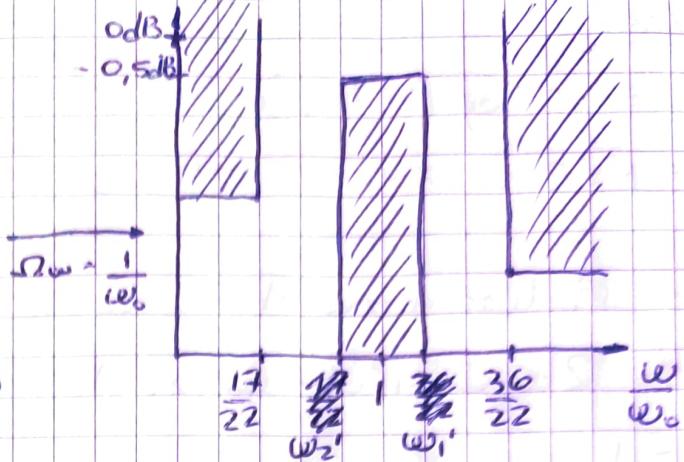
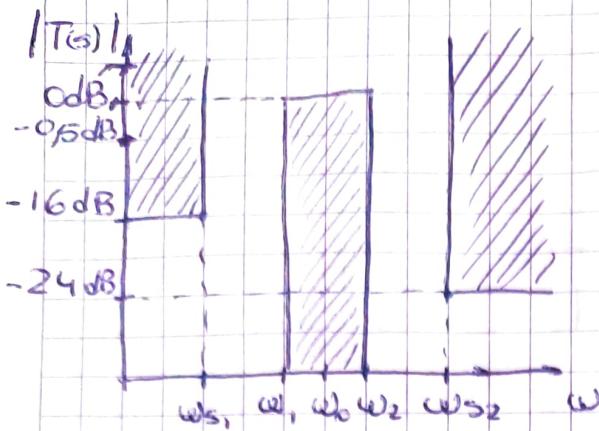
\* De esta manera calculamos todos los

componentes de nuestro filtro. Ahora, debemos desnormalizar los componentes que dependen de la frecuencia con muestra  $\pi w = 3,2 \times 4\pi \cdot 2\pi$

$$\cdot C_1 = C_2 = 10 \text{ mF} / \pi w = 4,974 \times 10^{-4} \text{ F.}$$

$$\cdot C = 8,007 \times 10^{-8} \text{ F.}$$

Ejercicio 4)



$$\omega_0 = \sqrt{\omega_1 \omega_2} = 1 \rightarrow \omega_2 = \frac{1}{\omega_1}$$

$$Q = \frac{\omega_0}{\omega_2 - \text{leq}_1} = 5 \rightarrow \frac{1}{\omega_2 - \frac{1}{\omega_1}} = 5 \rightarrow \omega_2^2 - \frac{1}{5} \omega_2 - 1 = 0$$

$$\omega_{S1} = \frac{17}{22}, \quad \omega_{S2} = \frac{36}{22}$$

$$\Omega_{S1} = \frac{Q(\omega_{S1}^2 - 1)}{\omega_{S1}} = -2,607$$

$$\Omega_{S2} = \frac{Q(\omega_{S2}^2 - 1)}{\omega_{S2}} = 5,126$$

Chebyshev:

$$|T(j\omega)|^2 = \frac{1}{1 + \xi^2 C_n^2(\omega)}, \quad |\overline{T(j\omega_0)}|^2 = \frac{1}{1 + \xi^2}$$

$$\alpha_{\max} = 10 \log(1 + \xi^2)$$

$$\xi^2 = 10 \frac{\alpha_{\max}}{10} - 1 \rightarrow \boxed{\xi^2 = 0,122}$$

Para  $\Omega_{S1}$ :

$$\alpha_{\min} = 10 \log(1 + \xi^2 C_n^2(\omega))$$

$$\alpha_{\min} = 10 \log(1 + \xi^2 \cosh^2(N \cosh^{-1}(\Omega_{S1})))$$

$$\begin{cases} N=2: \alpha = 13,085 \text{ dB} \\ N=3: \alpha = 26,87 \text{ dB} \end{cases} \quad \text{X} > \alpha_{\min}$$

Para  $\omega_{S2}$ :

$$\alpha_{\min} = 10 \log (1 + \xi^2 \cosh^2 (N \cosh^{-1}(\omega_{S2})))$$

$$\hookrightarrow N=3; \quad \alpha = 45,24 \text{ dB} \quad \textcircled{V} \quad > \alpha_{\min}$$

## Funciones Polinómicas Armónicas de Chebyshev

$$C_n(\omega) = 2\omega C_{n-1}(\omega) - C_{n-2}(\omega)$$

$$C_0(\omega) = 1$$

$$C_1(\omega) = \omega$$

$$C_2(\omega) = 2\omega^2 - 1$$

$$C_3(\omega) = 4\omega^3 - 3\omega$$

$$|T_L(\omega)|^2 = \frac{1}{1 + \xi^2 C_3^2(\omega)} = \frac{1}{1 + \xi^2 (4\omega^3 - 3\omega)} = \frac{1}{1 + 16\xi^2 \omega^6 - 24\xi^2 \omega^4 + 9\xi^2 \omega^2}$$

$$|T(s)|^2 = T(s) \cdot \overline{T(-s)} = \frac{1}{1 - 16\xi^2 s^6 - 24\xi^2 s^4 + 9\xi^2 s^2} = \frac{1}{(s^3 + as^2 + bs + c)(s^3 + as^2 - bs + c)}$$

$$|T_L(s)|^2 = \frac{1/16\xi^2}{-s^6 - \frac{3}{2}s^4 - \frac{9}{16}s^2 + 1/16\xi^2} = \frac{1}{-s^6 + (a^2 - 2b)s^4 + (2ac - b^2)s^2 + c^2}$$

$$\textcircled{1} \quad -\frac{3}{2} = a^2 - 2b \rightarrow b = \frac{a^2}{2} + \frac{3}{4} \rightarrow b^2 = \frac{a^4}{4} + a^2 \cdot \frac{3}{2} + \frac{9}{16} \quad \textcircled{4}$$

$$\textcircled{2} \quad -\frac{9}{16} = 2ac - b^2$$

$$\textcircled{3} \quad c^2 = \frac{1}{16\xi^2} \rightarrow \boxed{c = 0,7157}$$

$$\textcircled{4} \text{ en } \textcircled{2}: \quad -\frac{9}{16} = 2ac - \frac{a^4}{4} - a^2 \cdot \frac{3}{2} - \frac{9}{16} \Rightarrow 2ac - \frac{a^4}{4} - a^2 \cdot \frac{3}{2} = 0 \\ -a \left( \frac{a^3}{4} + a^2 \cdot \frac{3}{2} - 2c \right) = 0$$

$$\textcircled{1}: \quad b = \frac{1,253^2}{2} + \frac{3}{4} = \boxed{1,535 = b} \quad \boxed{a = 1,253}$$

$$T_L(s) = \frac{c}{s^3 + as^2 + bs + c} = \frac{0,7157}{s^3 + 1,253s^2 + 1,535s + 0,7157}$$

$$\text{Factorizo: } T_L(s) = \frac{0,7157}{(s+0,6266)(s^2 + 0,6266s + 1,1425)}$$

$$T_L(s) = \frac{0,6266}{s+0,6266} \cdot \frac{1,142}{s^2 + s \cdot 0,6266 + 1,142}$$

$T_1(s)$        $T_2(s)$

$T_1(s)$ :     $s \rightarrow Q \frac{(s^2 + 1)}{s}$

$$T_1(s) = \frac{0,6266}{Q \frac{(s^2 + 1)}{s} + 0,6266} = \frac{s \frac{0,6266}{Q}}{s^2 + Q \frac{0,6266}{s} + 1} = \frac{s \cdot 0,1253}{s^2 + s \cdot 0,1253 + 1}$$

$T_2(s)$ :     $s \rightarrow Q \frac{(s^2 + 1)}{s}$

$$T_2(s) = \frac{1,142}{Q^2 \frac{(s^2 + 1)^2}{s^2} + Q \frac{(s^2 + 1)}{s} \cdot 0,6266 + 1,142}$$

$$T_2(s) = \frac{s^2 \cdot 1,142}{s^4 Q^2 + s^3 (0,6266 \cdot Q) + s^2 (2Q^2 + 1,142) + s (0,6266 \cdot Q) + Q^2}$$

Con  $Q=5$ :

$$T_2(s) = \frac{s^2 \frac{1,142}{Q^2}}{s^4 + s^3 \frac{0,6266}{Q} + s^2 \left(2 + \frac{1,142}{Q^2}\right) + s \frac{0,6266}{Q} + 1}$$

$$T_2(s) = \frac{s^2 \cdot 0,0457}{s^4 + s^3 \cdot 0,1253 + s^2 \cdot 2,046 + s \cdot 0,1253 + 1}$$

↳ Polos en:  $(-0,03452 \pm j1,107) \times (-0,02813 \pm j0,9022)$  12,58

$$\therefore T_2(s) = \frac{s \cdot 0,06904}{s^2 + s \cdot 0,06904 + 1,227} \cdot \frac{s \cdot 0,0526}{s^2 + s \cdot 0,0526 + 0,8148}$$

$$\Rightarrow T_B(s) = 12,58 \underbrace{\frac{s \cdot 0,1253}{s^2 + s \cdot 0,1253 + 1}}_{H} \cdot \underbrace{\frac{s \cdot 0,06904}{s^2 + s \cdot 0,06904 + 1,227}}_{SOS\ 2} \cdot \underbrace{\frac{s \cdot 0,0526}{s^2 + s \cdot 0,0526 + 0,8148}}_{SOS\ 3}$$

$\omega_{01} = 1$   
 $Q_1 = 7,98$

$\omega_{02} = 1,1077$   
 $Q_2 = 16,04$

$\omega_{03} = 0,9022$   
 $Q_3 = 16,04$

(EJ 5)

$$\lambda = 5$$

$$Att_{MIN} = 43 \text{ dB}$$

$$Att_{MAX} = 0,4 \text{ dB}$$

CHEBYSHEV

$$|T(s)|^2 = \frac{1}{1 + g^2 G_s^2} = \frac{1}{1 + g^2 (16\omega^5 - 20\omega^3 - 4\omega)^2}$$

$$G_1 = 2\omega(4\omega^3 - 3\omega) - \cancel{G_2} \quad 2\omega^2 - 1$$

$$G_5 = 2\omega(4\omega^5 - 4\omega^3)(4\omega^3 - 3\omega) - 4\omega^3 - 2\omega - 4\omega^3 - 3\omega$$

$$G_S = 16\omega^5 - 20\omega^3 - 8\omega^3 - 4\omega - \cancel{4\omega^3}$$

$$G_S = 16\omega^5 - 24\omega^3 - 4\omega$$

$$1 + g^2 (16\omega^5 - 24\omega^3 - 4\omega)$$

$$P_1 = -0,386$$

$$P_{2,3} = -0,312 \pm j0,63$$

$$P_{4,5} = -0,119 \pm j1,019$$

~~SOS 1~~

$$\frac{0,386}{s + 0,386} \cdot \frac{0,494}{s^2 + 0,624s + 0,494} = \frac{0,386}{s + 0,386} \cdot \frac{0,494}{s^2 + 0,624s + 0,494}$$

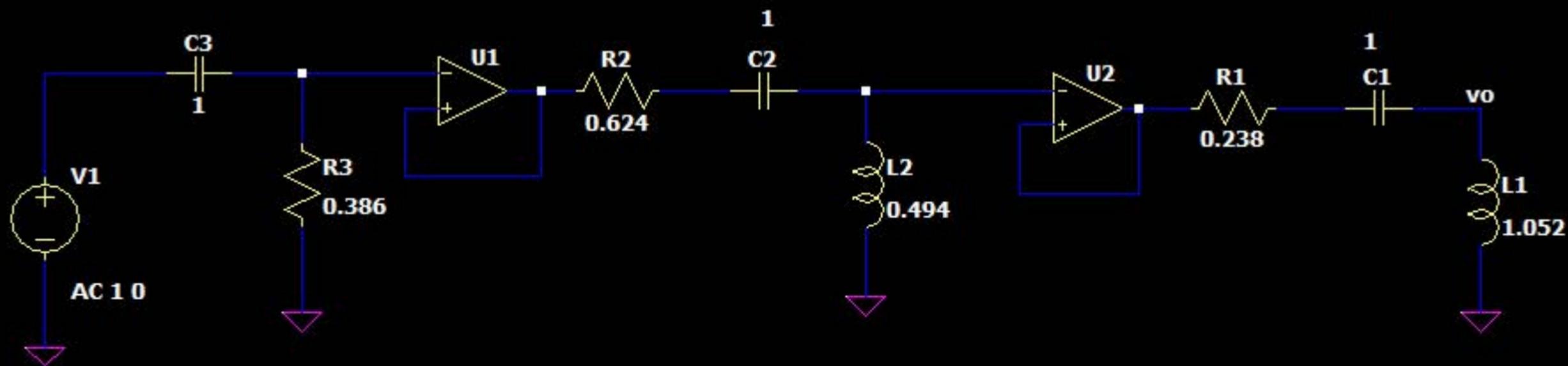
~~SOS<sub>1</sub>~~

$$\frac{1,052}{s^2 + 0,238s + 1,052} = \frac{1,052}{s^2 + 0,238s + 1,052}$$

~~SOS<sub>3</sub>~~

$$\begin{array}{c}
 \frac{s}{s+2,59} \quad \frac{s^2}{s^2 + 1,263s + 2,024} \quad \frac{s^2}{s^2 + 59226 + 0,95} \\
 \text{SOS\_HP}_1 \quad \text{SOS\_HP}_2 \quad \text{SOS\_HP}_3
 \end{array}$$

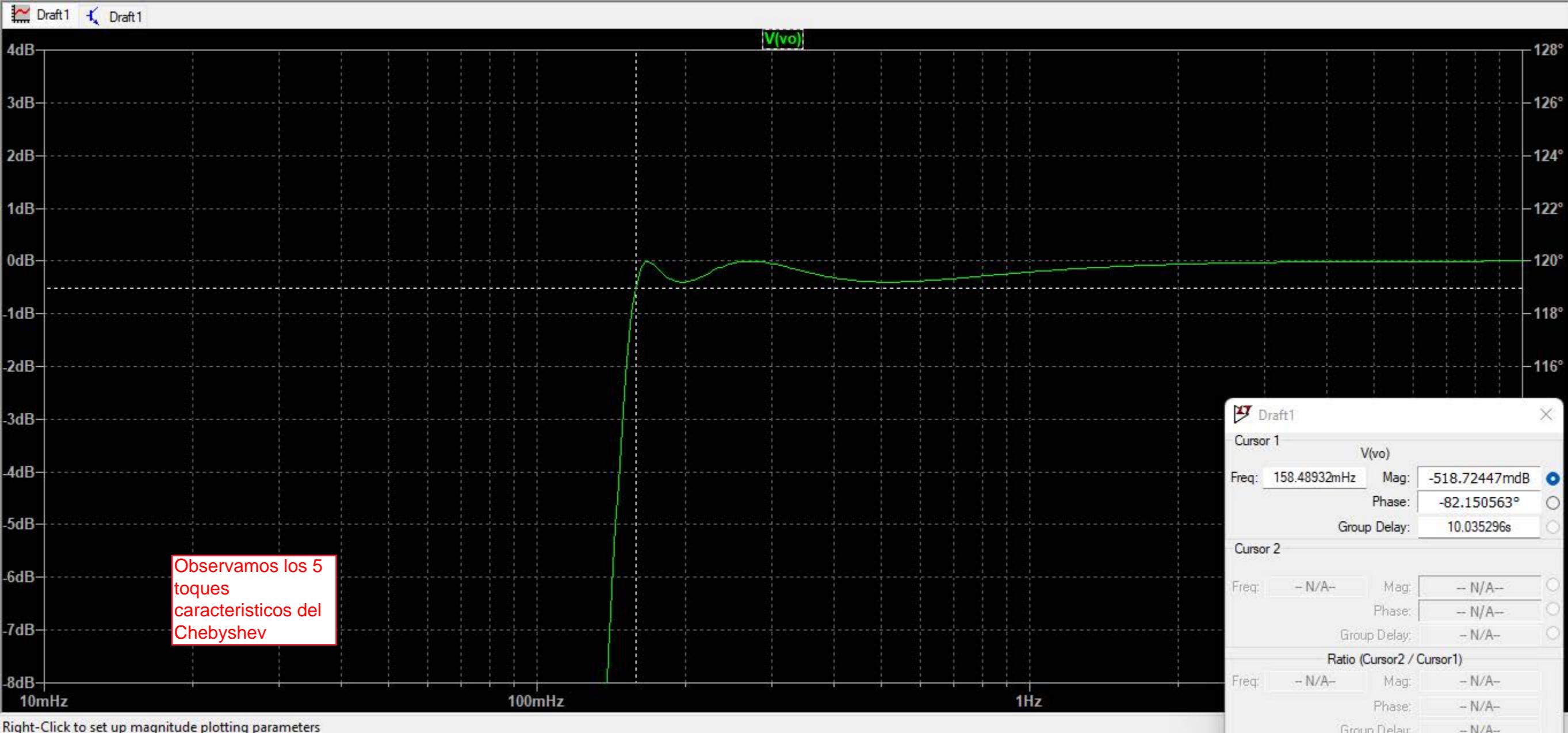
formula<sub>HP</sub> =  $\frac{s^2}{s^2 + s\frac{R}{L} + \frac{1}{LC}}$ 
~~descripción~~  
C = 1 F

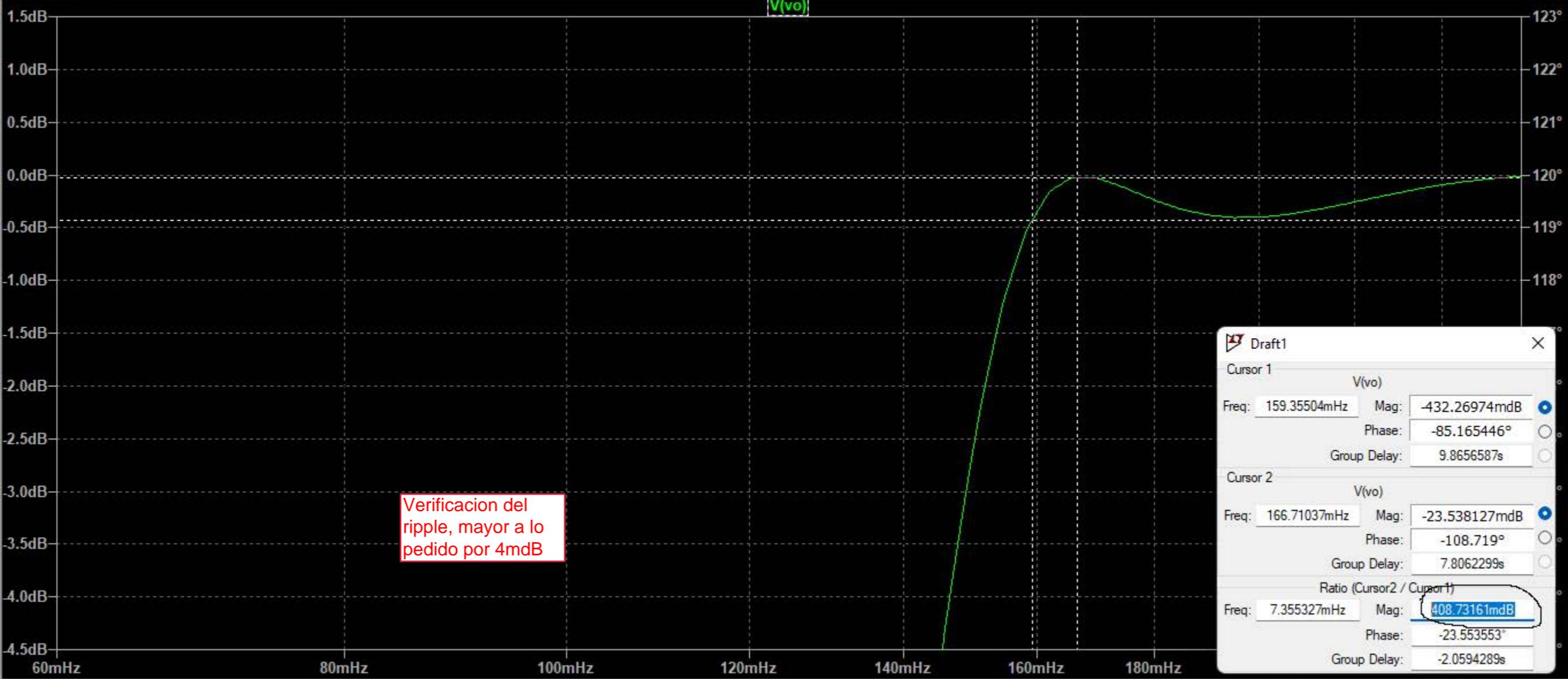


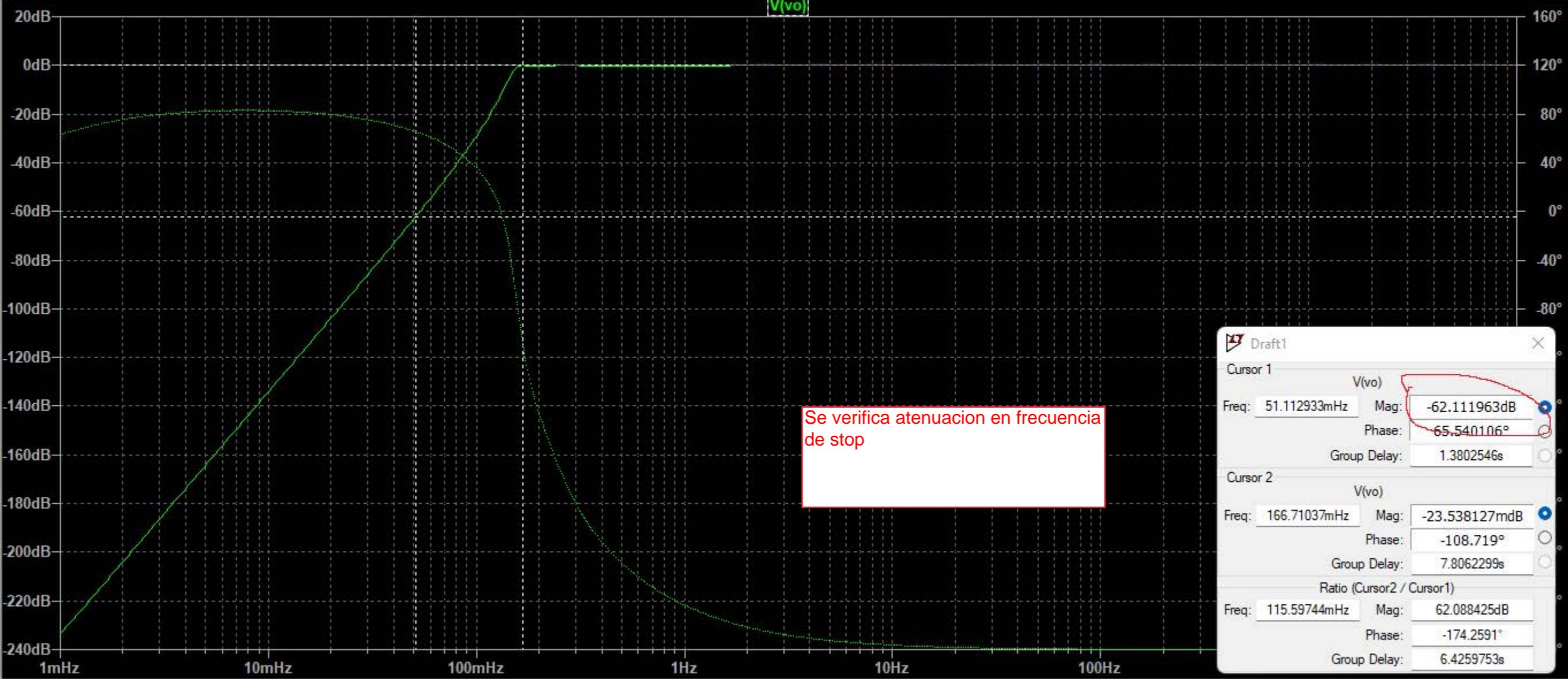
.lib opamp.sub

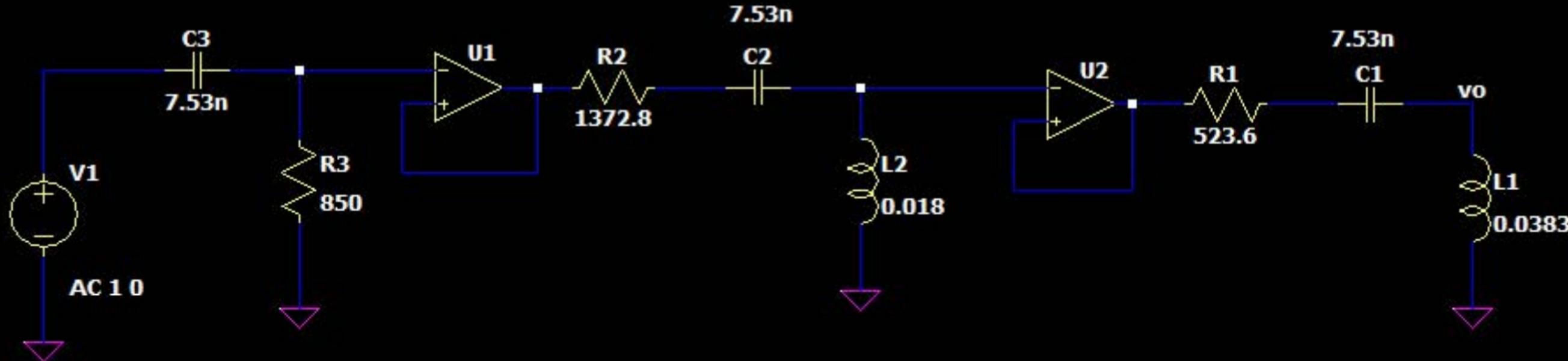
.ac dec 100 0.001 10K

Circuito normalizado









.lib opamp.sub

.ac dec 100 0.001 1Meg

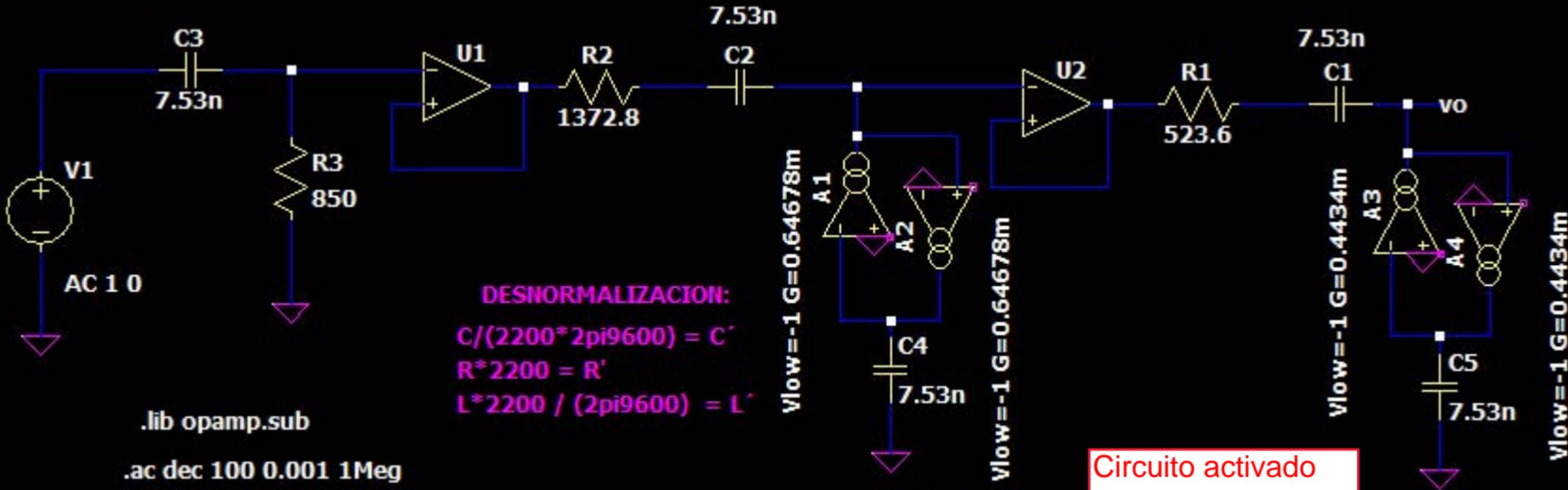
### DESNORMALIZACION:

$$C / (2200 * 2\pi 9600) = C'$$

$$R * 2200 = R'$$

$$L * 2200 / (2\pi 9600) = L'$$

Circuito desnormalizado



.lib opamp.sub

.ac dec 100 0.001 1Meg

6 Dibujar un filtro para-bajos con

$$D(\text{retardo}) = 100\mu s$$

$$\text{Retardo de retardo} = 10\% \text{ para } \omega_1 = 25 \text{ K} \cdot 2\pi \text{ Hz}$$

$$\text{Aumentación de } 1 \text{ dB a la } \omega_2 = 10 \text{ K} \cdot 2\pi \text{ Hz}$$

$$\Omega_\omega = \frac{1}{100\mu s} = 10 \text{ KHz} = \omega_0$$

Por analogía del gráfico en el eje horizontal = 2,5 y en el 10% y luego los que están por debajo de ese punto, .

$$\text{Otro} m = 4$$

$$\Delta \text{med} = 1 \text{ dB}$$

$$\sqrt{10}^{\frac{1}{10}} = 1 + 0,2589$$

utilizar aproximación de Bessel

$$\omega_0 = \frac{2}{D}$$

$$H(s) = \frac{P(s)}{Q(s)} = \frac{1}{\operatorname{senh}(s) + \operatorname{coth}(s)}$$

$$\operatorname{senh}(s) = s + \frac{s^3}{3!} + \frac{s^5}{5!} + \frac{s^7}{7!}$$

$$\operatorname{coth}(s) = 1 + \frac{s^2}{2!} + \frac{s^4}{4!} + \frac{s^6}{6!}$$

$$\operatorname{coth}(s)_{m=4} = \frac{1}{s} + \frac{1}{\frac{3}{s} + \frac{1}{\frac{5}{s} + \frac{1}{\frac{7}{s}}}}$$

$$\operatorname{coth}(s) = \frac{1}{s} + \frac{1}{\frac{3}{s} + \frac{1}{\frac{5}{s} + \frac{1}{\frac{5+s}{35+s}}}} = \frac{1}{s} + \frac{1}{\frac{3}{s} + \frac{7-s}{35+s^2}}$$

$$\operatorname{coth}(s) = \frac{1}{s} + \frac{s^3 + 35s^2 + s}{10s^2 + 105}$$

$$C_{th}(s) = \frac{1(10 \cdot s^2 + 105) + s^4 + 35 \cdot s^2}{10 \cdot s^3 + 105 \cdot s}$$

$$C_{th}^P(s) = \frac{s^4 + 4s \cdot s^2 + 105}{10 \cdot s^3 + 105 \cdot s}$$

$$H_4(s) = \frac{105}{s^4 + 10 \cdot s^3 + 4s \cdot s^2 + 105 \cdot s + 105}$$

Ej. 7)

$$f_{ci} = 1600 \text{ kHz}$$

$$f_{cs} = 2500 \text{ kHz}$$

RIPPLE MAXIMO 3dB

MP.

GANANCIA MAXIMA EN LA BANDA DE PASO: 10 dB

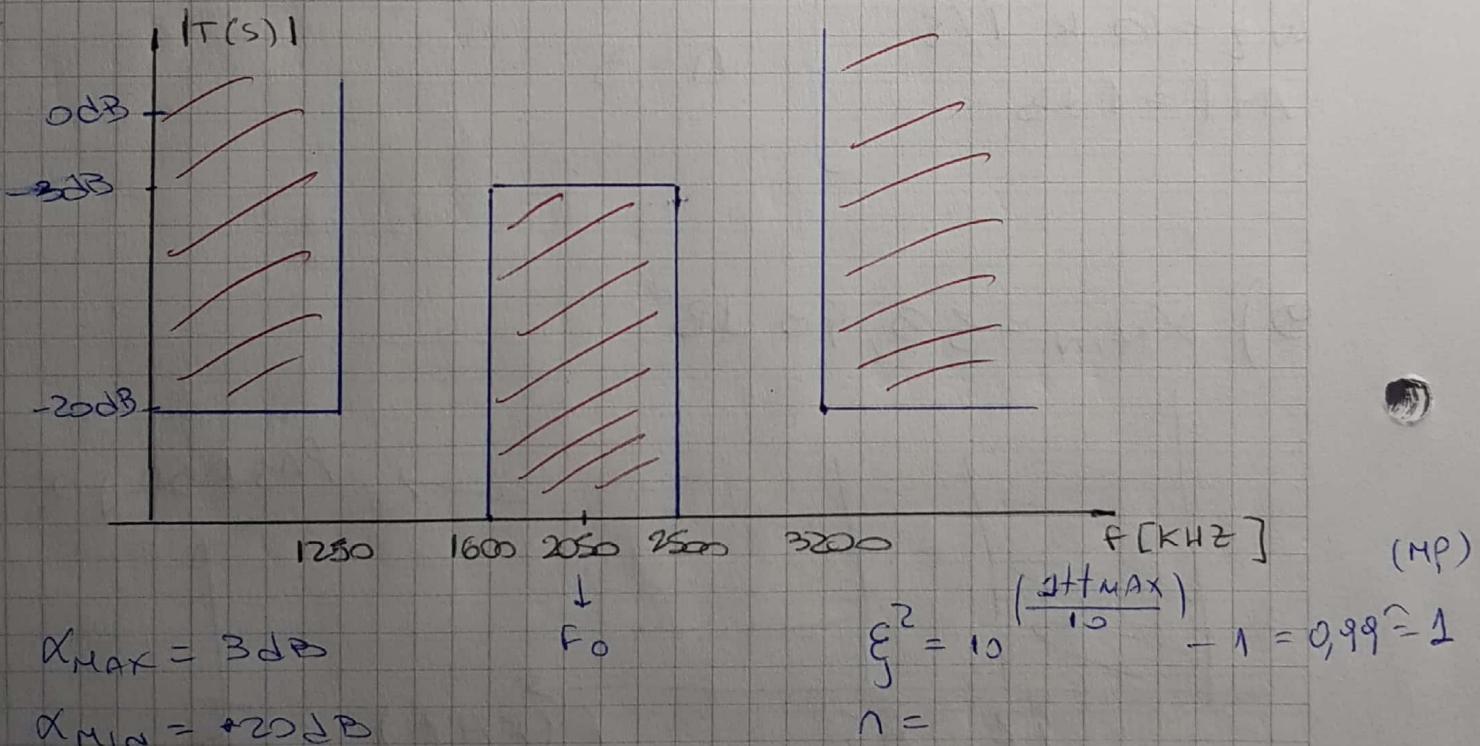
Att<sub>MIN</sub>: 20 dB → 1250 kHz × 3200 kHz

a) T(s)

b) P y Z

c) GRAFICAR TRANSF. MODUL Y FASE

d) SINTETIZAR C/ ACKERBERG-MOSBERG



$W_{ci} = \text{Angulo de FB } 0,8$

$W_{cs} = 1,25$

$W_{sn} = 0,625$

$W_{sr} = 1,6$

NOTA

$$K(s) = Q \cdot \frac{s^2 + 1}{s}$$

$$\omega_n \rightarrow 1 \quad \rightarrow Q = \frac{\omega_n}{BW}$$

$$BW = W_{cs} - W_{ci}$$

$$Q = 2,273$$

~~EN~~ = ~~PARA~~  
~~EN~~ = ~~PARA~~

$$\left. \begin{array}{l} S_{LS} = 2,16 \\ S_{LP} = 1 \end{array} \right\} \rightarrow \text{MAS 1 AD 4 O AS A PASABAJO}$$

$$n=3 \rightarrow Atf = 20,16 \downarrow B$$

INTERAN

$$\chi_{MIN} = 10 \log_{10} (1 + \xi^2 S_{LS}^{2n})$$

MODELOS PASABAJO

$$\frac{1}{1 - \xi^2 s^6} = \frac{1}{as^3 + bs^2 + cs + d} \quad \frac{1}{-as^3 + bs^2 - cs + d}$$

$$+\xi^2 = +a^2 \Rightarrow a = \xi$$

$$d = 1 \rightarrow d = 1$$

$$n=4 \\ 0 = b^2 + 2ac - ac \Rightarrow +2ac = b^2$$

$$n=2$$

$$c^2 = 2bd$$

$$c^2 = 2b \rightarrow c = \sqrt{2b}$$

$$c = \sqrt{2b} = \sqrt{\frac{4\xi^2}{3}} = 2\xi^{2/3}$$

$$= 2\xi^{2/3} = 2\xi^{1/3} = c$$

$$2\xi c = b^2 \rightarrow 2\xi \sqrt{2b} = b^2$$

$$4\xi^2 \sqrt{2b} = b^2$$

$$2\xi^{7/3} = b$$

$$\frac{1}{\xi s^3 + 2\xi^{2/3}s^2 + 2\xi^{1/3}s + 1} = T(s)$$

$$P_1 = \text{elbow } s + 1$$

$$P_2 = s - (-0,5 + j0,866)$$

$$P_3 = s - (-0,5 - j0,866)$$

$$T(s) = \frac{1}{s+1} \quad \frac{1}{s^2 + s + 1}$$

$$\text{DESNORMALIZADO} \quad \Leftrightarrow s = \frac{\$}{\$^{1/3}}$$

$$T(s) = \frac{1}{\frac{\$}{\$^{1/3}} + 1} \quad \frac{1}{\frac{\$^2}{\$^{1/3}} + \frac{\$}{\$^{1/3}} + 1}$$
$$= \frac{1}{s+1} \quad \frac{1}{s^2 + s + 1}$$

$$\text{NUCLEO: } Q \frac{(s^2 + 1)}{s}$$

$$T(s)_{BP} = \frac{1}{\frac{Q(s^2 + 1)}{s} + 1} \quad \frac{1}{\frac{Q^2(s^2 + 1)^2}{s^2} + \frac{Q(s^2 + 1)}{s} + 1} =$$

$$= \frac{s}{Qs^2 + s + Q} \quad \frac{s^2}{Q^2s^4 + 2Q^2s^2 + Q^2 + Qs^3 + Qs + \$^2}$$

$$= \frac{s/Q}{s^2 + \frac{s}{Q} + 1} \quad \frac{s^2/Q^2}{s^4 + \frac{s^3}{Q} + 3s^2 + \frac{s}{Q} + 1}$$

$$-0,25s \pm 0,874$$

$$\text{Polos } s \rightarrow -0,162 \pm j0,895 \\ + 0,063 \pm j0,62$$

$$= \frac{s/Q}{s^2 + \frac{s}{Q} + 1} \quad \frac{s/Q}{s^2 + 50,324 + 3s^2} \quad \frac{s/Q}{s^2 + 50,126 + 0,358}$$

Pobs:

$$P_{1,2} = -0,134 \pm j1,207$$

$$P_{3,4} = -0,225 \pm 0,0174$$

$$P_{5,6} = -0,09 \pm j0,813$$

$$z = (0)^3$$

SOS 1

$$\frac{1}{s^2 + \frac{s}{Q} + 1}$$

~~$\frac{\omega_1}{Q_1}$~~  SOS 2 ✓

$$0,268 \cdot s \cancel{\frac{1}{Q}} \left( \frac{1}{s+0,268} \right)$$

$$s^2 + 0,268s + 1,475$$

$K_2$

$$\frac{\omega_3}{Q_3}$$

$J_3$

$$0,18 \cancel{s \frac{1}{Q}} \left( \frac{1}{s+0,18} \right)$$

$$s^2 + 0,18s + 0,677$$

$$\omega_{01} = 1$$

$$\omega_{02} = 1,21$$

$$\omega_{03} = 0,372$$

$$Q_1 = 1,21$$

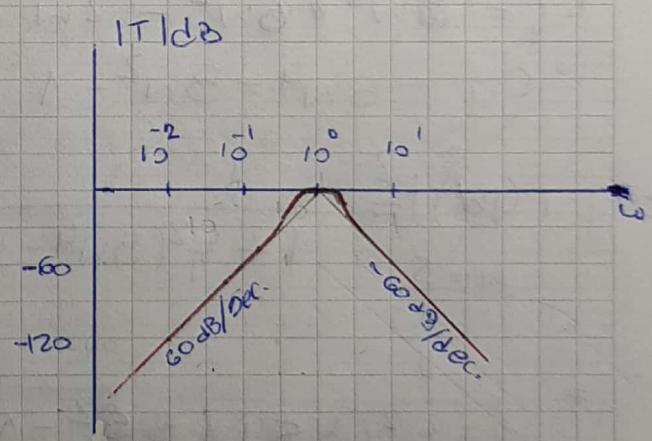
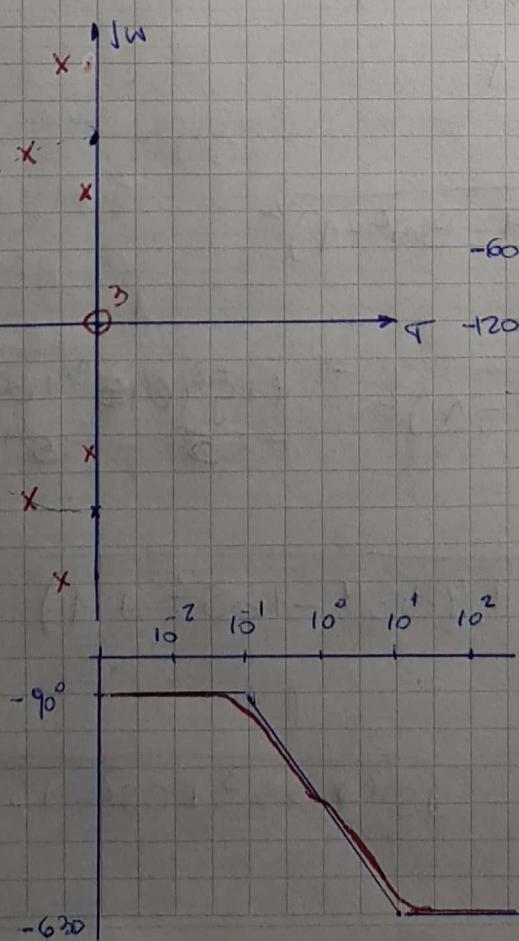
$$Q_2 = 4,53$$

$$Q_3 = 4,156$$

$$K_1 = 1$$

$$K_2 = 1,68$$

$$K_3 = 2,5$$



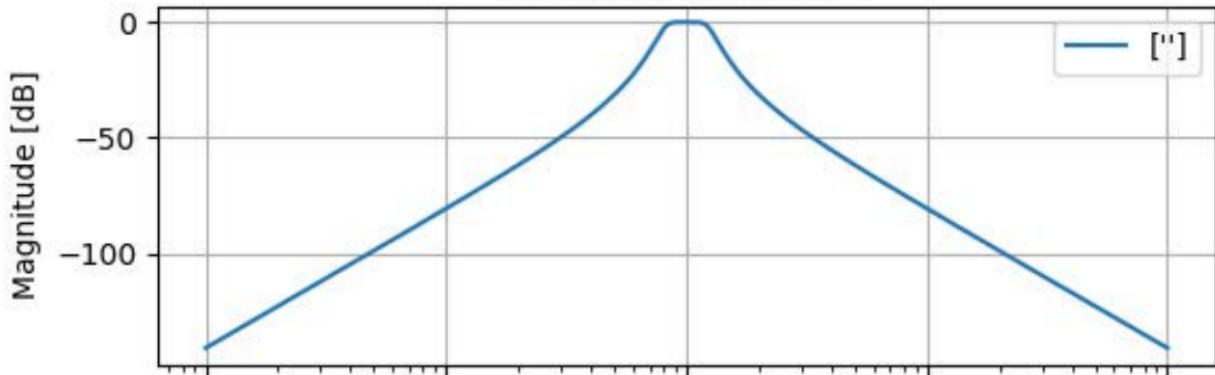
TENES EL APORTO DE LOS CEROS  $\rightarrow 60 \text{ dB/dec}$  QUE SE VENAN COMPENSADOS CON LOS CEROS, LOS CUales TERMINAN APORTANDO  $-60 \text{ dB/dec}$

$$z^3 \rightarrow 270^\circ$$

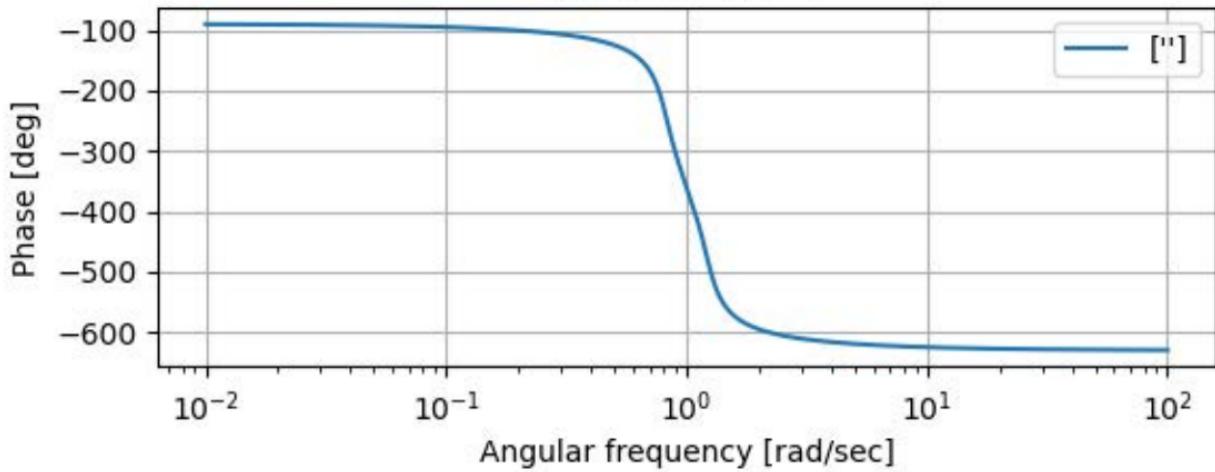
$$-90^\circ$$

$$P^2 \rightarrow 3 \cdot 180^\circ \\ -540^\circ$$

Magnitude response



Phase response



Poles and Zeros map

$Q = 4.53$

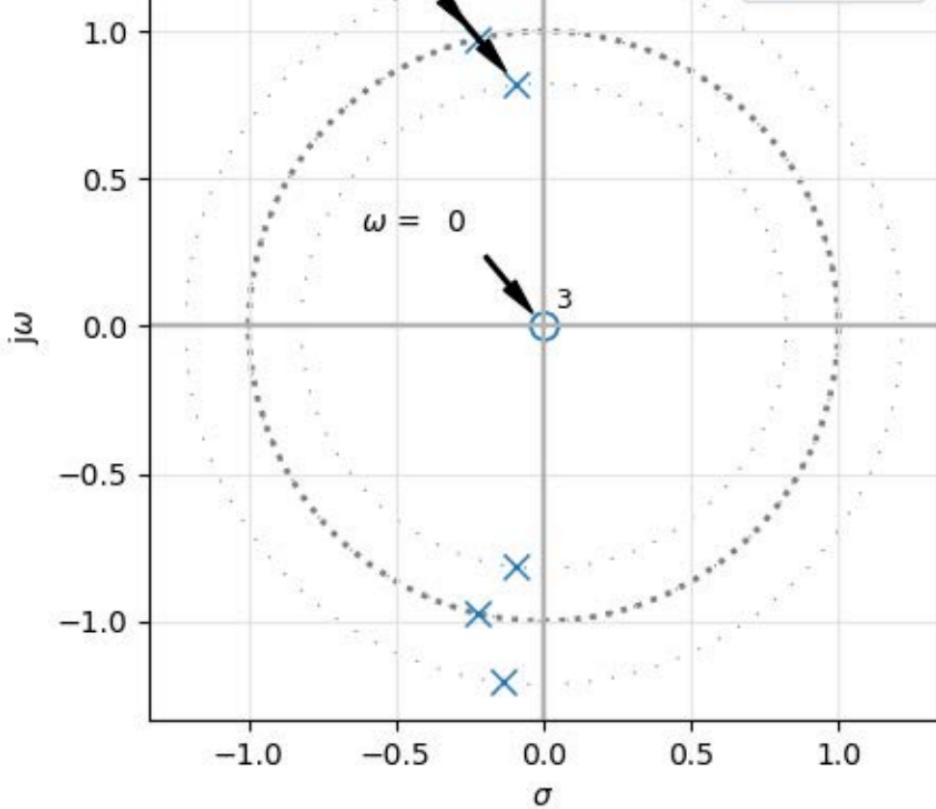
$\omega = 1$

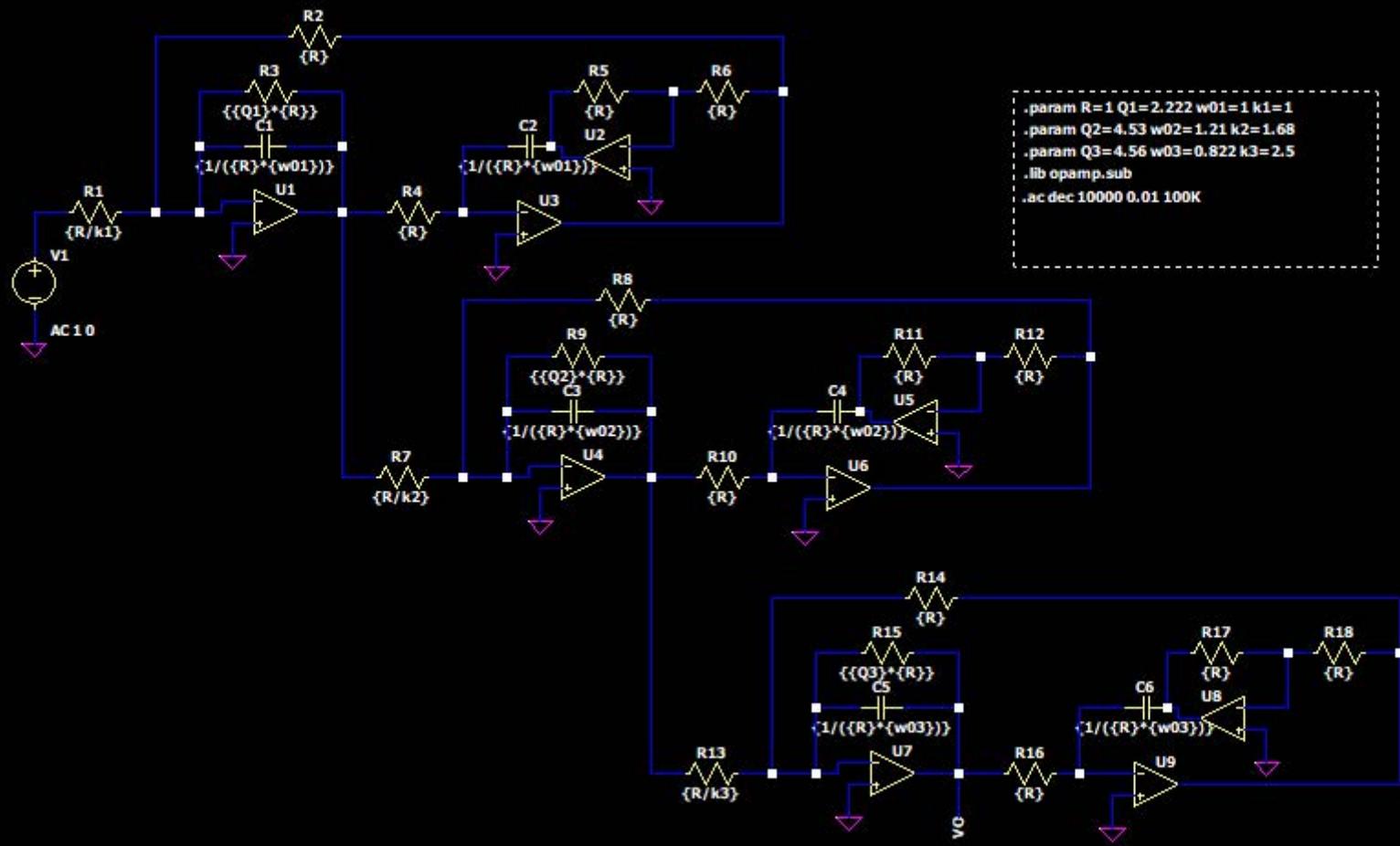
$\omega = 2.22$

$\omega = 0.823$

$Q = 4.53$

 none

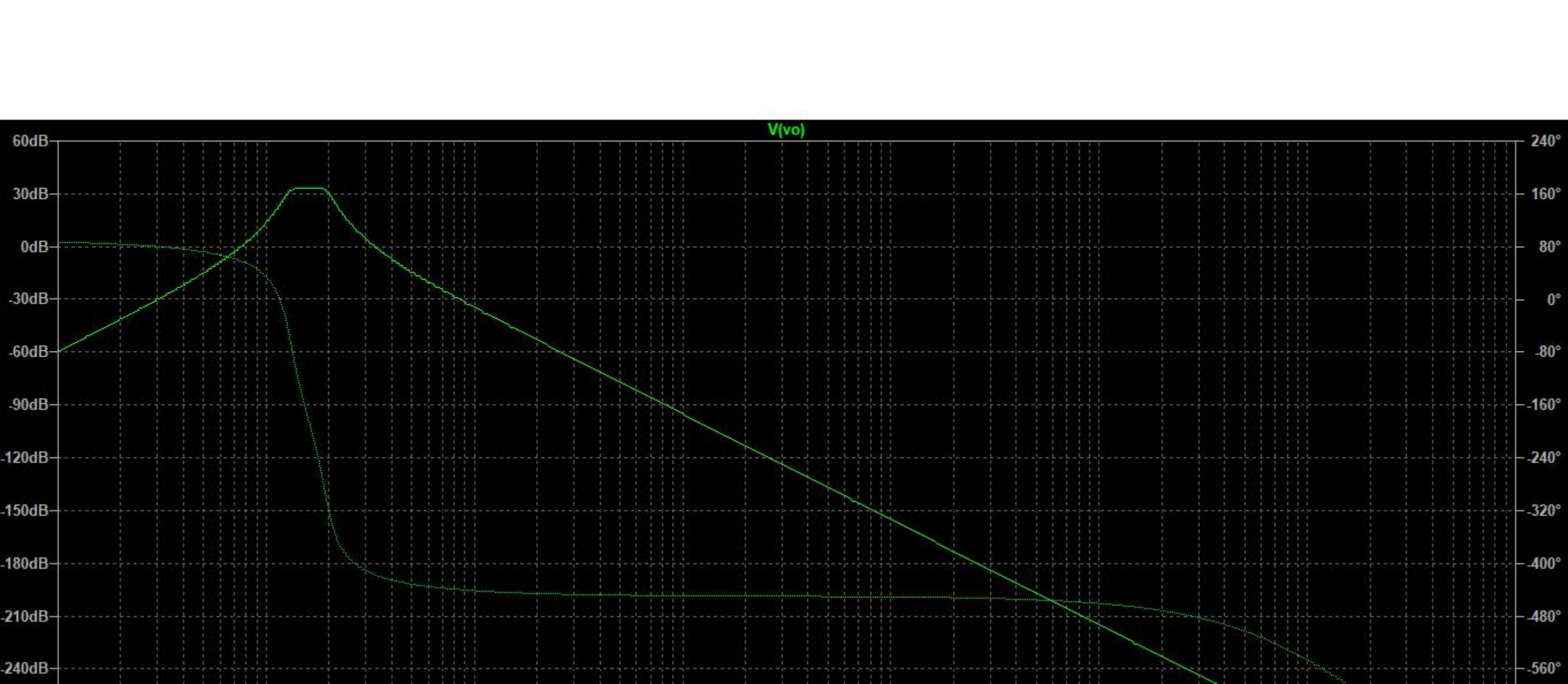


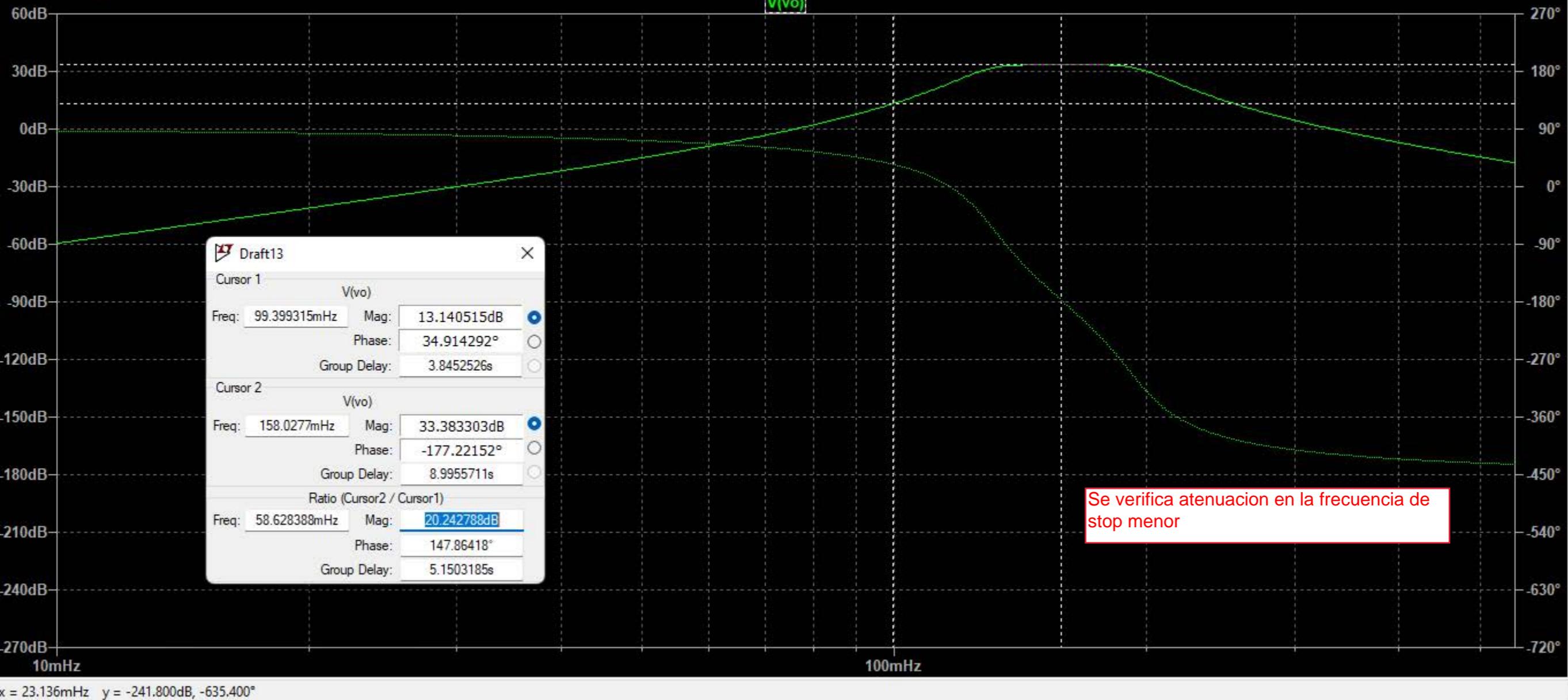


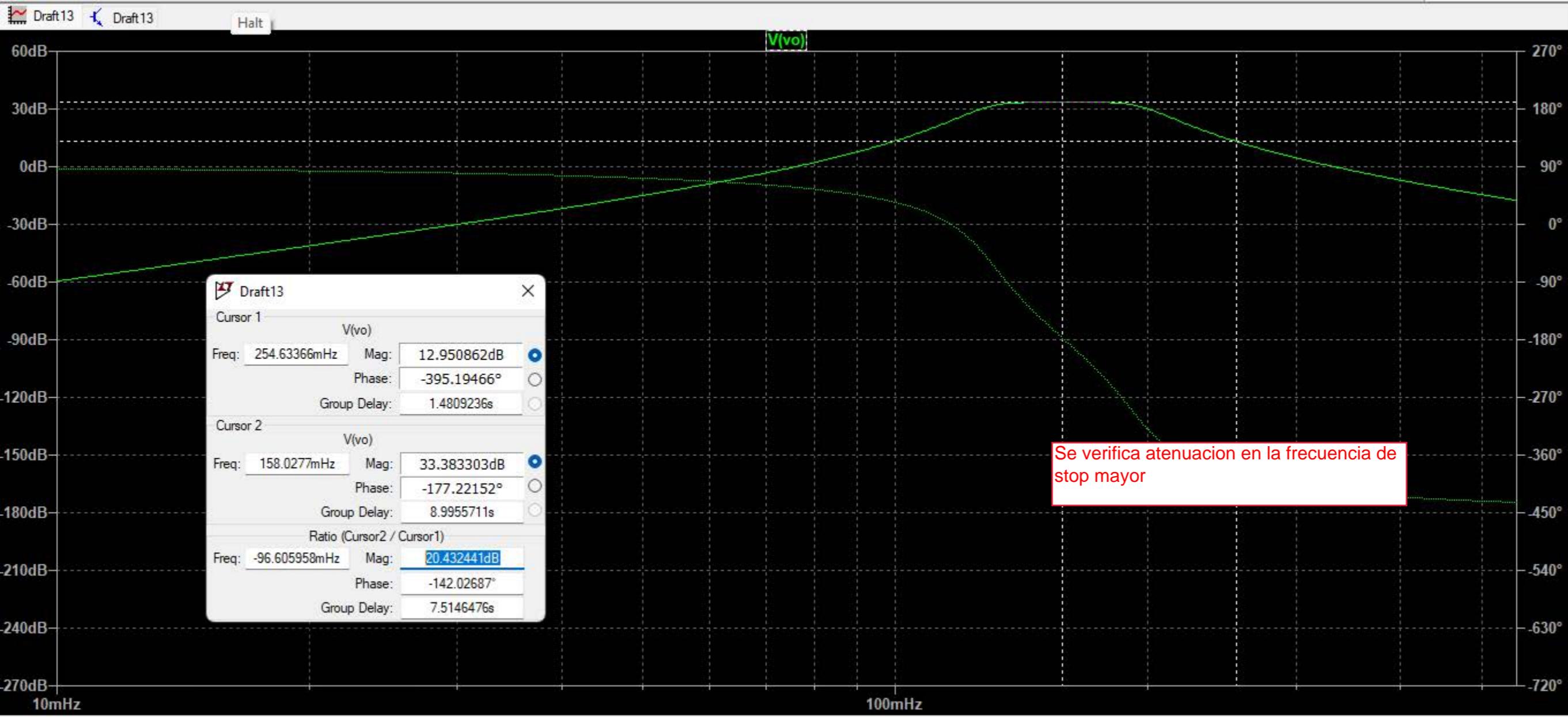
```

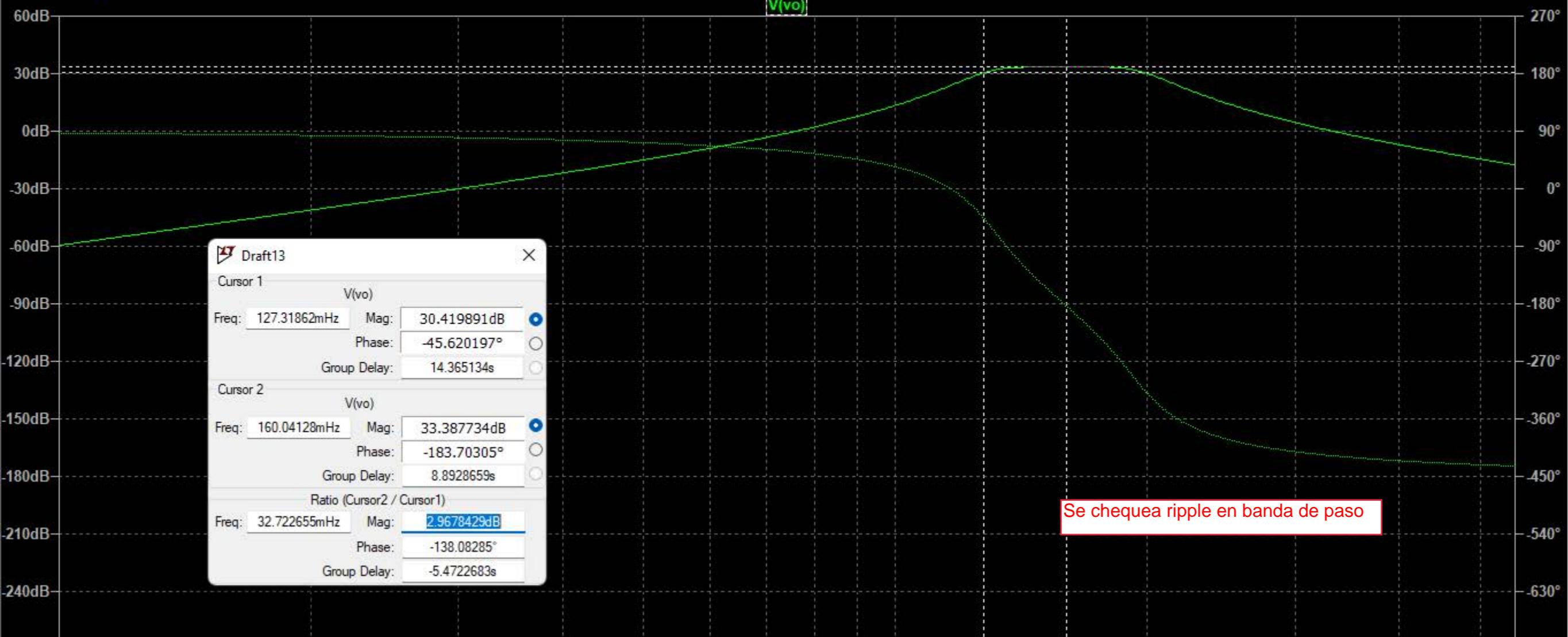
.param R=1 Q1=2.222 w01=1 k1=1
.param Q2=4.53 w02=1.21 k2=1.68
.param Q3=4.56 w03=0.822 k3=2.5
.lib opamp.sub
.ac dec 10000 0.01 100K

```



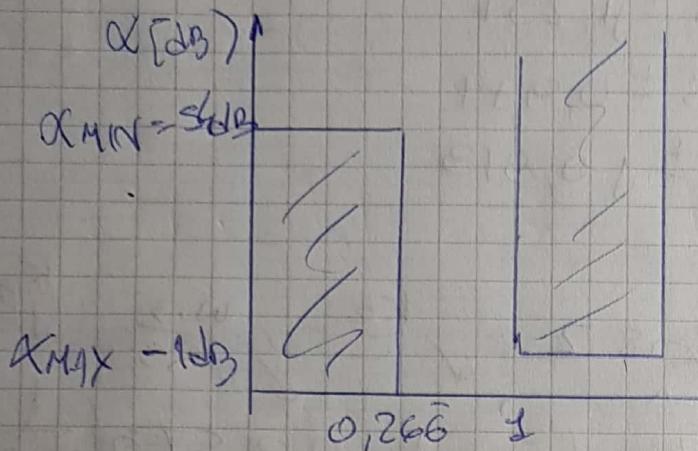






$$3) \quad X_{MIN} = 53,98 dB \quad \omega_B = 2\pi 45 kHz$$

$$X_{MAX} = 1 dB \quad \omega_S = 2\pi 12 kHz$$



~~$$\Sigma S = 3,75$$~~

$$\Sigma p = 1$$

$$\xi_j^2 = 0,259$$

$$\lambda = 4$$

$$C_4 = 2w(4w^3 - 3w) - 2w^2 - 1$$

$$C_4 = 8w^4 + 8w^2 - 2w^2 - 1$$

$$C_4 = 8w^4 - 8w^2 - 1$$

$$|T(j\omega)|^2 = \frac{1}{1 + \xi_j^2(8w^4 - 8w^2 - 1)^2}$$

$$= \frac{1}{1 + \xi^2(8s^4 + 8s^2 - 1)^2} = \frac{1 + \xi^2(64s^8 + 64s^6 - 8s^4 + 64s^6 + 64s^4 - 8s^2 - 8s^4 - 8s^2 + 1)}{(1 + \xi^2(64s^8 + 64s^6 - 8s^4 + 64s^6 + 64s^4 - 8s^2 - 8s^4 - 8s^2 + 1))}$$

$$= \frac{1}{1 + \xi^2(64s^8 + 128s^6 + 48s^4 - 16s^2 + 1)}$$

$$\frac{1}{as^4 + bs^3 + cs^2 + ds + e} = \frac{1}{as^4 + bs^3 + cs^2 - ds + e}$$

NOTA

$$e = \sqrt{1+g^2}$$

De

$$g^2 64 = d^2 \rightarrow \boxed{d = 8\sqrt{2}}$$

n=6

$$g^2 128 = 2dc + b^2 \quad \text{y} \quad b^2 = \sqrt{288c - g^2 128}$$

n=4

$$48g^2 = 2de + bd - bd + c^2$$

n=2

$$-16g^2 = 2ce - d^2 \rightarrow$$

$$d = \sqrt{2\sqrt{(1+g^2)}c + 16g^2}$$

$$48g^2 = 2de - 2bd + c^2$$

$$48g^2 = 2\sqrt{2\sqrt{(1+g^2)}c + 16g^2} \sqrt{(1+g^2)} - 2\sqrt{288c - g^2 128}$$

Python:

$$T(s) = \frac{0,2456}{s^4 + 0,9528s^3 + 1,4539s^2 + 0,7426s + 0,2756}$$

$$\text{Peso } s = \frac{\$}{\$}$$

$$T(\$) = \frac{0,2456}{\frac{1}{\$^4} + 0,9528 \frac{1}{\$^3} + 1,4539 \frac{1}{\$^2} + 0,7426 \frac{1}{\$} + 0,2756}$$

$$T(\$) = \frac{\$^4 0,2456}{\$^4 0,2756 + \$^3 0,7426 + \$^2 1,4539 + \$ 0,9528 + 1}$$

$$T(\$) = \frac{0,891 \$^4}{\$^4 + 2,694 \$^3 + 5,275 \$^2 + 3,457 \$ + 3,62}$$

$$P_{1,2} = -0,143 \pm j0,996$$

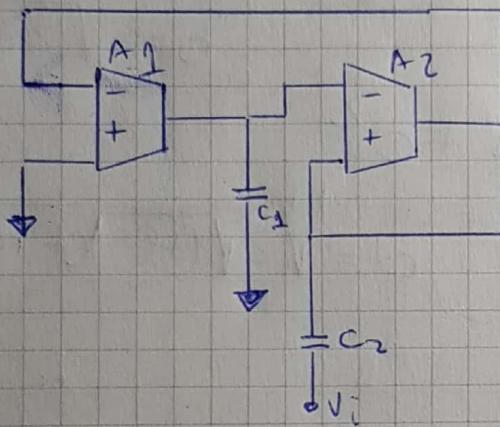
$$P_{3,4} = -1,2 \pm j1,46$$

K

$$\frac{0,891}{s^2 + 0,286s + 1,012}$$

SOS 2

$$\frac{s^2}{s^2 + 2,4s + 3,572}$$



$$\frac{s^2 c_1 c_2}{s^2 c_1 c_2 + s c_1 g_m 2 + g_m 1 g_m 2}$$

SOS ④

$$\omega_0 = \frac{g_m}{\sqrt{c_1 c_2}} \sqrt{\frac{c_2}{c_1}} = Q$$

$$c_1 g_m 2 = 0,286$$

$$g_m 1 g_m 2 = 1,012$$

$$c_1 c_2 = 1$$

SOS ②

$$c_1 g_m 2 = 2,4$$

$$g_m 1 g_m 2 = 3,572$$

$$c_1 c_2 = 1$$

