

$$I_1 = \frac{V_1}{R_1} + \frac{V_1 - V_2}{R_2} + I_1'$$

$$I_2 = \frac{V_2}{R_3} + \frac{V_2 - V_1}{R_2} + I_2'$$

$$I_1 = V_1 \left(\frac{1}{R_1} + \frac{2}{R_2} \right) + I_1'$$

$$I_2 = \left(\frac{1}{R_3} + \frac{2}{R_2} \right) V_2 + I_2'$$

$$Z_{11} = \frac{V_1}{I_1} \quad I_2 = 0$$



$$-\frac{V_2}{V_1} \left(\frac{1}{R_3} + \frac{2}{R_2} \right) = \frac{I_2'}{I_1'} = I_1'$$

$$I_1 = V_1 \left(\frac{1}{R_1} + \frac{2}{R_2} \right) + V_1 \left(\frac{1}{R_3} + \frac{2}{R_2} \right)$$

$$I_1 = V_1 \left(\frac{1}{R_1} + \frac{4}{R_2} + \frac{1}{R_3} \right)$$

$$I_2' = (-I_2')(-a)$$

$$V_1 = -V_2 \cdot \frac{1}{a}$$

$$a = 1$$

$$I_2' = \frac{1}{a} (-I_2')$$

$$V_1 = -a V_2$$

$$a = 1$$

$$I_1' = I_2'$$

$$V_1 = -V_2$$

$$Z_{12} = 0,3$$

$$Z_{12} = \left. \frac{V_1}{I_2} \right|_{I_1=0} = -0,3 \rightarrow \text{COMO SON COMPONENTES PASIVOS}$$

$$Z_{12} = Z_{21}$$

$$-V_1 \left(\frac{1}{R_1} + \frac{2}{R_2} \right) = I_1'$$

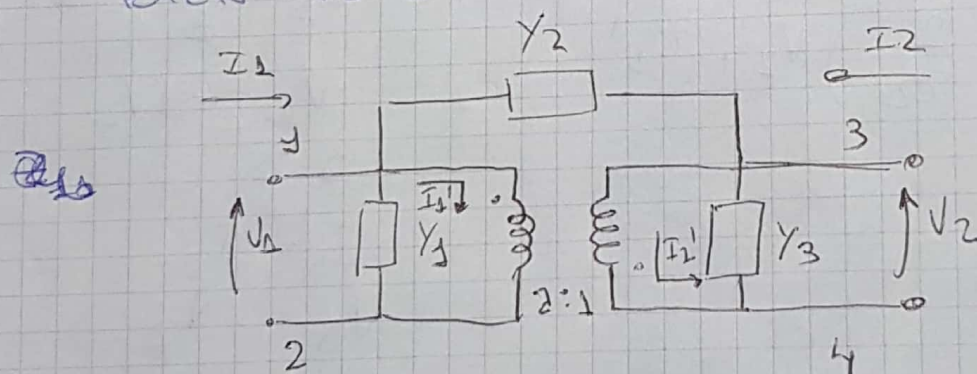
$$I_2 = \left(\frac{1}{R_3} + \frac{2}{R_2} \right) V_1 - V_1 \left(\frac{1}{R_1} + \frac{2}{R_2} \right)$$

$$Z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0} = 0,3$$

$$I_2 = \left(\frac{1}{R_3} + \frac{2}{R_2} \right) V_2 + V_2 \left(\frac{1}{R_1} + \frac{2}{R_2} \right)$$

$$\frac{V_2}{I_2} = \frac{1}{\frac{1}{R_3} + \frac{4}{R_2} + \frac{1}{R_1}} = 0,3$$

NO SOLO ES RECIPROCO, SINO QUE TAMBIEN ES SIMETRICO.



$$V_1 = -2V_2$$

$$I_1' = \left(-\frac{1}{2} \right) (-I_2')$$

$$V_1 Y_1 + \frac{(V_1 - V_2)}{Y_2} + I_1' = I_1$$

$$V_2 Y_3 + \frac{(V_2 - V_1)}{Y_2} + I_2' = I_2$$

$$V_1 Y_1 + \left(\frac{1}{a} + 1 \right) V_1 Y_2 + I_1' = I_1$$

$$V_2 Y_3 + (1+a) Y_2 V_2 + I_2' = I_2$$

$$\text{if } I_2 = 0$$

$$-V_2 Y_3 + (1+a) Y_2 V_2 = I_2'$$

$$\frac{V_1}{a} (Y_3 + Y_2 + Y_2 a) = a I_1'$$

$$V_1 Y_1 + \left(1 + \frac{1}{a} \right) V_1 Y_2 + \frac{V_1}{a^2} Y_3 + \frac{V_1}{a^2} Y_2 + \frac{V_1}{a} Y_2 = I_1$$

$$V_1 Y_1 + \left(\frac{a+1}{a} \right) V_1 Y_2 + \frac{V_1 Y_3}{a^2} + V_1 Y_2 + \frac{V_1 Y_2}{a} = I_1$$

$$V_1 (Y_1 a^2 + a^2 Y_2 + Y_2 a^2 + \frac{Y_3}{a^2} + Y_2 a^2 + Y_2 a) = I_1 a^2$$

$$\frac{V_1}{I_1} = \frac{a^2}{Y_1 a^2 + a^2 Y_2 + a^2 Y_2 + Y_3 + Y_2 a^2 + Y_2 a} = Z_{11}$$

$$Z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0}$$

$$I_1' = -V_1 \left(Y_1 + \left(1 + \frac{1}{a} \right) Y_2 \right)$$

$$\frac{1}{a} I_2' = a V_2 \left(Y_1 + \left(1 + \frac{1}{a} \right) Y_2 \right)$$

$$V_2 Y_3 + (1+a) Y_2 V_2 + a^2 V_2 Y_1 + a^2 Y_2 V_2 + a V_2 Y_2 = I_2$$

$$V_2 (Y_3 + (1+a) Y_2 + a^2 Y_1 + a^2 Y_2 + a Y_2) = I_2$$

$$\frac{V_2}{I_2} = \frac{1}{Y_3 + (1+a) Y_2 + a^2 Y_1 + a^2 Y_2 + a Y_2} = Z_{22}$$

$$z_{12} = \left. \frac{V_1}{I_2} \right|_{I_1=0}$$

$$I_1' = -V_1 \left(Y_1 + \left(1 + \frac{1}{a} \right) Y_2 \right)$$

$$I_2 = V_2 Y_3 + (1+a) Y_2 V_2 + I_2' = 0$$

$$\frac{1}{a} I_1' = -V_1 \left(Y_1 + \left(1 + \frac{1}{a} \right) Y_2 \right)$$

$$I_2 = -\frac{V_1}{a} Y_3 + (1+a) Y_2 \left(-\frac{V_1}{a} \right) - a V_1 \left(Y_1 + \left(1 + \frac{1}{a} \right) Y_2 \right)$$

$$I_2 = \cancel{a V_1} - V_1 \left(Y_3 + (1+a) Y_2 + a Y_1 + a \left(1 + \frac{1}{a} \right) Y_2 \right)$$

$$\frac{V_1}{I_2} = \frac{-1}{Y_3 + (1+a) Y_2 + a Y_1 + a \left(1 + \frac{1}{a} \right) Y_2} = z_{12}$$

$$z_{21} = \left. \frac{V_2}{I_1} \right|_{I_2=0}$$

$$I_1 = V_1 Y_1 + \left(1 + \frac{1}{a} \right) V_2 Y_2 + I_1'$$

$$-V_2 \left(Y_3 + (1+a) Y_2 \right) = I_2'$$

$$\frac{V_2}{a} \left(Y_3 + (1+a) Y_2 \right) = a I_1'$$

$$I_1 = -a V_2 Y_1 + \left(1 + \frac{1}{a} \right) (-a V_2) Y_2 + \frac{-V_2 \left(Y_3 + (1+a) Y_2 \right)}{a}$$

$$I_1 = -V_2 \left(a Y_1 + \left(1 + \frac{1}{a} \right) a Y_2 + \frac{Y_3}{a} + \frac{(1+a) Y_2}{a} \right)$$

$$\frac{V_2}{I_1} = \frac{1}{a^2 Y_1 + \left(1 + \frac{1}{a} \right) a^2 Y_2 + \frac{Y_3}{a} + \frac{(1+a) Y_2}{a}} = z_{21}$$